

Quantum fluids of light in semiconductor microcavities

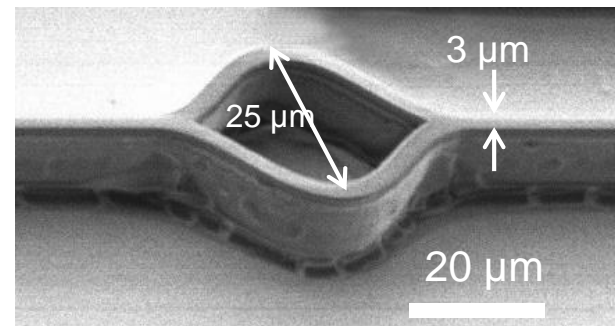
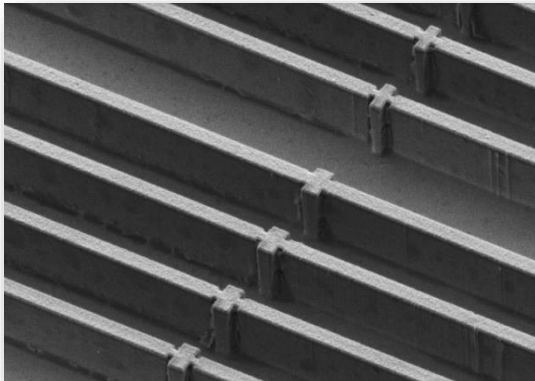
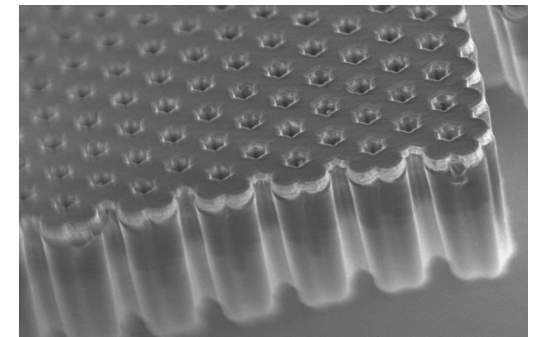
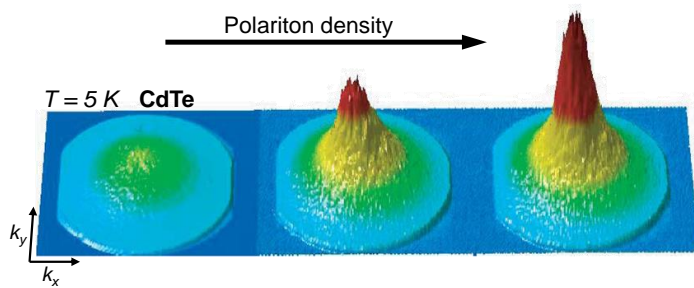
Jacqueline Bloch

Centre de Nanosciences et de Nanotechnologies

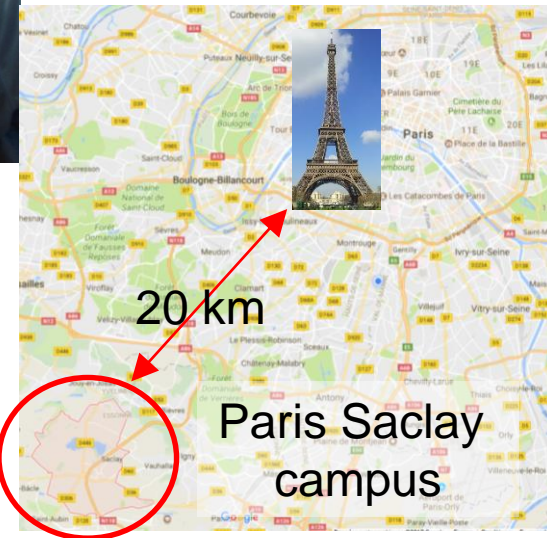
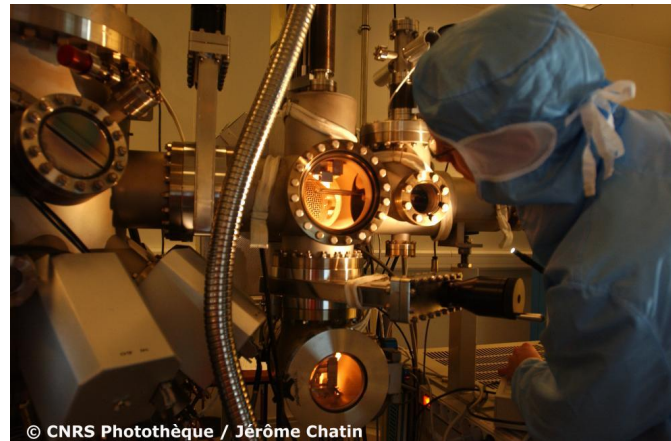
C2N

CNRS/ Université Paris Sud / Université Paris Saclay

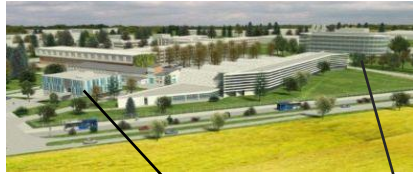
France



A new laboratory: C2N



New Academic Buildings at Campus Paris – Saclay



**Doseo
2014**

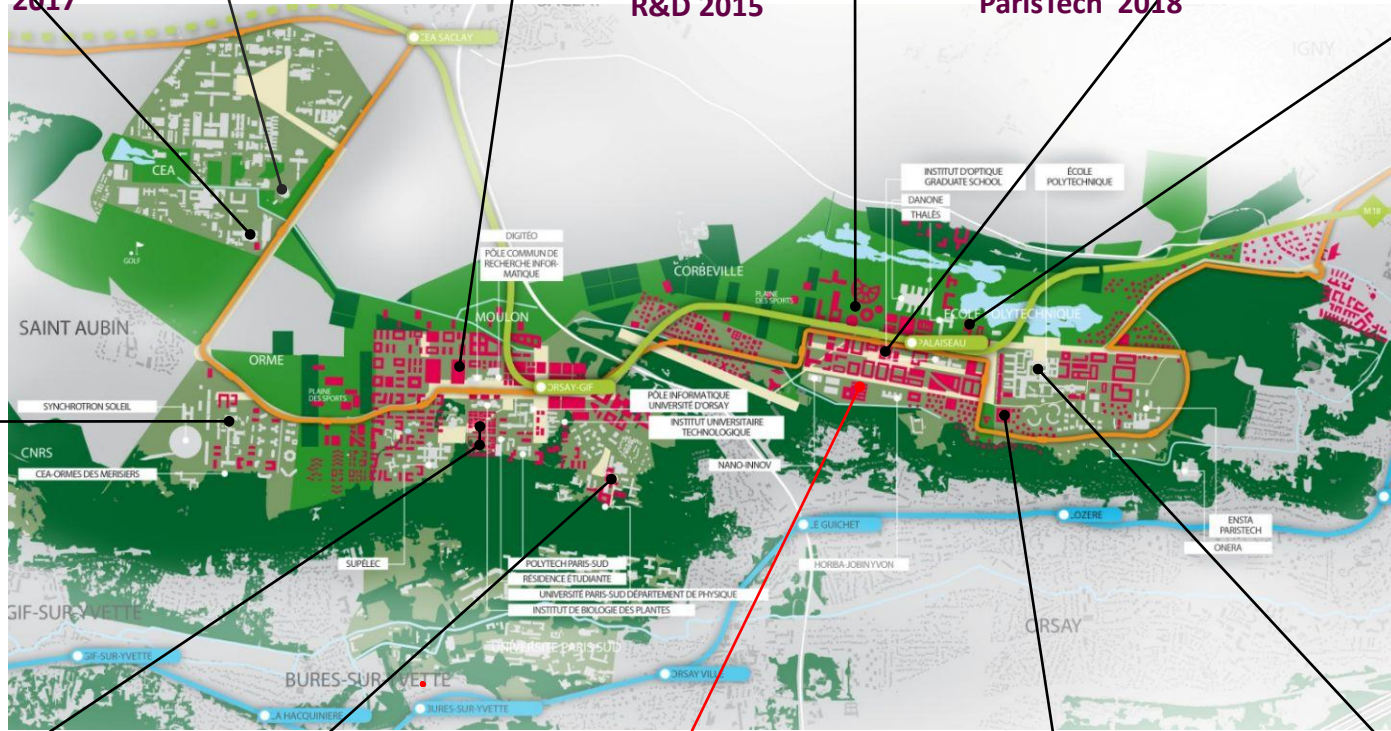
**Neuro Sciences
2017**

ENS Cachan 2018

**EDF Campus and
R&D 2015**

**Mines-Telecom
ParisTech 2018**

Digiteo2 2015



- On-going projects
- Existing buildings
- Grand Paris subway
- RER B
- Bus



Cilex 2017



**Ecole Centrale Paris
2013**



**Institut des Sciences
Moléculaires 2014**



C2N 2017

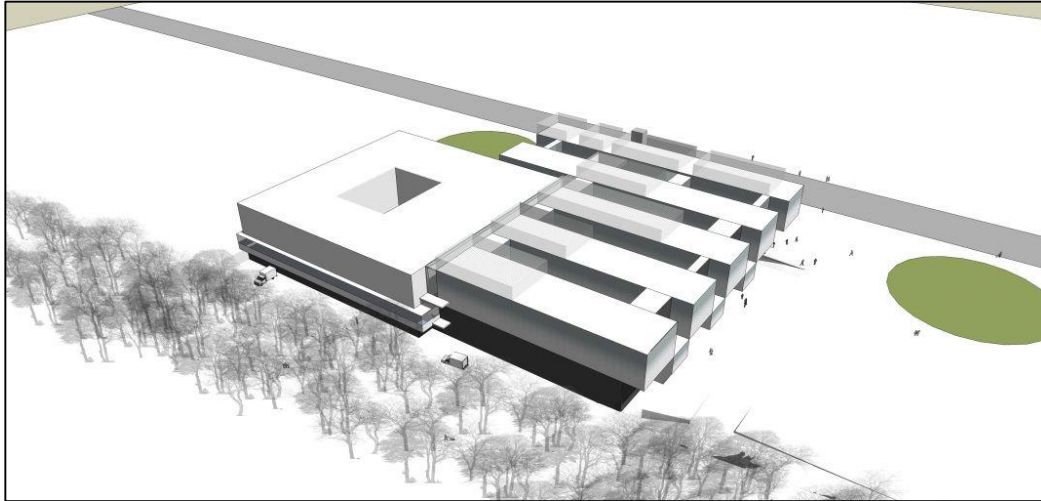


**ENSAE ParisTech
2016**



**Laboratoires
Polytechnique 2015**

C2N by numbers



~ **450** researchers, post-doc, PhD students,
engineers, technicians, administrative staff

4 Departments:

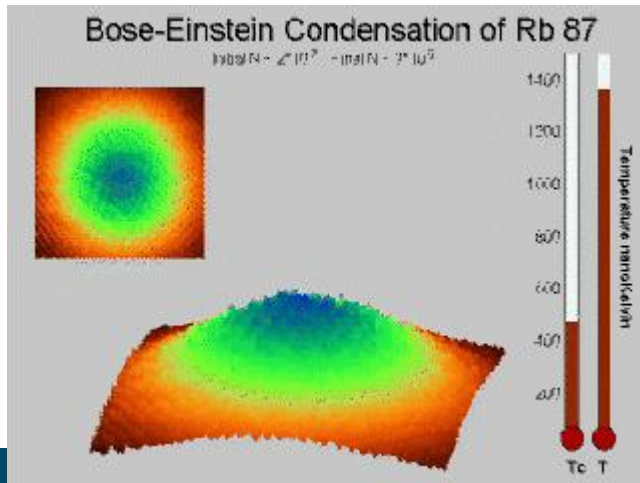
Photonics, Nanoelectronics,
Microsystems & NanoBioFluidics, Materials

2,800 m² high-class clean-room facility



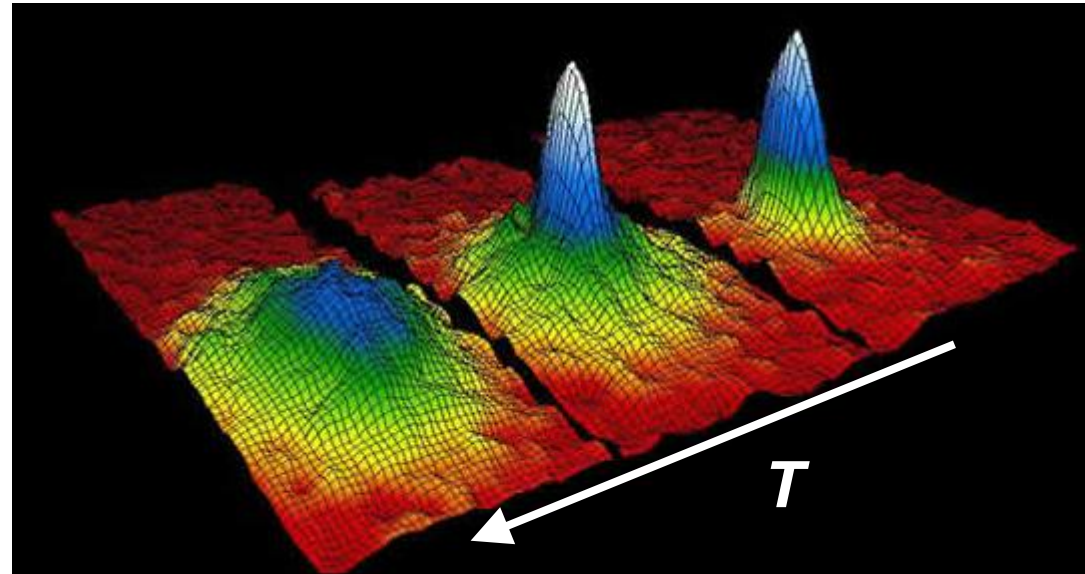
New physical systems appearing in the 1990's

Bose Einstein Condensation in atoms



Macroscopic wavefunction

$$\lambda_T = \left(\frac{2\pi\hbar^2}{mk_B T} \right)^{\frac{1}{2}}$$



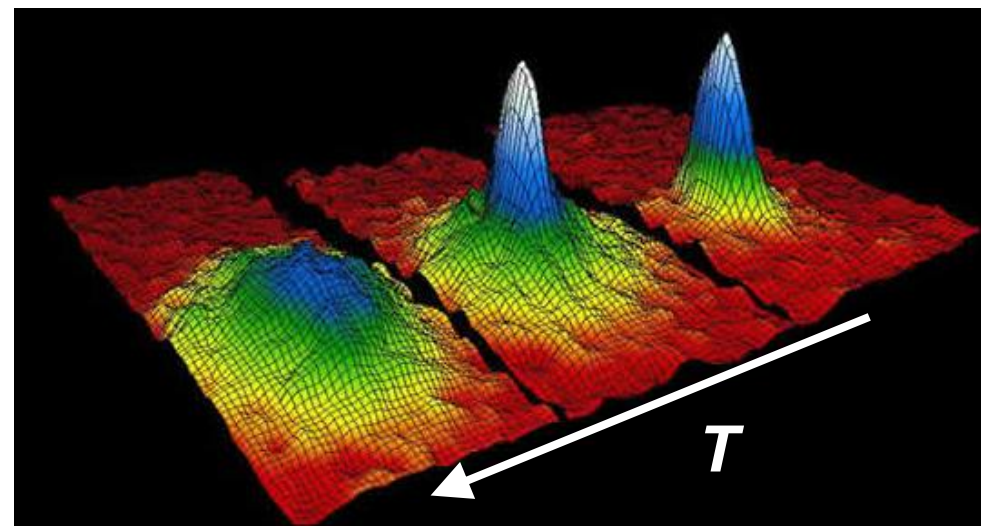
Cornell and Wieman's groups :
condensation of Rb atoms (1995)

- $m = 10^4 m_e$
- $T_c = 200$ nK

<http://jilawwww.colorado.edu/bec/>

New physical systems appearing in the 1990's

Atomic condensates



<http://jilawww.colorado.edu/bec/>

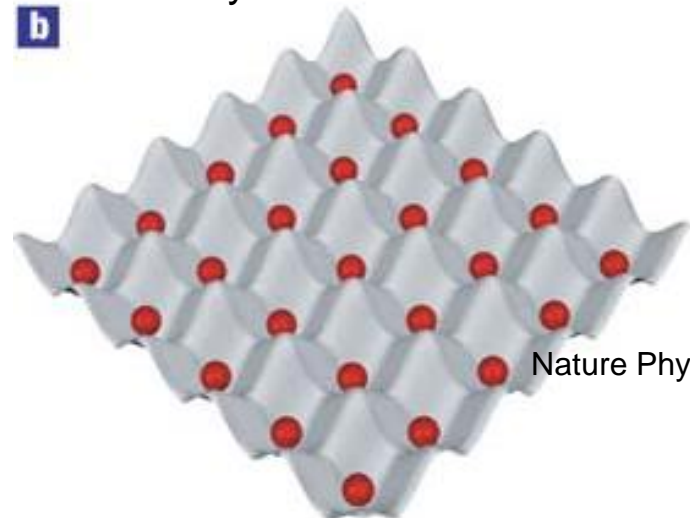
Cornell and Wieman's groups :
condensation of Rb atoms (1995)

- $m = 10^4 m_e$
- $T_c = 200 \text{ nK}$

- Atom laser
- Superfluidity
- Vortex lattices
- Insulator-superfluid transition
- Anderson localisation
- Artificial gauge fields

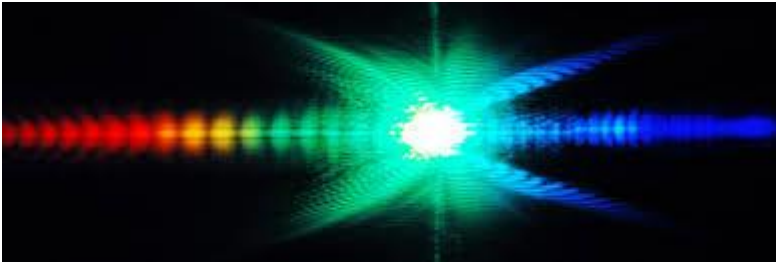
Quantum simulators

*Fabricate the Hamiltonian
of system difficult to access*



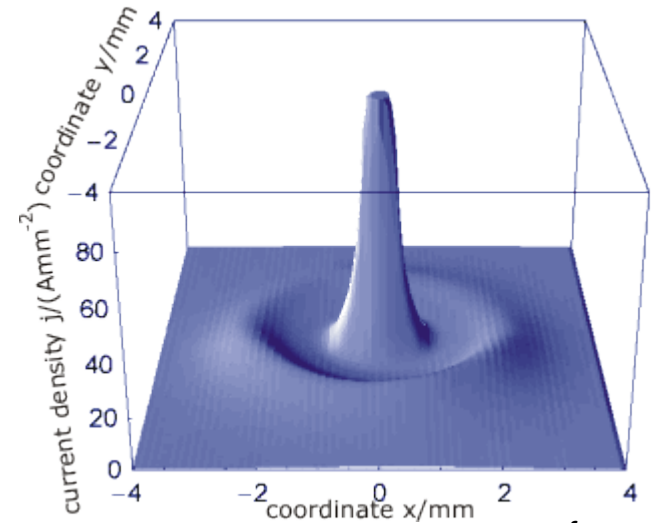
I. Bloch et al.
Nature Physics 1, 23 (2005)

New physical systems appearing in the 1990's



- Spatial and temporal solitons
- Fiber solitons
- Non-linear waveguide arrays
- Bi-stability
- Optical parametric oscillation
- Parametric down-conversion
- Photon quantum state manipulation
- ...

Non-linear optics



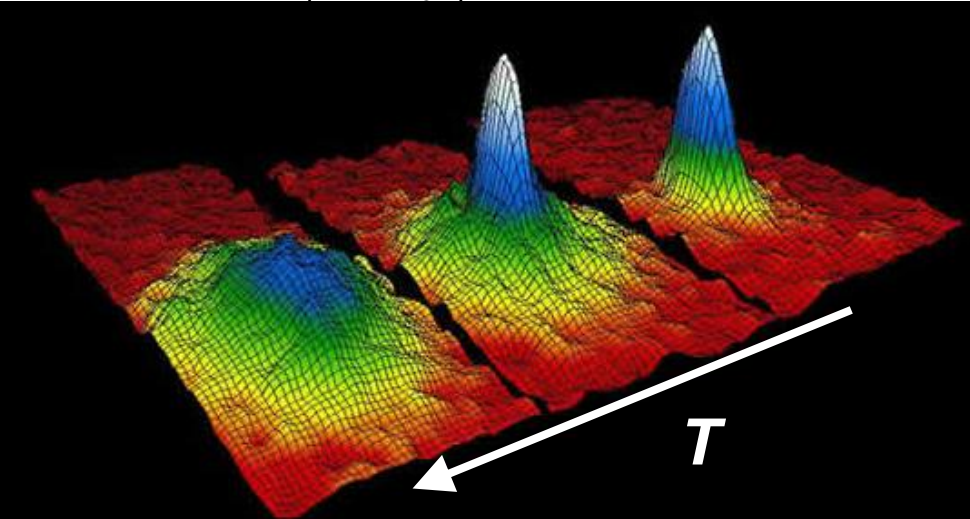
from wikipedia

Development of non-linear optical media $\chi^{(2)}$, $\chi^{(3)}$

New physical systems appearing in the 1990's

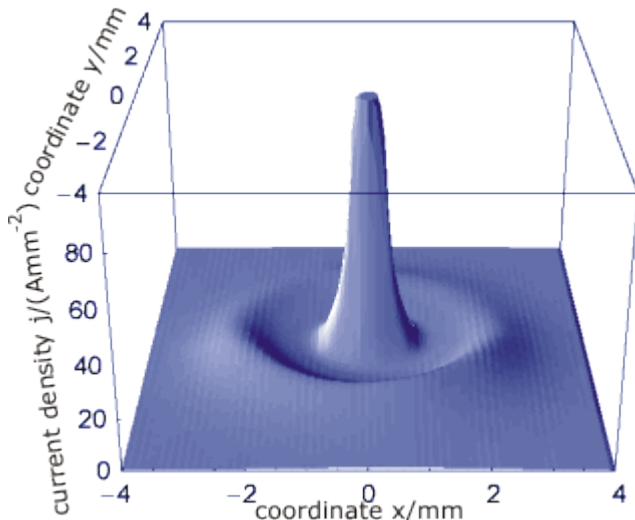
Macroscopic wavefunction

Atomic condensates



<http://jilawww.colorado.edu/bec/>

Non-linear optics



from wikipedia

atoms

photons

$\chi^{(3)}$

Show common phenomena

$$i\partial_t \psi(x,t) = \left[\nabla + V(x) + g |\psi(x,t)|^2 \right] \psi(x,t)$$

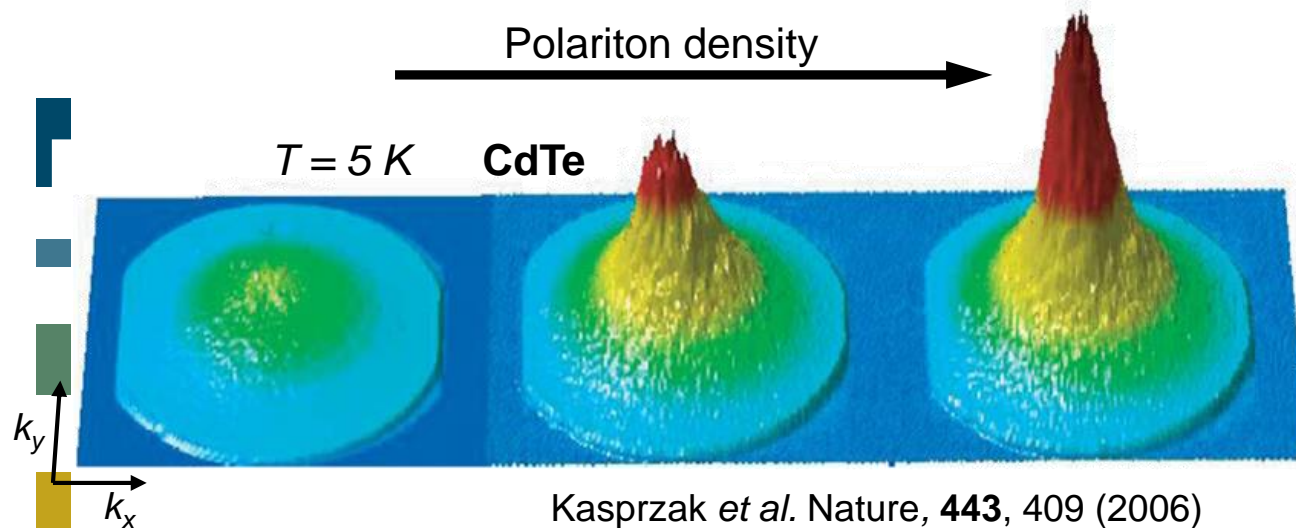
Cavity polaritons mix both worlds in a semiconductor structure

Bose-Einstein condensation of exciton polaritons

J. Kasprzak¹, M. Richard², S. Kundermann², A. Baas², P. Jeambrun², J. M. J. Keeling³, F. M. Marchetti⁴, M. H. Szymańska⁵, R. André¹, J. L. Staehli², V. Savona², P. B. Littlewood⁴, B. Deveaud² & Le Si Dang¹

Nature 443, 409 (2006)

$T = 10\text{ K}$



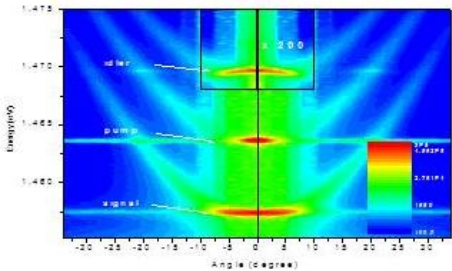
Benoid Deveaud



Le Si Dang

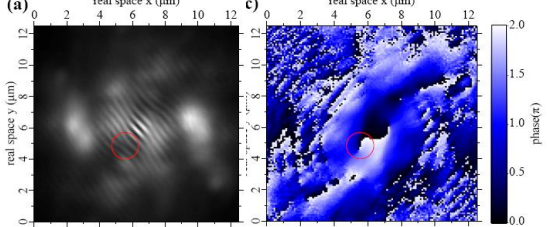
Polaritons: non-linear properties

Optical Parametric Oscillation



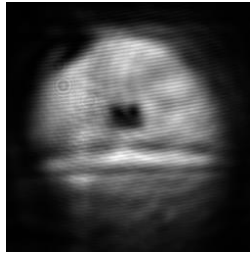
Diederichs *et al.*, *Nature* **440**, 904 (2006)

Quantised vortices



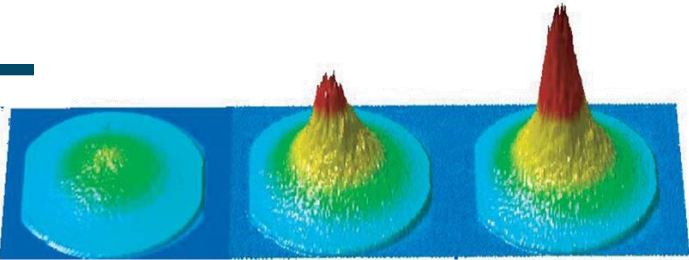
Lagoudakis *et al.*, *Nature Phys.* **4**, 706 (2008), and *Science* **326**, 974 (2009)

Superfluidity



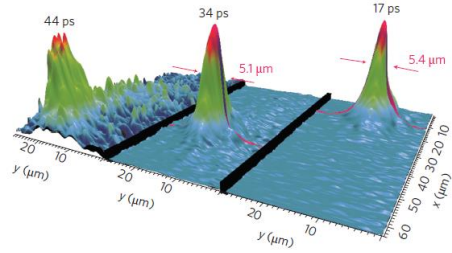
AA, Lefrère *et al.*, *Nature Phys.* **5**, 805 (2009)

Bosonic condensation



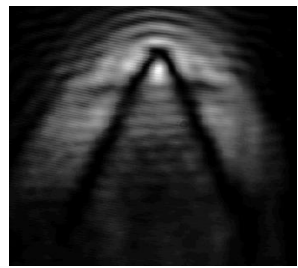
Kasprzak *et al.* *Nature*, **443**, 409 (2006)

Bright solitons



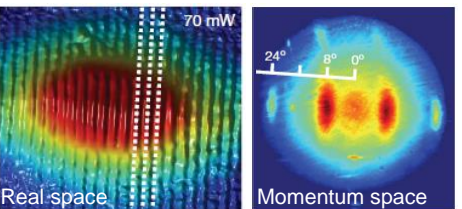
Sich *et al.*, *Nature Phot.* **6**, 50 (2012)

Dark solitons



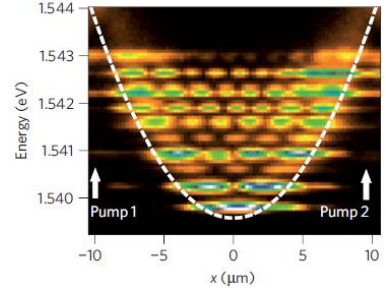
A.A., Pigeon *et al.*, *Science* **332**, 1167 (2012)

Long-range order phases



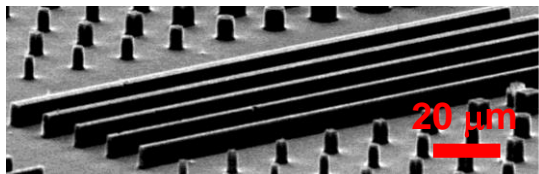
Lai *et al.*, *Nature* **450**, 529 (2007)
Kim *et al.* *Nature Phys.* (2011)

Non-linear oscillators



Tosi *et al.*, *Nature Phys.* **8**, 190 (2012)

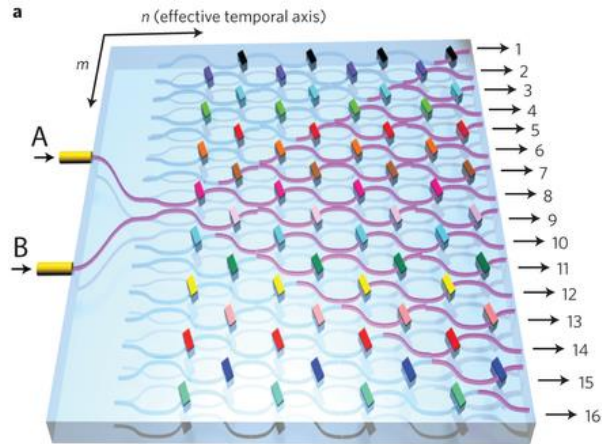
Condensates in low dimensions



Wertz *et al.*, *Nature Phys.* **6**, 860 (2010)

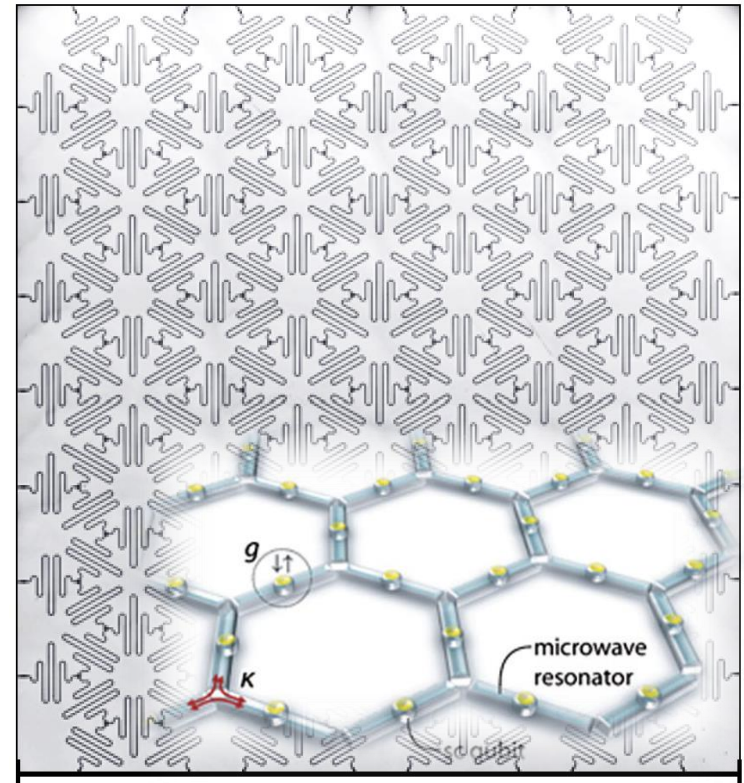
Emulation with photons

Random quantum walk



A. Crespi, Nature Photonics 7, 322 (2013)

Strongly interacting microwave photons



A. Houck et al., Nature Physics 8, 292 (2012)

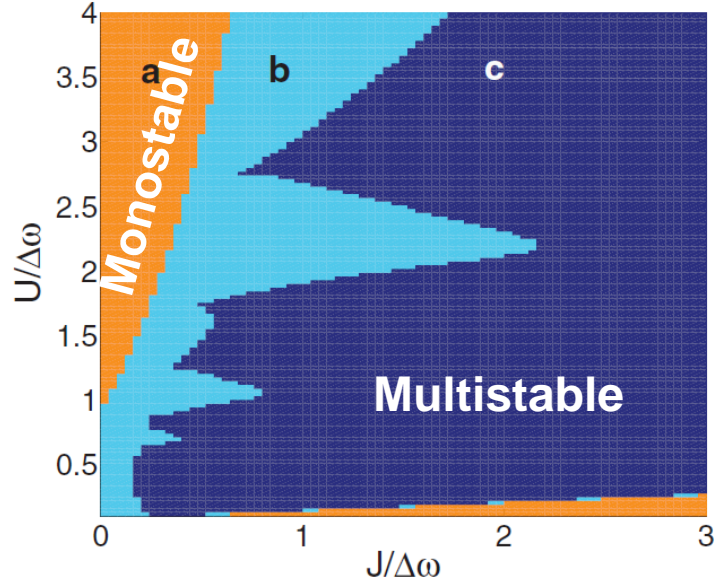
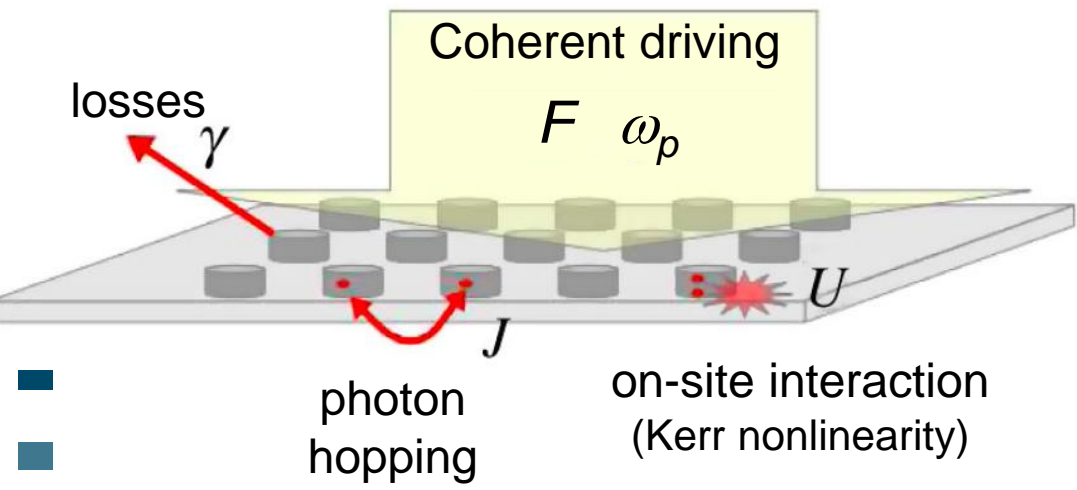
Topological photonics



M. Hafezi et al., Nature Photonics, 7, 1001 (2013)

Driven-dissipative photonic Bose-Hubbard model

Interplay of photon hopping, interaction, coherent driving, and decay, leads to strongly correlated steady-state phases and instabilities.



Le Boite *et al.*, PRL 110, 233601 (2013); PRA **90**, 063821 (2014).

Review on Quantum Fluids of Light: Ciuti & Carusotto, Rev. Mod. Phys. **85**, 299 (2013)

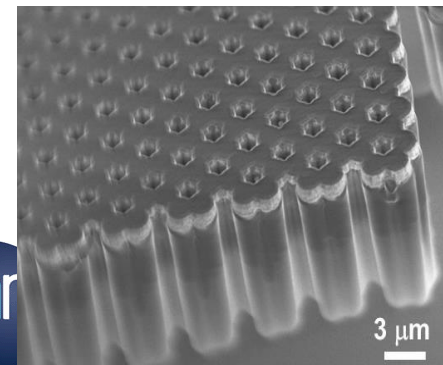
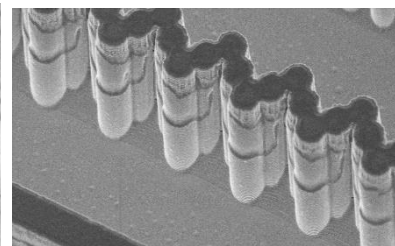
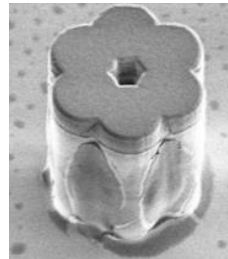
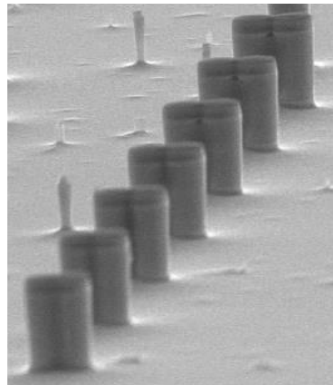
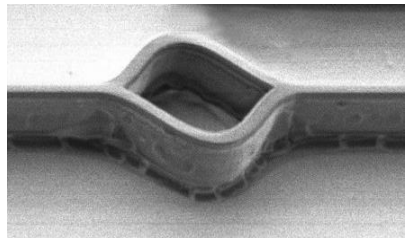
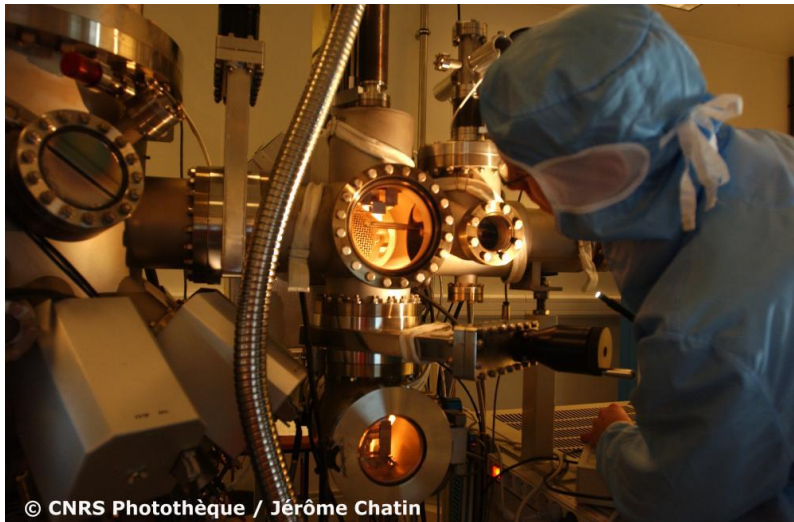
Quantum simulation with photons:

- M. J Hartmann, et al., Nature Phys. 2, 849{855 (2006).
- A. D Greentree, et al., Nature Phys. 2, 856{861 (2006).
- D. G. Angelakis, et al., Phys. Rev. A 76, 031805 (2007).

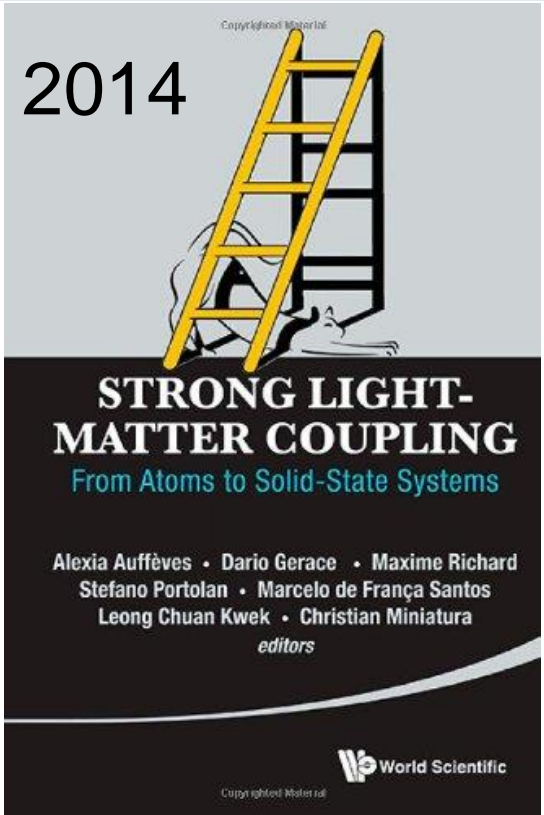
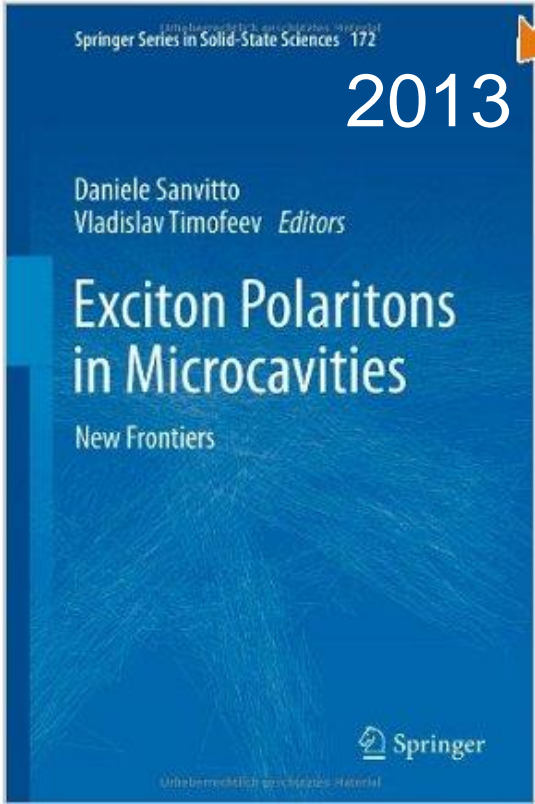
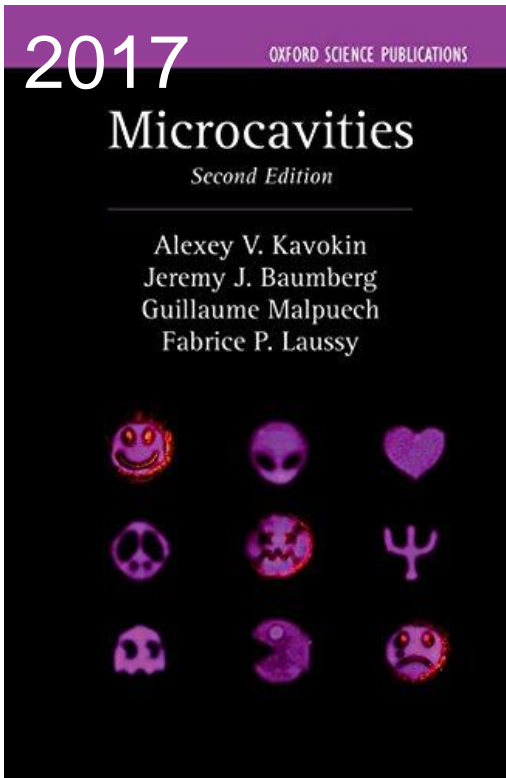
Our research at C2N

Use of nanotechnology to pattern microcavities

- * Manipulation of quantum fluids of light
- * A photonic emulator



Recent reviews



REVIEWS OF MODERN PHYSICS, VOLUME 85, JANUARY–MARCH 2013

Quantum fluids of light

Iacopo Carusotto*

INO-CNR BEC Center and Dipartimento di Fisica, Università di Trento, I-38123 Povo, Italy

Cristiano Ciuti†

Laboratoire Matériaux et Phénomènes Quantiques, Université Paris Diderot-Paris 7 et CNRS, Bâtiment Condorcet, 10 rue Alice Domon et Léonie Duquet, 75205 Paris Cedex 13, France

Outline

Lecture 1 : **Introduction to cavity polaritons**

- Hybrid light-matter quasi-particle: basic properties
- Confinement in microstructures
- Interactions

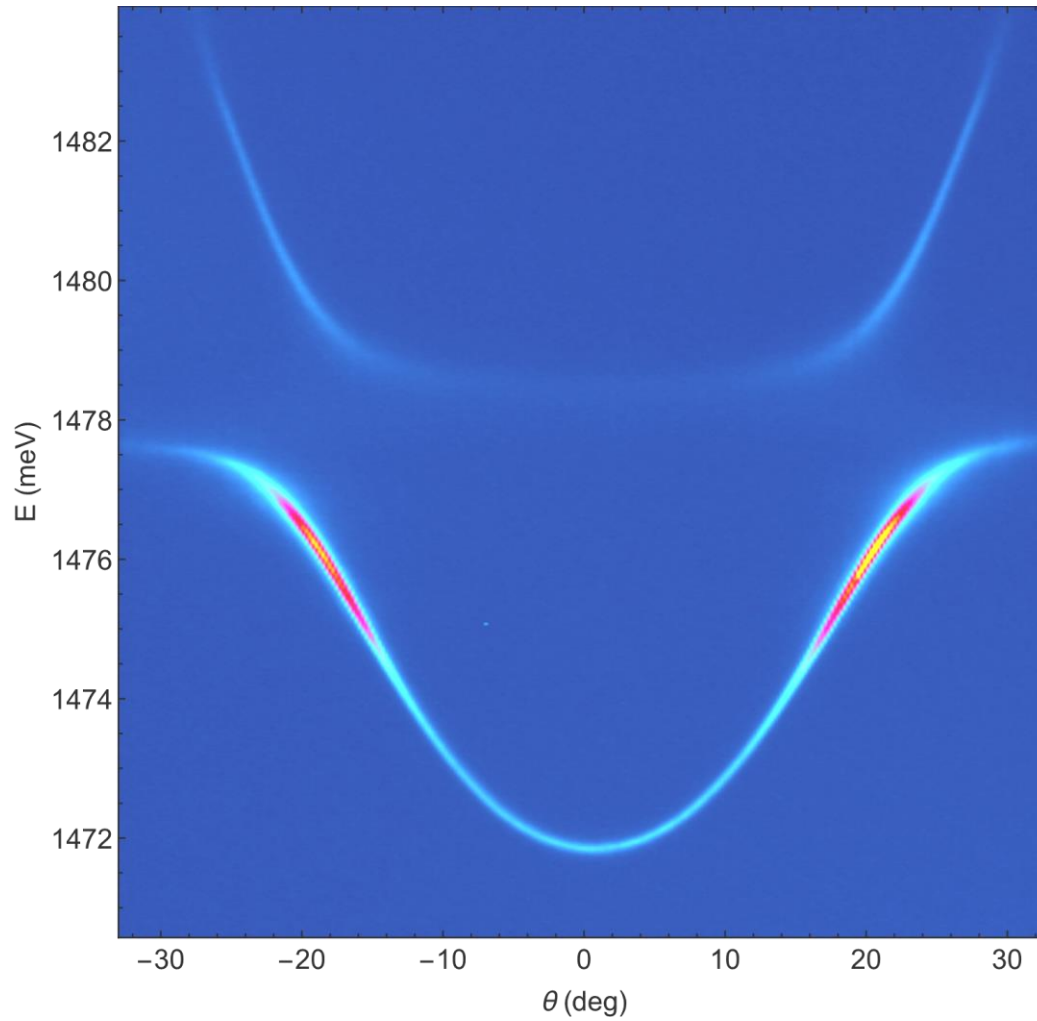
II Lecture 2: **Polariton condensation; Quantum fluids of light**

Coherence; Instability; Superfluidity; Dark solitons

III Lecture 3: **Polariton in lattices : quantum simulation**

- 1D Fibonacci quasi-crystals: fractal spectrum, edge states
- 1D SSH : topological laser
- 2D Honeycomb lattice: Dirac cones, edge states

Introduction to cavity polaritons



Microcavity polaritons

→ Mixed light-matter particles

Photons confined in an optical cavity

- **Very light ($m=0$ in vacuum)**
- Very fast
- No interactions

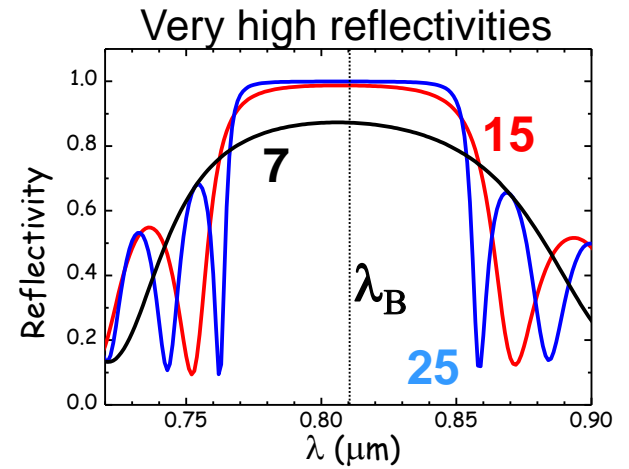
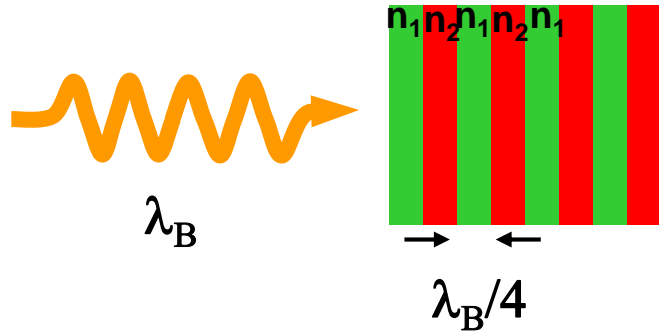
Excitons confined in a quantum well

- Very heavy
- Very slow
- **Strong interactions**



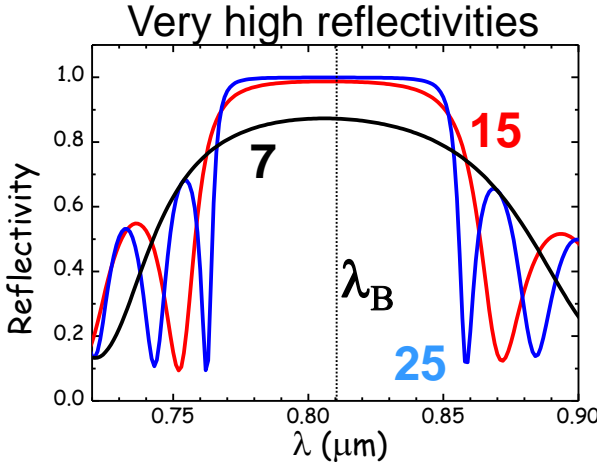
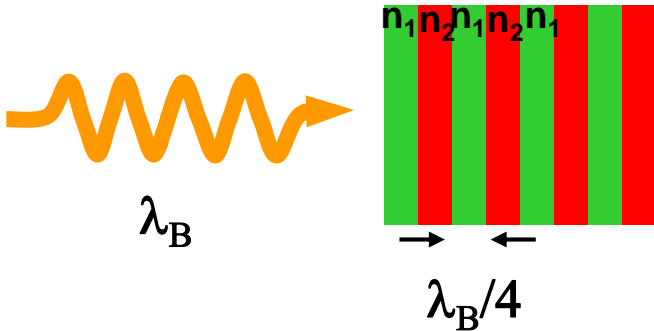
Photon confinement

→ Distributed Bragg reflector

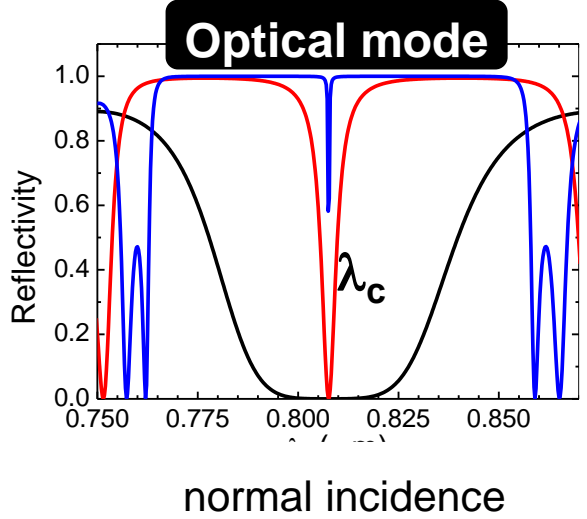
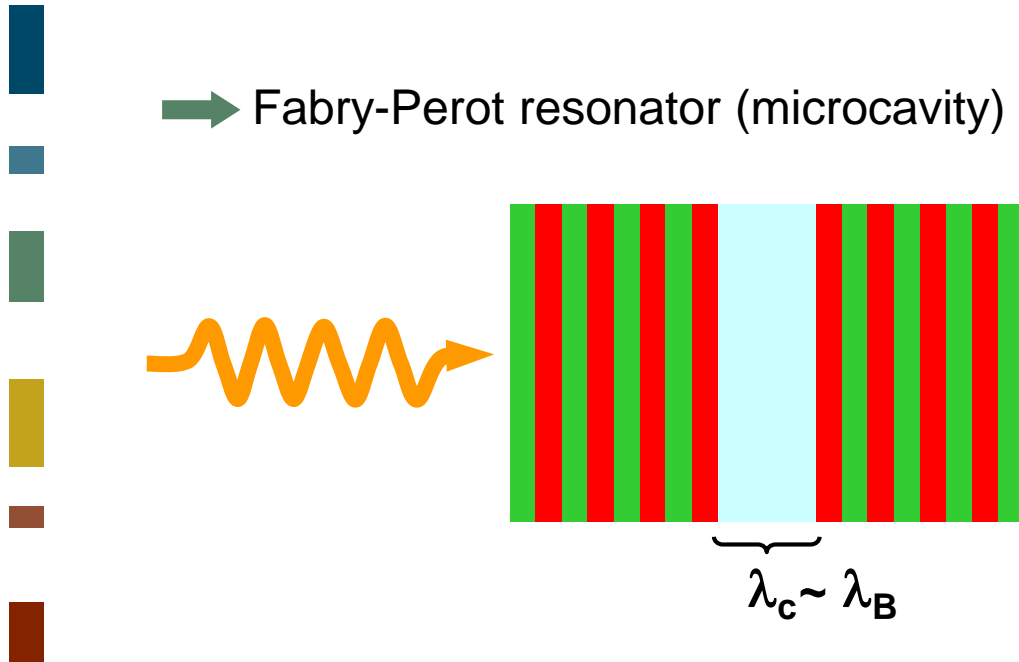


Photon confinement

→ Distributed Bragg reflector



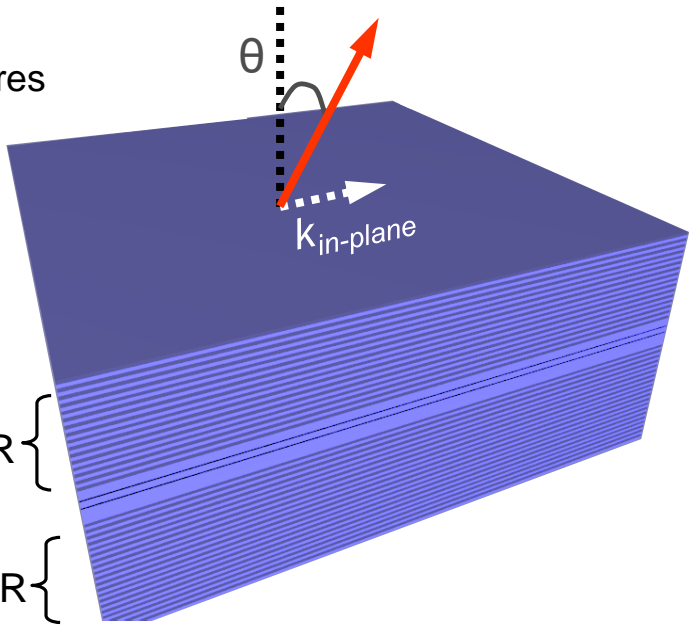
→ Fabry-Perot resonator (microcavity)



Microcavity polaritons

GaAs/AlGaAs based structures

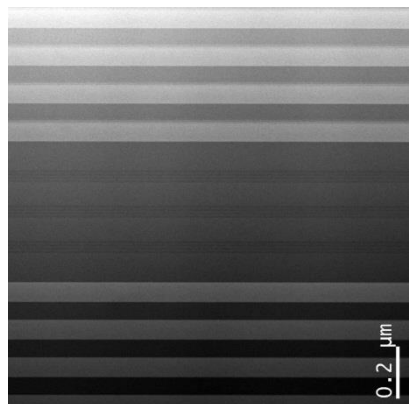
5 K



Top DBR

Bottom DBR

Optical cavity

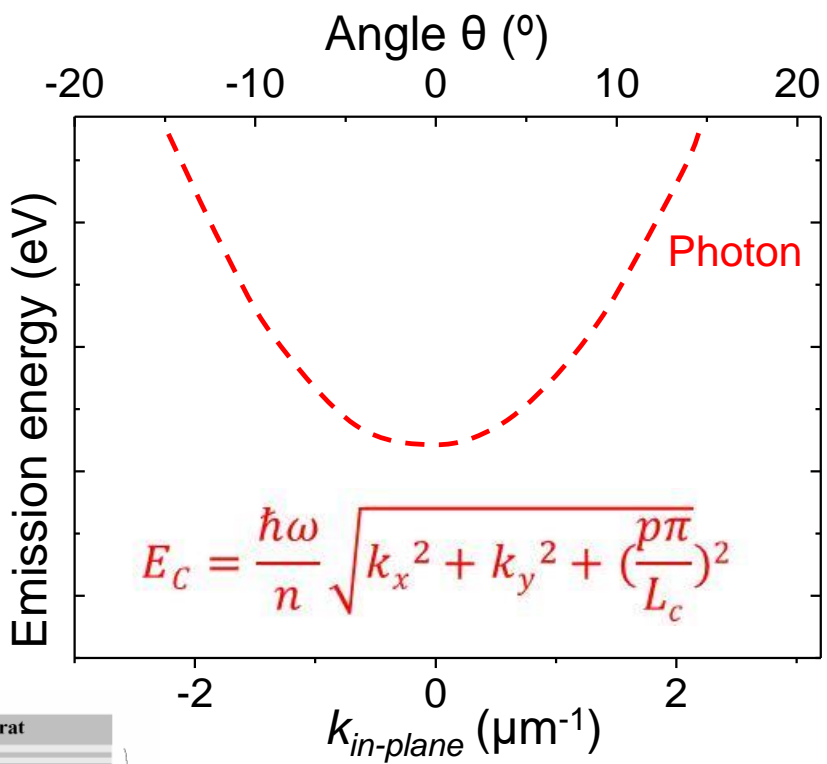
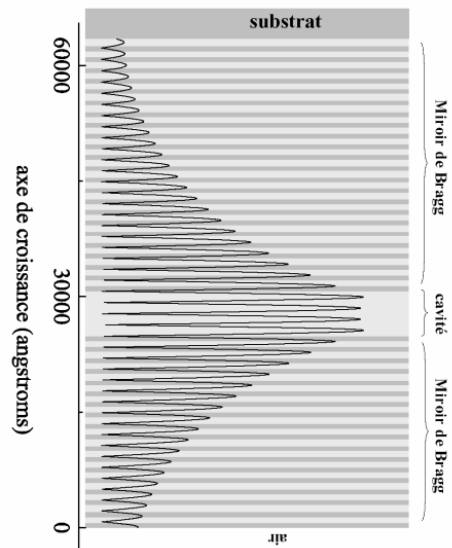


Bragg mirror
GaAs/AlAs

Cavity

Bragg mirror
GaAs/AlAs

TEM, G. Patriarche, LPN



$$E_c(k) = E_c(k=0) + \frac{\hbar^2 k^2}{2M_{phot}}$$

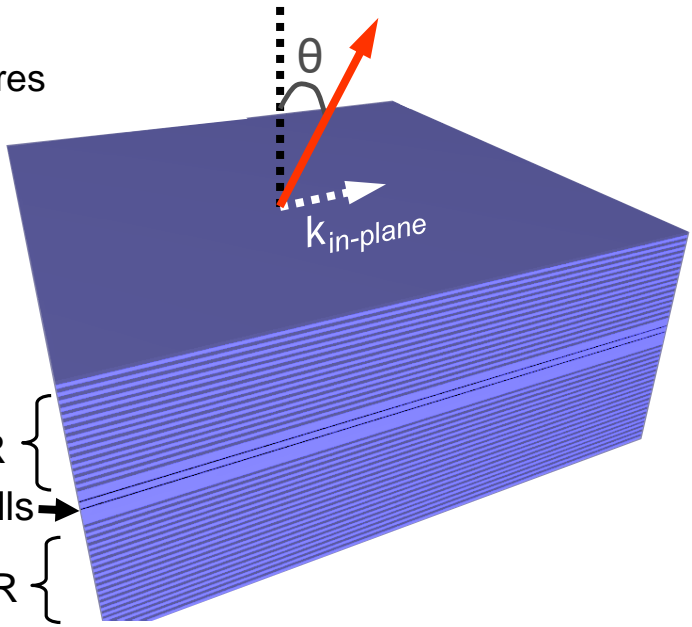
$$\text{with } M_{phot} = \frac{p^2 \pi^2 \hbar^2}{L_c^2 n^2}$$



Microcavity polaritons

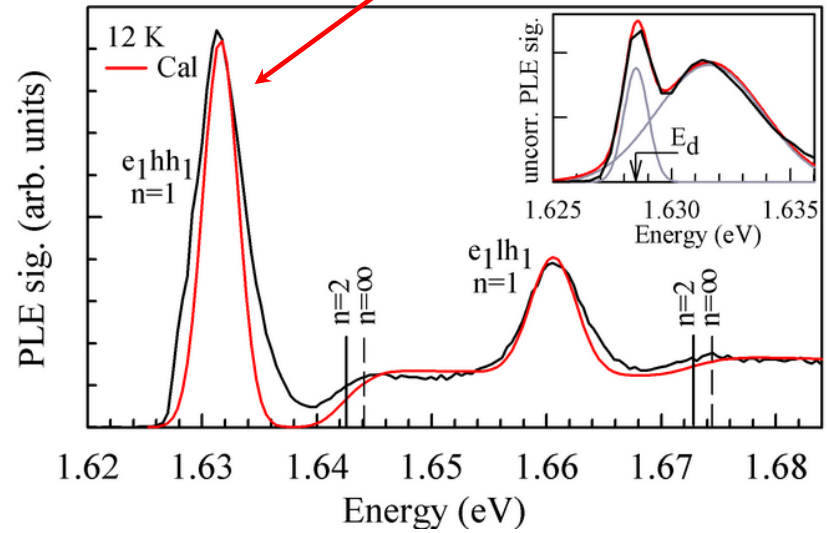
GaAs/AlGaAs based structures

5 K

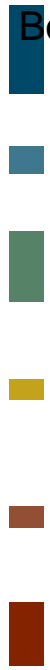
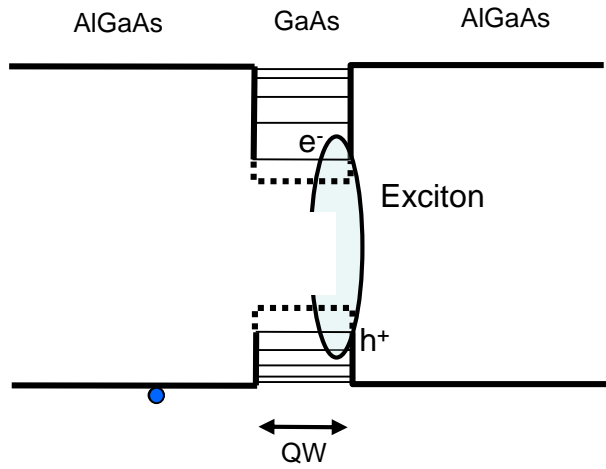


Top DBR
Quantum Wells
Bottom DBR

Excitonic resonance



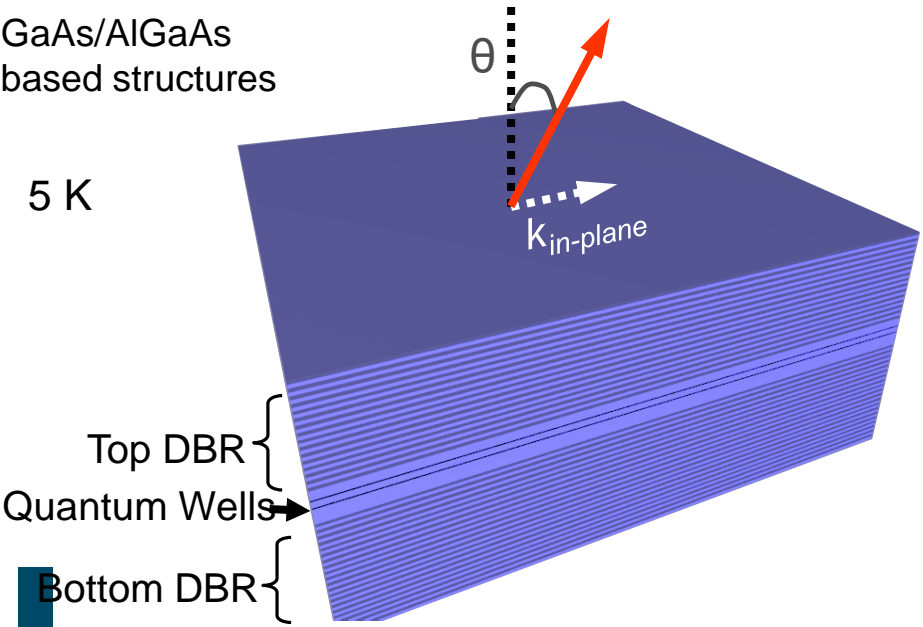
Quantum well exciton



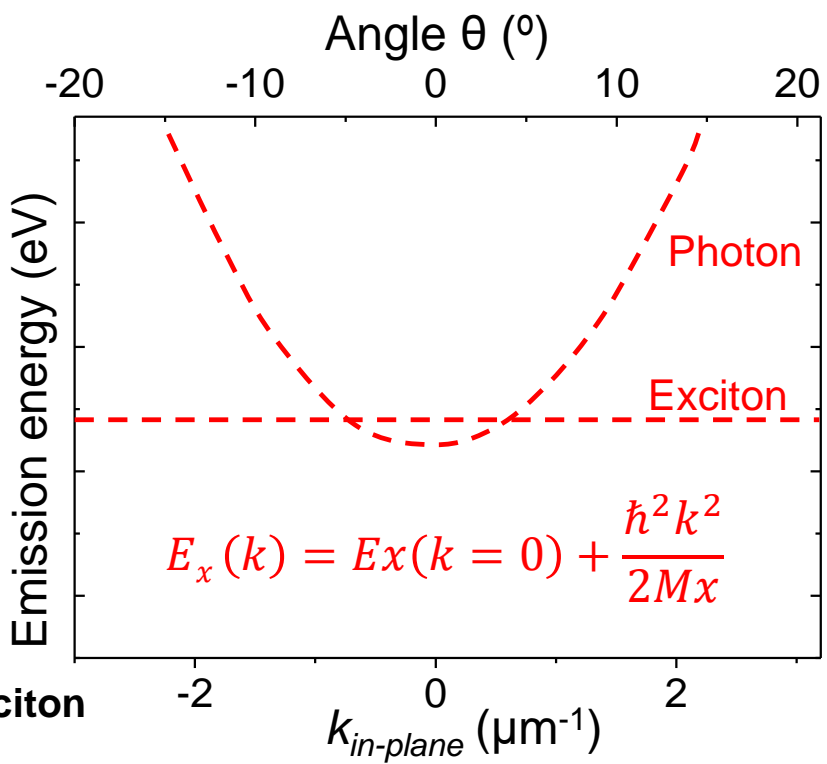
Microcavity polaritons

GaAs/AlGaAs based structures

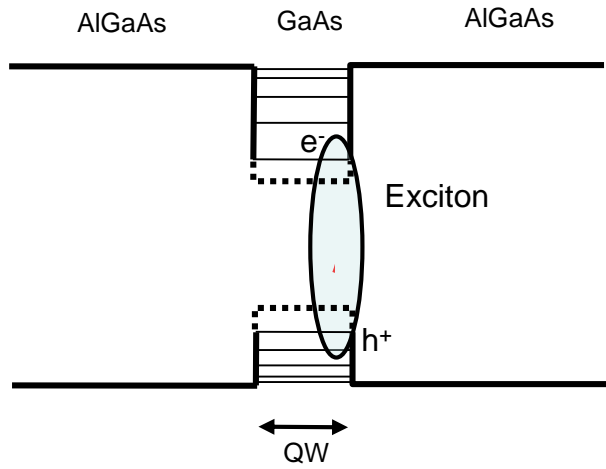
5 K



-
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Quantum well exciton



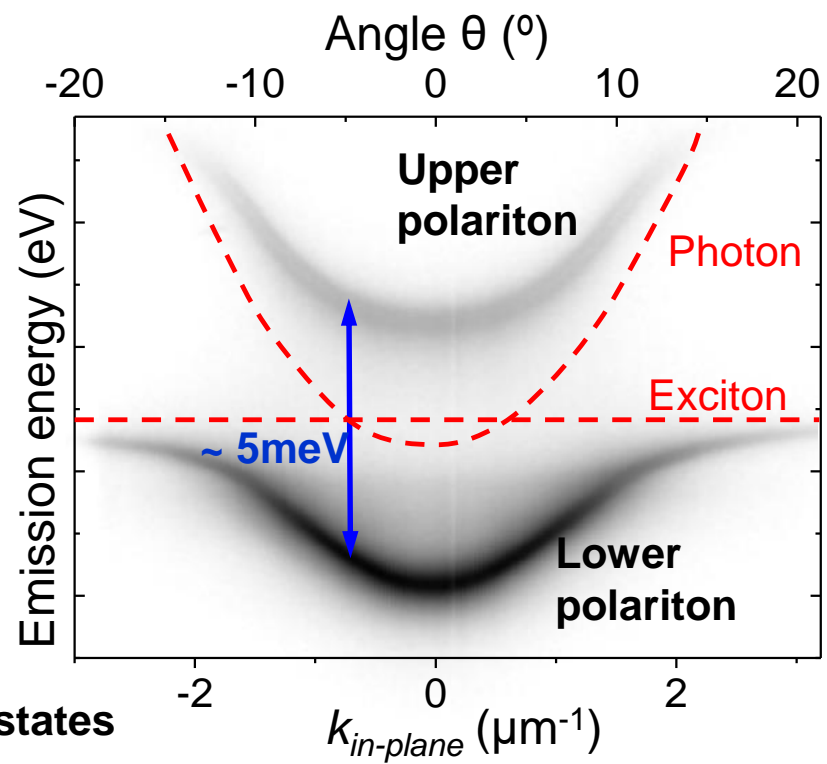
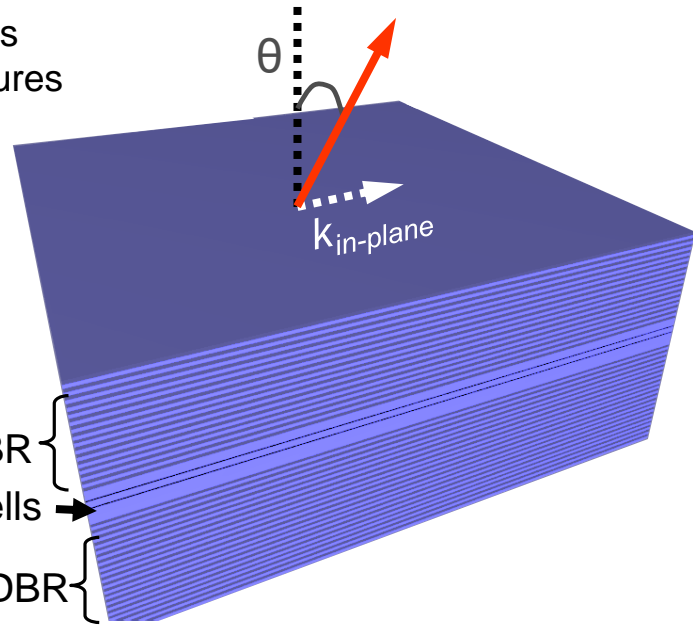
with $M_x = m_e + m_h$

Typically $\frac{M_x}{M_{phot}} = 10^4$

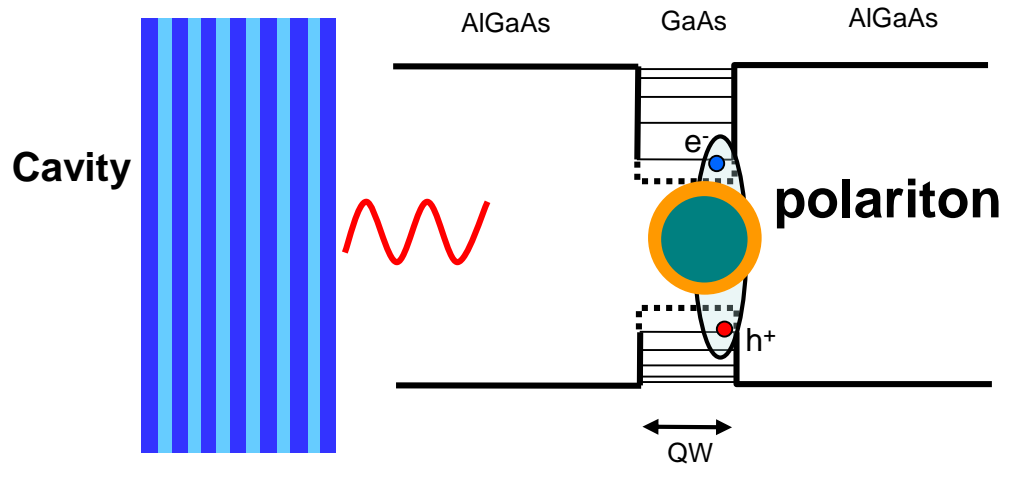
Microcavity polaritons

GaAs/AlGaAs based structures

5 K



Top DBR
 Quantum Wells
 Bottom DBR
Microcavity polaritons : mixed exciton-photon states



-
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Observation of the Coupled Exciton-Photon Mode Splitting in a Semiconductor Quantum Microcavity

C. Weisbuch,^(a) M. Nishioka,^(b) A. Ishikawa, and Y. Arakawa

Research Center for Advanced Science and Technology, University of Tokyo, 4-6-1 Meguro-ku, Tokyo 153, Japan

(Received 12 May 1992)

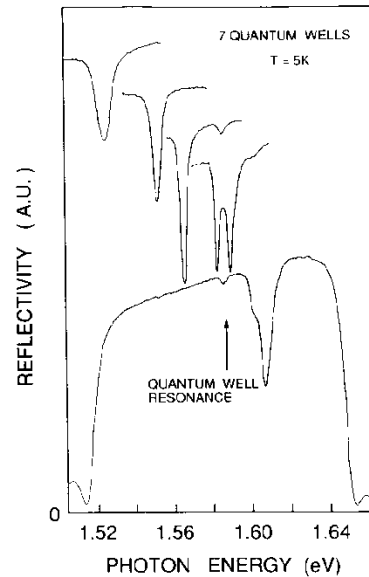
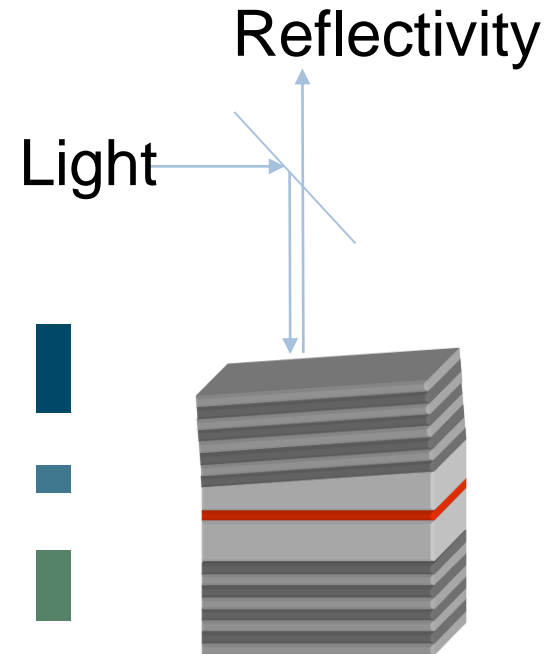


FIG. 2. 5-K reflectivity curves on a seven-QW microcavity structure. Various detuning conditions between cavity and QW exciton frequencies are obtained by choosing various points on the wafer, typically 0.5 mm apart. Note the line narrowing approaching and at resonance, the resonance mode splitting, and the indication of a light-hole exciton mode splitting around 1.605 eV for the lowest trace.

3316

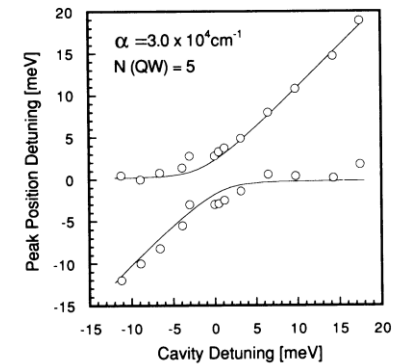
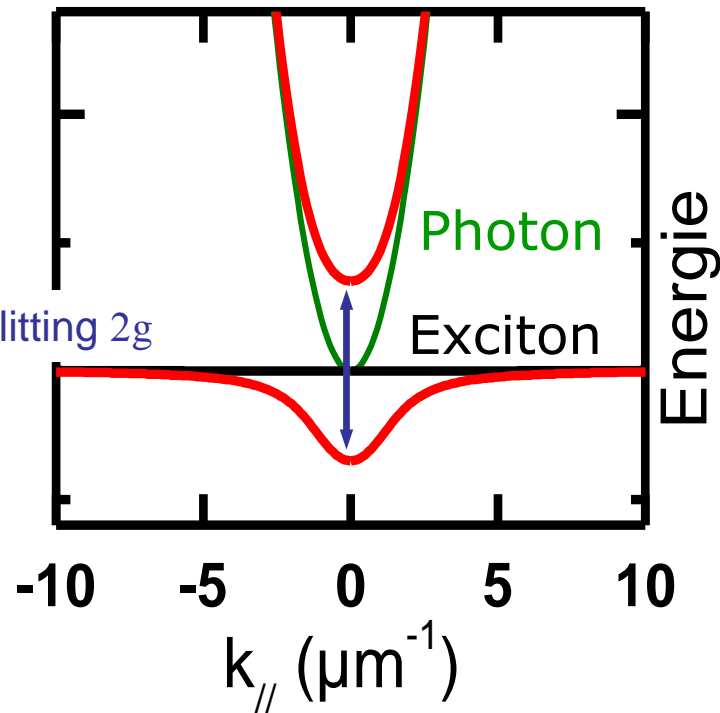
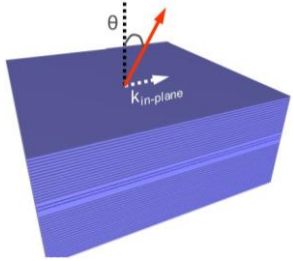


FIG. 3. Reflectivity peak positions as a function of cavity detuning for a five-quantum-well sample at $T = 5$ K. The theoretical fit is obtained through a standard multiple-interference analysis of the DBR-Fabry-Pérot-quantum-well structure.



Claude Weisbuch
PRL **69**, 3314 (1992)

Microcavity polaritons



$$H_{k_{\parallel}} = \begin{pmatrix} E_X(k_{\parallel}) & g \\ g & E_C(k_{\parallel}) \end{pmatrix}$$

$$E_1 = \frac{E_X(k_{\parallel}) + E_C(k_{\parallel})}{2} - \frac{\Delta(k_{\parallel})}{2}$$

$$E_2 = \frac{E_X(k_{\parallel}) + E_C(k_{\parallel})}{2} + \frac{\Delta(k_{\parallel})}{2}$$

with

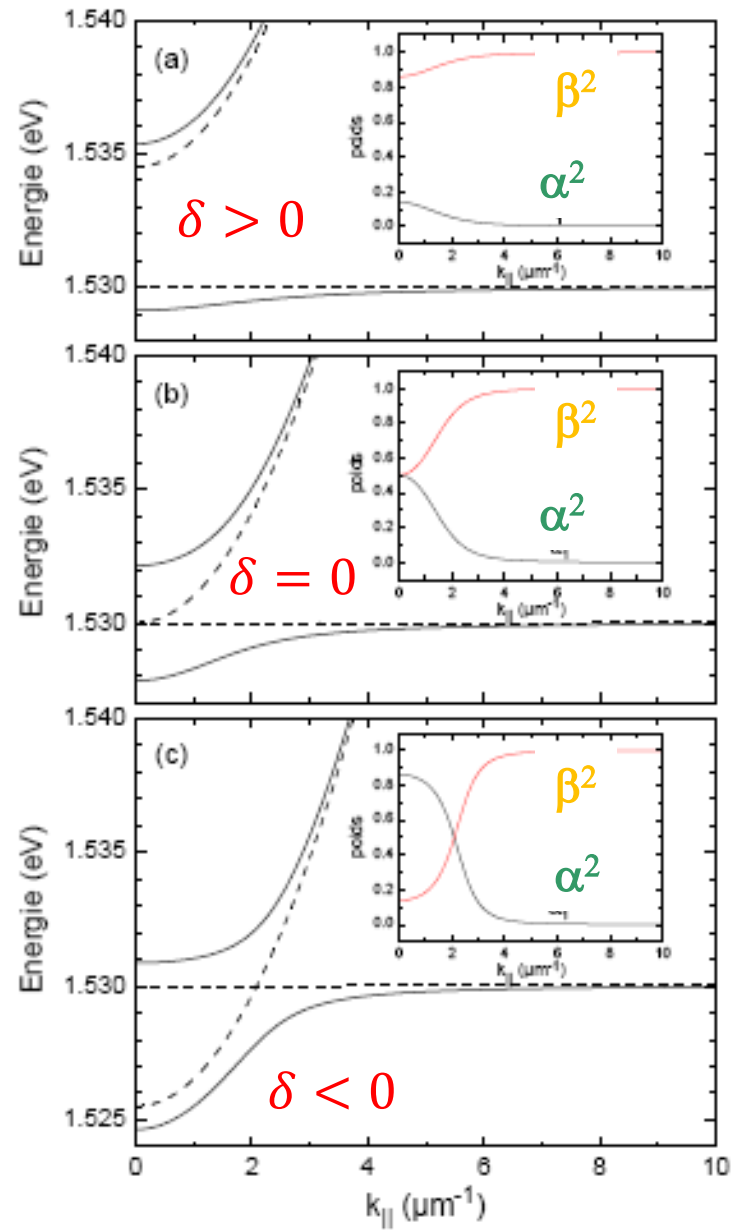
$$\Delta(k_{\parallel}) = \sqrt{(E_C(k_{\parallel}) - E_X(k_{\parallel}))^2 + 4g^2}$$

Microcavity polaritons

$$|\text{polariton}\rangle = \alpha |\text{photon}\rangle + \beta |\text{exciton}\rangle$$

Exciton photon detuning:
 $\delta = E_c(k=0) - E_x(k=0)$

s-shaped dispersion : inflexion point



Microcavity polaritons

$$|\text{polariton}\rangle = \alpha |\text{photon}\rangle + \beta |\text{exciton}\rangle$$

Exciton photon detuning:

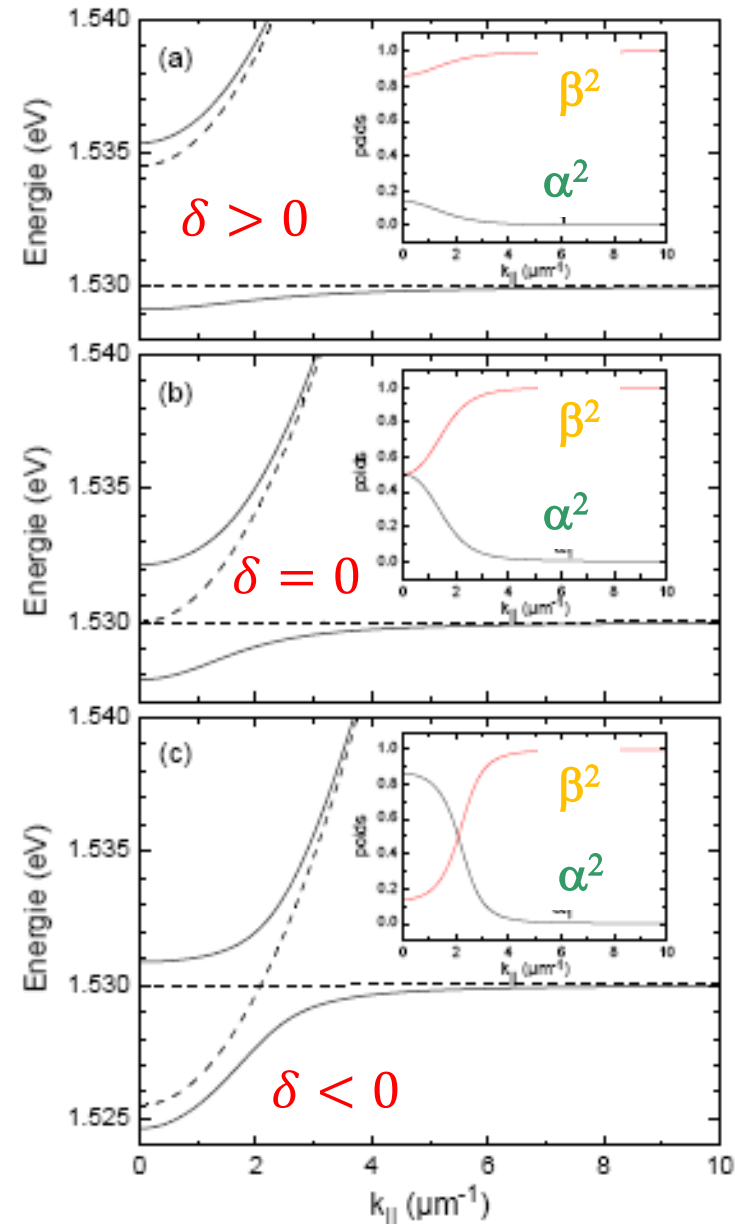
$$\delta = E_c(k=0) - E_x(k=0)$$

s-shaped dispersion : inflexion point

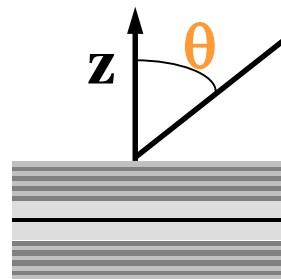
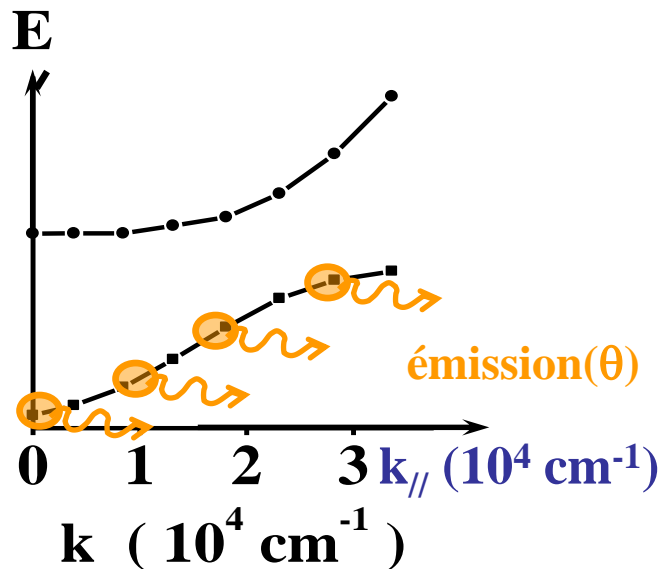
$$\text{Effective mass: } \frac{1}{M_{pol}} = \frac{1}{\hbar^2} \frac{\partial^2 E}{\partial k^2}$$

$$\text{At } k=0: \frac{1}{M_{pol}} = \frac{\alpha^2}{M_{phot}} + \frac{\beta^2}{M_{exc}}$$

Beyond inflexion point: negative effective mass



Probing polariton states: Angle resolved experiments

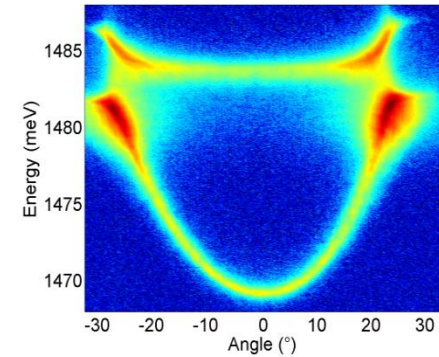
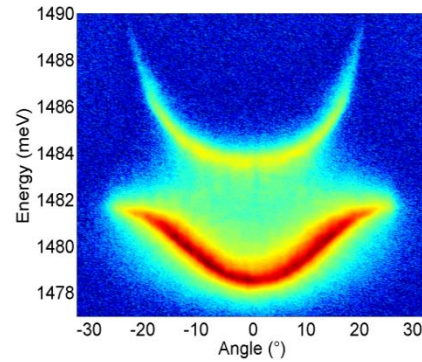
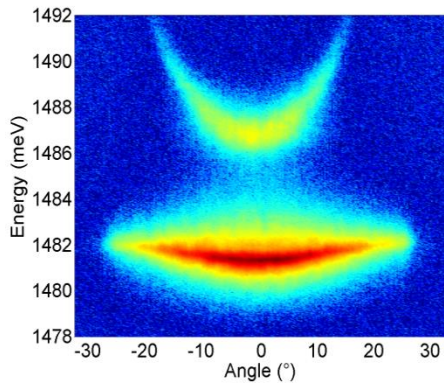
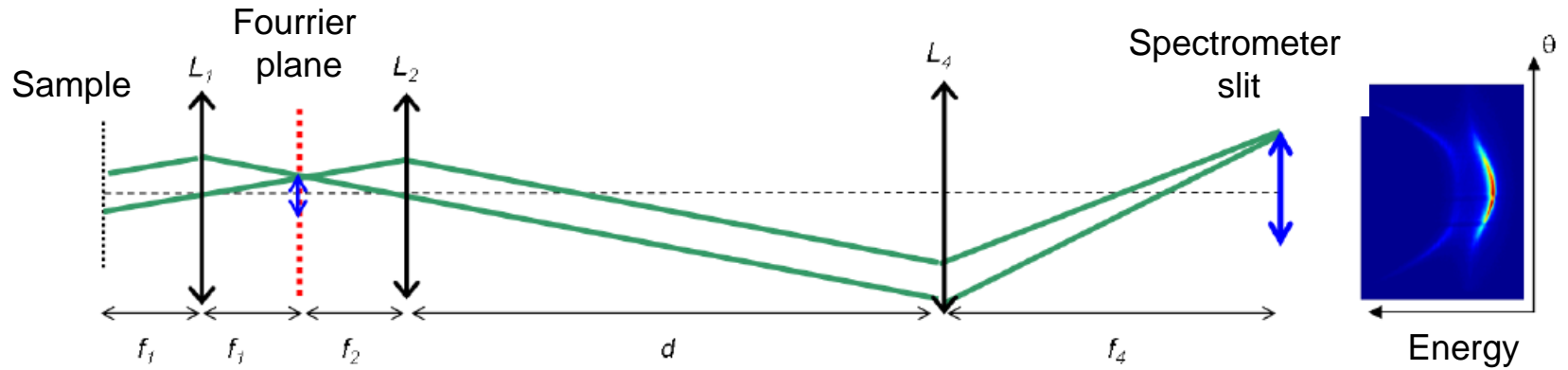


$$\theta \longleftrightarrow k_{//}$$

$$k_{//} = \omega/c \sin(\theta)$$

Selective excitation and probe of polariton states

Probing polariton states: Angle resolved experiments



Measurement of Cavity-Polariton Dispersion Curve from Angle-Resolved Photoluminescence Experiments

R. Houdré,¹ C. Weisbuch,^{1,2} R. P. Stanley,¹ U. Oesterle,¹ P. Pellandini,¹ and M. Ilegems¹

¹*Institut de Micro- et Optoélectronique, Ecole Polytechnique Fédérale de Lausanne, CH 1015, Lausanne, Switzerland*

²*Laboratoire de Physique de la Matière Condensée, Ecole Polytechnique, F 91128 Palaiseau, France*

(Received 11 March 1994)

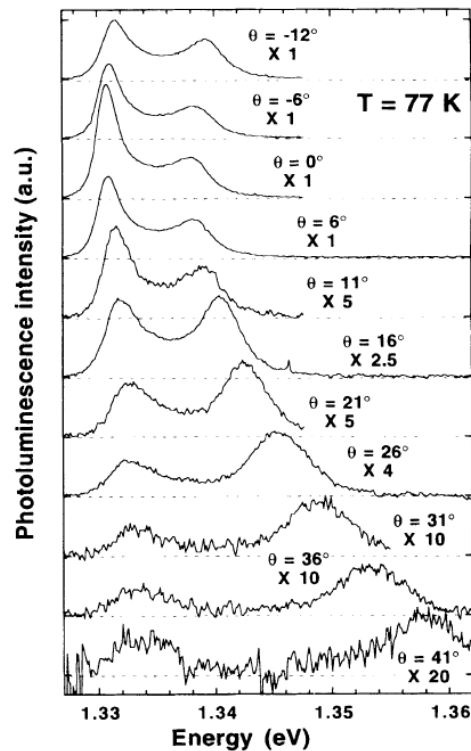


FIG. 2. Series of photoluminescence spectra at $T = 77$ K, for an emission angle from -12° to 41° . The Fabry-Pérot at normal incidence is resonant with the quantum well exciton.

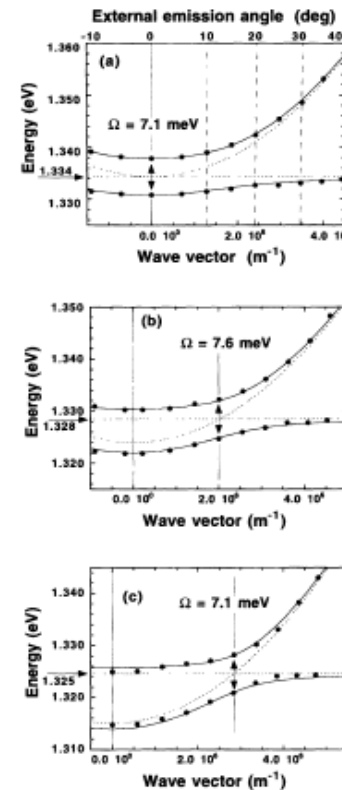


FIG. 3. Cavity-polariton dispersion curves, deduced from angle-resolved photoluminescence measurements, for different resonance conditions. (a) Resonance at $\theta = 0^\circ$ (case of Fig. 2), (b) resonance at $\theta = 29^\circ$, and (c) $\theta = 35^\circ$. The continuous lines are theoretical calculations and the dashed lines are the uncoupled exciton and cavity dispersion curves. The interaction energy Ω and exact resonance position are determined from the minimum splitting between both photoluminescence lines. An external emission angle grid is drawn on (a).

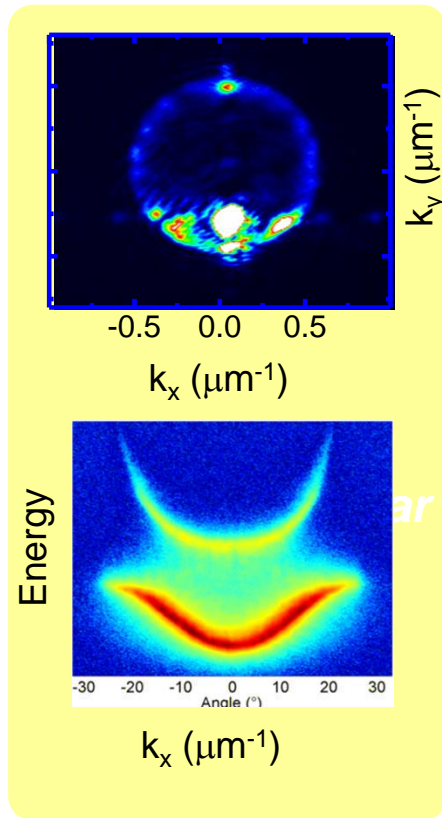
Phys. Rev. Lett. **73**, 2043 (1994)



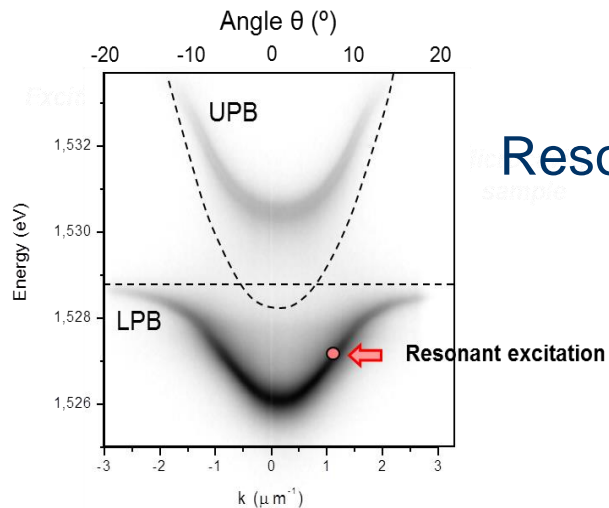
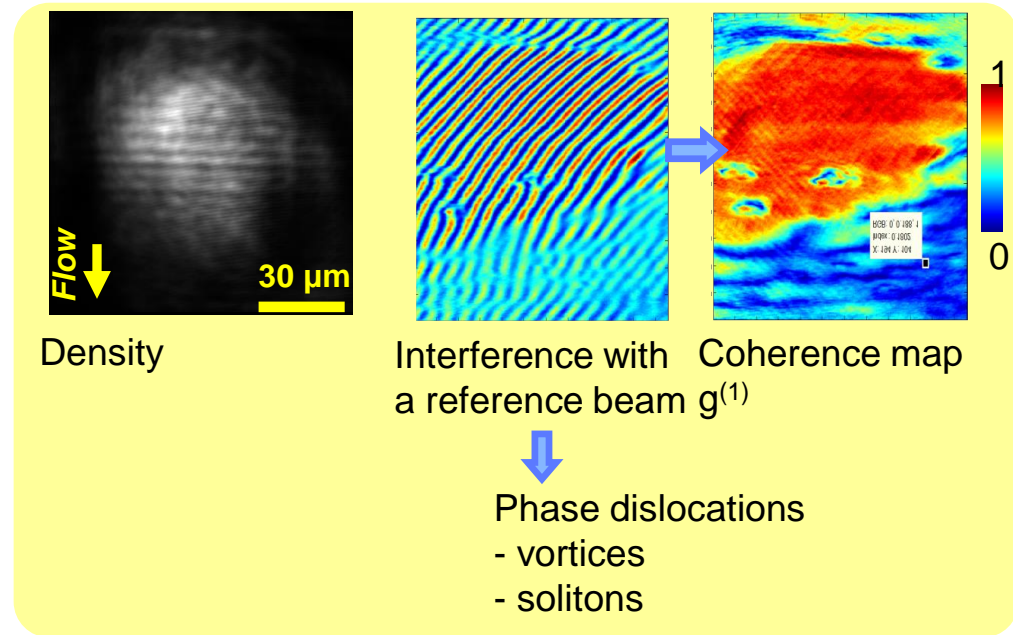
Romuald Houdré

Typical experimental scheme

Far field imaging: k space



Real space imaging



Resonant injection of polaritons

Cavity polaritons : an exciton-photon mixed state

$$|\text{polariton}\rangle = \alpha |\text{photon}\rangle + \beta |\text{exciton}\rangle$$

α^2 photon part

Coupling to free space optical modes

Low effective mass

β^2 exciton part

Polariton-phonon Interactions
Polariton-polariton Interactions

Properties

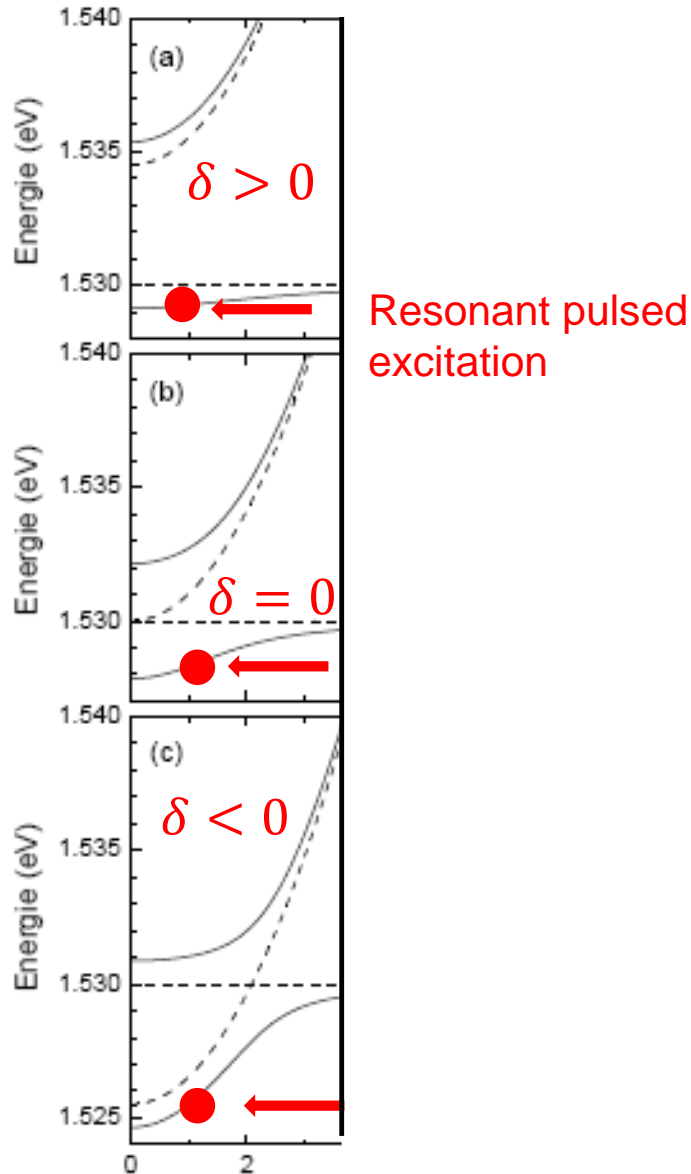
- Photonic component \rightarrow low mass ($10^{-5} m_e$)
-
-
-

Probing polariton states: Real space propagation

PHYSICAL REVIEW B

VOLUME 61, NUMBER 11

15 MARCH 2000-



In-plane propagation of excitonic cavity polaritons

T. Freixanet

Laboratoire de Microstructures et de Microélectronique, Boîte Postale 107, 92225 Bagneux, France

B. Sermage and A. Tiberj

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R. Planel

Laboratoire de Microstructures et de Microélectronique, Boîte Postale 107, 92225 Bagneux, France

(Received 16 November 1999)

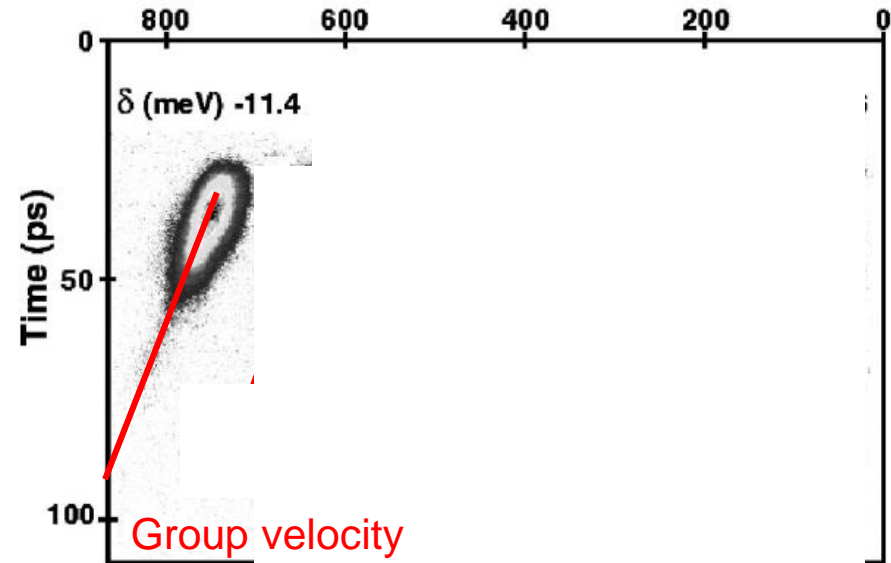


FIG. 2. Propagation in real space of the secondary emission source as observed on the streak camera for several detunings. The diaphragm is close to the reflection and $\theta_i = 7.8^\circ$.

Probing polariton states: Real space propagation

PHYSICAL REVIEW B

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In-plane propagation of excitonic cavity polaritons

T. Freixanet

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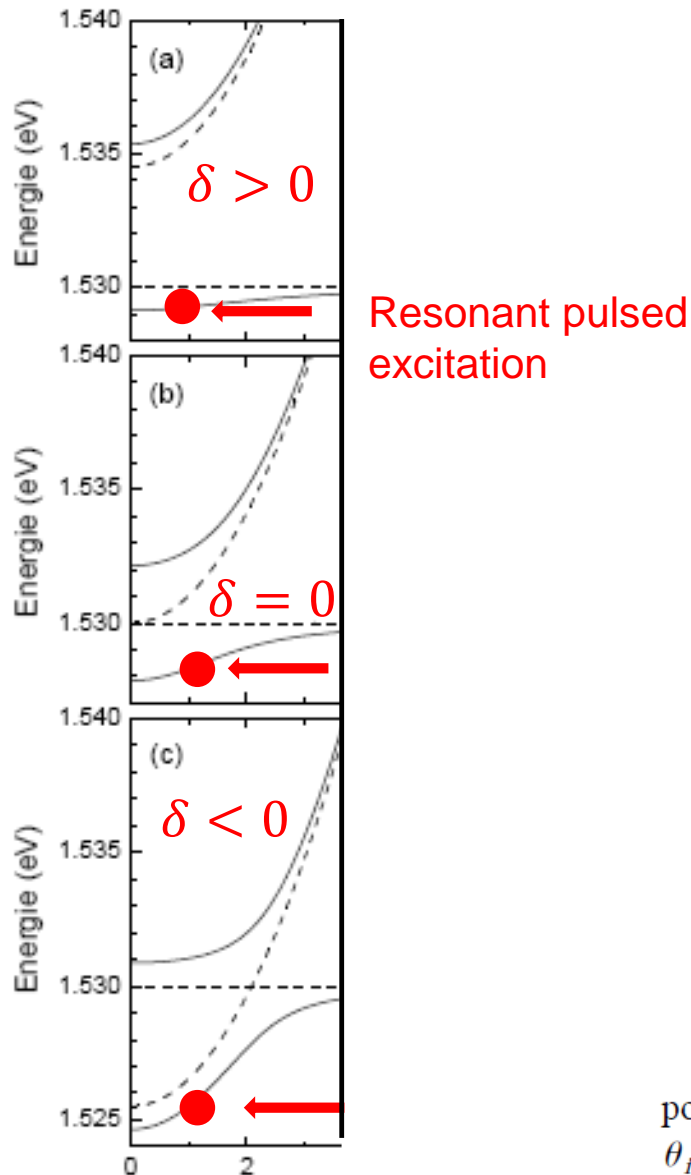
B. Sermage and A. Tiberj

Centre National d'Etudes des Télécommunications, Boîte Postale 107, 92225 Bagneux, France

R. Planel

Laboratoire de Microstructures et de Microélectronique, Boîte Postale 107, 92225 Bagneux, France

(Received 16 November 1999)



$$v_g = \frac{1}{\hbar} \frac{\partial E}{\partial k} \quad v_g(k) = \alpha^2 v_{phot}(k) + \beta^2 v_{exc}(k)$$

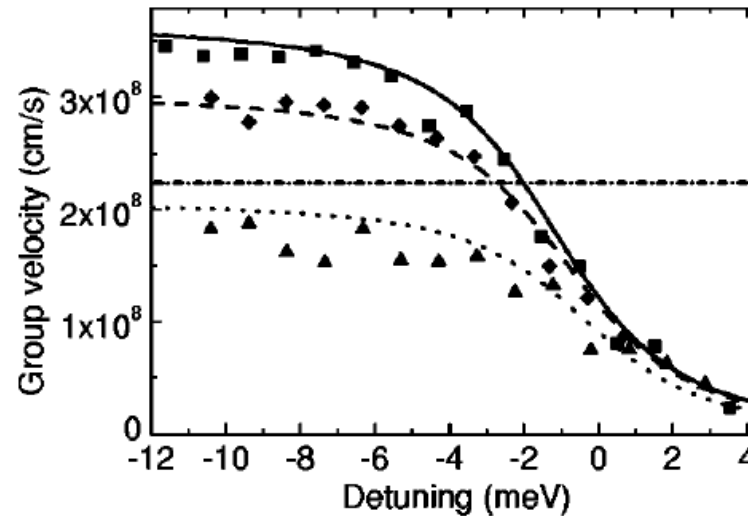
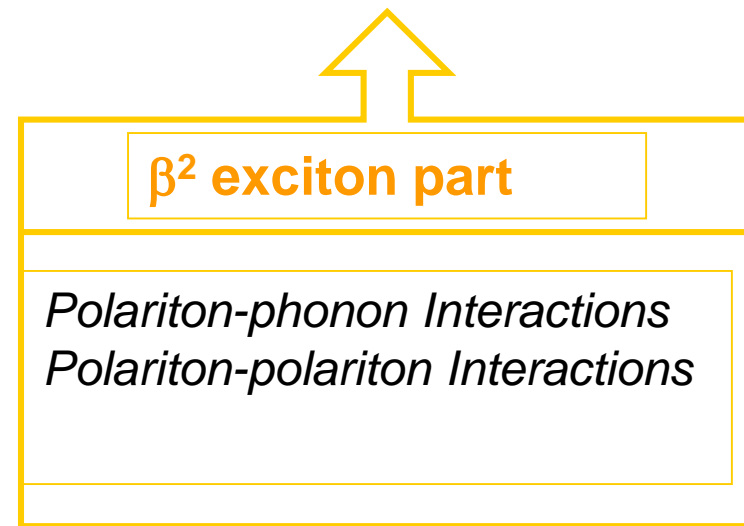
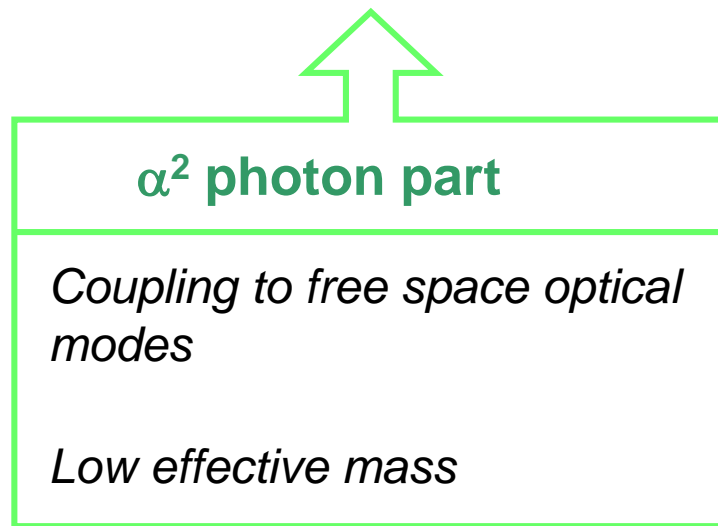


FIG. 3. Group velocity of the resonantly excited lower branch polaritons as a function of the detuning for different incident angles θ_i . The points are the measured values for $\theta_i=7.8^\circ$ (■), $\theta_i=6.2^\circ$ (◆), and $\theta_i=4.3^\circ$ (▲). The solid, dashed, and dotted lines

Cavity polaritons : an exciton-photon mixed state

$$|\text{polariton}\rangle = \alpha |\text{photon}\rangle + \beta |\text{exciton}\rangle$$



Properties

- Photonic component \Rightarrow low mass ($10^{-5} m_e$)
- Short lifetime (\sim ps) \Rightarrow escape out of the cavity
-
-

Polariton lifetime

PHYSICAL REVIEW B

VOLUME 53, NUMBER 24

15 JUNE 1996-II

Time-resolved spontaneous emission of excitons in a microcavity: Behavior of the individual exciton-photon mixed states

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FRANCE TELECOM, Centre National d'Etudes des Télécommunications, Paris B, Laboratoire de Bagneux, Boite Postale 107,
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J. Bloch, R. Planel, and V. Thierry-Mieg

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92225 Bagneux Cedex, France

(Received 1 May 1995; revised manuscript received 12 January 1996)

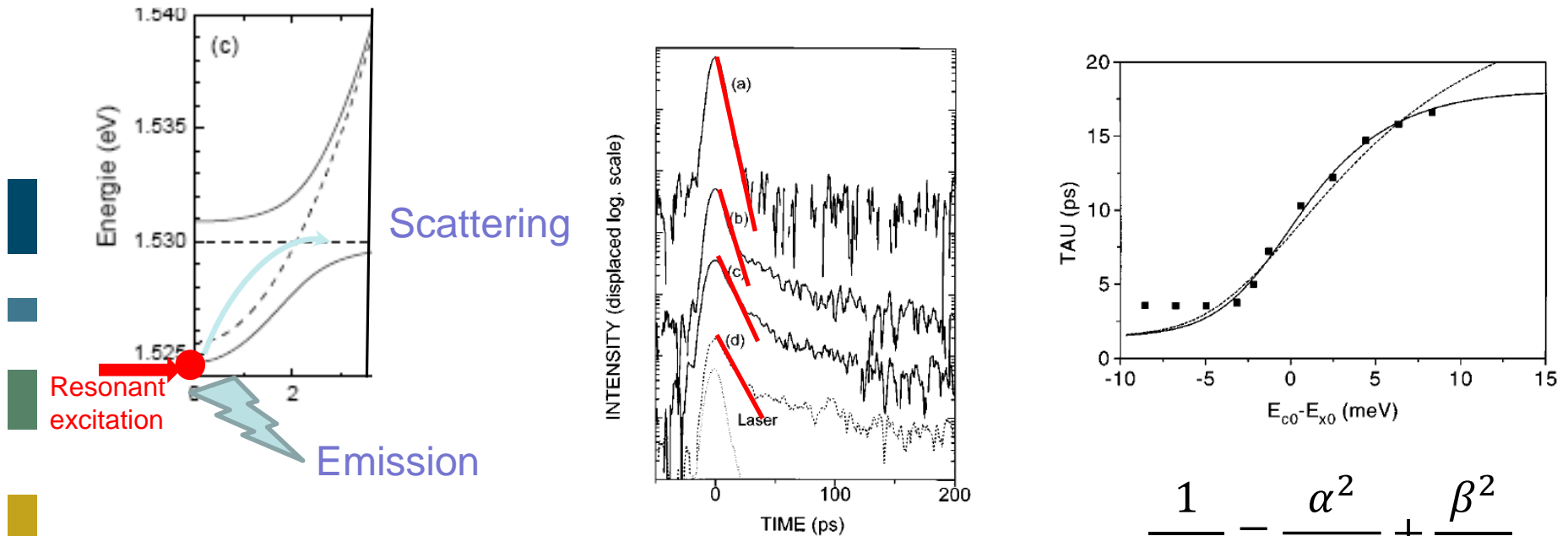


FIG. 1. Luminescence decay curves obtained with a laser excitation resonant with the lower state for different values of the detuning: (a) $\delta_0 = E_{c0} - E_{x0} = -8.5$ meV, (b) $\delta_0 = -1.5$, and (c) $\delta_0 = 3.5$ meV. The dashed curve (d) is the luminescence decay of the reference sample excited resonantly. The dotted curve (labeled "Laser") is the instrument response function.

$$\frac{1}{\tau_{pol}} = \frac{\alpha^2}{\tau_{phot}} + \frac{\beta^2}{\tau_{exc}}$$

Polariton have a short lifetime : 1-100 ps

Cavity polaritons : an exciton-photon mixed state

$$|\text{polariton}\rangle = \alpha |\text{photon}\rangle + \beta |\text{exciton}\rangle$$

α^2 photon part

Coupling to free space optical modes

Low effective mass

β^2 exciton part

Polariton-phonon Interactions
Polariton-polariton Interactions

Properties

- Photonic component \Rightarrow **low mass ($10^{-5} m_e$)**
- Short lifetime (\sim ps) \Rightarrow **escape out of the cavity**
- Pseudo spin

Polariton spin

→ Spin : electron : $\pm \frac{1}{2}$
 heavy hole : $\pm \frac{3}{2}$

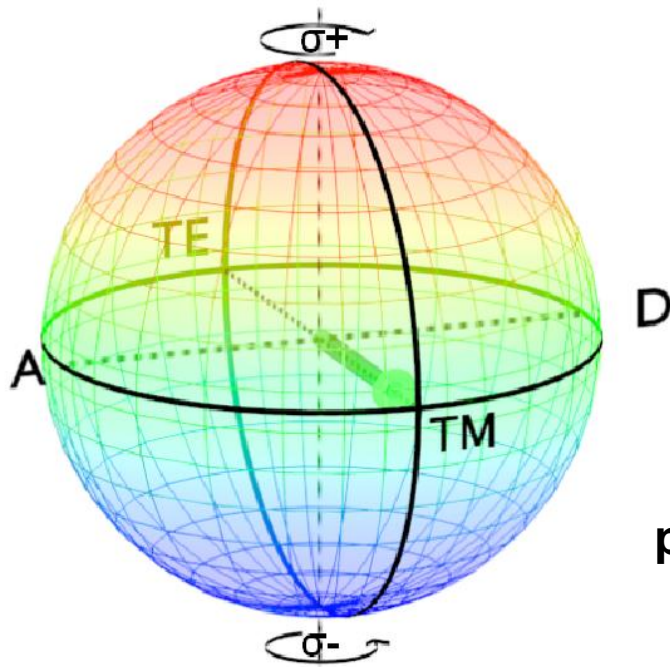
Exciton : $J_z = \pm 1$ $e \uparrow \downarrow h$ $e \downarrow \uparrow h$
 $J_z = \pm 2$ $e \uparrow \uparrow h$ $e \downarrow \downarrow h$

→ Photon have an angular momentum : ± 1

→ Only $J=1$ excitons are coupled to light

Polaritons have two spin projections:

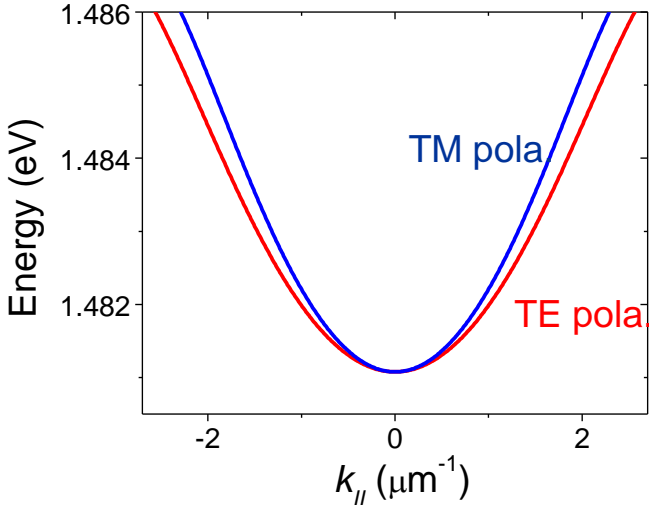
$j_z = +1$ σ^+
 $j_z = -1$ σ^- } $\frac{1}{2}$ pseudospin



One-to-one relationship between pseudospin state and polarisation degree

Polariton spin: Intrinsic magnetic field

Cavity modes linearly polarized: TE-TM splitting

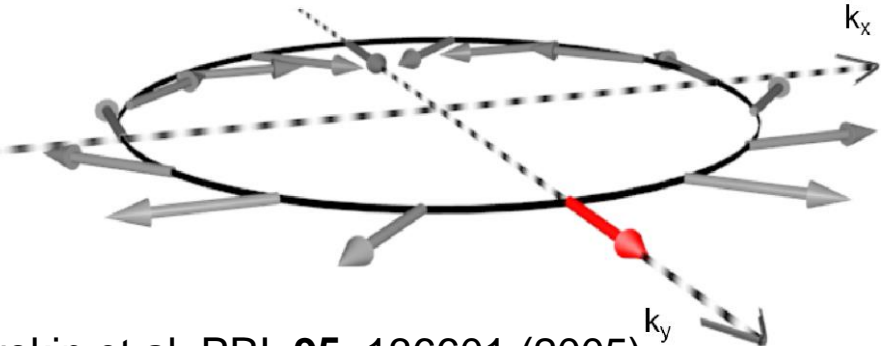


boundary conditions for the electromagnetic field at the interface of the different dielectric layers

Effective magnetic field $\mathbf{H}_{\text{eff}} = \frac{\hbar}{\mu_B g} \boldsymbol{\Omega}_{\mathbf{k}}$

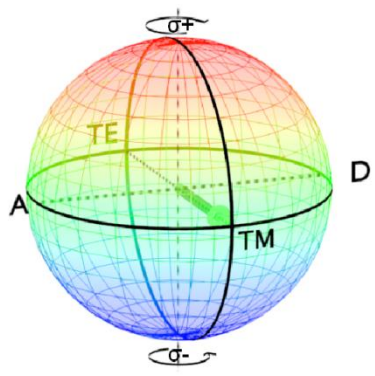
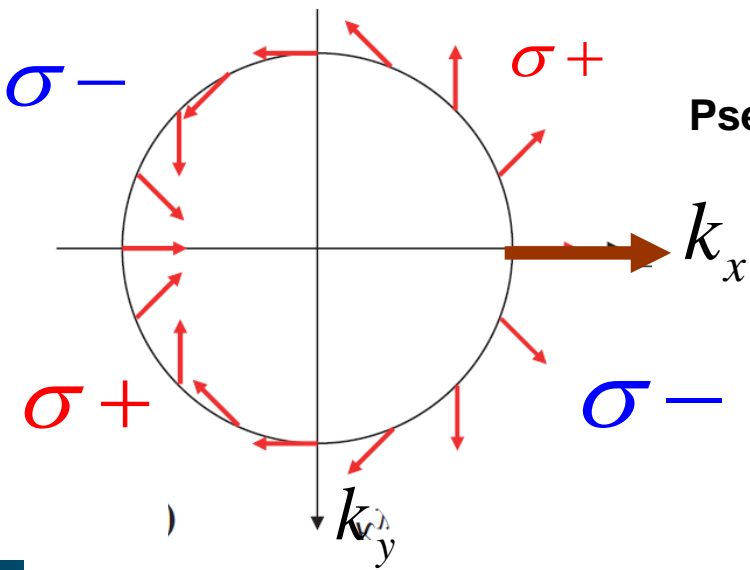
$$\Omega_x = \frac{\Omega}{k^2} (k_x^2 - k_y^2), \quad \Omega_y = 2 \frac{\Omega}{k^2} k_x k_y,$$

$$\Omega = \frac{\Delta_{\text{LT}}}{\hbar}$$



Kavokin et al. PRL **95**, 136601 (2005)

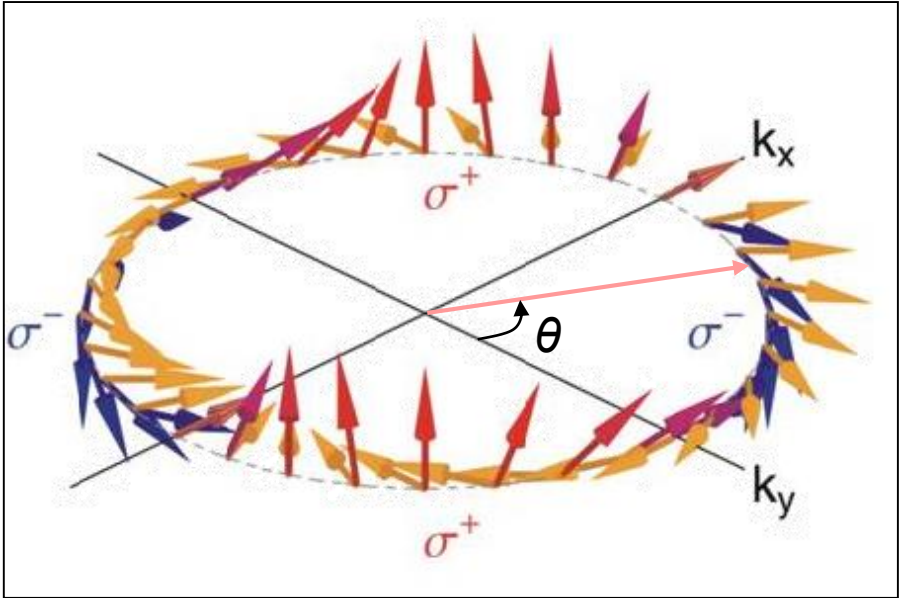
Optical spin Hall effect



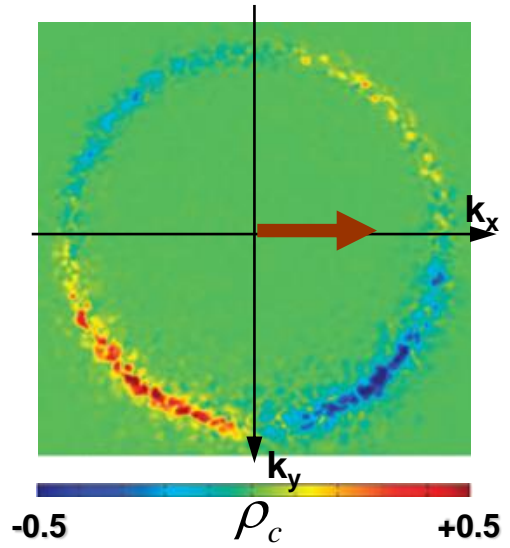
$$\frac{\partial \vec{S}}{\partial t} = \vec{S} \wedge \vec{\Omega}(\theta) + \frac{\vec{S}_0}{\tau_1} - \frac{\vec{S}}{\tau}$$



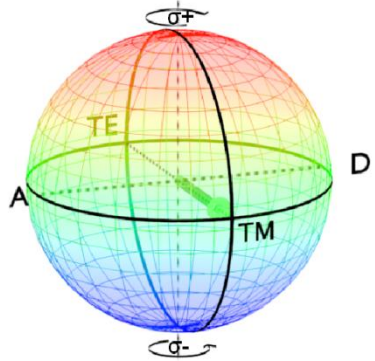
Optical spin Hall effect



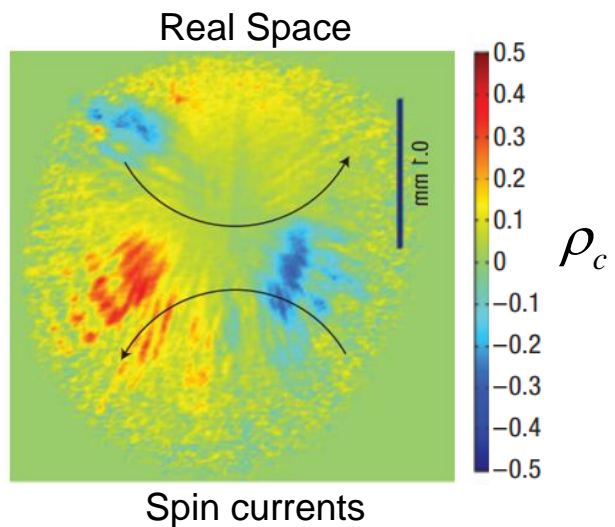
$\tau_{pol} = 10ps$



Kavokin et al. PRL **95**, 136601 (2005)
 Leyder et al. Nature Phys. **3**, 628 (2007).

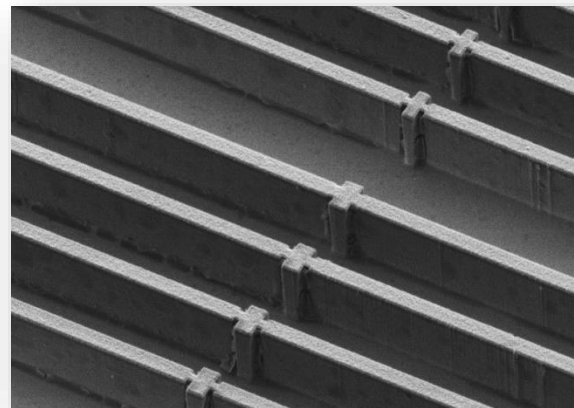
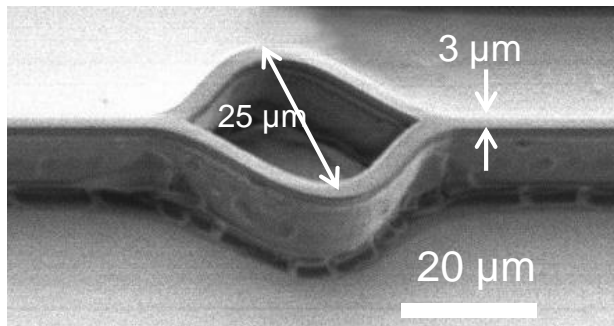
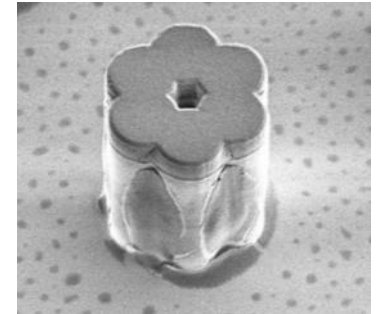
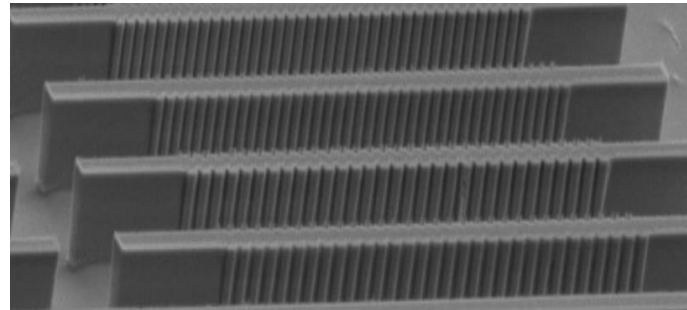
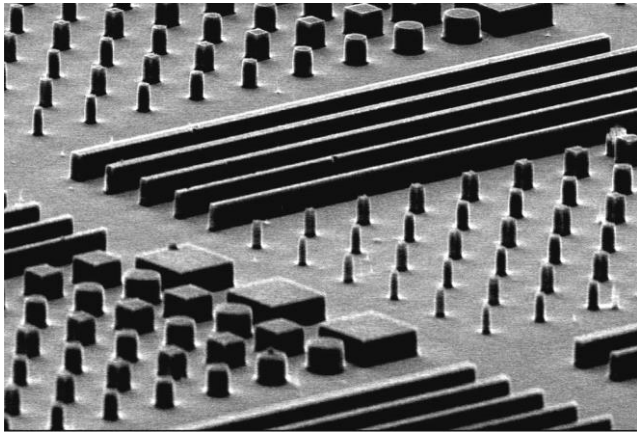


$$\frac{\partial \vec{S}}{\partial t} = \vec{S} \wedge \vec{\Omega}(\theta) + \frac{\vec{S}_0}{\tau_1} - \frac{\vec{S}}{\tau}$$



Cavity polariton in microstructures

Use of nanotechnology to engineer the potential landscape
Polaritonic circuits and quantum simulation

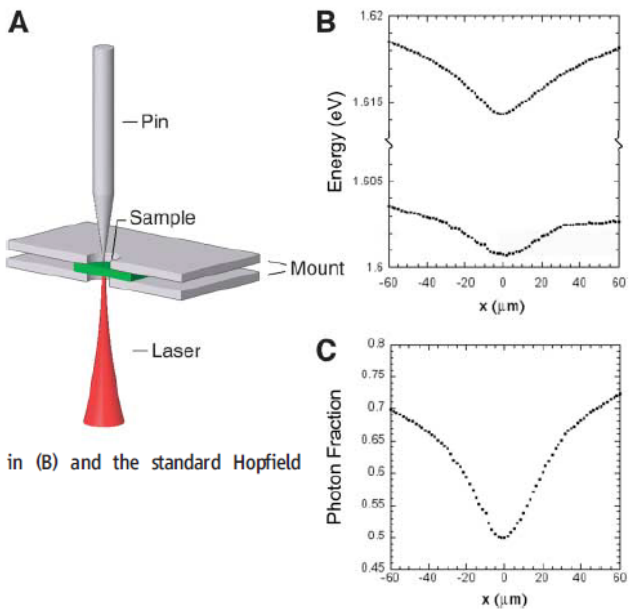


Polariton confinement

$$|pol\rangle = C_k |phot\rangle + X_k |exc\rangle \quad \text{excitonic component}$$

Pressure induced traps Snoko's group

Fig. 1. (A) Stress geometry for the microcavity structure. (B) Upper and lower polariton energies (top and bottom traces, respectively), deduced from photoluminescence and reflectivity spectra at very low excitation density and low lattice temperature ($T = 4$ K), when a force of 0.975 N on the pin stressor is applied to the sample. (C) Photon fraction of the lower polariton branch as a function of position in the trap, calculated from the polariton energies shown in (B) and the standard Hopfield coefficients.

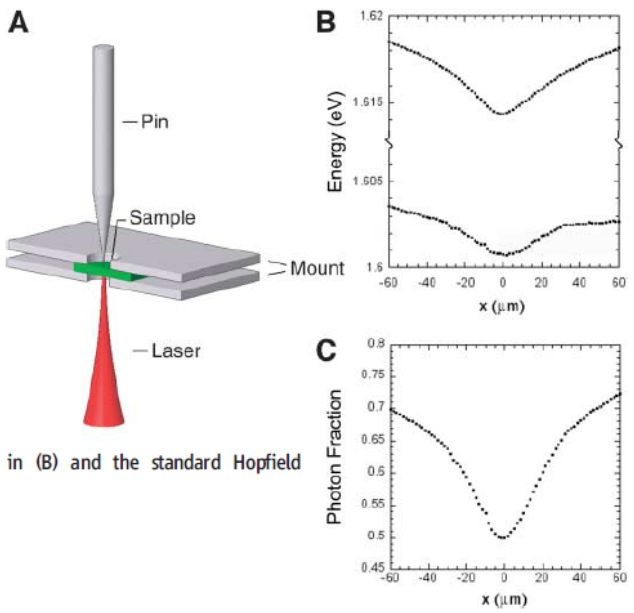


Polariton confinement

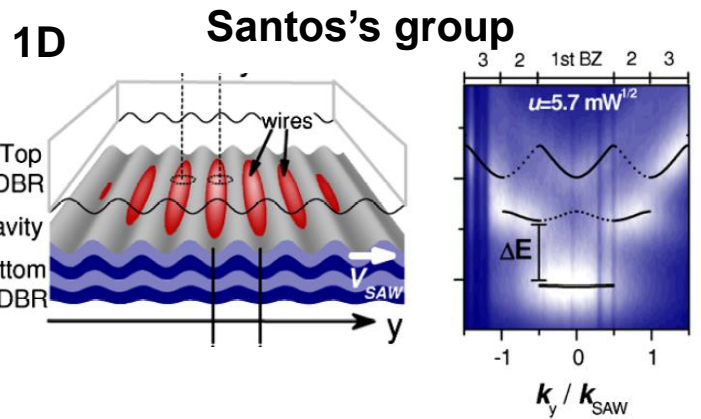
$$|pol\rangle = C_k |phot\rangle + X_k |exc\rangle \quad \text{excitonic component}$$

Pressure induced traps Snoke's group

Fig. 1. (A) Stress geometry for the microcavity structure. (B) Upper and lower polariton energies (top and bottom traces, respectively), deduced from photoluminescence and reflectivity spectra at very low excitation density and low lattice temperature ($T = 4$ K), when a force of 0.975 N on the pin stressor is applied to the sample. (C) Photon fraction of the lower polariton branch as a function of position in the trap, calculated from the polariton energies shown in (B) and the standard Hopfield coefficients.

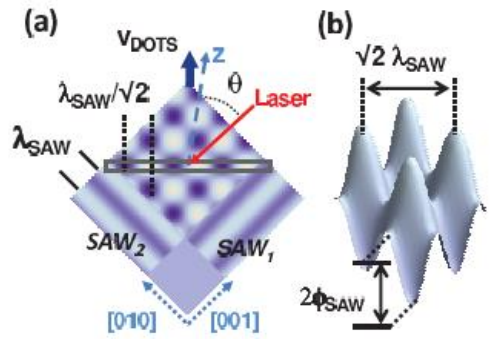


Surface acoustic waves



Cerda-Méndez *et al.*, PRL **105**, 116402 (2010)
de Lima *et al.*, PRL **97**, 045501 (2006)

2D



Cerda-Méndez *et al.* PRB **86**, 100301(R) (2012)

Balili *et al.*, Science **316**, 1007 (2007)

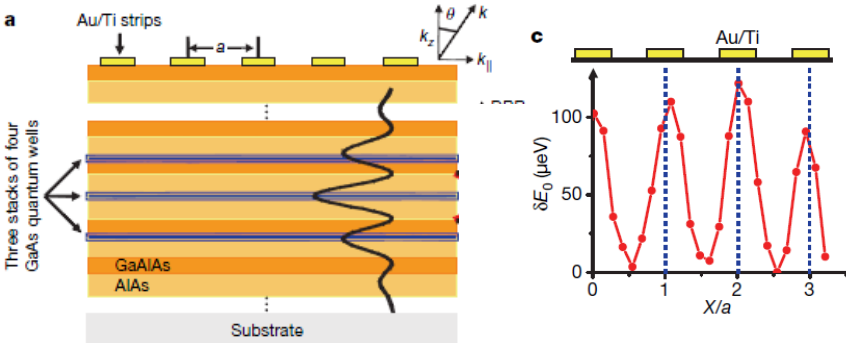
Polariton confinement

$$|pol\rangle = C_k |phot\rangle + X_k |exc\rangle \quad \text{photonic component}$$



Metal deposition

Metallic deposition



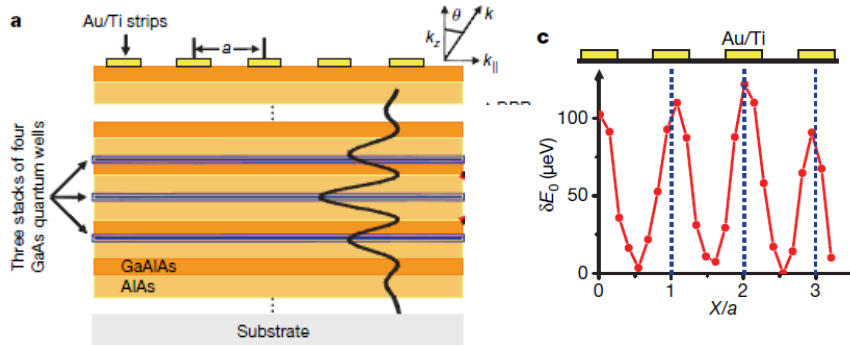
Yamamoto's group

➡ Optical potential: up to 200 μeV



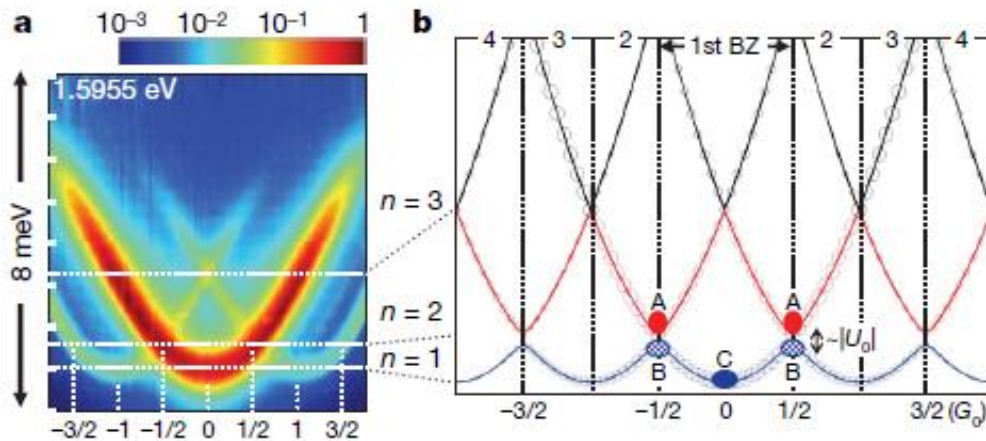
Metal deposition

Metallic deposition



1D array

π -wave condensation

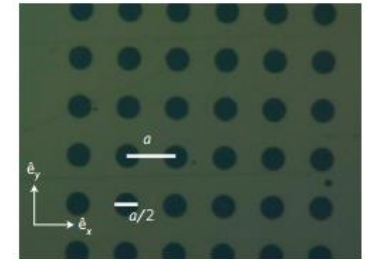


Lai et al., Nature **450**, 529 (2007)

Yamamoto's group

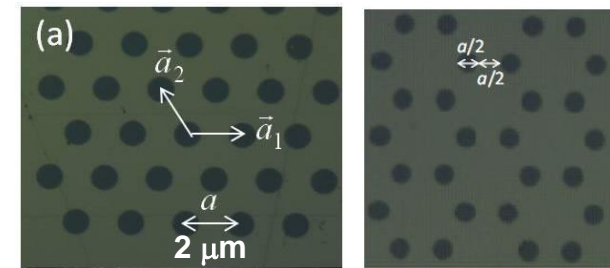
➔ Optical potential: up to 200 μeV

2D square lattice



Kim et al., Nature Phys **7**, 681 (2011)

Other 2D lattices



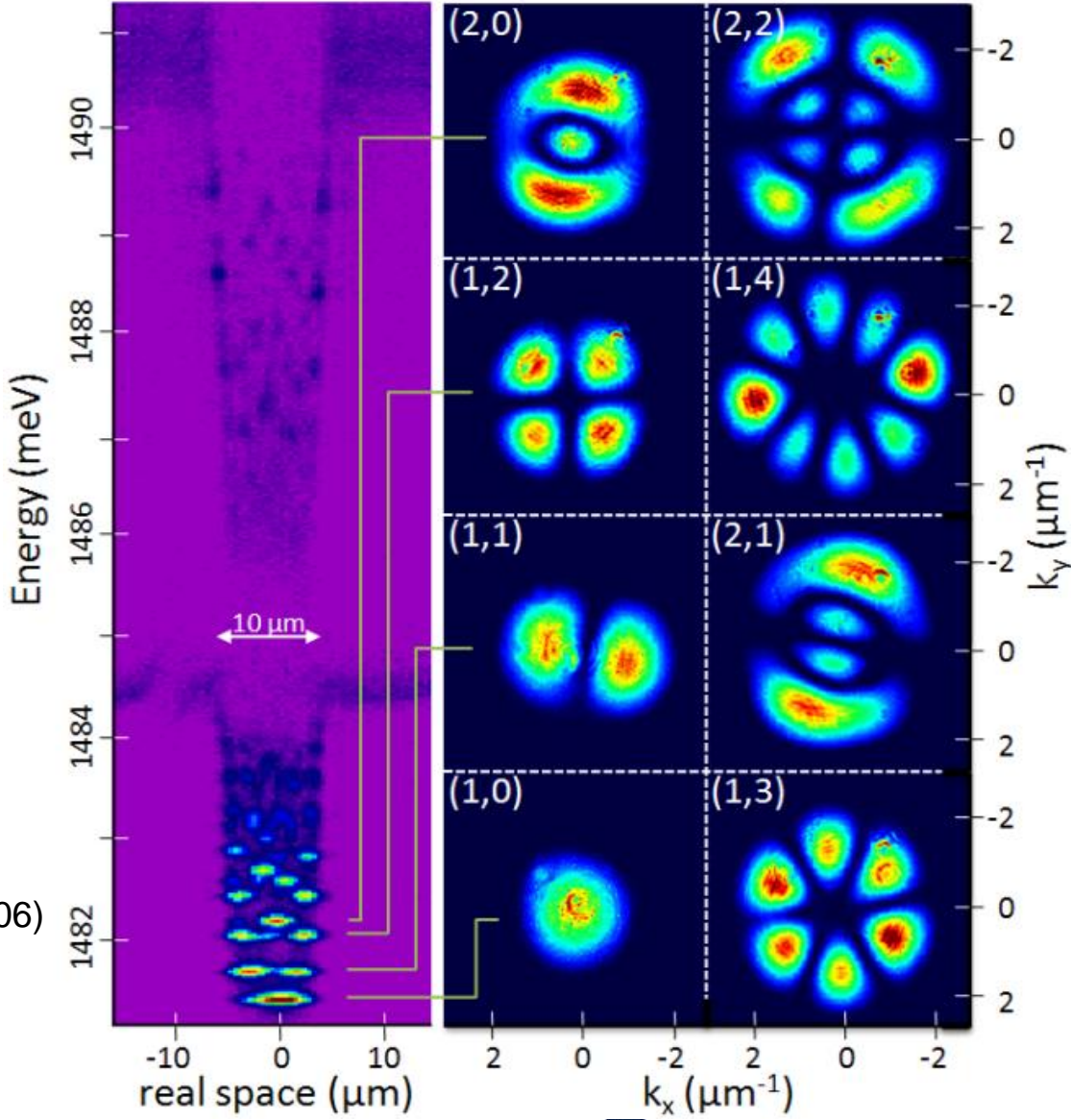
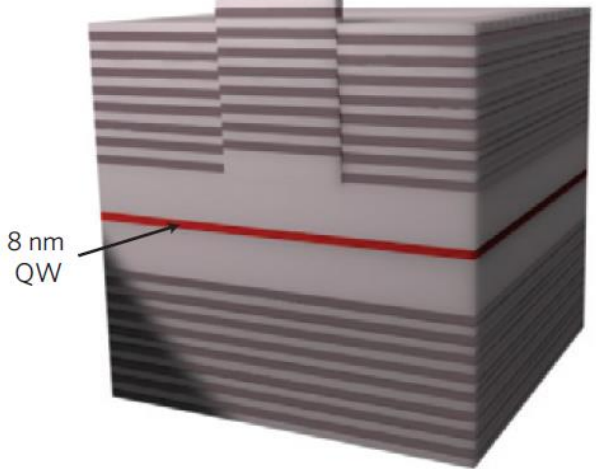
Kim et al., arXiv:1210.2153

Kusudo et al., arXiv:1211.3833

During-growth photonic trap

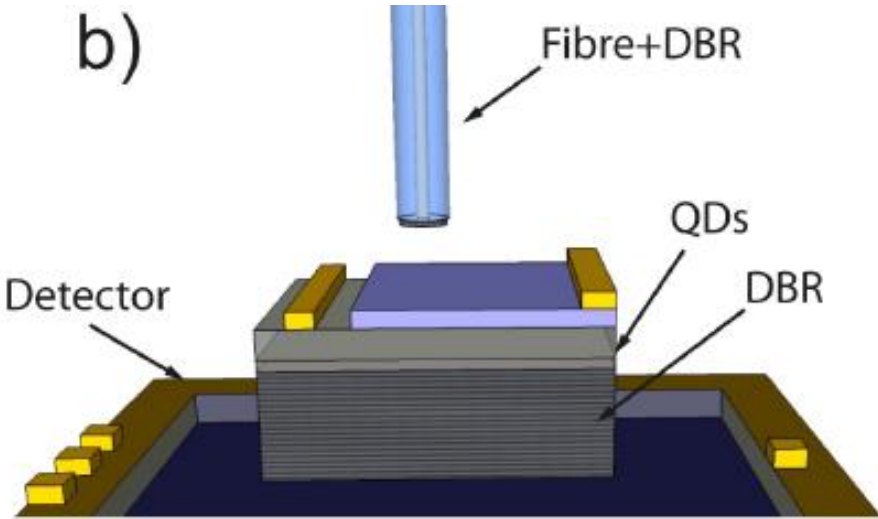
Deveaud's group at EPFL

6-nm-high mesa, \varnothing 3 μm



El Daïf et al., APL **88**, 061105 (2006)
Idrissi Kaitouni et al., PRB **74**, 155311 (2006)
Cerna et al., PRB **80**, 121309 (2009)

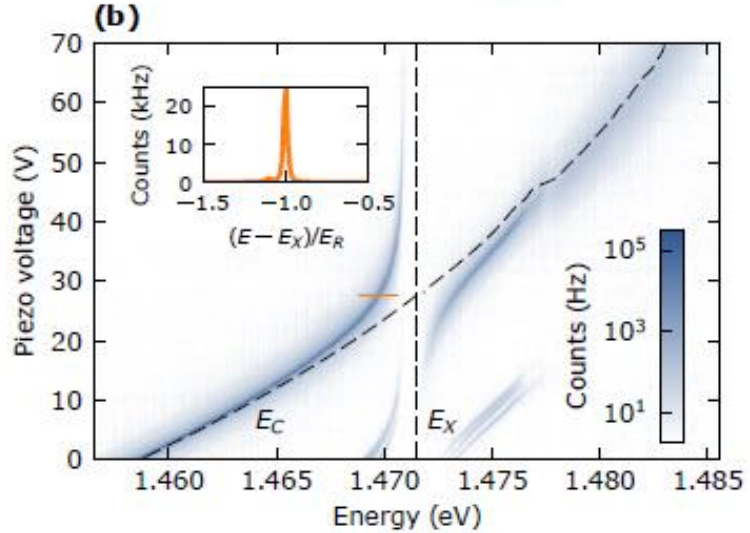
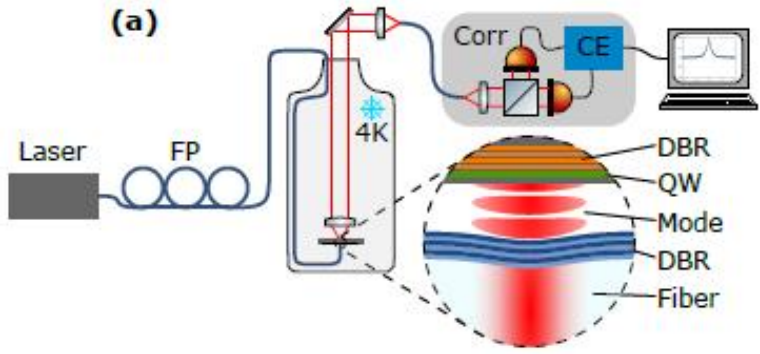
Hybrid cavities



Besga et al., Light: S&A 3, e135 (2014)
 S. Dufferwiel et al. Appl. Phys. Lett. 104, 192107 (2014)
 Also T. Fink et al., arXiv:1707.01837

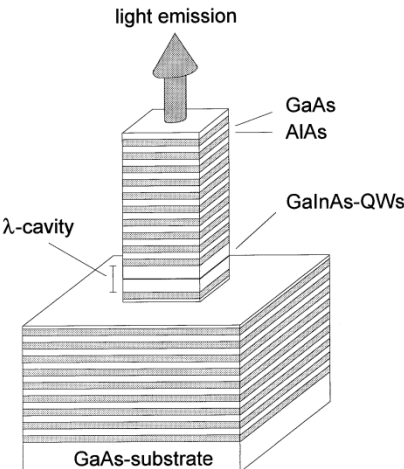
Fiber-closed cavity

Imamoglu, Reichel,

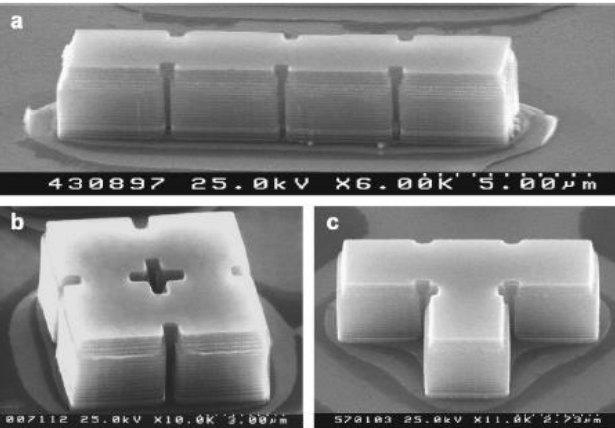
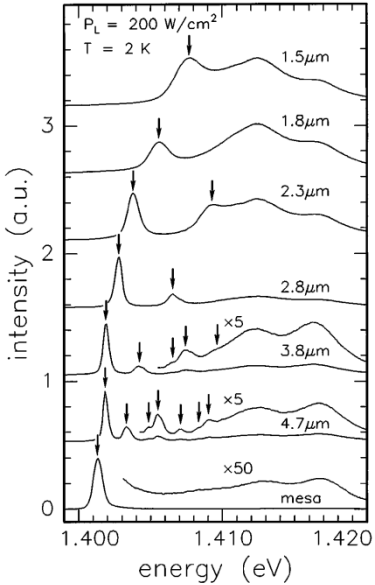


Post-growth etching

Bayer-Forchel



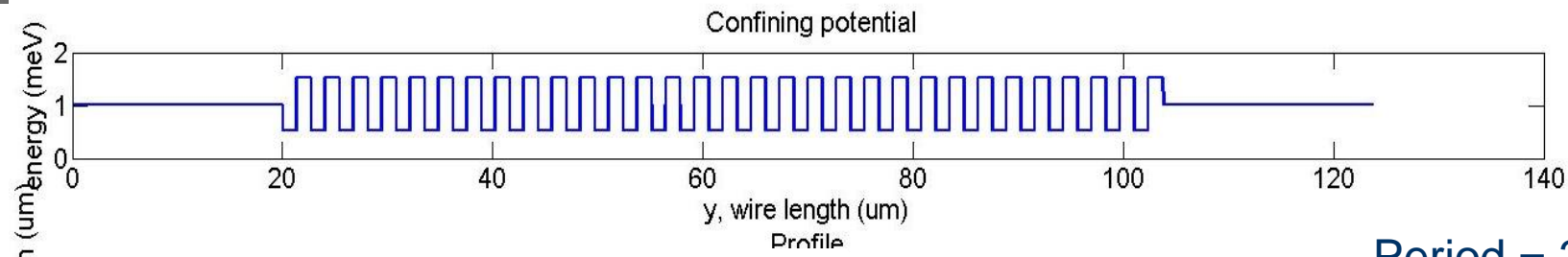
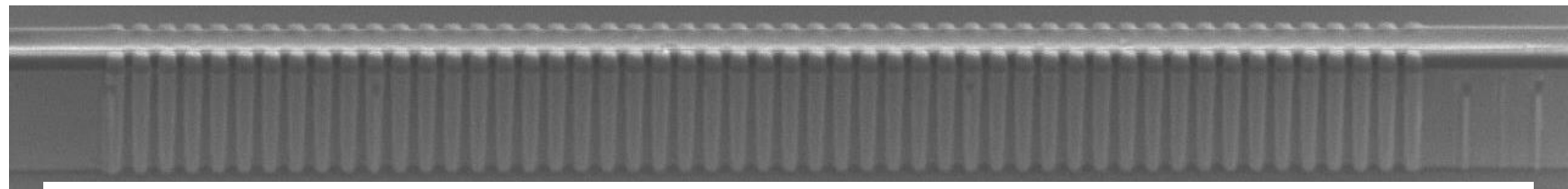
Reithmaier et al., PRL **78**, 378 (1997)



Gutroff et al., PRE **63**, 036611 (2001)

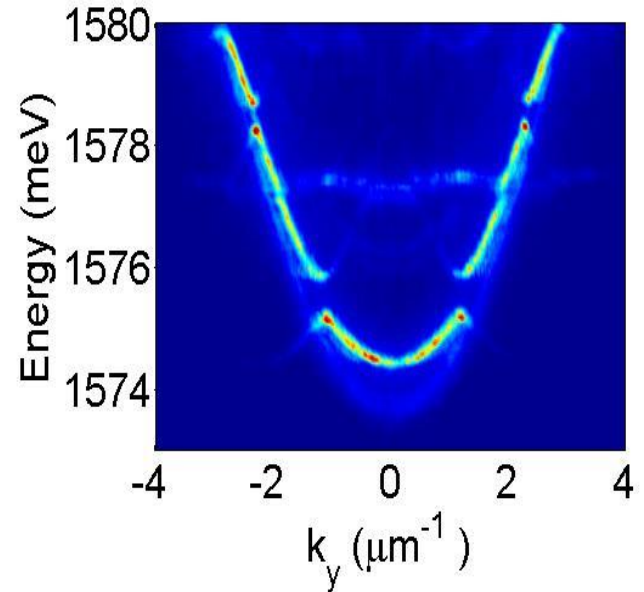
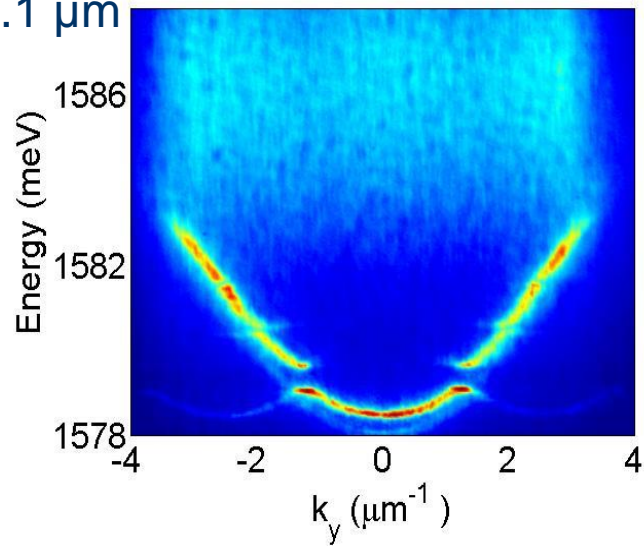
- ➡ Quasi infinite barrier
- ➡ Sub micrometer resolution

1D Periodic potential



Period = 2.7 μm

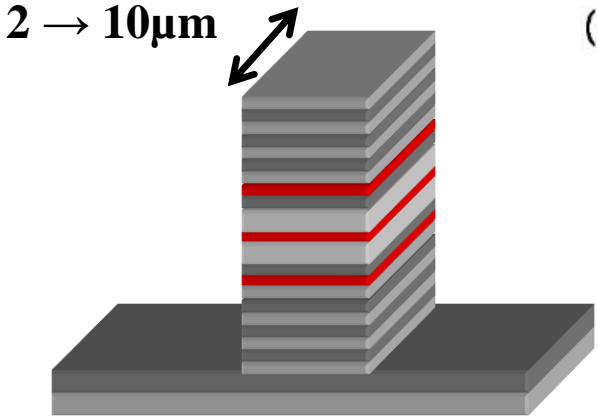
Period = 2.1 μm



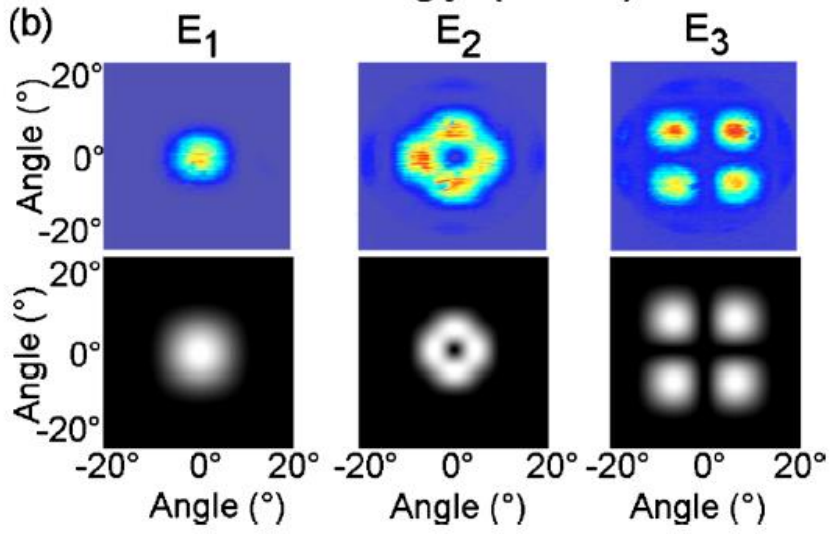
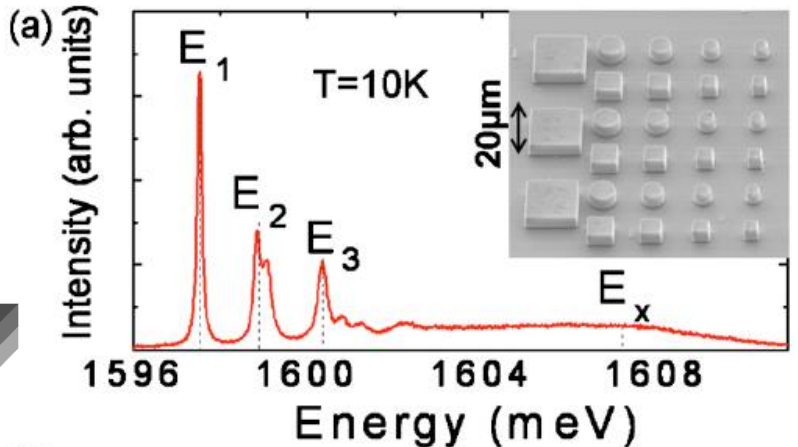
Other methods:
Metallic pattern : Lai et al., Nature **450**, 529 (2007)
SAW :E. A. Cerda-Méndez, PRL (2010).

Polaritons in micropillars

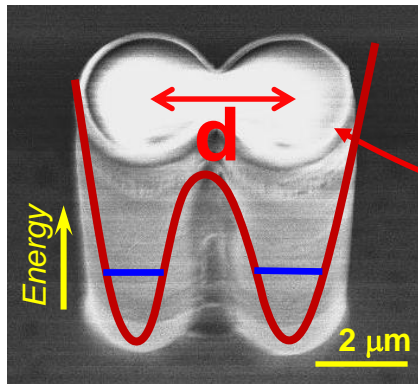
Micropillars: photonic atoms



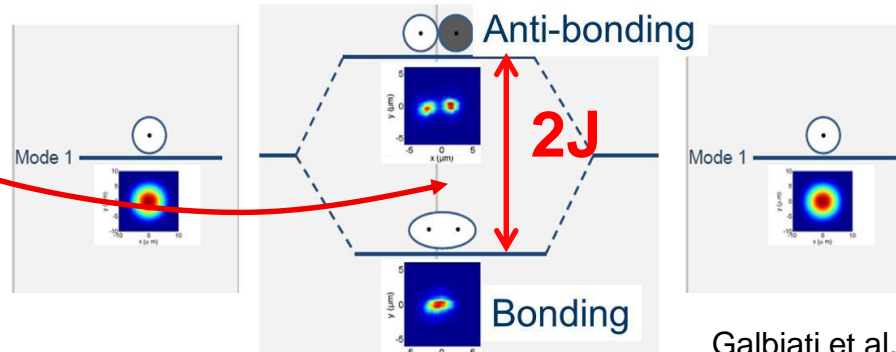
$$k_x = p_x \pi / L_x$$
$$k_y = p_y \pi / L_y$$



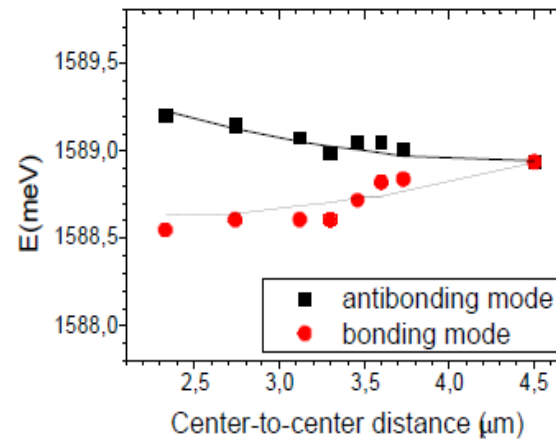
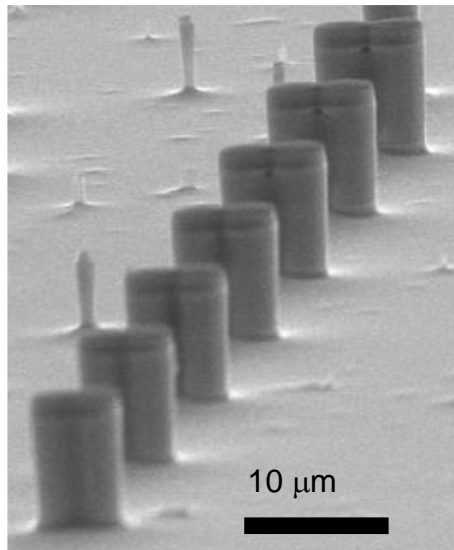
Two coupled micropillars



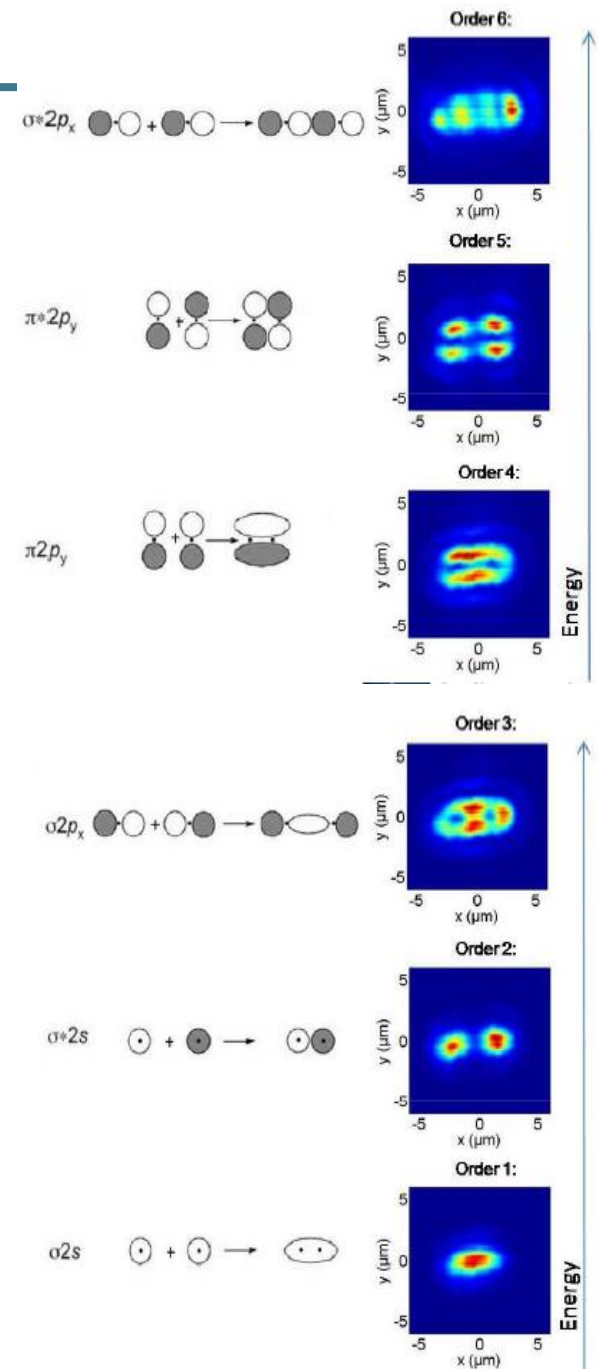
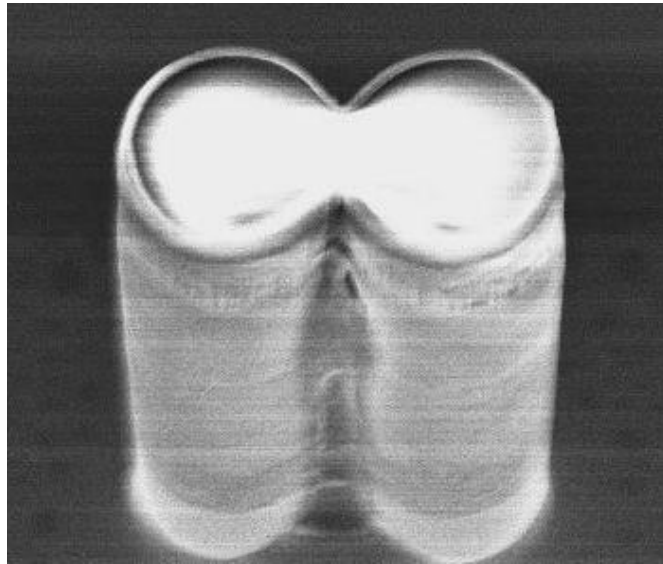
Michaelis de Vasconcellos et al., APL **99**, 101103 (2011)



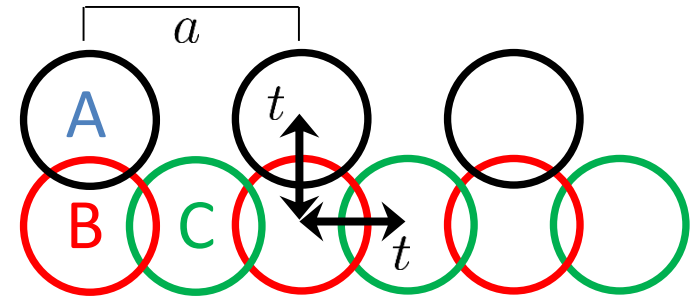
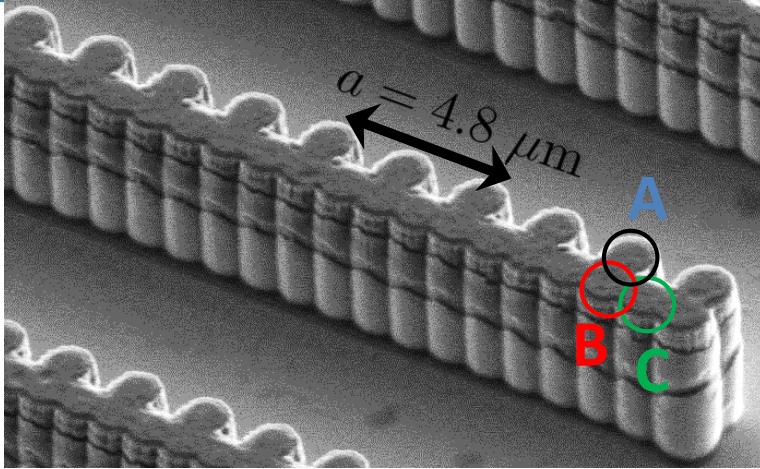
Galbiati et al., PRL **108**, 126403 (2012)



Hybridization of the p-states in a photonic molecule



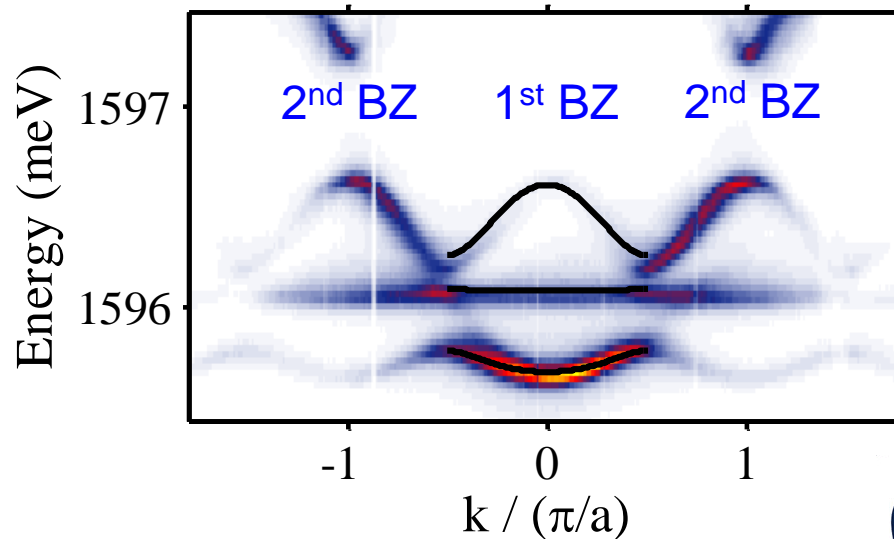
Engineering of a 1D flat band : 1D Lieb lattice



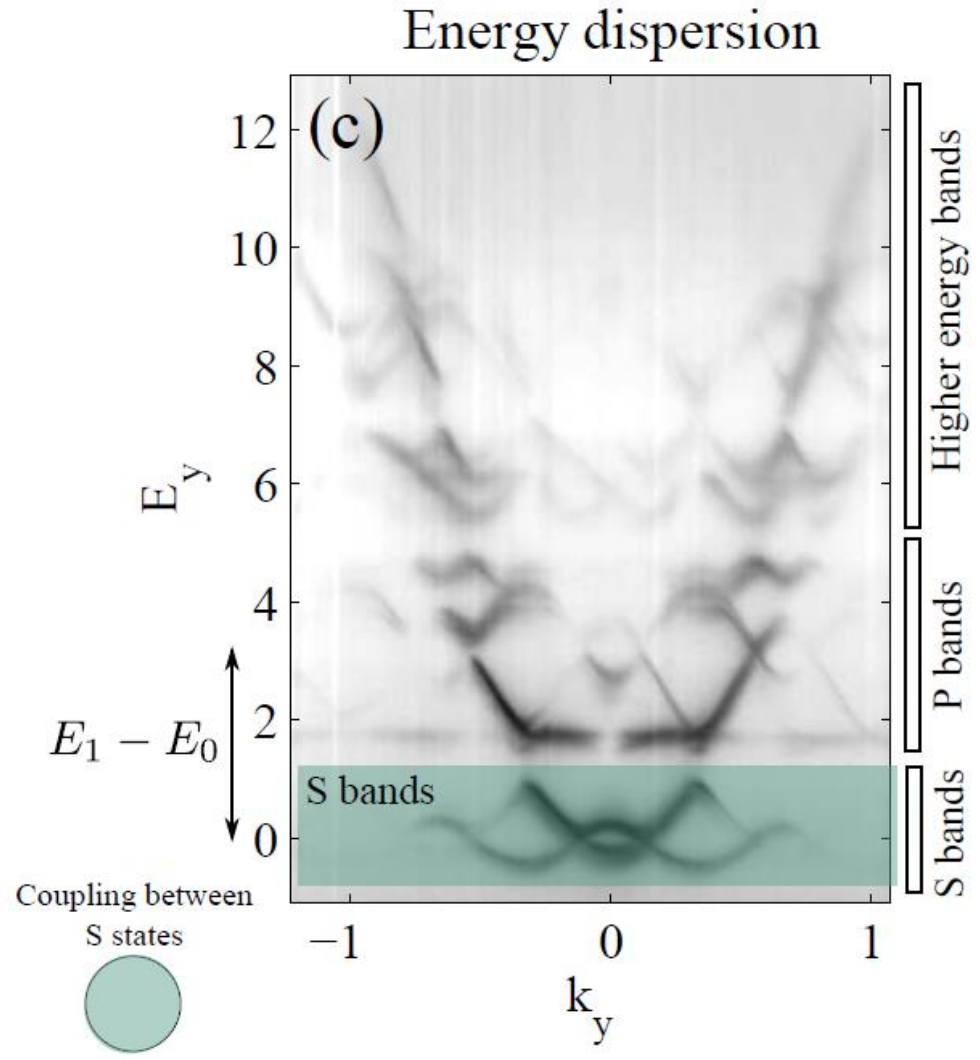
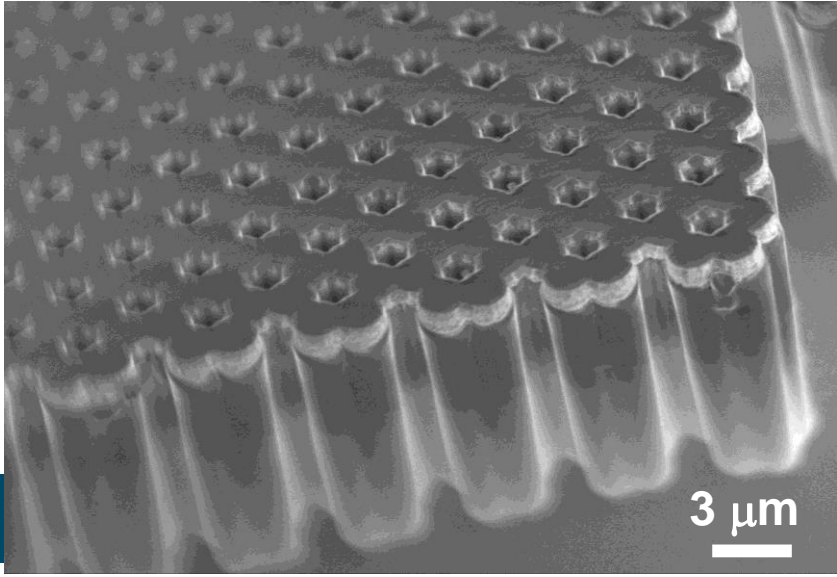
See e.g. Hyrkäs et al., PRA **87**, 023614 (2013)

Pillar diameter = $3 \mu\text{m}$
Interpillar distance = $2,4 \mu\text{m}$

Far field emission



Polariton in honeycomb lattices: Dirac cones



Cavity polaritons : an exciton-photon mixed state

$$|\text{polariton}\rangle = \alpha |\text{photon}\rangle + \beta |\text{exciton}\rangle$$

α^2 photon part

Coupling to free space optical modes

Low effective mass

β^2 exciton part

Polariton-phonon Interactions
Polariton-polariton Interactions

Properties

- Photonic component \rightarrow low mass ($10^{-5} m_e$)
- Short lifetime (\sim ps) \rightarrow escape out of the cavity
- Pseudo spin
- Excitonic component \rightarrow strong non-linearity
- Bosons

Polariton-polariton interaction

Exciton-exciton interaction

Exciton wavefunction:

$$\Psi_Q(\mathbf{r}_e, \mathbf{r}_h) = \frac{1}{\sqrt{A}} \exp[iQ \cdot (\beta_e \mathbf{r}_e + \beta_h \mathbf{r}_h)]$$
$$\times \sqrt{\frac{2}{\pi \lambda_{2D}}} \exp\left(-\frac{|\mathbf{r}_e - \mathbf{r}_h|}{\lambda_{2D}}\right),$$

Spin : electron : $\pm \frac{1}{2}$
heavy hole : $\pm \frac{3}{2}$

Exciton : $J = \pm 1$ $e \uparrow \downarrow h$ $e \downarrow \uparrow h$
 $J = \pm 2$ $e \uparrow \uparrow h$ $e \downarrow \downarrow h$

Polariton-polariton interaction

Exciton-exciton interaction

PHYSICAL REVIEW B

VOLUME 58, NUMBER 12

15 SEPTEMBER 1998-II

Role of the exchange of carriers in elastic exciton-exciton scattering in quantum wells

C. Ciuti, V. Savona, C. Piermarocchi, and A. Quattropani
Institut de Physique Théorique, Ecole Polytechnique Fédérale, CH-1015 Lausanne, Switzerland

P. Schwendimann
Defense Procurement, System Analysis Division, CH-3003 Bern, Switzerland
(Received 15 December 1997)

Two Excitons:

$$H = -\frac{\hbar^2}{2m_e} \nabla_e^2 - \frac{\hbar^2}{2m_h} \nabla_h^2 - \frac{\hbar^2}{2m_e} \nabla_{e'}^2 - \frac{\hbar^2}{2m_h} \nabla_{h'}^2 - V(|\mathbf{r}_e - \mathbf{r}_h|) - V(|\mathbf{r}_{e'} - \mathbf{r}_{h'}|) + \underline{V(|\mathbf{r}_e - \mathbf{r}_{e'}|)} + \underline{V(|\mathbf{r}_h - \mathbf{r}_{h'}|)} - \underline{V(|\mathbf{r}_e - \mathbf{r}_{h'}|)} - \underline{V(|\mathbf{r}_h - \mathbf{r}_{e'}|)}, \quad (5)$$

$$H = H_0(\text{exc1}) - H_0(\text{exc2}) - W$$

Polariton-polariton interaction

Exciton-exciton interaction

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Exc 1 Exc 1

$$(1s, \mathbf{Q}, S) + (1s, \mathbf{Q}', S') \rightarrow (1s, \mathbf{Q} + \mathbf{q}, S_f) + (1s, \mathbf{Q}' - \mathbf{q}, S'_f).$$

$$H_{SS'}^{S_f S'_f}(\mathbf{Q}, \mathbf{Q}', \mathbf{q}) = \langle S | S_f \rangle \langle S' | S'_f \rangle H_{\text{dir}}(\mathbf{Q}, \mathbf{Q}', \mathbf{q}) \quad \text{Direct term}$$

$$+ \langle S | S'_f \rangle \langle S' | S_f \rangle H_{\text{exch}}^X(\mathbf{Q}, \mathbf{Q}', \mathbf{q}) \quad \text{Exchange of both electrons and holes}$$

$$+ \mathcal{S}_{\text{exch}}^e(S, S', S_f, S'_f) H_{\text{exch}}^e(\mathbf{Q}, \mathbf{Q}', \mathbf{q})$$

Exchange of electrons

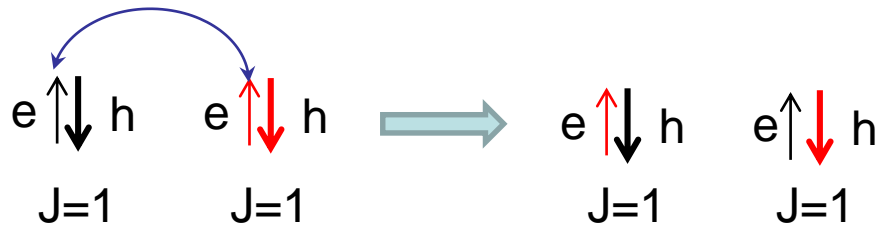
$$+ \mathcal{S}_{\text{exch}}^h(S, S', S_f, S'_f) H_{\text{exch}}^h(\mathbf{Q}, \mathbf{Q}', \mathbf{q}).$$

Exchange of holes

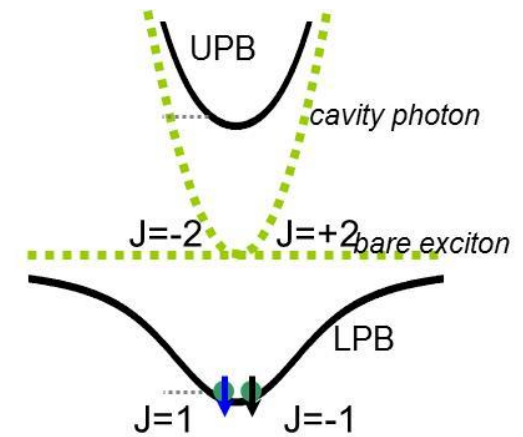
Dominant terms

Spin dependant polariton-polariton interaction

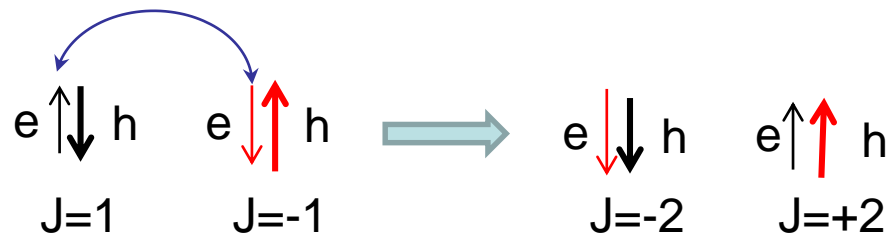
Interactions between 2 polaritons with **parallel** spins :



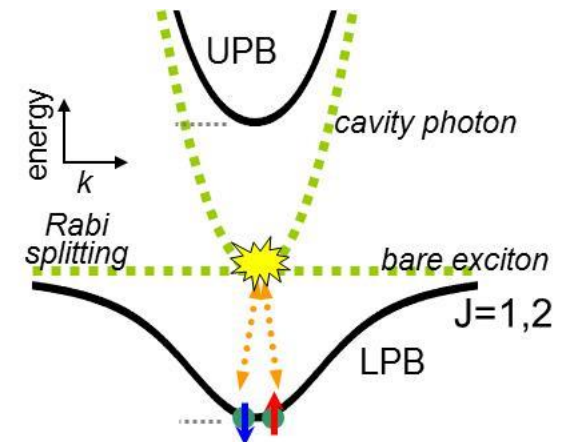
Resonant term



Interactions between 2 polaritons with **opposite** spins :



Non Resonant term => much weaker



Wouters, PRB 76, 045319 (2007)

Schumacher *et al.*, PRB 76, 245324 (2007)

Spin dependent polariton-polariton interaction

Parallel spin : resonant process: **Strong and Repulsive interaction**

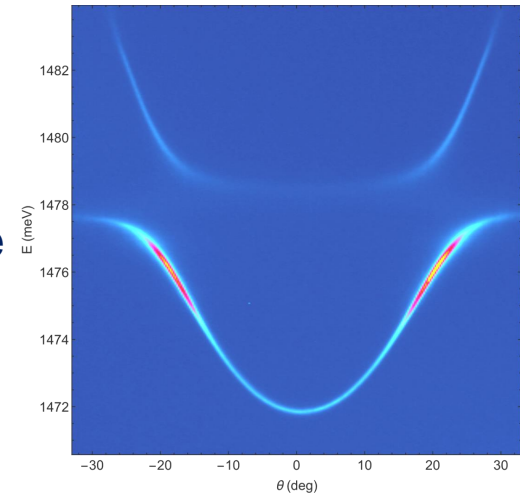
Anti-parallel : via dark exciton intermediate states: **Weaker and attractive interaction**

$$|\alpha_{\uparrow\uparrow}\rangle \gg |\alpha_{\uparrow\downarrow}\rangle$$

Interactions : a tool to manipulate polaritons
highly non-linear system
spin dependant

Summary

- Hybrid exciton-photon quasi-particles
- Tunable properties : lifetime, effective mass
- Lateral confinement : engineering of band structure
- Optical access to all physical properties



Why so interesting ? Because of interactions, strong non-linearity

- Spin dependent polariton polariton interactions
- Repulsive polariton-exciton interactions

Outline

Lecture 1 : **Introduction to cavity polaritons**

- Hybrid light-matter quasi-particle: basic properties
- Confinement in microstructures
- Interactions

II Lecture 2: **Polariton condensation; Quantum fluids of light**

Coherence; Instability; Superfluidity; solitons

III Lecture 3: **Polariton in lattices : quantum simulation**

- 1D Fibonacci quasi-crystals: fractal spectrum, edge states
- 1D SSH : topological laser
- 2D Honeycomb lattice: Dirac cones, edge states