

Yonatan Dubi

Department of Chemistry
Ben-Gurion University of the Negev
Beer-Sheva, Israel



Interplay Between Dephasing and Geometry: Directed Heat Flow in Exciton Transfer Complexes



Non-Equilibrium Statistical Physics

26 Oct, 2015 - 20 Nov, 2015

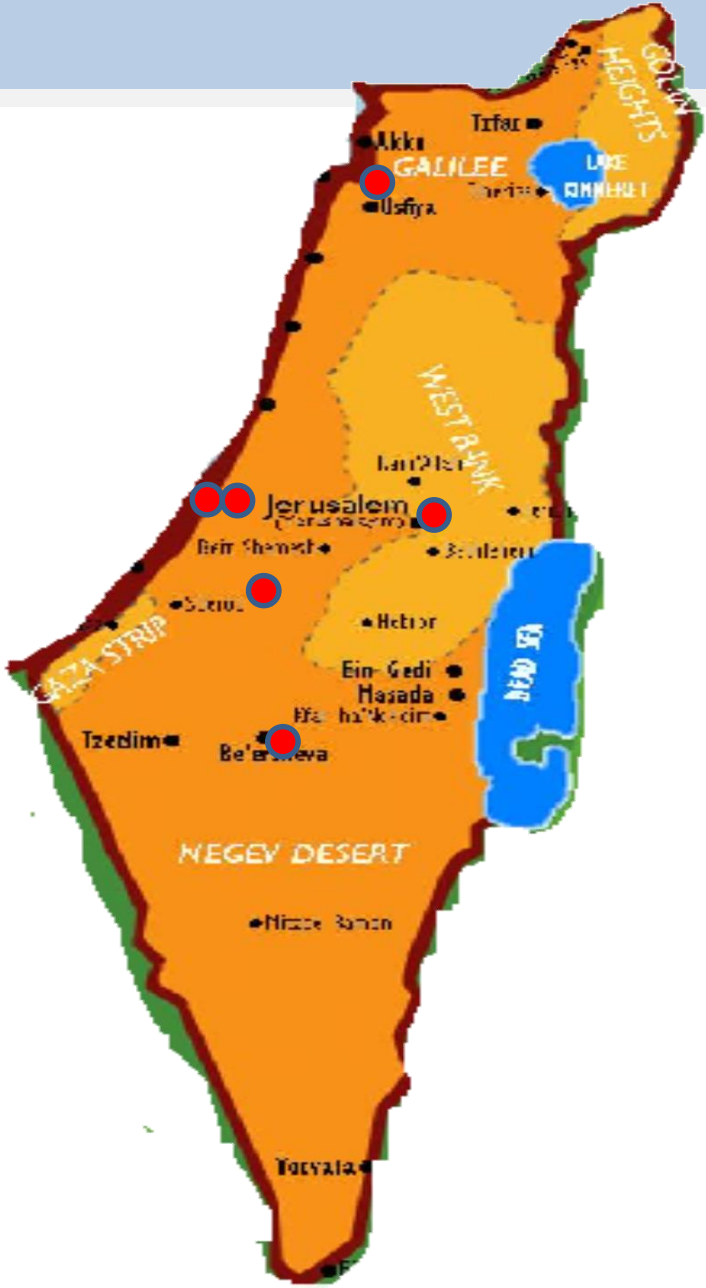
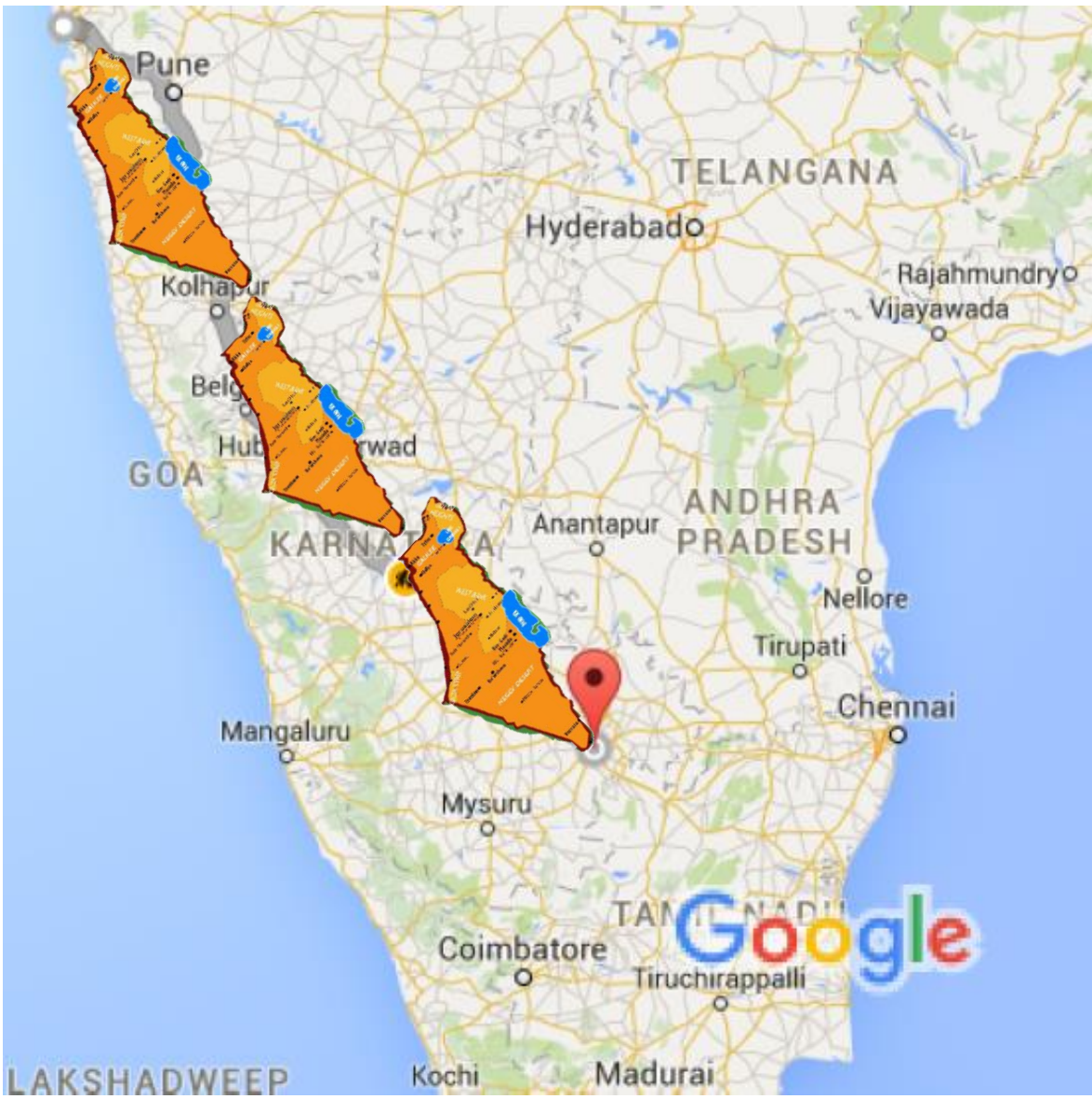
Fondation
Adelis



Feel the
Energy



Ben-Gurion University
of the Negev

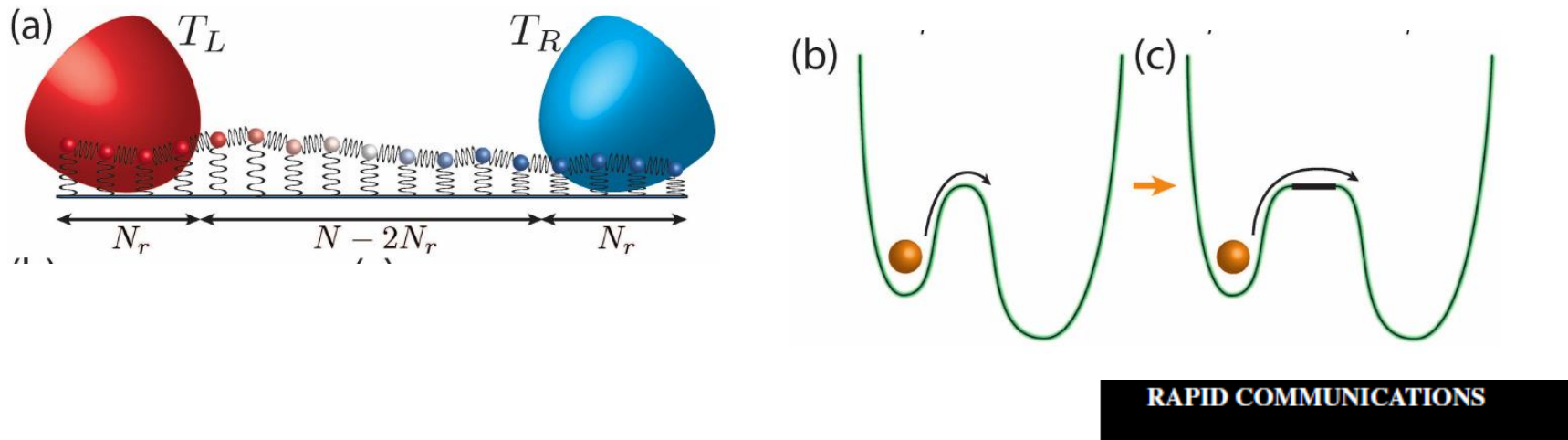


Ask me about thermal transport...

Crossover behavior of the thermal conductance and Kramers' transition rate theory

Kirill A. Velizhanin,^{1,*} Subin Sahu,^{2,3,4} Chih-Chun Chien,⁵ Yonatan Dubi,⁶ and Michael Zwolak^{2,4,†}

(NPG Scientific Reports, *in press*)



PHYSICAL REVIEW E 83, 050906(R) (2011)

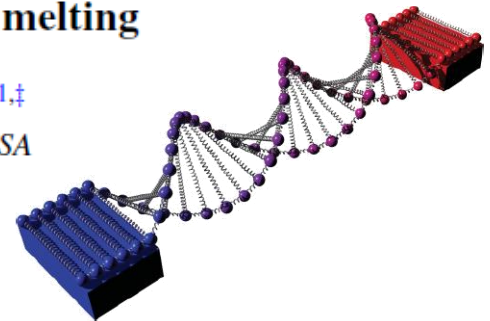
Driving denaturation: Nanoscale thermal transport as a probe of DNA melting

Kirill A. Velizhanin,^{1,2,*} Chih-Chun Chien,¹ Yonatan Dubi,^{1,†} and Michael Zwolak^{1,‡}

¹Theoretical Division, Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA

²CNLS, Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA

(Received 15 December 2010; published 19 May 2011)



Outline

Part I:

- Introduction – Quantum Biology?
- Motivation – optical experiments on photosynthetic complexes
- Quick review of current theory

Part II:

- Thinking about *Power*
- Interplay between performance, Geometry and Environment

- Summary & Conclusions

Outline

Part I:

- Introduction – Quantum Biology?
- Motivation – optical experiments on photosynthetic complexes
- Quick review of current theory

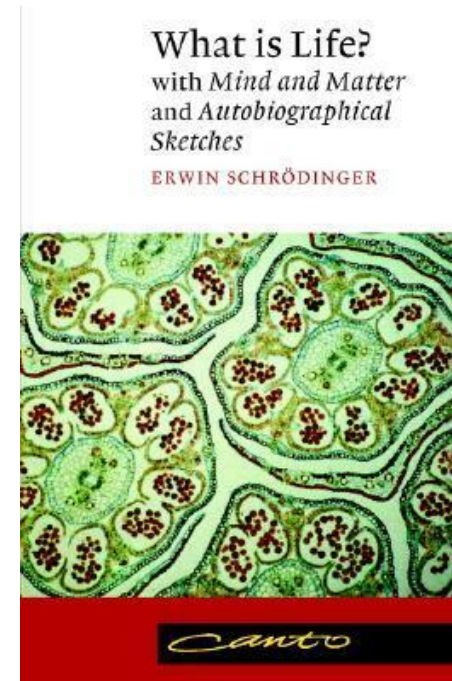
Part II:

- Thinking about Power
- Interplay between performance, Geometry and Environment
- Summary & Conclusions

Introduction – Quantum Biology?

Quantum Biology:

the search for “non-trivial” quantum effects in biological systems



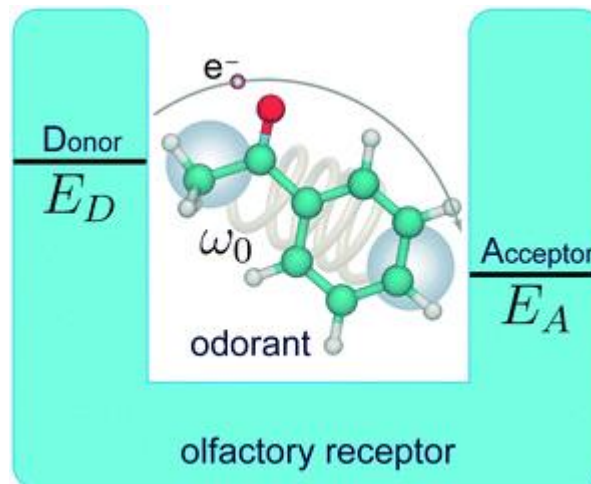
Introduction – Quantum Biology?

Quantum Biology:

the search for “non-trivial” quantum effects in biological systems

Candidates:

- Olfaction (how do we sense molecules by smell?)



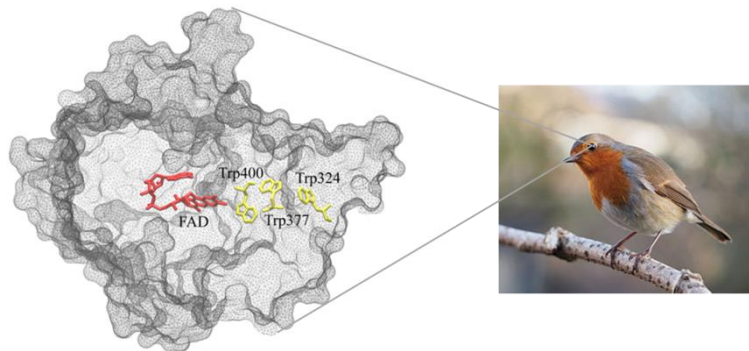
Introduction – Quantum Biology?

Quantum Biology:

the search for “non-trivial” quantum effects in biological systems

Candidates:

- Olfaction (how do we sense molecules by smell?)
- Avian navigation (how does a Robin find its way from Norway to Egypt?)



Introduction – Quantum Biology?

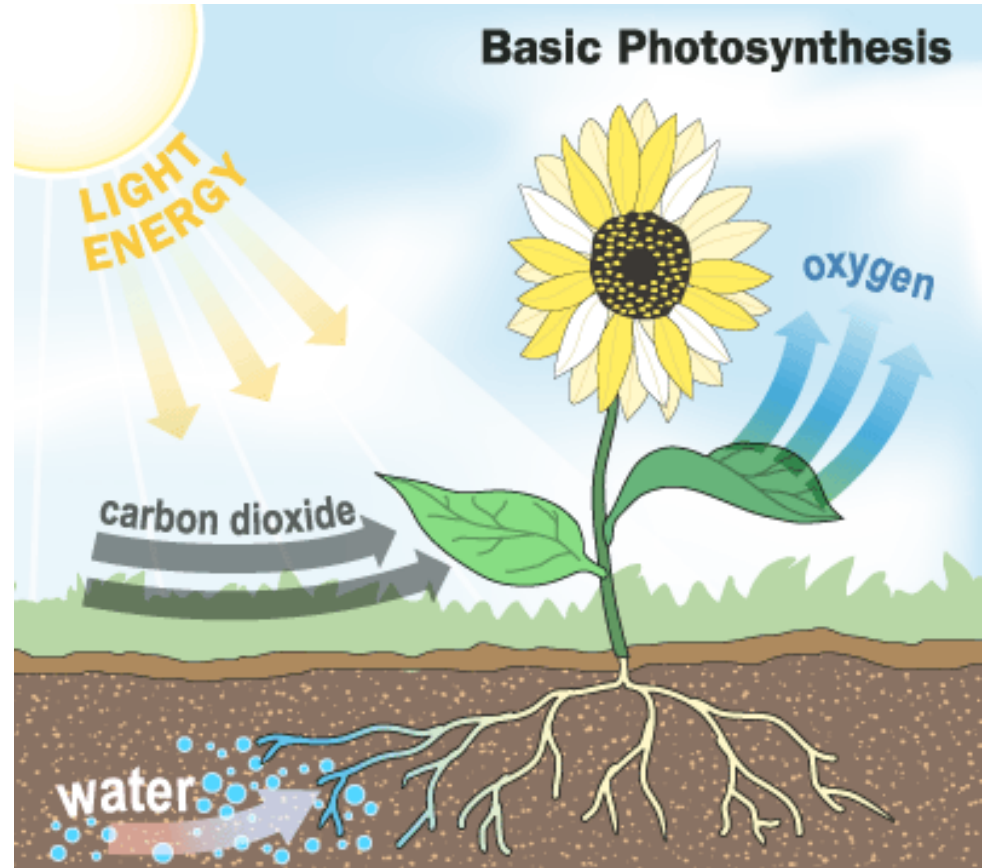
Quantum Biology:

the search for “non-trivial” quantum effects in biological systems

Candidates:

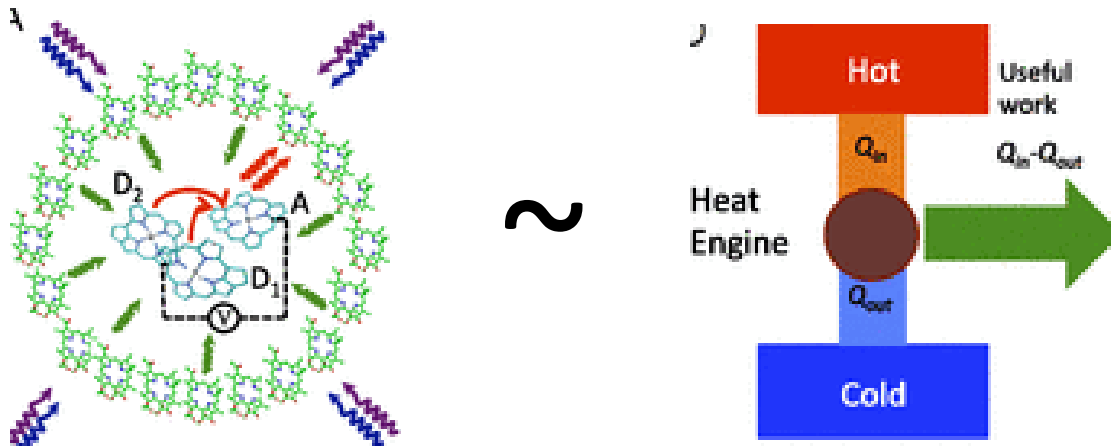
- Olfaction (how do we sense molecules by smell?)
- Avian navigation (how does a Robin find its way from Norway to Egypt?)
- **Photosynthesis**

Intro to Photosynthesis



Intro to Photosynthesis

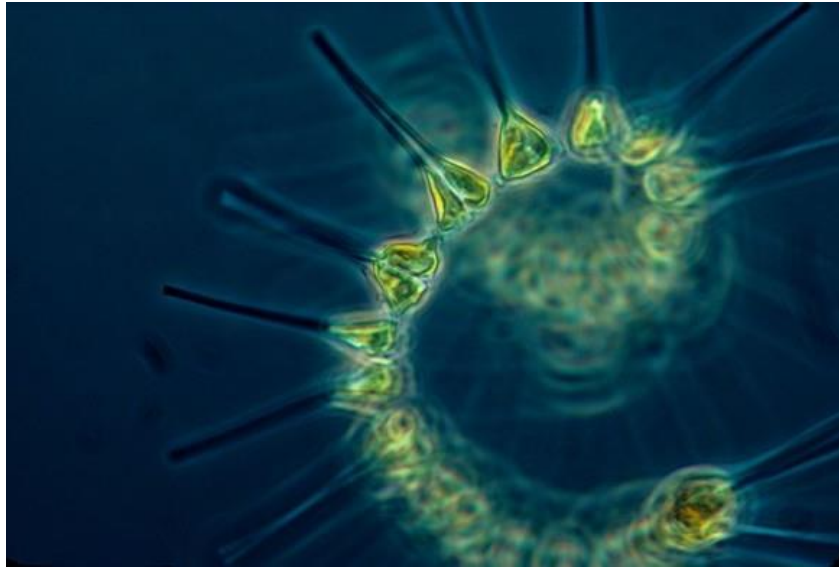
- PS cells – like solar cells – can be viewed as *heat engines*
- They *always* work very far from equilibrium



Dorfman, Voronin, Mukamel & Scully PNAS **110**, 2746(2012)

See also Einax, Dierl & Nitzan, J. Phys. Chem. C **115**, 21396–21401 (2011);
Ajisaka, Zunkovitz & Dubi, Sci. Rep. **5**, 8312 (2015).

Intro to Photosynthesis



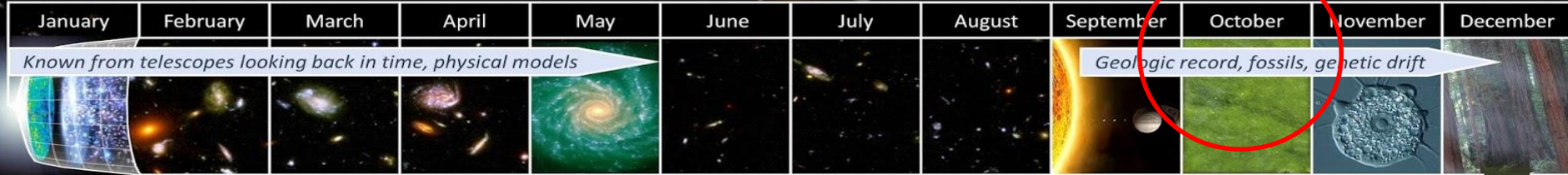
Phytoplankton – 50-85% of the oxygen on planet earth



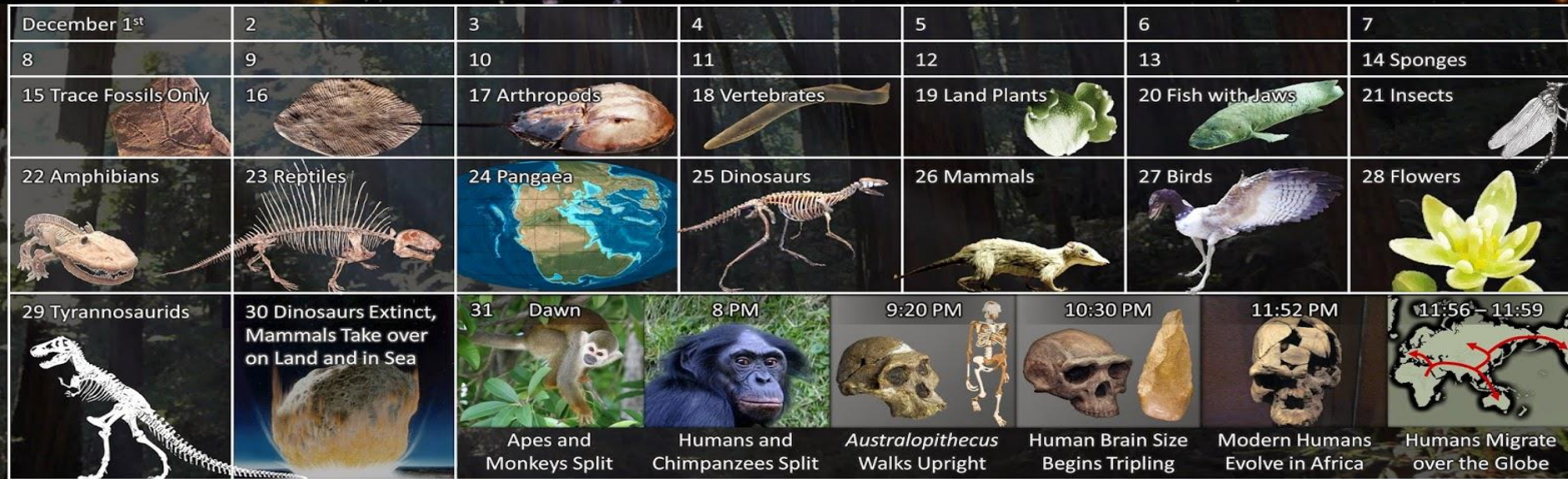
Intro to Photosynthesis

The Cosmic Calendar

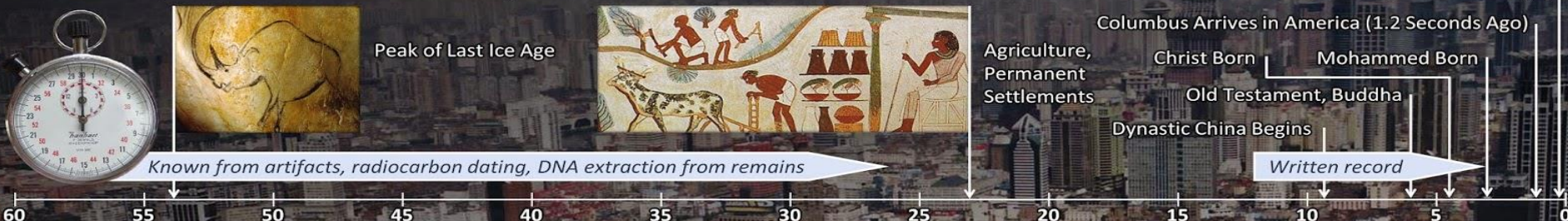
The 13.8 billion year history of the universe scaled down to a single year, where the Big Bang is January 1st at midnight, and right now is midnight 1 year later



The Big Bang, Stars Begin Fusing Elements The Milky Way Thin Disk Forms The Solar System, Life Oxygen from Photosynthesis Eukaryotic Cells



The final minute, where each cosmic second lasts 434 years



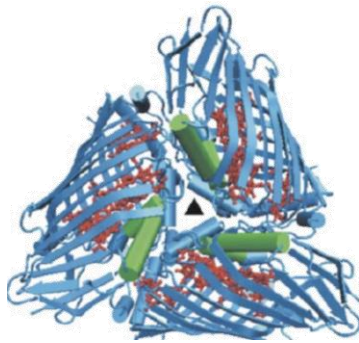
Intro to Photosynthesis

The “fruit-fly” of
photosynthesis –
the Green Sulfur Bacteria

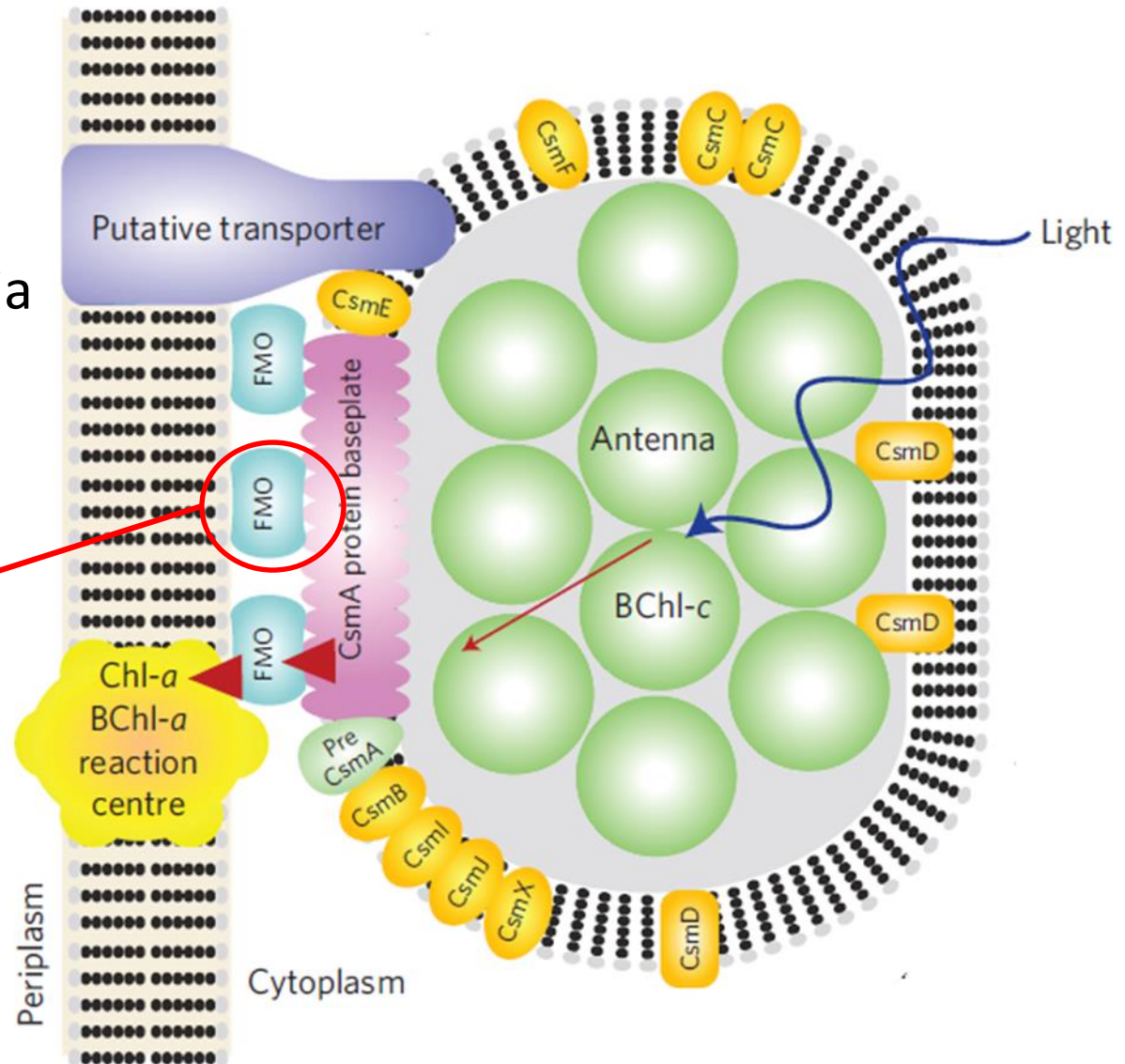


Intro to Photosynthesis

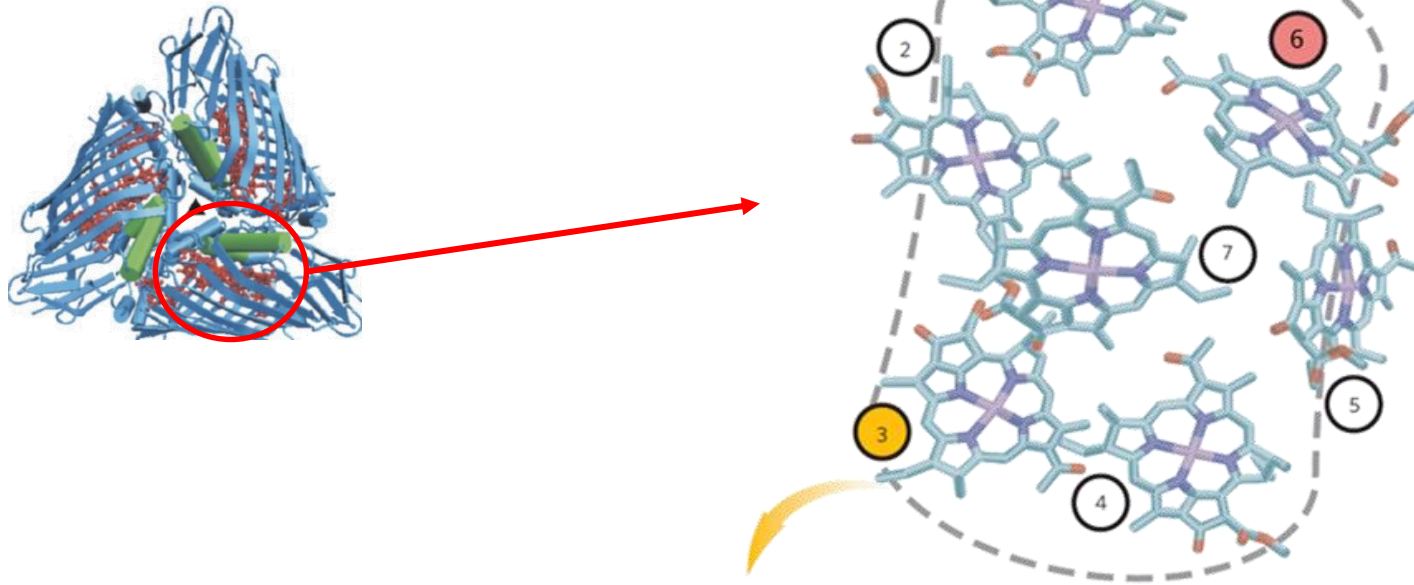
The “fruit-fly” of photosynthesis – the Green Sulfur Bacteria



Muh *et al.*, PNAS **104**, 16862 (2007)



Intro to Photosynthesis



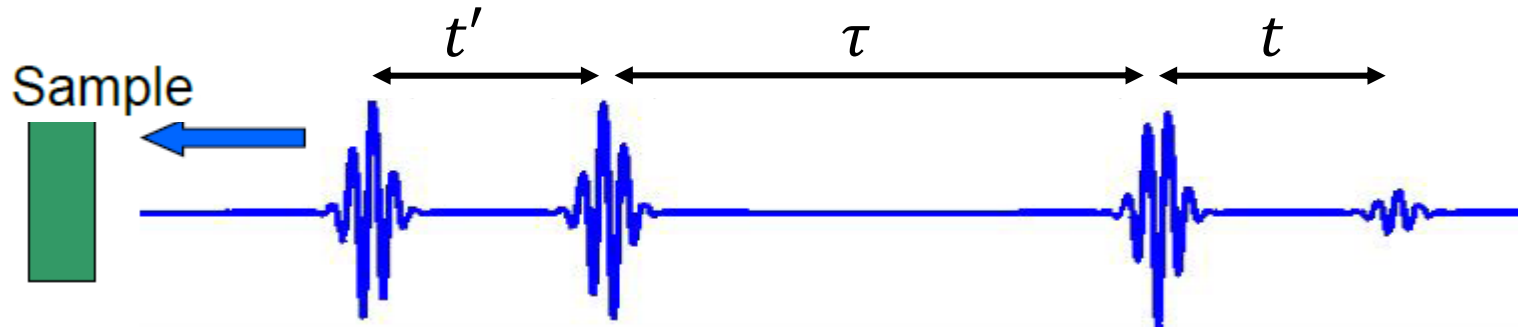
The system is well-characterized:

$$\mathcal{H} = \sum_{n=1}^7 \binom{8}{n} E_n |n\rangle\langle n| + \sum_{n,m} t_{nm} |n\rangle\langle m|,$$

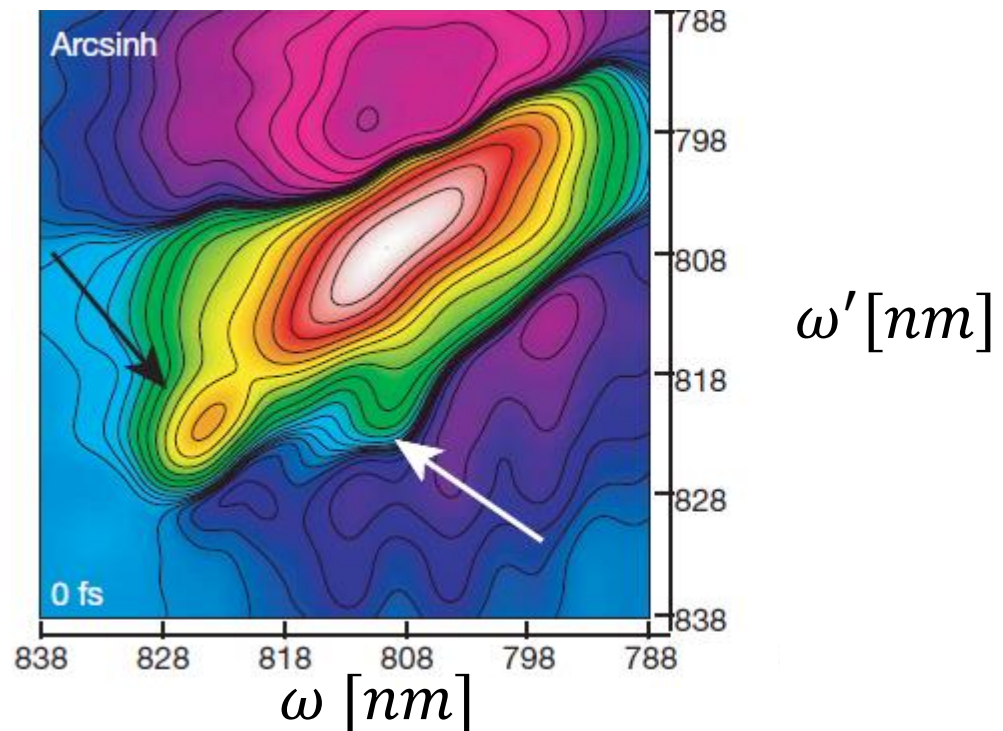
E_n, t_{nm} extracted from pump-probe experiments

Experiments revile Quantum Coherence

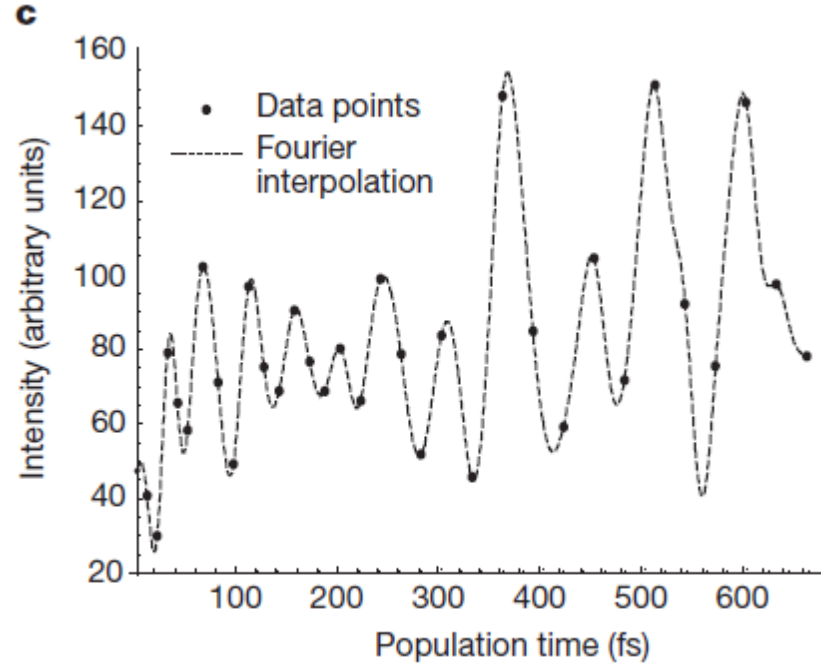
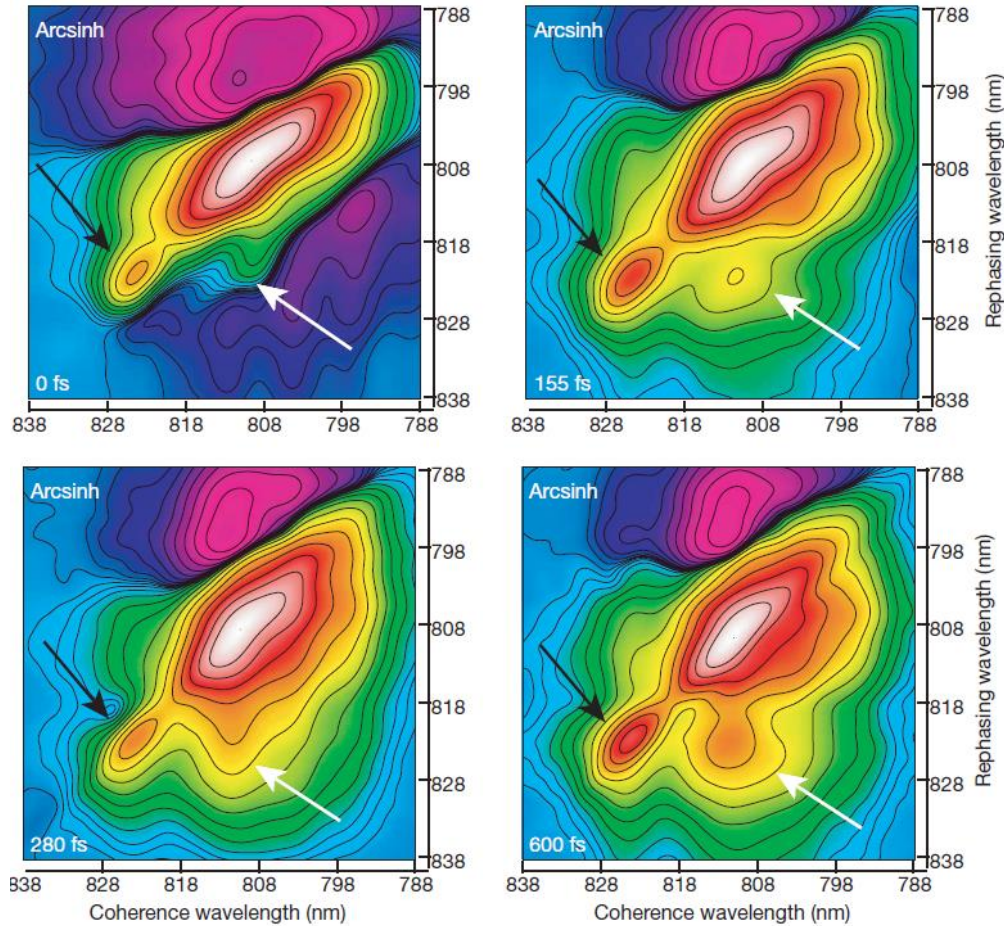
2D-Electronic Spectroscopy:



Fourier transform in t, t'



Experiments revile Quantum Coherence



Engel *et al.*, Nature **446**, 5678 (2007)

Quantum Coherence in Exciton Transfer Complexes (ETC):

1. Is it real?
2. How is coherence maintained in a “wet and floppy environment”?
3. Does nature *use* this coherence for ETC optimization?

(Optimization: Stability, Photoprotection, Efficiency)*

Theory of Quantum coherence in ETC – short intro

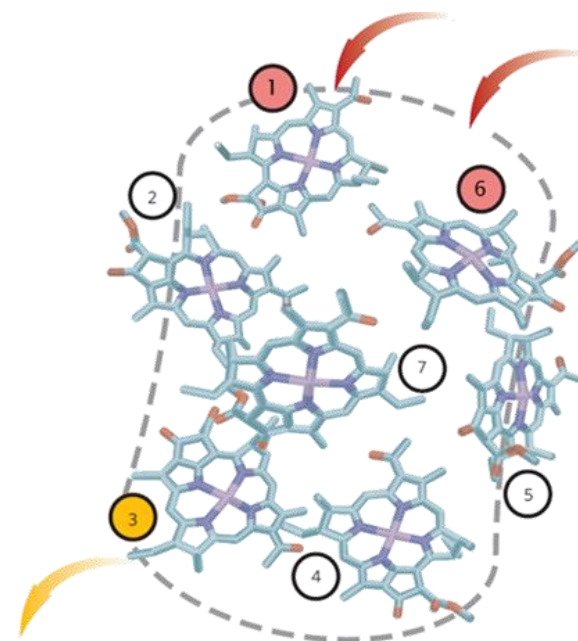
The general structure of theory in ETC analysis:

(i) Hamiltonian: $\mathcal{H}_{FMO} = \sum_{n=1}^{7(8)} E_n |n\rangle\langle n| + \sum_{n,m} t_{nm} |n\rangle\langle m|$

(ii) Environment: $\mathcal{H}_{env} = \sum_q \omega_q a_q^\dagger a_q$

(iii) Coupling: $\mathcal{H}_c = \sum_{n,q} \lambda_{n,q} (a_q^\dagger + a_q) e_n^\dagger e_n$

(iv) Spectral density $J(\omega) = \sum_q \lambda_q^2 \delta(\omega - \omega_q)$



Theory of Quantum coherence in ETC – short intro

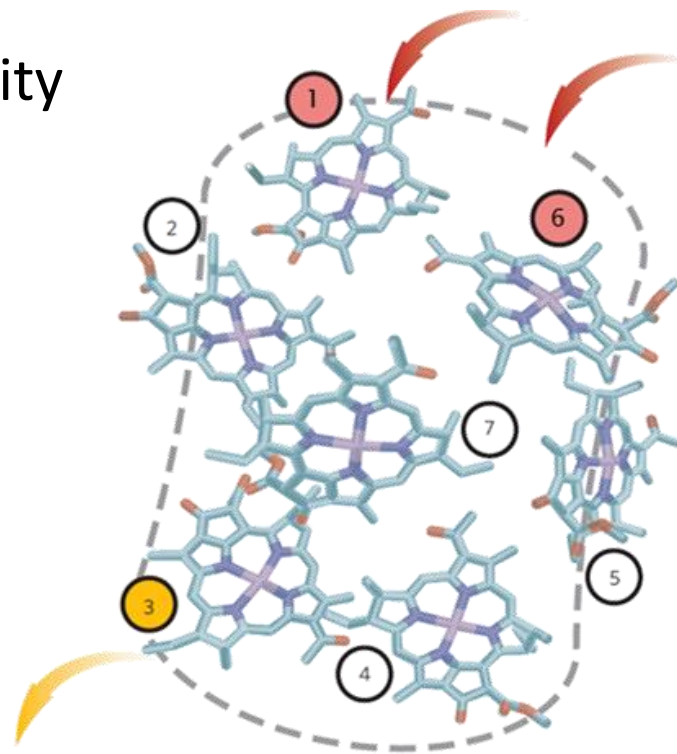
What to calculate? *Vast* majority: local density

1. Excite exciton at site 1 or 6 or both

2. Evaluate dynamics

(via density matrix, $\dot{\rho} = -i[\mathcal{H}, \rho] + \mathcal{L}\rho$)

3. Calculate exciton density at cite 3

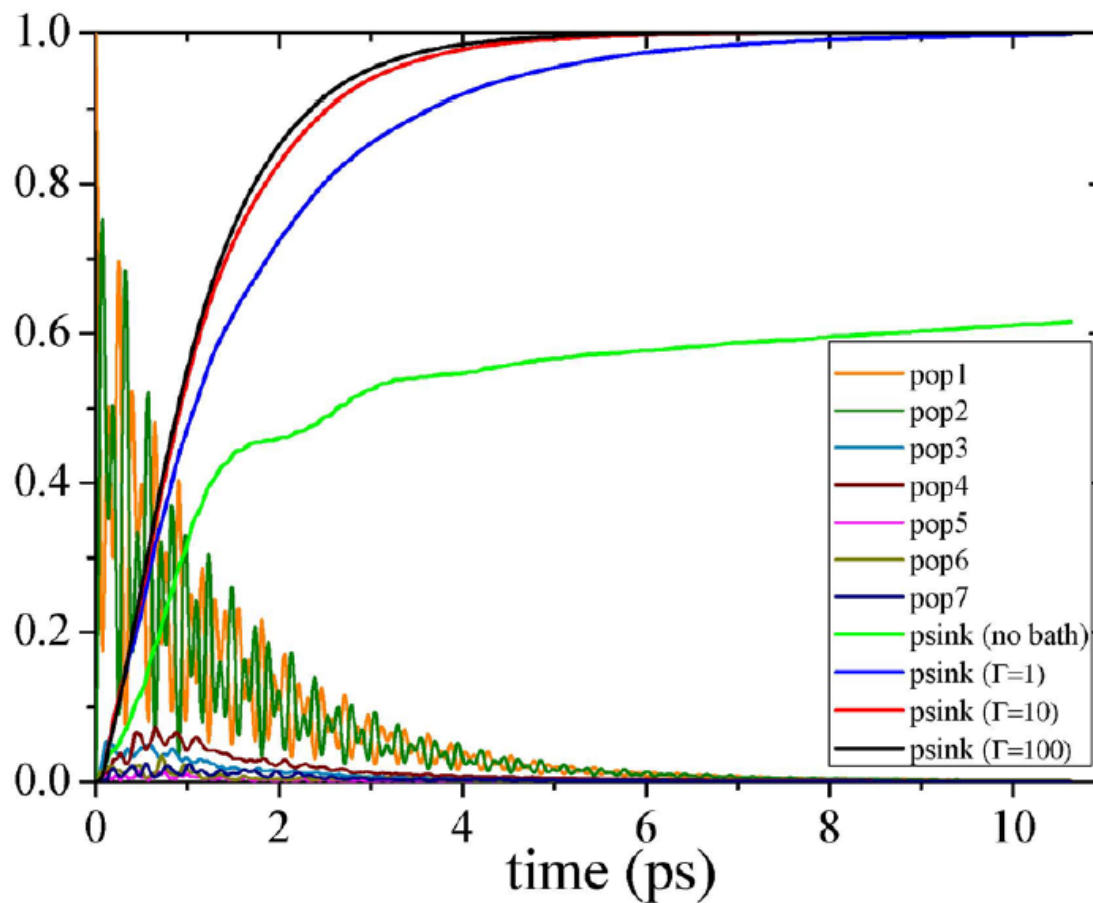


Efficiency is *defined* as :

$$\eta_3 = \gamma_3 \int_0^{\infty} \rho_{33}(t) dt$$

Theory of Quantum coherence in ETC – short intro

Typically looks something like this:



Theory of Quantum coherence in ETC – short intro

Efficiency is enhanced in the presence of dephasing

Plenio, M. B. and Huelga, S. F. *New Journal of Physics* **10**, 113019 (2008);

Rebentrost, P., Mohseni, M., Kassal, I., Lloyd, S.; Aspuru-Guzik, A., *New Journal of Physics* **11**, 033003 (2009).

(mechanism still unclear...)

Some Review:

Ishizaki & Fleming, *Annu. Rev. Condens. Matter Phys* (2012);

Huelga & Plenio, *Nature Phys.* (2014); Fleming, Huelga & Plenio, *New J. Phys.* (2011);

Collini, *Chem. Soc. Rev.* (2013); Scholes & Fleming, *Adv. Chem. Phys.* (2005);

Pachon & Brumer, *PCCP* (2012); Scholes, *Nat. Phys.* (2011);

Scholes & Smyth, *J. Chem. Phys.* (2014).

What can we add? (*aims*)

- How is the (standard) efficiency behaves?
- What is its relation to η_3 ?
- What is the *origin* for dephasing-enhanced efficiency?

- The ETC is an *energy-conversion* device
- Excitons (as opposed to electrons) do not carry charge:
Exciton current is not simply related to energy current!

Outline

Part I:

- Introduction – Quantum Biology?
- Motivation – optical experiments on photosynthetic complexes
- Quick review of current theory

Part II:

- Thinking about Power
- Interplay between performance, Geometry and Environment
- Summary & Conclusions

A *Heat-Current* approach to exciton transport

This approach:

- Takes into account the source (antenna) and sink (reaction center)
- Implies incoherent energy input
- Directly calculate Power output

A Heat-Current approach to exciton transport

Starting point: the full (many-body) FMO Hamiltonian

$$\mathcal{H}_{FMO} = \sum_{n=1}^7 E_n c_n^\dagger c_n + \sum_{n,m} t_{nm} c_n^\dagger c_m$$

Then use the Lindblad Equation

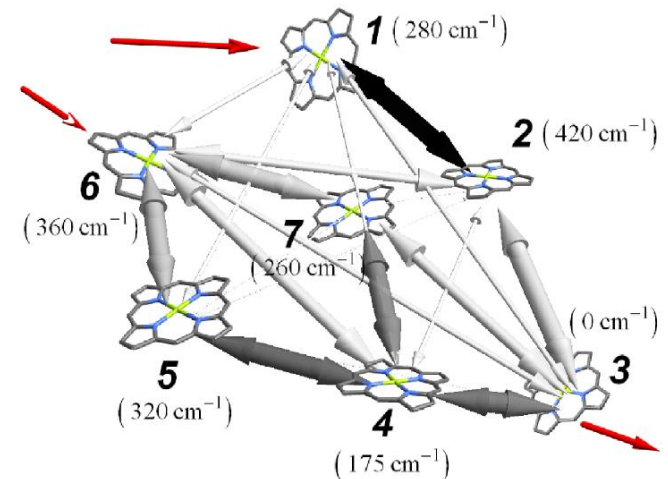
$$\dot{\rho}(t) = -\frac{i}{\hbar} [\mathcal{H}, \rho(t)] + \hat{\mathcal{L}}[\rho(t)],$$

$$\hat{\mathcal{L}}[\rho(t)] = \sum_i \left(-\frac{1}{2} \{V_i^\dagger V_i, \rho\} + V_i \rho V_i^\dagger \right)$$

Pros:

- Proper quantum equation
- Simple physical interpretation

Cons: Phenomenological, no memory



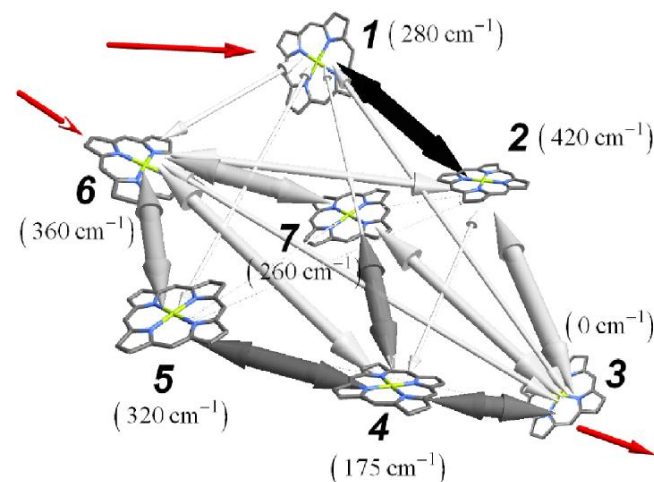
A Heat-Current approach to exciton transport

The V-operators encode different physical processes:

$$V_{deph} = \sqrt{\gamma_{deph}} c_n^\dagger c_n, \quad \gamma_{deph} = \tau_{deph}^{-1}$$

$$V_{in} = \sqrt{\gamma_{in}} c_1^\dagger, \sqrt{\gamma_{in}} c_6^\dagger,$$

$$V_{out} = \sqrt{\gamma_{out}} c_3$$



A Heat-Current approach to exciton transport

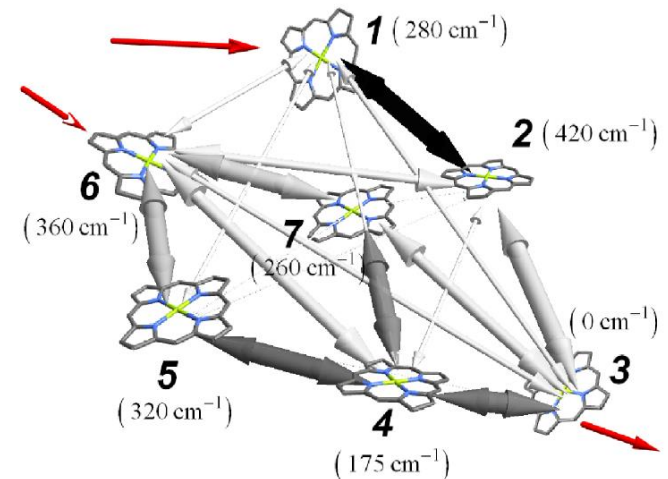
The properties of the system are determined from the *Steady state*:

$$\dot{\rho}_{\infty} = -\frac{i}{\hbar} [\mathcal{H}, \rho_{\infty}] + \hat{\mathcal{L}}[\rho_{\infty}] = 0$$

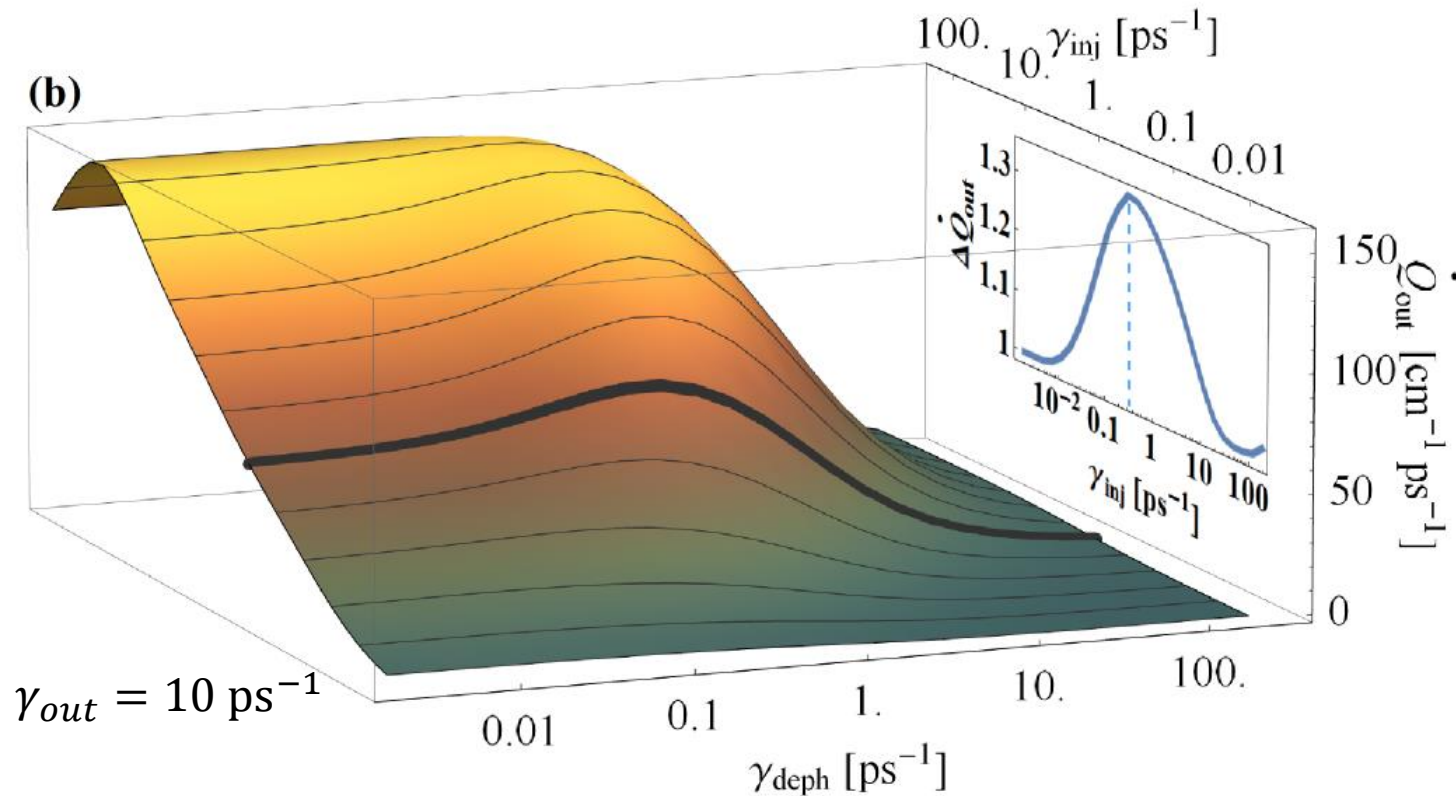
Heat currents can be calculated as:

$$\dot{Q}_{in} = Tr(-M_{source}\rho_{\infty}\mathcal{H})$$

$$\dot{Q}_{out} = Tr(-M_{sink}\rho_{\infty}\mathcal{H})$$

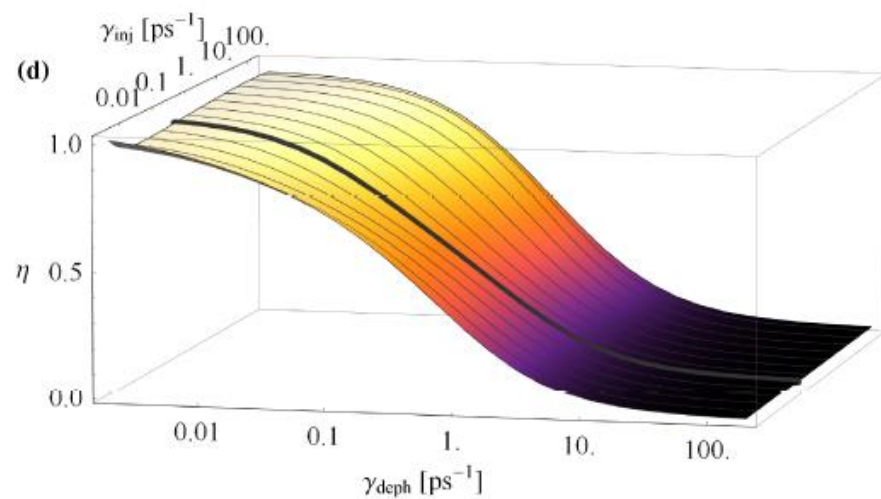
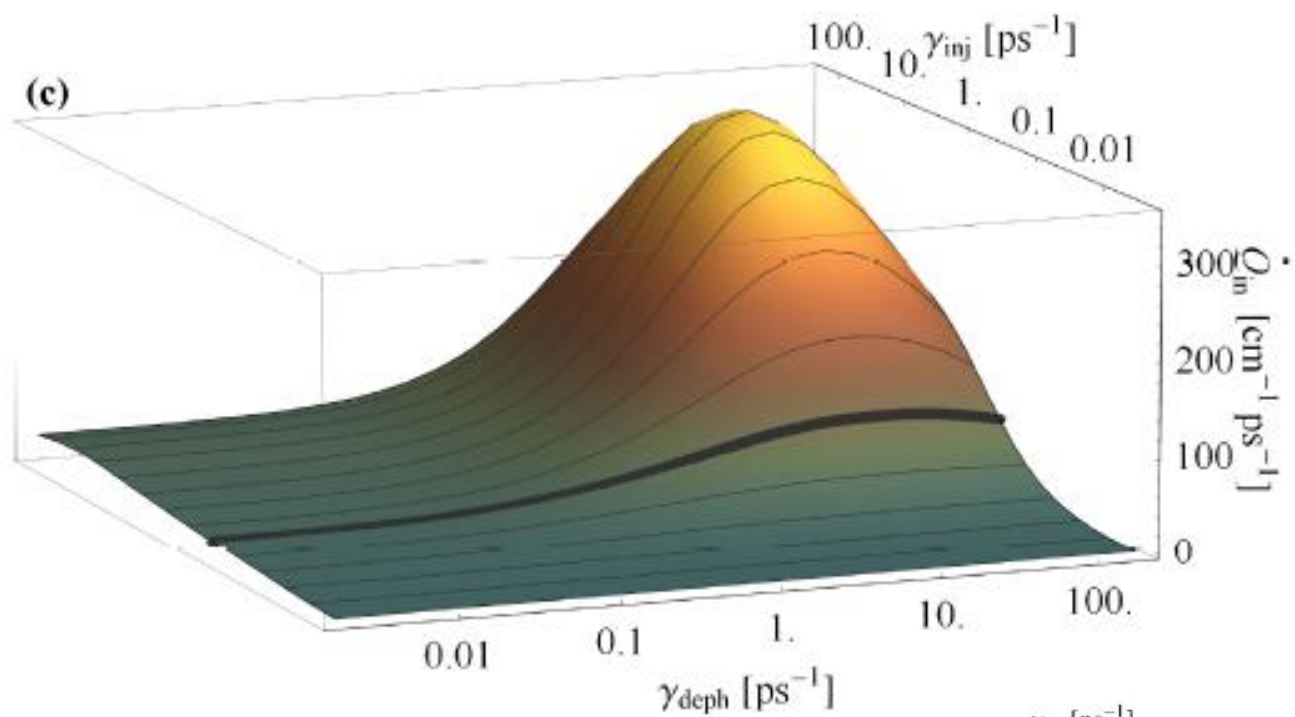


A Heat-Current approach to exciton transport



- Dephasing assists power output!
- Optimal rates $\gamma_{inj} \sim \gamma_{deph} \sim 0.5 \text{ ps}^{-1}$ (“Goldilocks” effect)

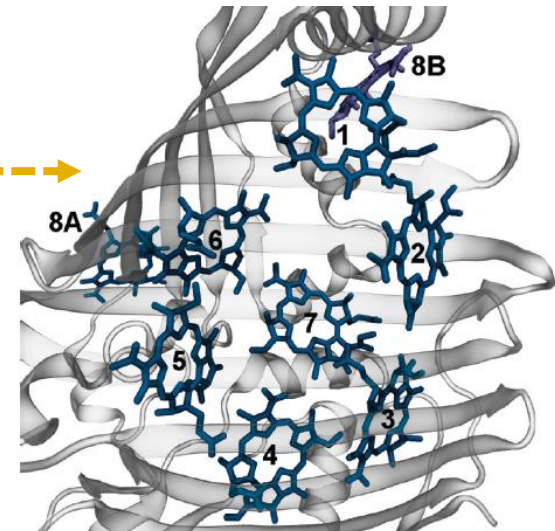
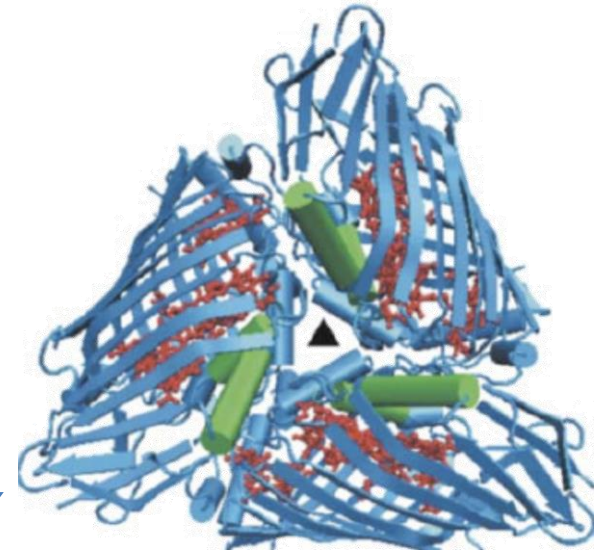
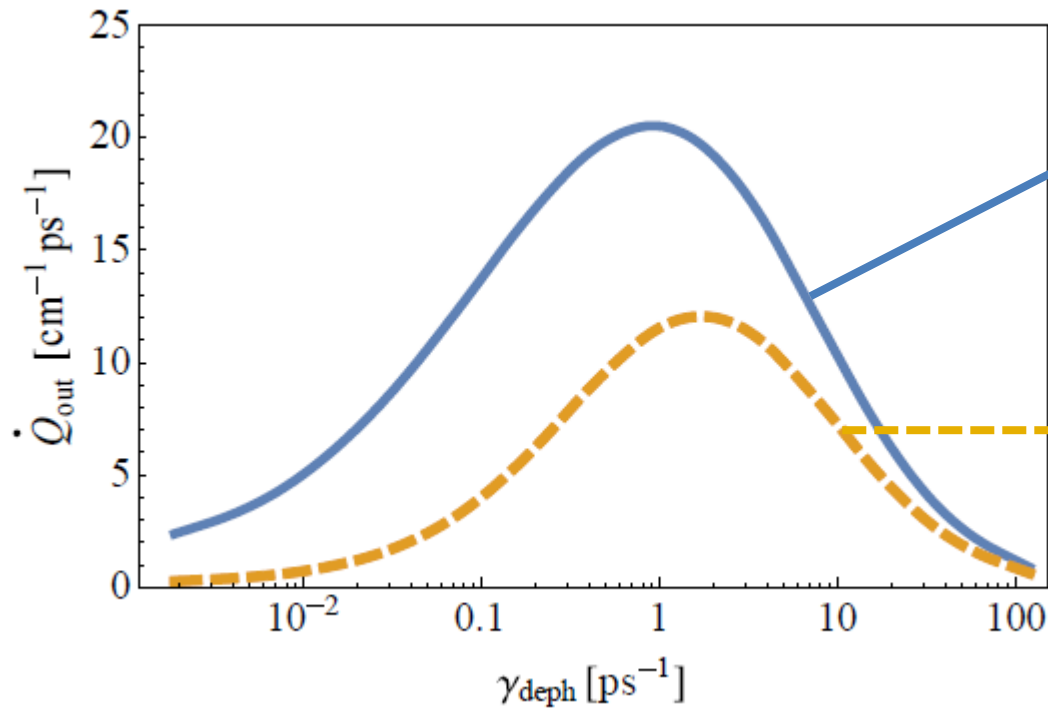
A Heat-Current approach to exciton transport



A Heat-Current approach to exciton transport

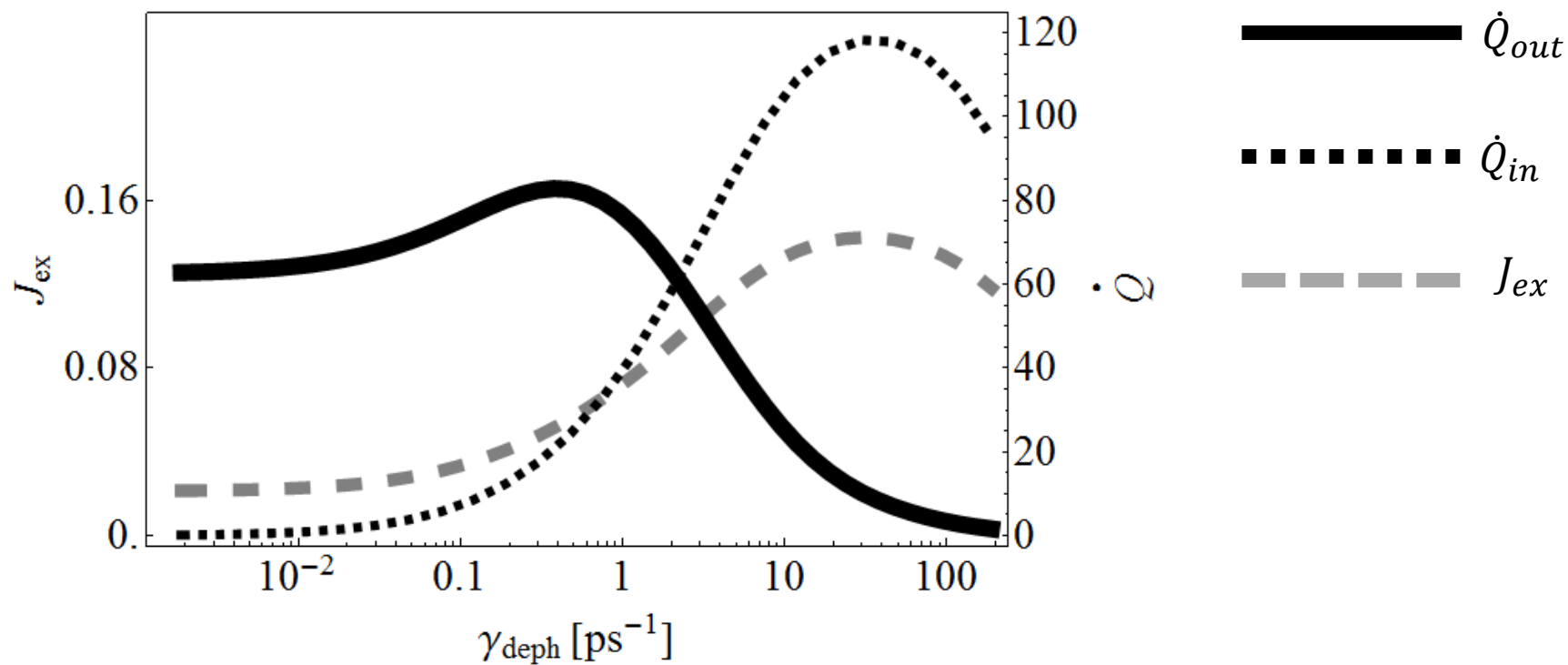
How general is this effect?

It holds for different geometries:



A Heat-Current approach to exciton transport

Heat current vs. *exciton current*:



Interplay between Geometry and Environment

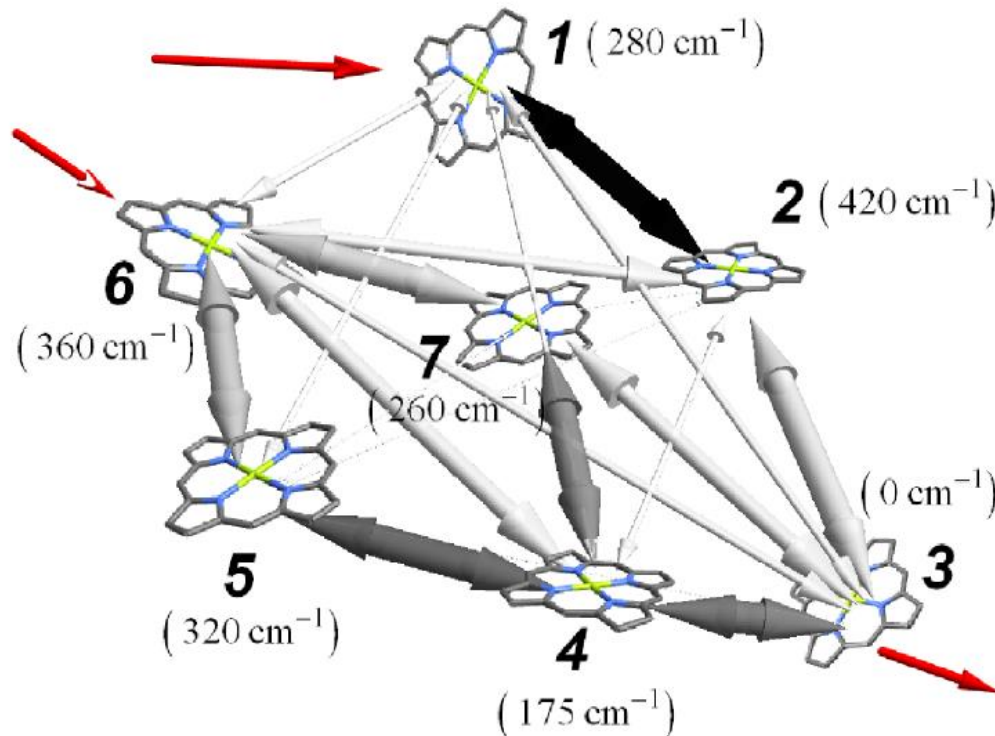
Dephasing-induced enhancement of power output:

- What is the origin for the excitonic effect?
 - delocalization (noise-induced level alignment)
 - Oscillation damping
 - Momentum rejuvenation (large lattices)
- Does (and how) it involve the Geometry of the network?

Interplay between Geometry and Environment

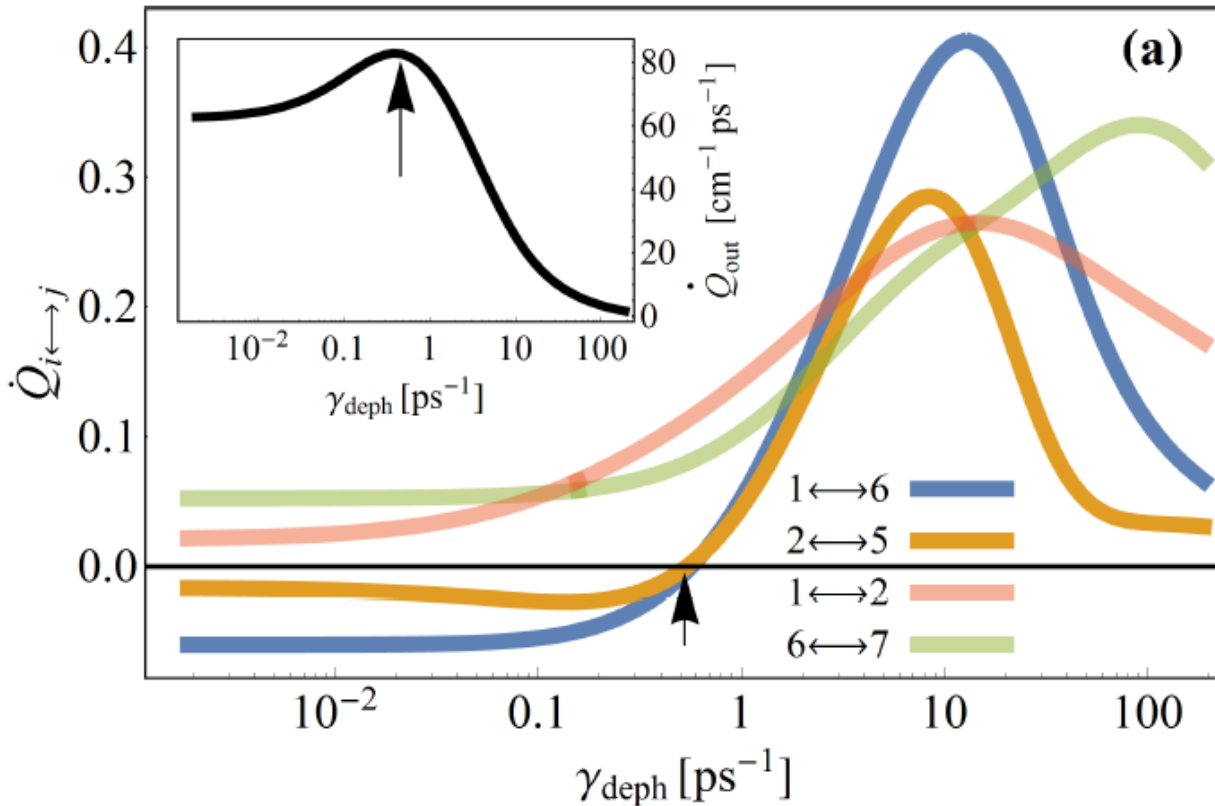
Calculating local heat currents:

$$\frac{d}{dt} \langle h_i \rangle = -i \text{Tr} ([h_i, \mathcal{H}] \rho_\infty) - \text{Tr} (h_i \hat{M} \rho_\infty) = \sum_j \dot{Q}_{i \leftrightarrow j}$$

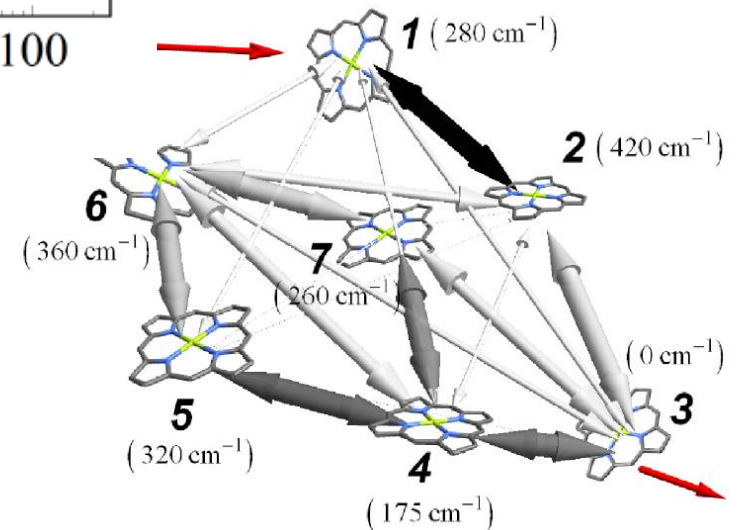


Wu & Segal., *J. Phys. A: Math. Theor.* **2009**, 42, 025302

Interplay between Geometry and Environment

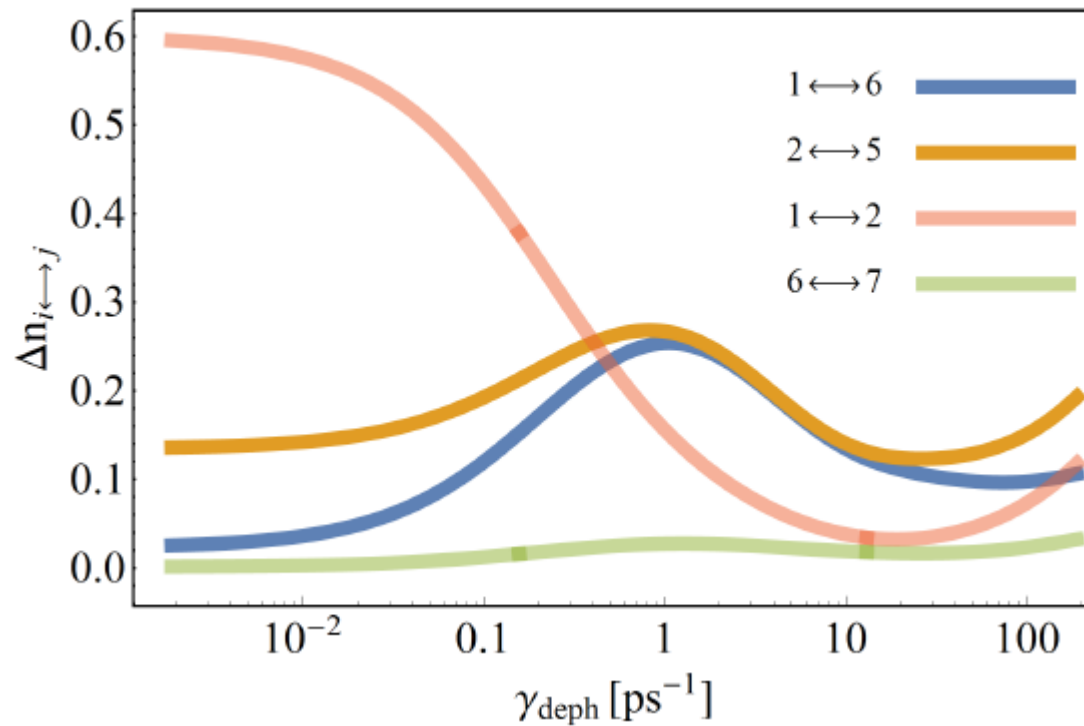


- “inter-branch” heat current vanishes at optimal dephasing!
- ...but “intra-branch” does not

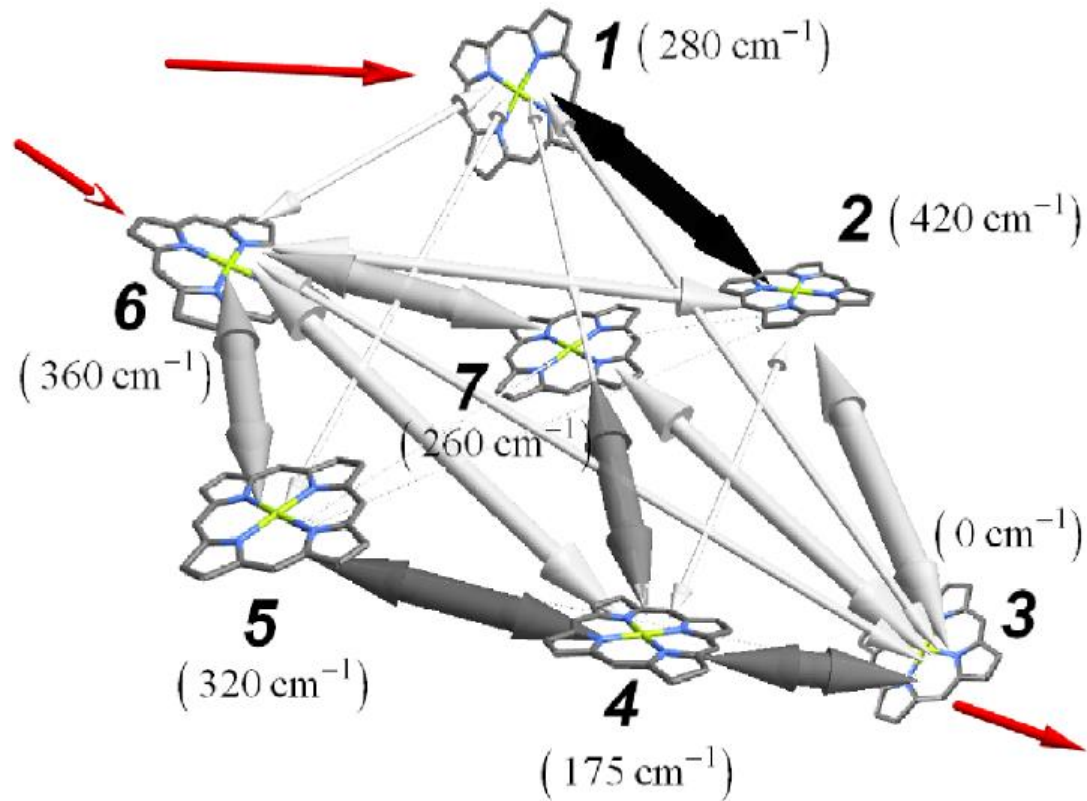


Interplay between Geometry and Environment

Immediate suspect: density differences - not the origin

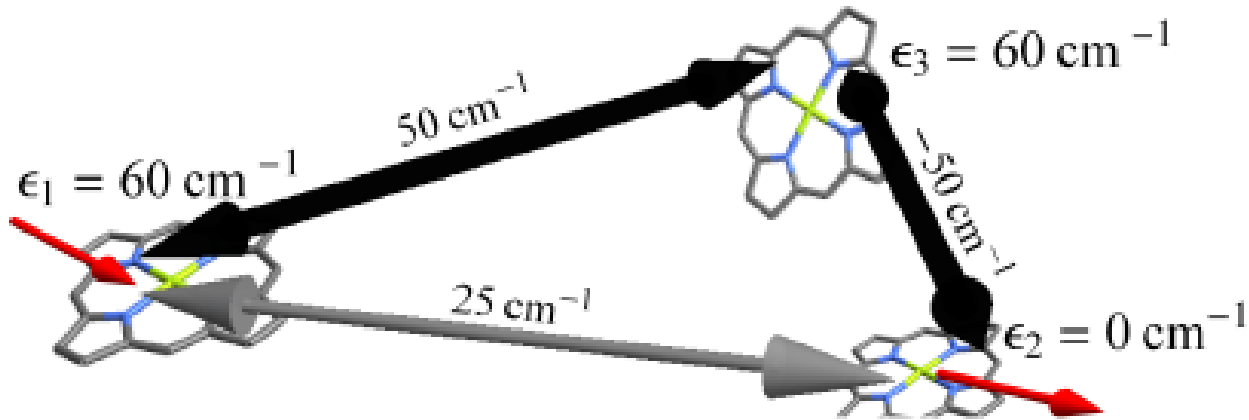


Directed Heat Flow



Directed Heat Flow

An analytically soluble minimal model:

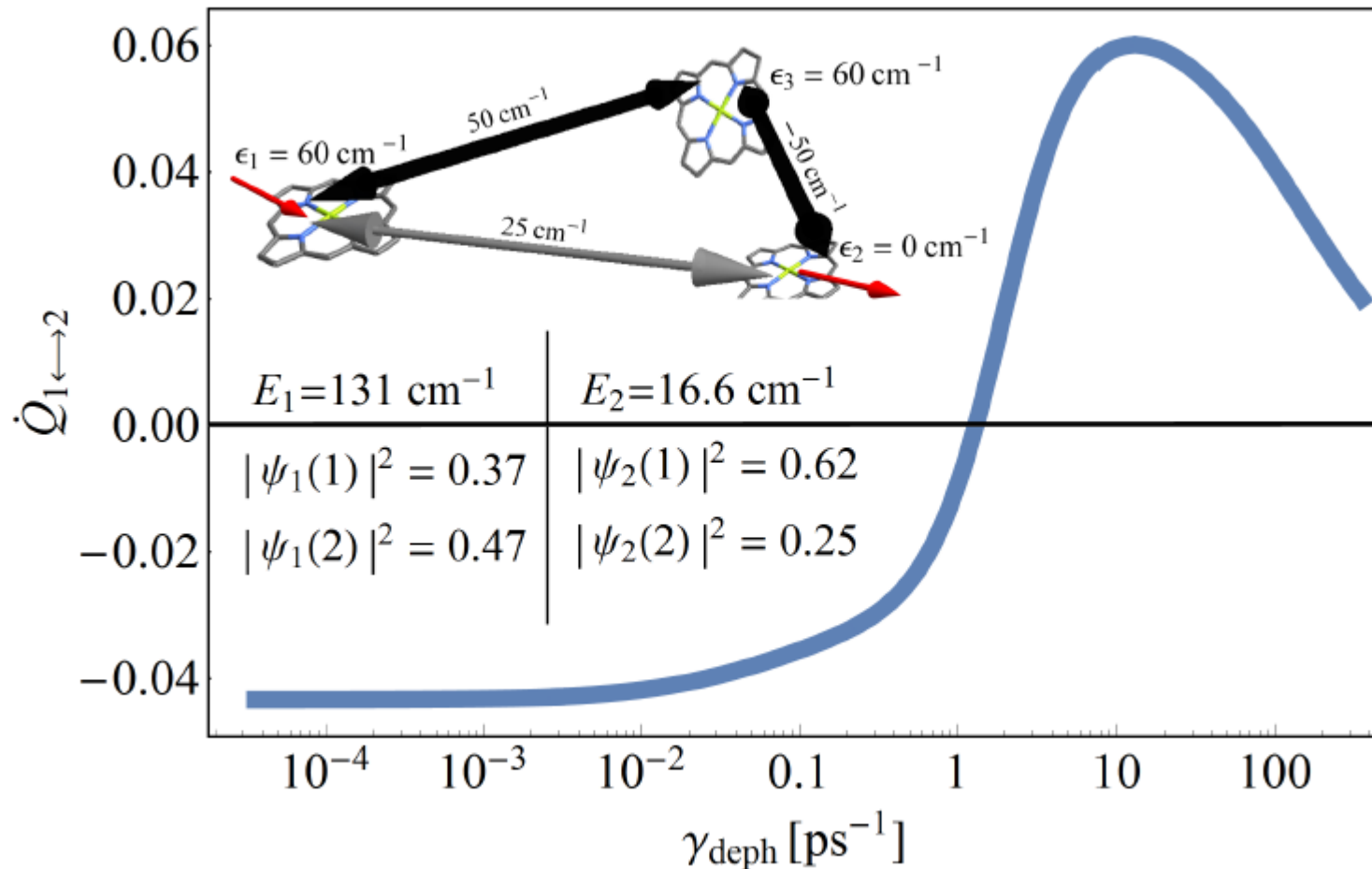


Vanishing dephasing limit: $\dot{Q}_{1\leftrightarrow 2} \approx -\frac{t_0 \gamma (\epsilon_1 - \epsilon_2) (\epsilon_1 - \epsilon_2 + t_0)}{(\epsilon_1 - \epsilon_2 + t_0)^2 + 6 t_0^2}$

Strong dephasing limit: $\dot{Q}_{1\leftrightarrow 2} \approx \frac{t_0 (\epsilon_1 - \epsilon_2)}{\gamma_{deph}}$

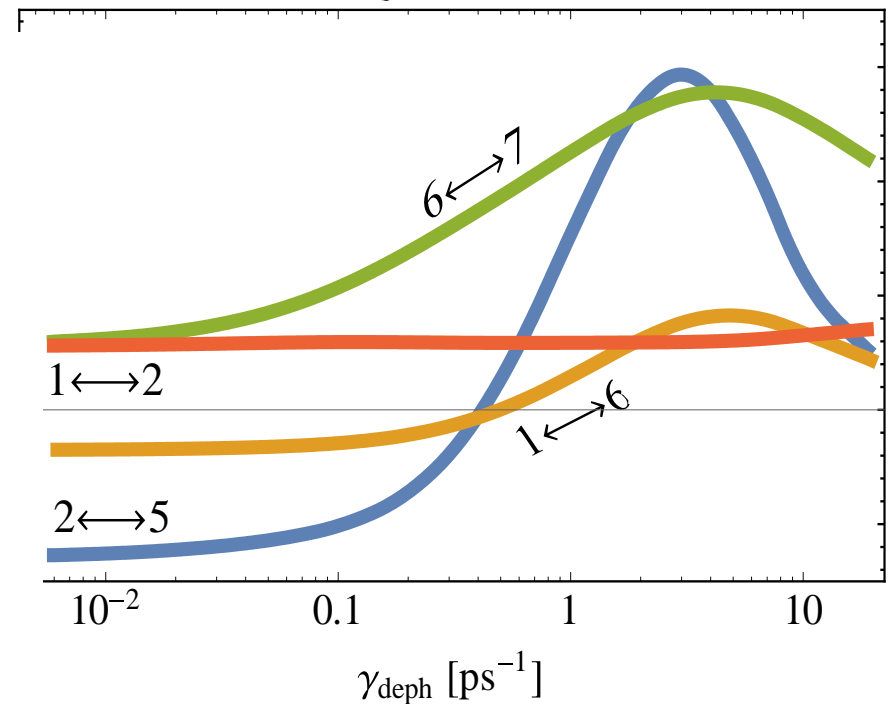
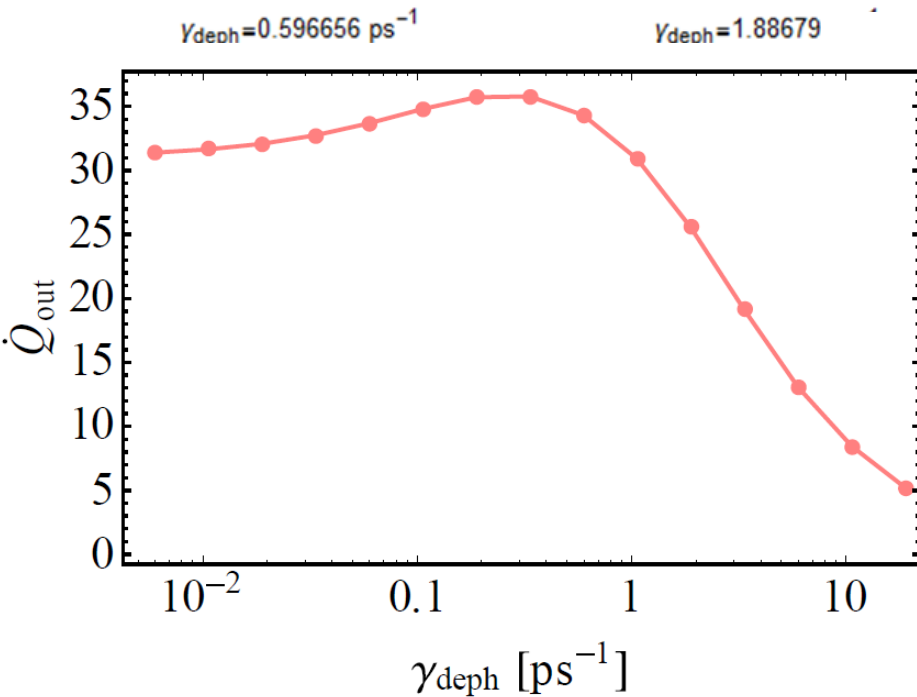
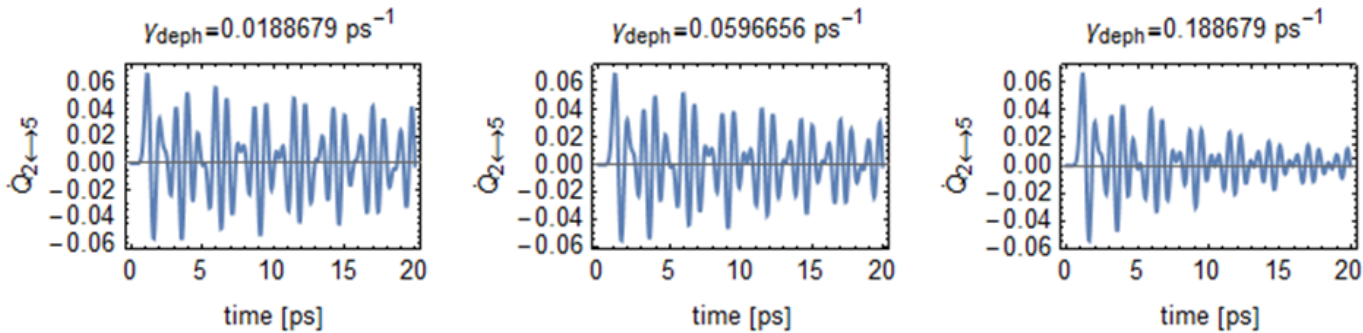
Directed Heat Flow

An analytically soluble minimal model:



Directed Heat Flow

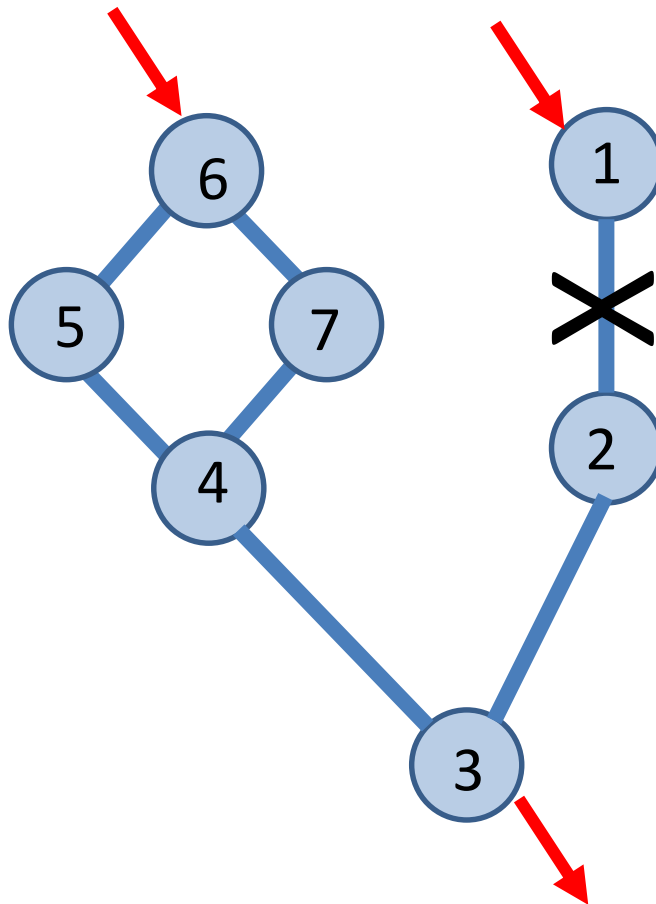
The mechanism works even for pulse-excitation:



Dephasing & Durability

Up till now: analysis driven by power output

The biologists' intuition: its all about ***stability*** and ***Durability***

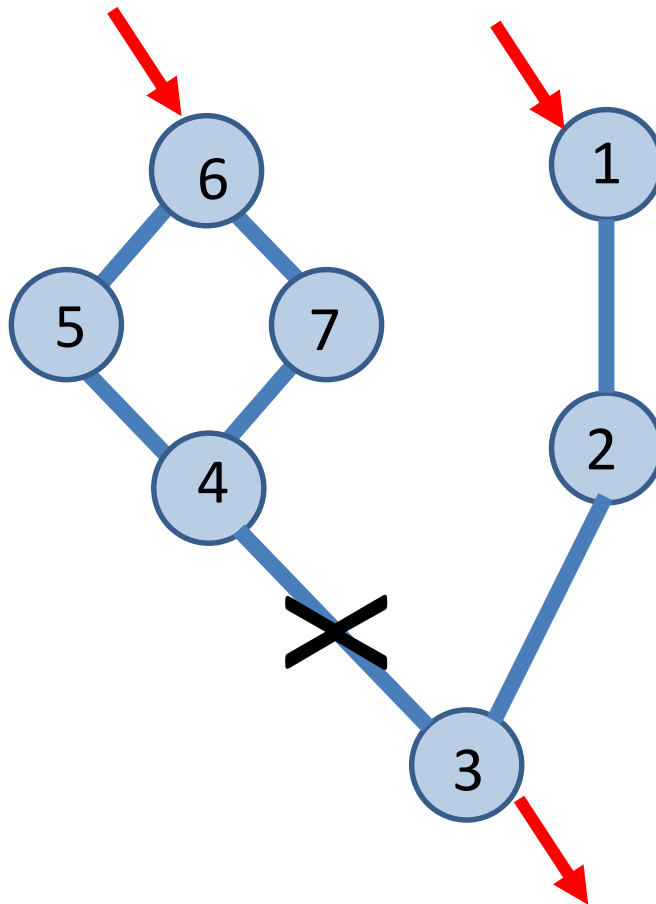


$$R_{1 \leftrightarrow 2} = \frac{\dot{Q}_{out}(no\ link)}{\dot{Q}_{out}}$$

Dephasing & Durability

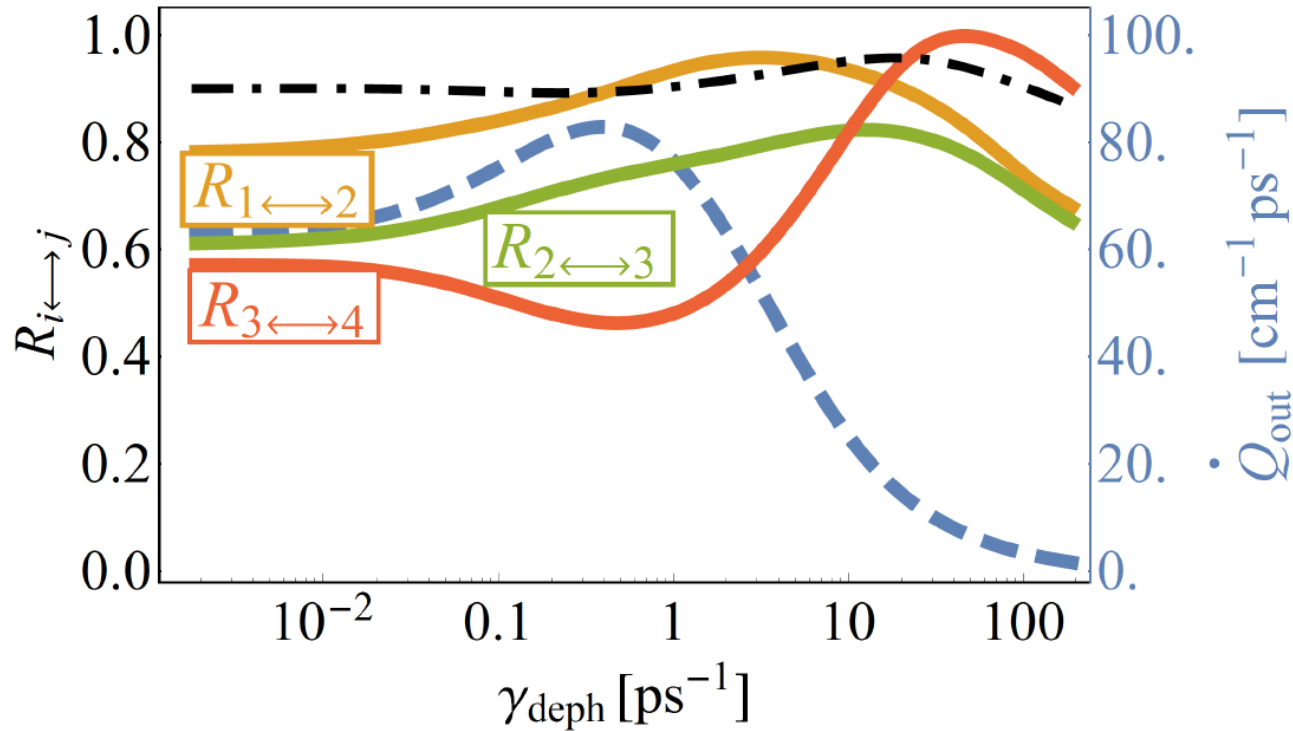
Up till now: analysis driven by power output

The biologists' intuition: its all about ***stability*** and ***Durability***



$$R_{3 \leftrightarrow 4} = \frac{\dot{Q}_{out}(no\ link)}{\dot{Q}_{out}}$$

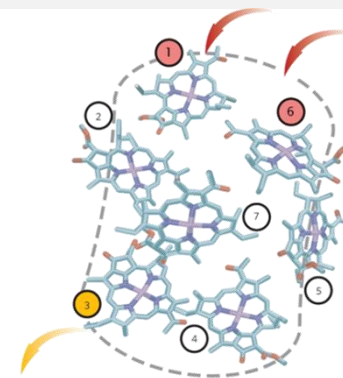
Dephasing & Durability



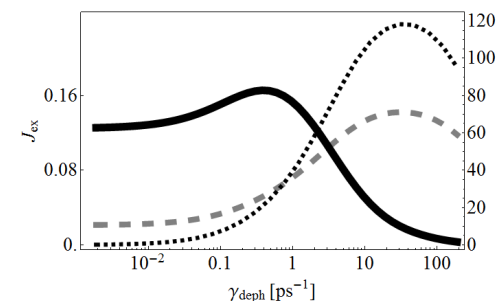
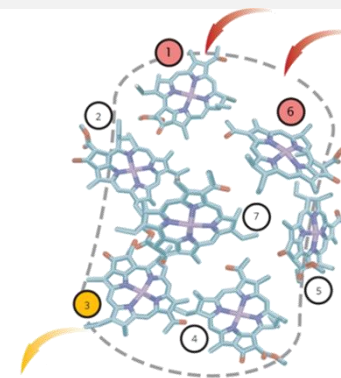
Conclusion: dephasing does not assist durability

Hypothesis: the two-branch structure developed to aid durability. The “right amount” of dephasing evolved to optimize power output, **given the two-branch structure.**

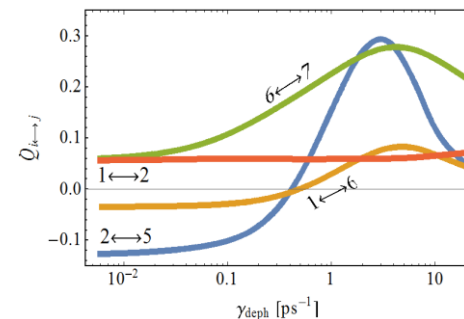
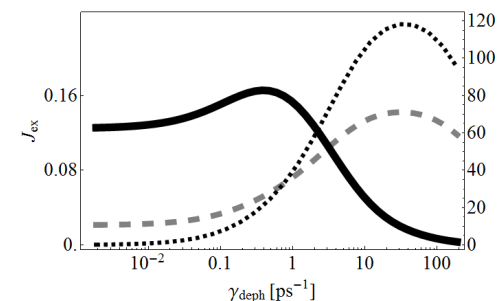
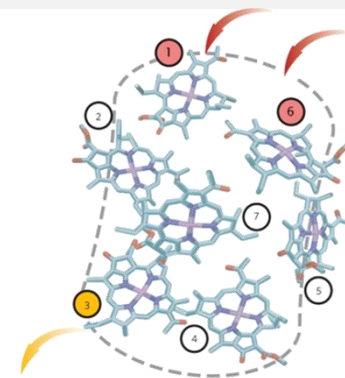
- A new approach to excitonic energy transfer:
Calculating heat currents



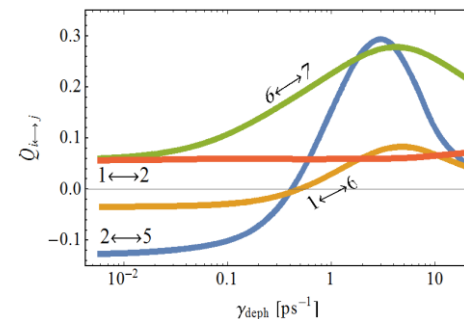
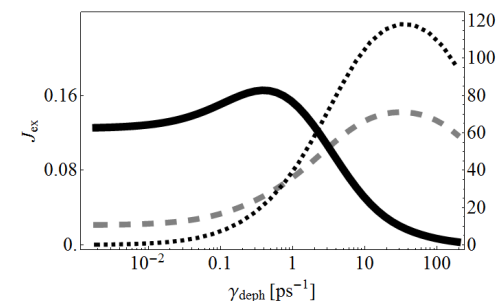
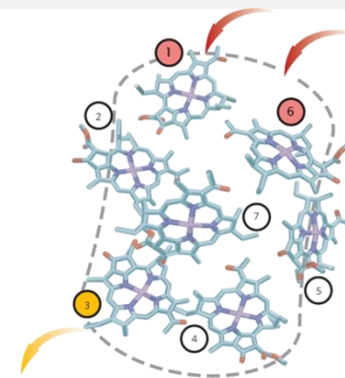
- A new approach to excitonic energy transfer:
Calculating heat currents
- There is an optimal dephasing time for which **power output is maximal**



- A new approach to excitonic energy transfer:
Calculating heat currents
- There is an optimal dephasing time for which **power output is maximal**
- This is due to *Directed Heat Flow*:
the interplay between classical and quantum heat currents forces heat to flow along the branches



- A new approach to excitonic energy transfer:
Calculating heat currents
- There is an optimal dephasing time for which **power output is maximal**
- This is due to *Directed Heat Flow*:
the interplay between classical and quantum heat currents forces heat to flow along the branches



Thank you for our attention...

&

Thanks to the organizers...