

# Phase Separation of Fluids in Confined Geometry – Partial and Complete Wetting

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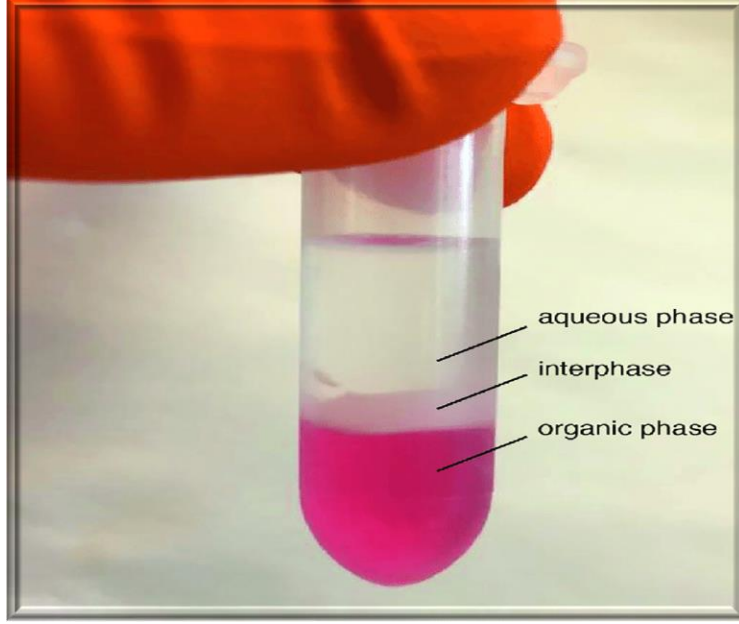
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# What is Phase Separation?

**RBC and Plasma**



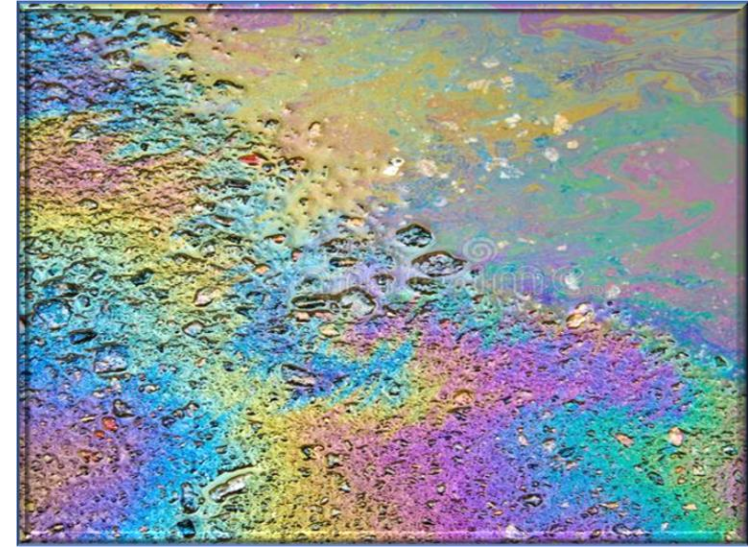
**Oil and Vinegar**



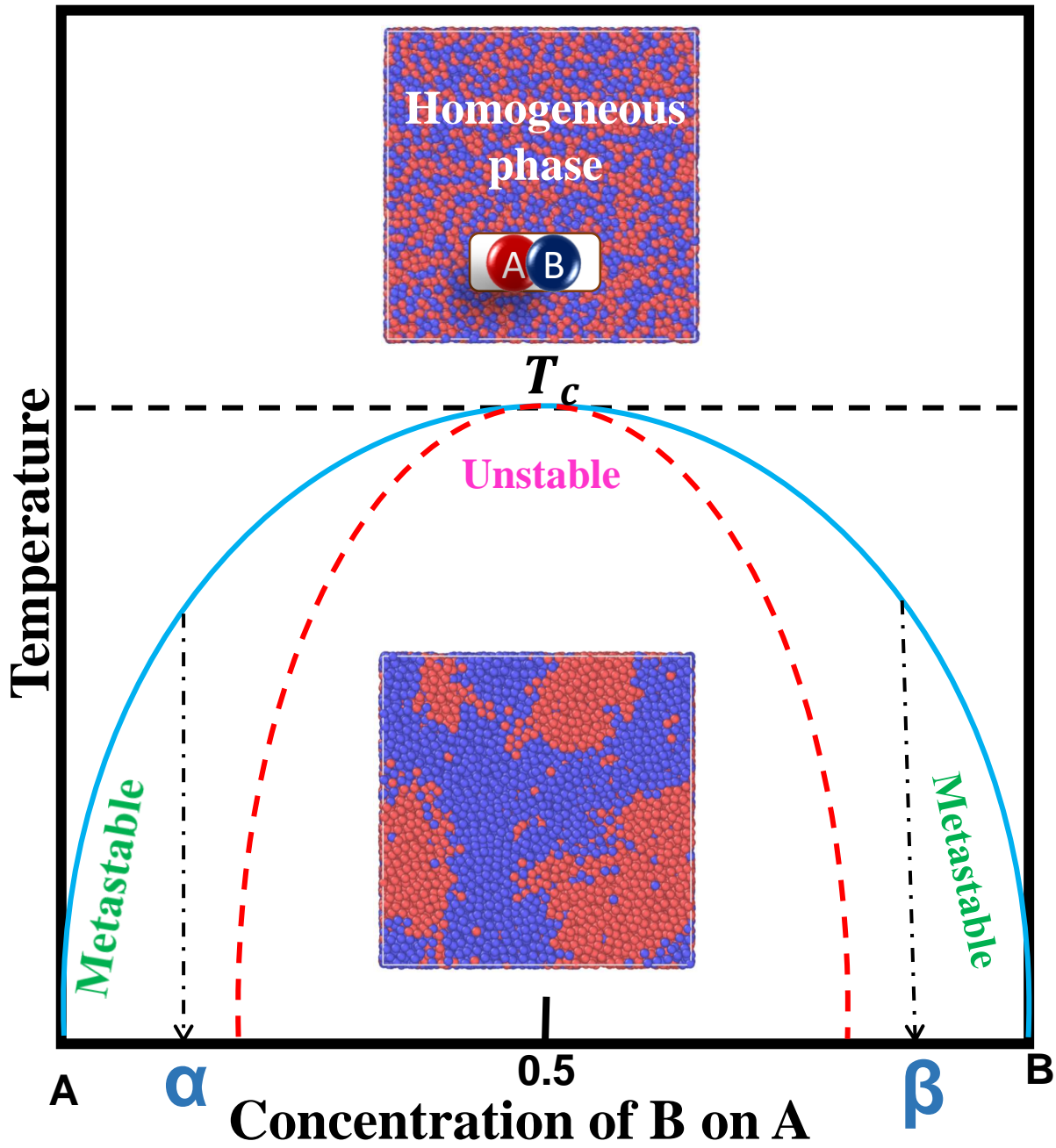
**Water and Oil**



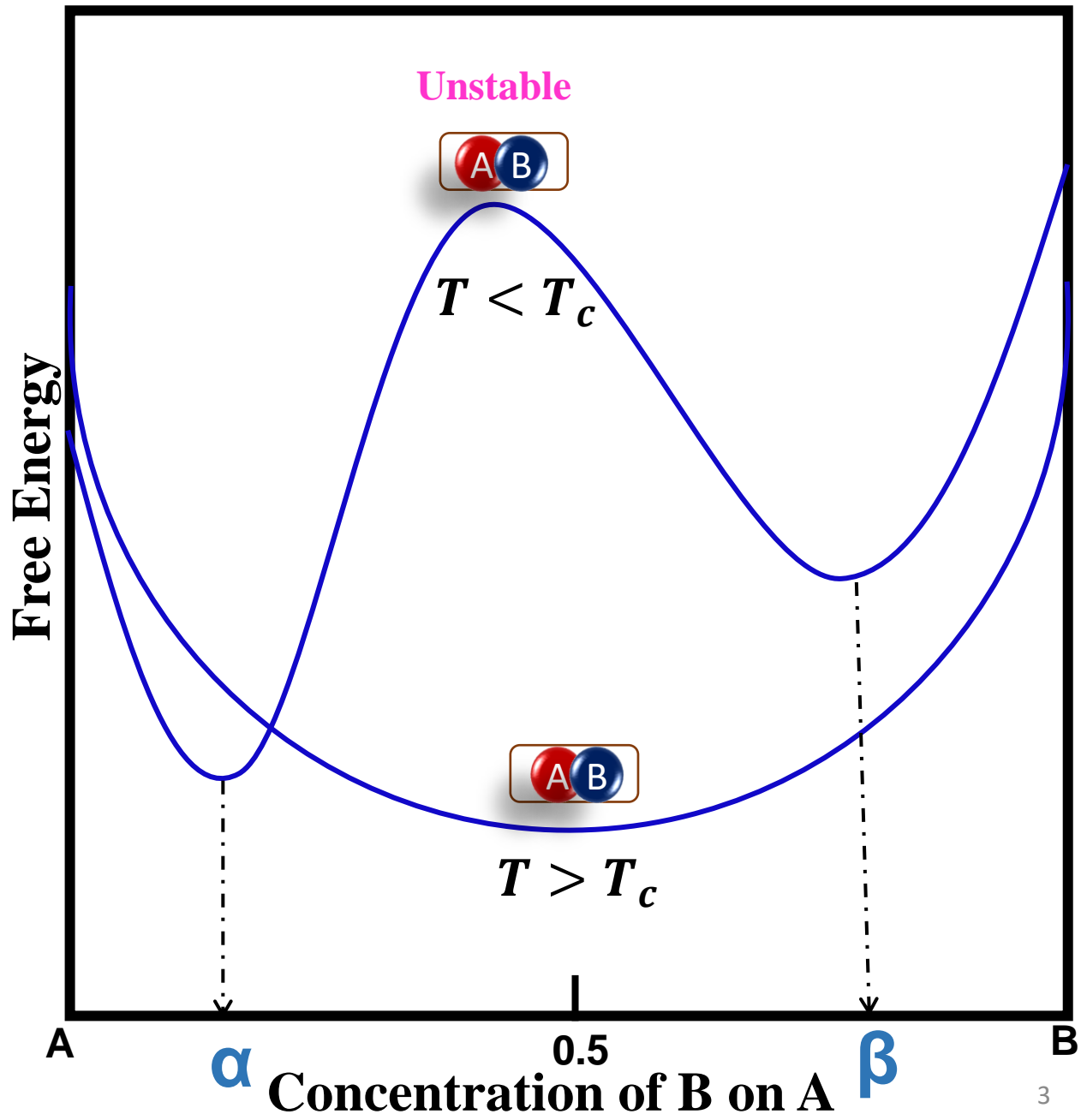
**Petrol and Water**



# Phase Diagram

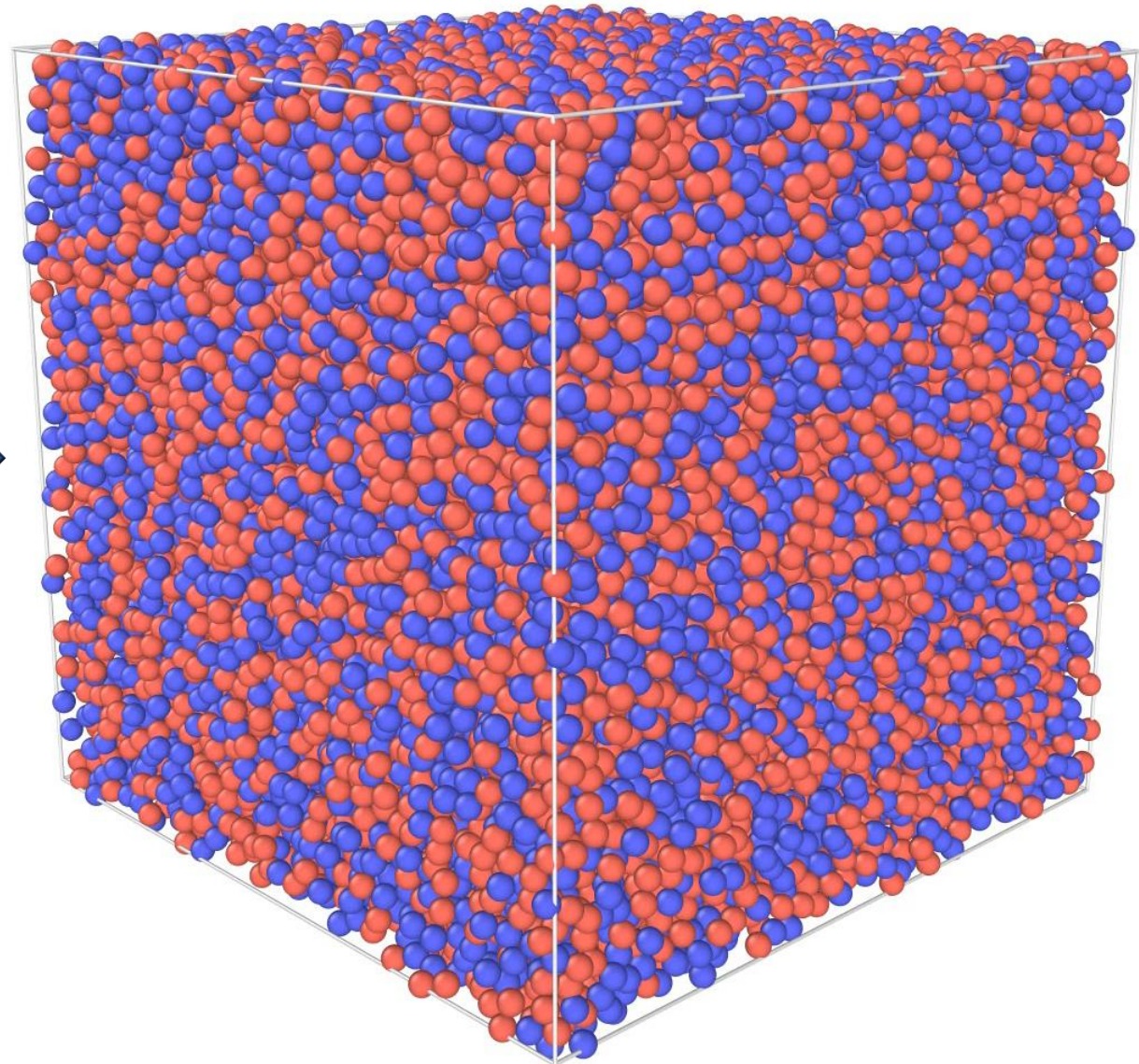
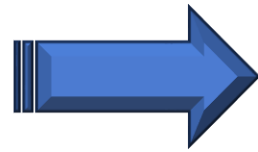


# Free Energy profile





# Phase Separation of Fluid Mixtures – Computer Simulation

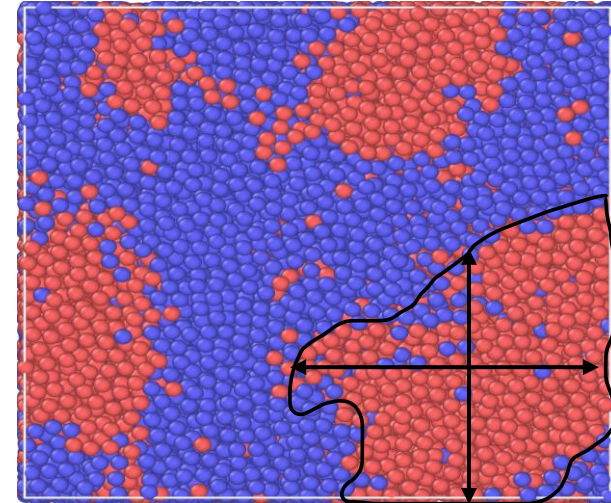


# DOMAIN Size Estimation

- **Domain size** (Length scale)  $\sim l(t)$

$$l(t) \sim A * t^\alpha$$

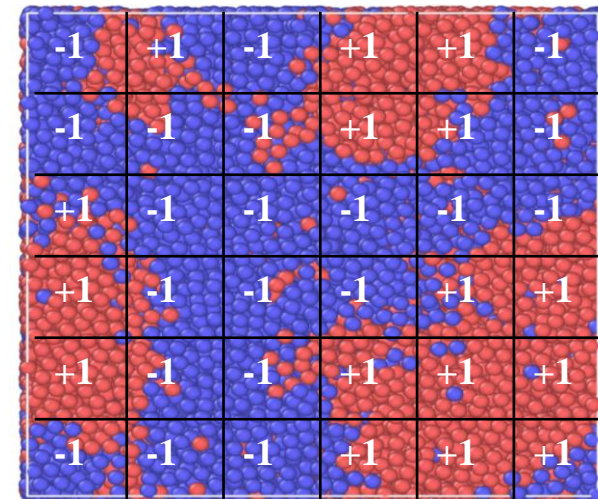
$\alpha$  = growth exponent, A = Pre-factor



- **Order parameter**

$$\varphi = \frac{N_A - N_B}{N_A + N_B} \quad \varphi = \{+1, -1\}$$

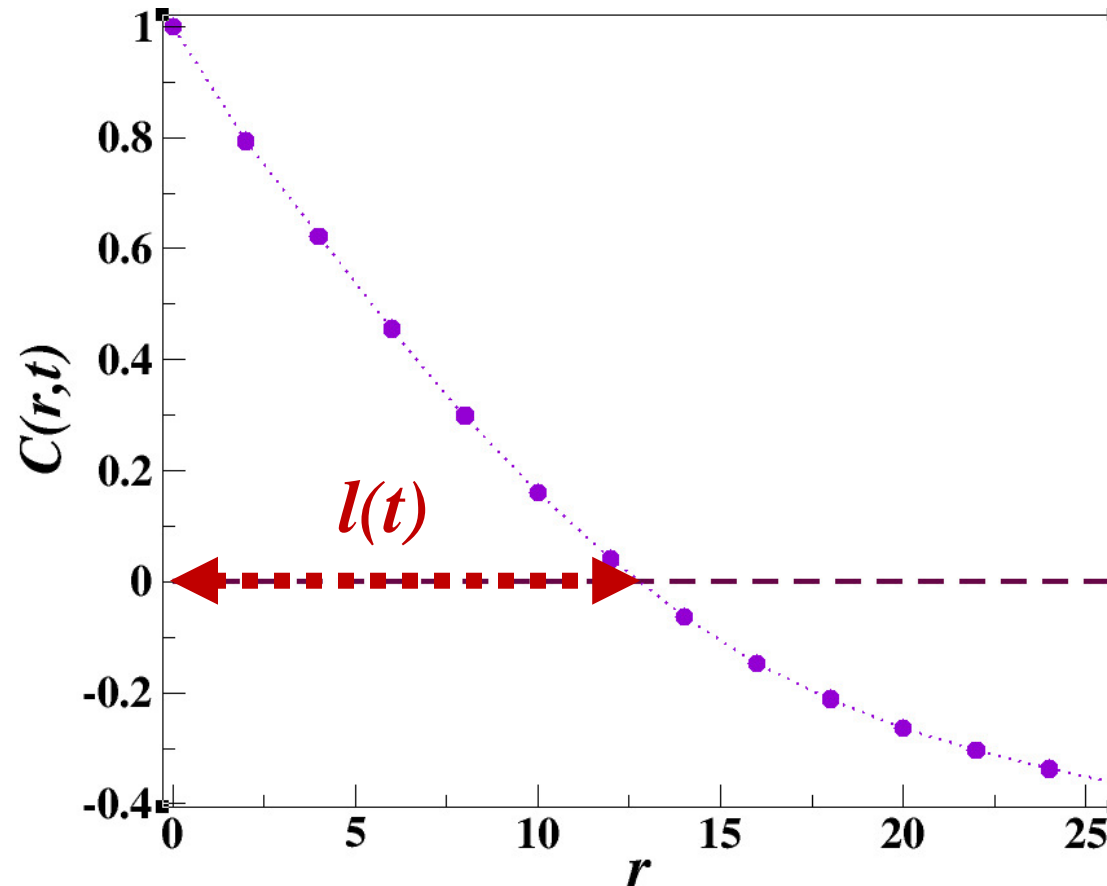
$N_A, N_B$  = No of A and B particles



# DOMAIN Size Estimation

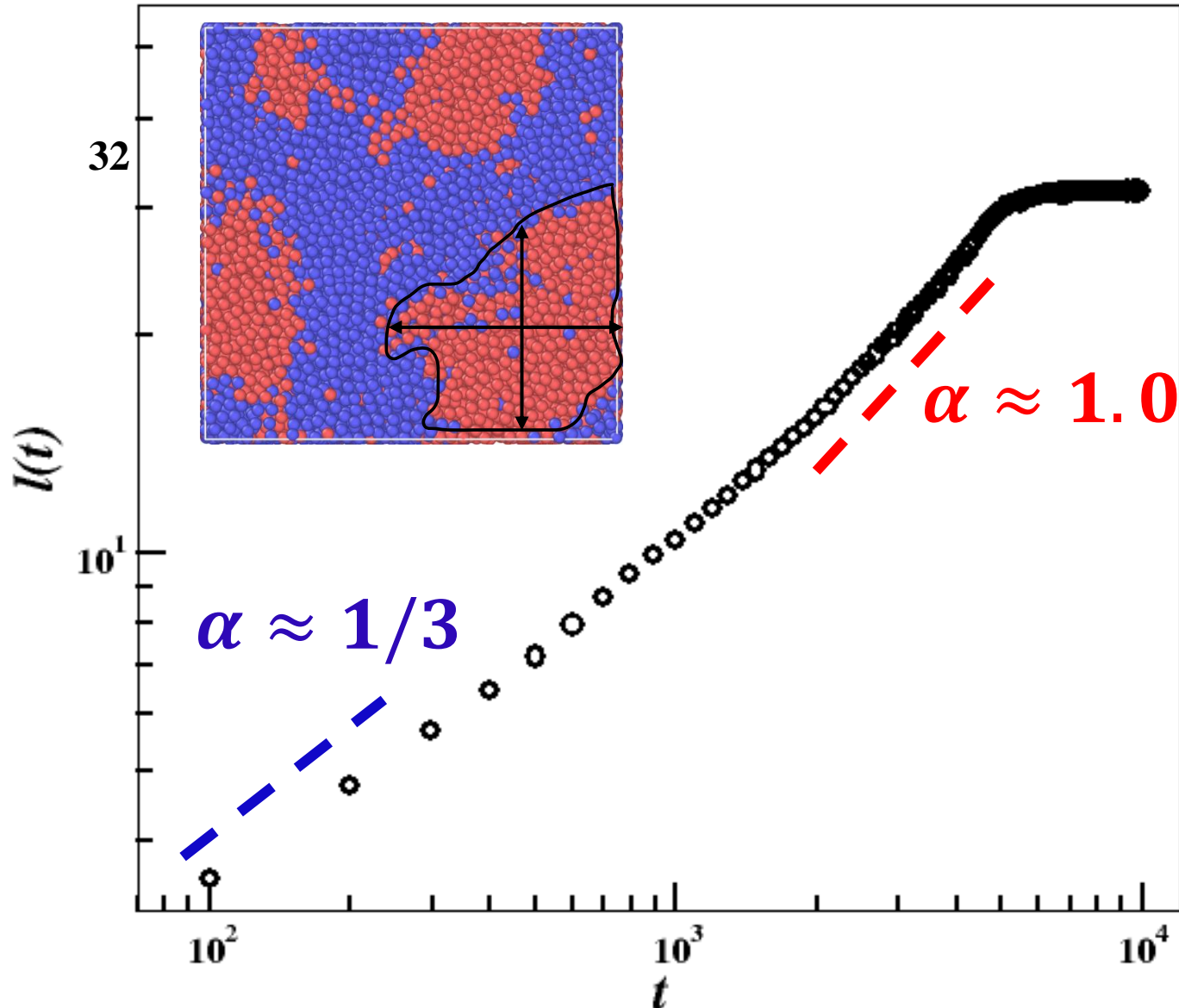
➤ First zero crossing of the Correlation function  $C(\vec{r}, t)$  gives  $l(t)$

$$C(\vec{r}, t) = \langle \varphi(\vec{R}, t) \varphi(\vec{R} + \vec{r}, t) \rangle - \langle \varphi(\vec{R}, t) \rangle \langle \varphi(\vec{R} + \vec{r}, t) \rangle$$





# Domain Growth Laws



- Initial time diffusive growth

Lifshitz-Slyozov law:  $l(t) \sim t^{\frac{1}{3}}$

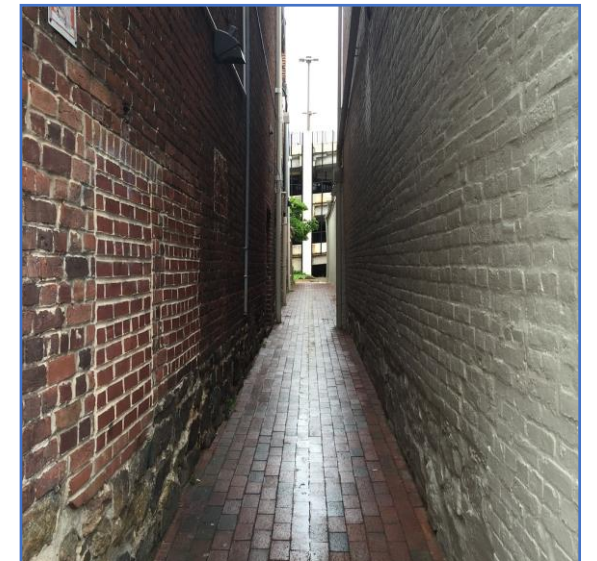
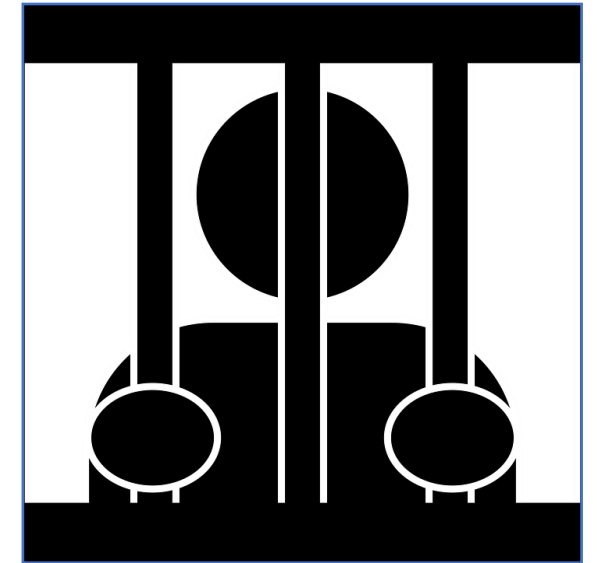
- Intermediate hydrodynamic growth

Viscous hydrodynamics:  $l(t) \sim t$

- Late time growth

Inertial hydrodynamic:  $l(t) \sim t^{\frac{2}{3}}$

What happens if  
the system is  
**CONFINED**  
instead of **BULK**

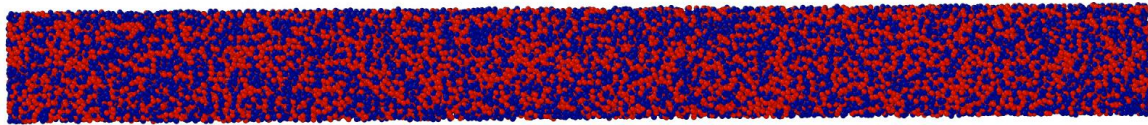




# Phase Separation In Confined Geometry

## Neutral Wall

### Simple Pore



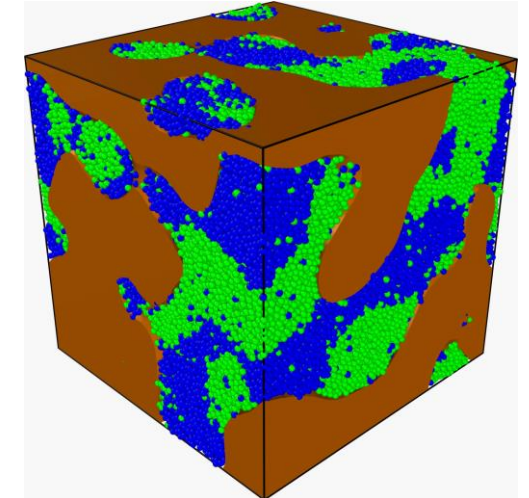
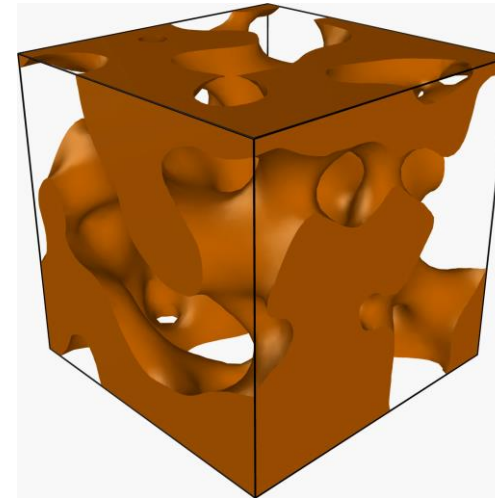
- **Plug-like** domains are formed
- **Metastable** state is obtained
- Full phase separation *not* possible

\*PRL **65** (1990) 1897

\*PRL **69** (1992) 1548

\*EPL **116** (2016) 56003

### Complex Topology



- Domain growth slows down
- Domain size depended on pore size

\*EPL **140** (2022) 47002

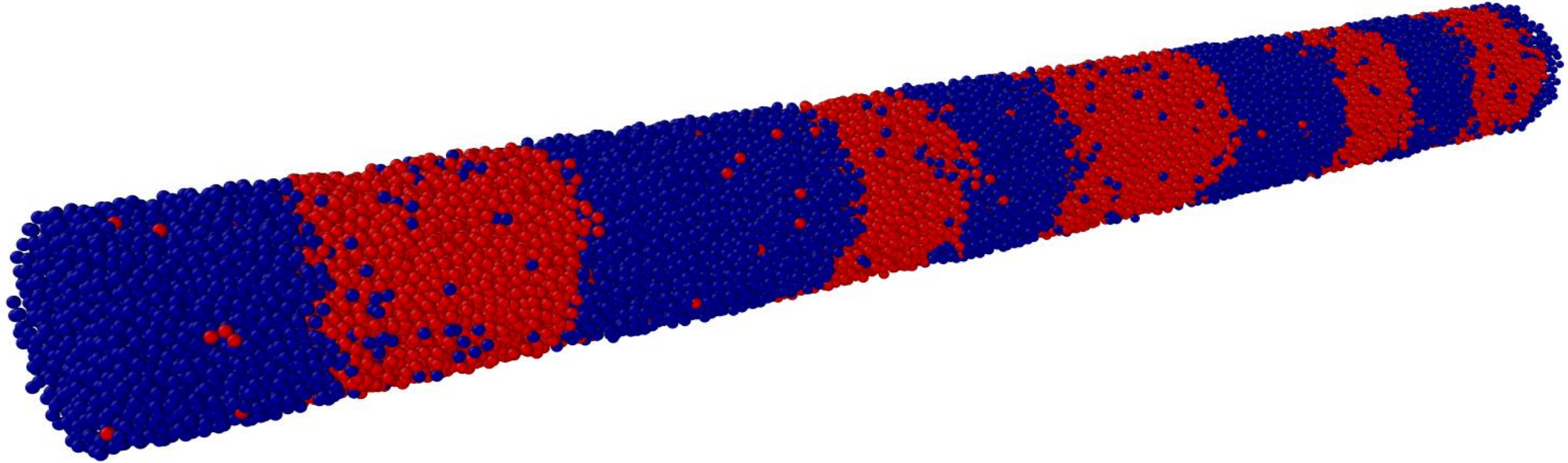
# MOTIVATION FOR THE WORK



**What happens in a real system where the fluids interact with the container?**

**PARTIAL or COMPLETE WETTING**

# Phase Separation in Cylindrical Pore

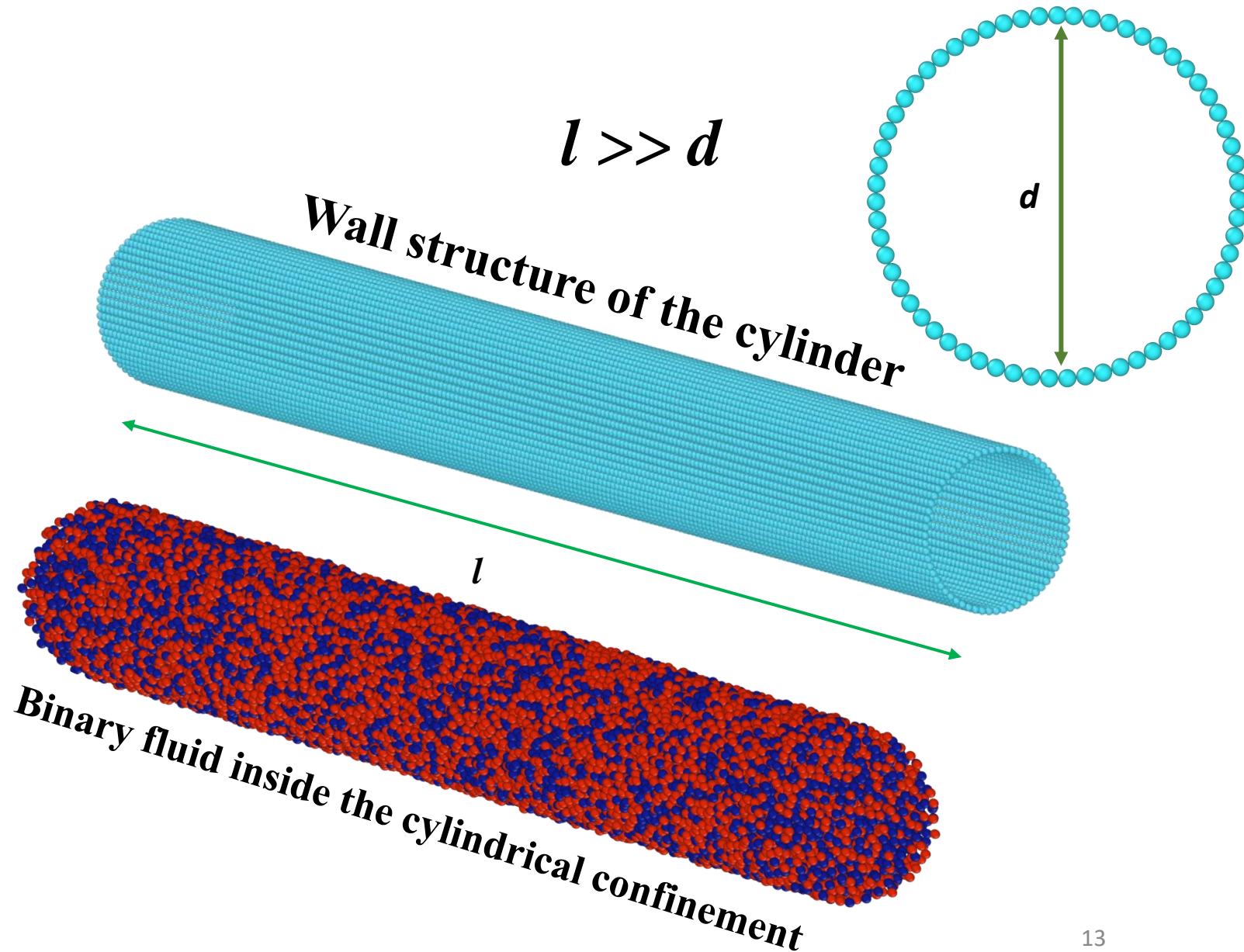


Whether it is **POSSIBLE** to –  
Break the **Metastable State?**  
Achieve the **Full Phase Separation?**



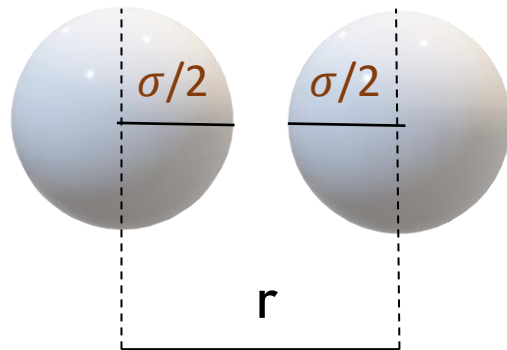
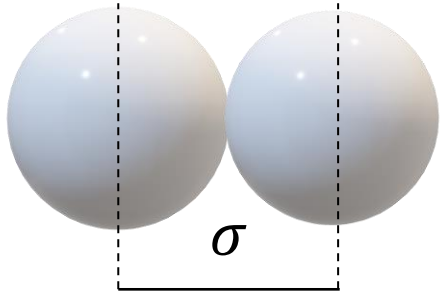
# **Partial and Complete Wetting Scenario**

# Wetting – Interaction with the Wall



# Interaction Potential : LENNARD JONES

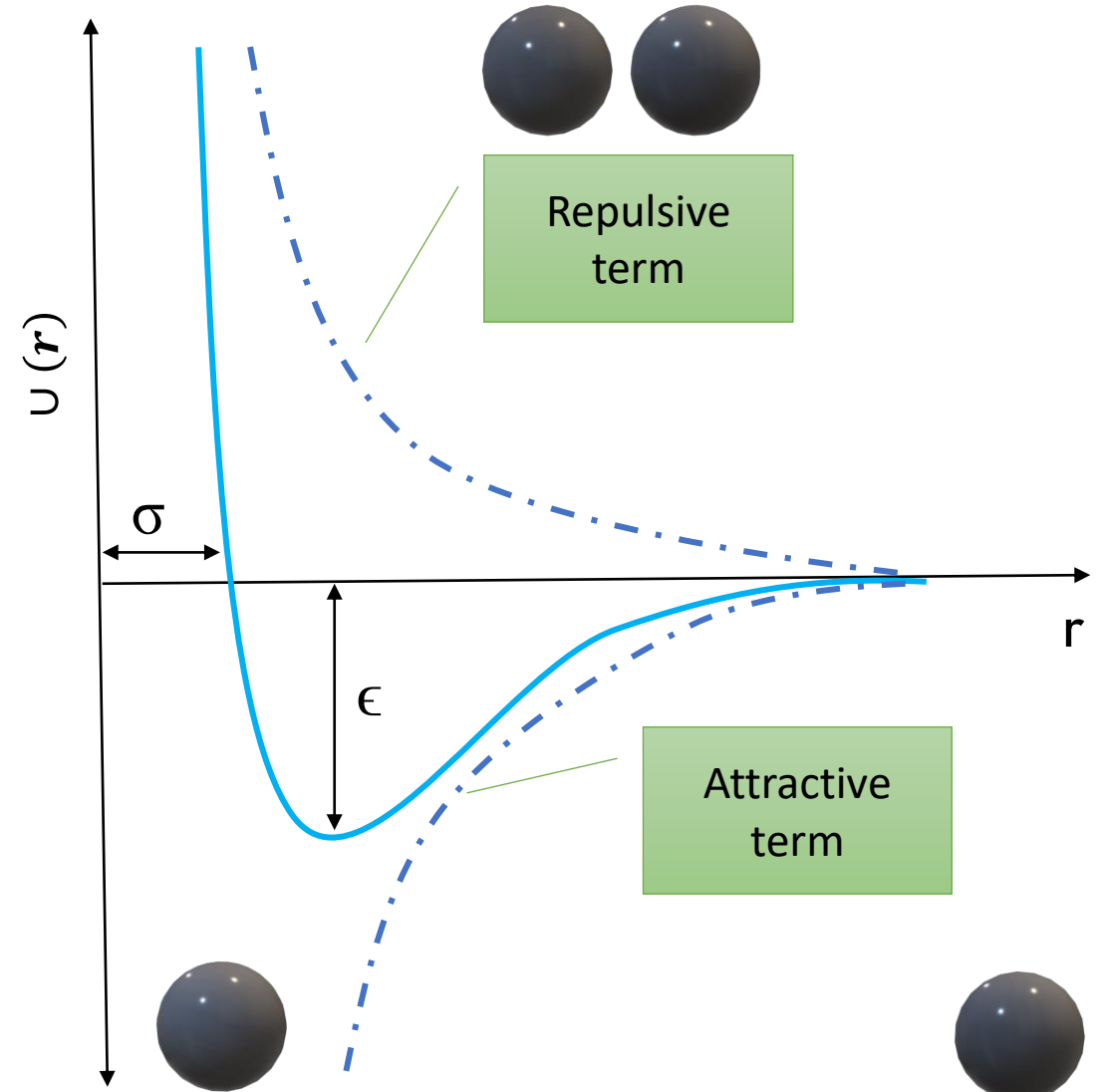
$$U(r) = 4 \epsilon \left[ \left( \frac{\sigma}{r} \right)^{12} - \left( \frac{\sigma}{r} \right)^6 \right]$$



$\sigma$  = Interparticle diameter

$\epsilon$  = Depth of the potential well

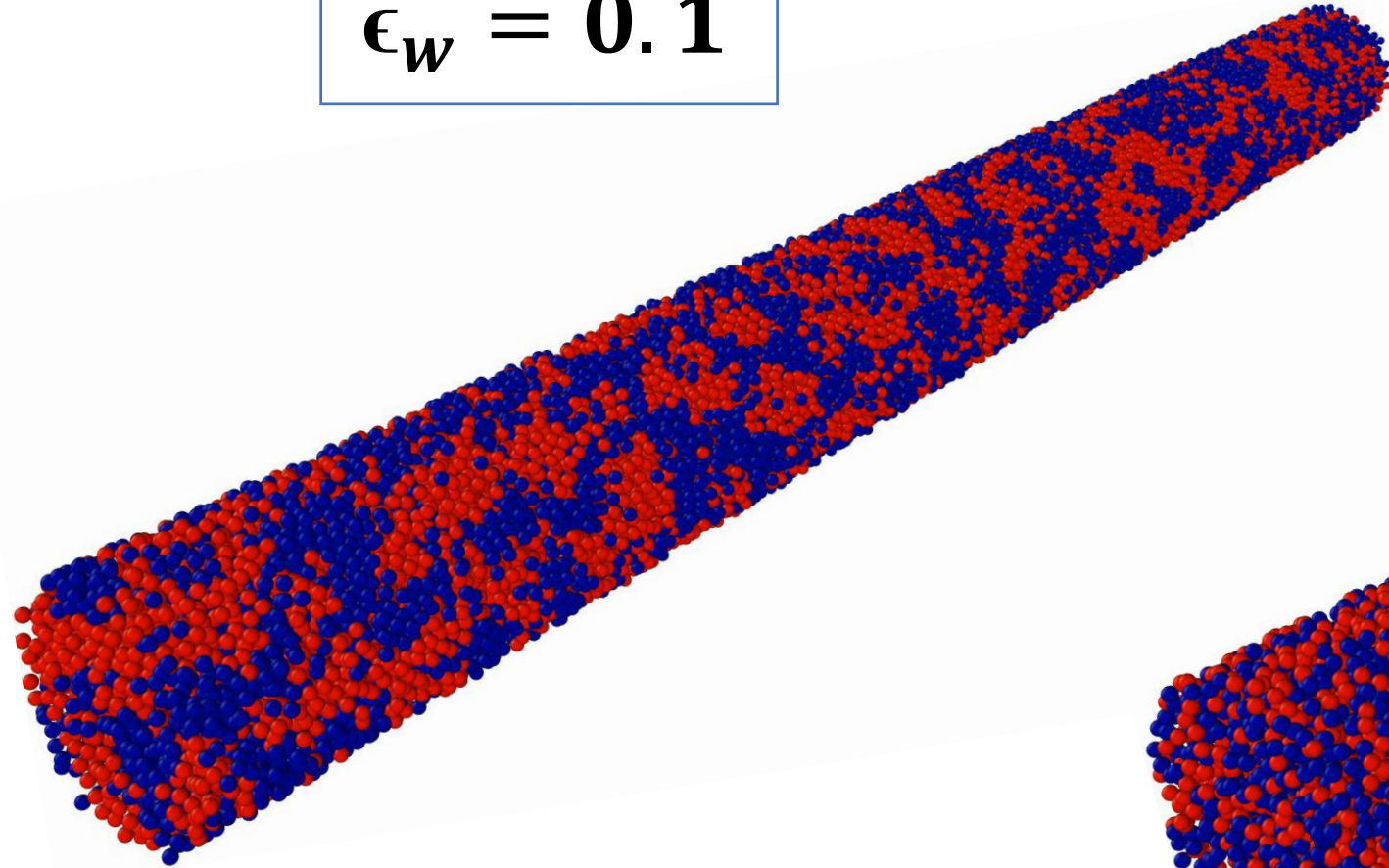
$r$  = Distance between the center of the particles



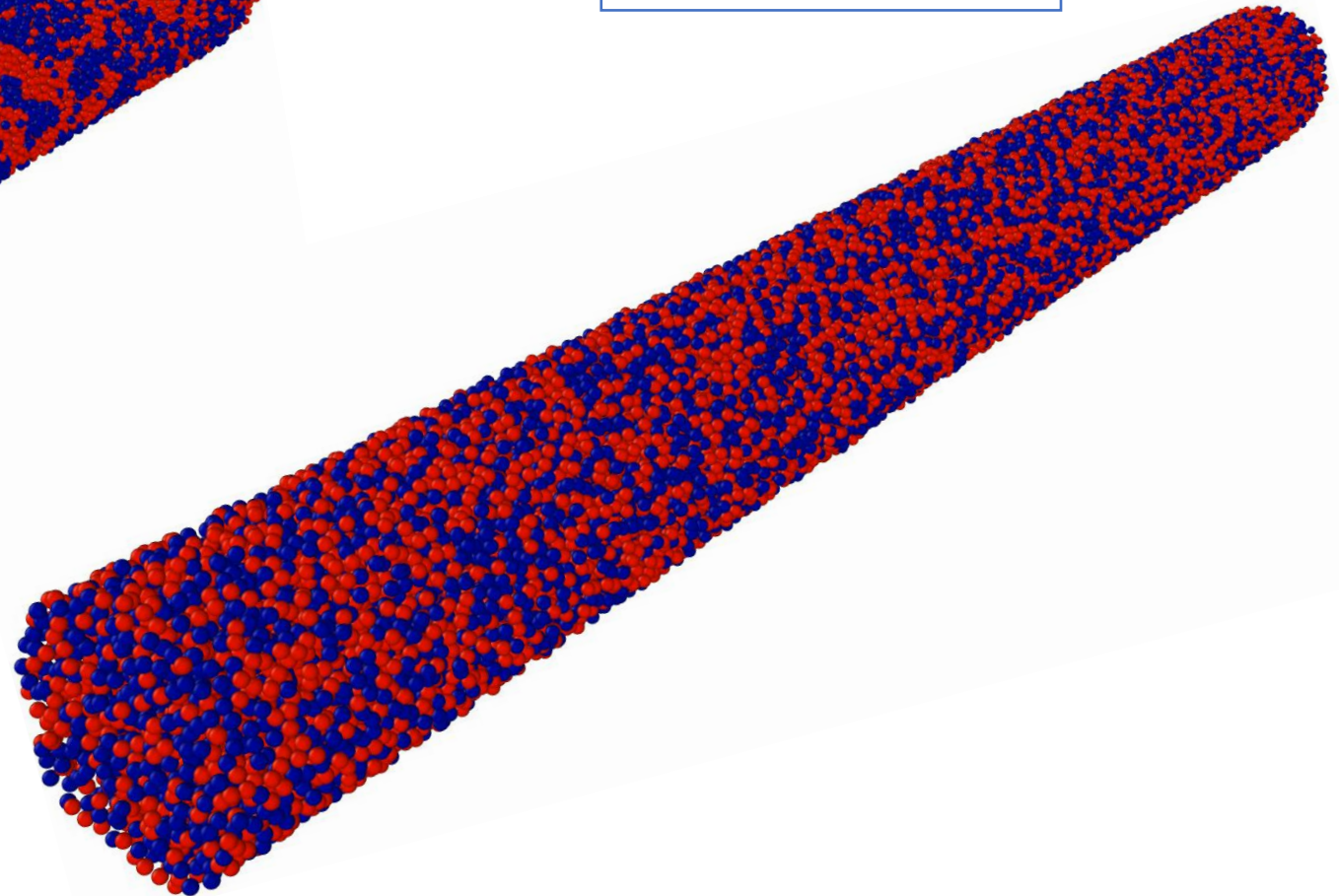


# PARTIAL WETTING (PW) $0.1 \leq \epsilon_w \leq 0.5$

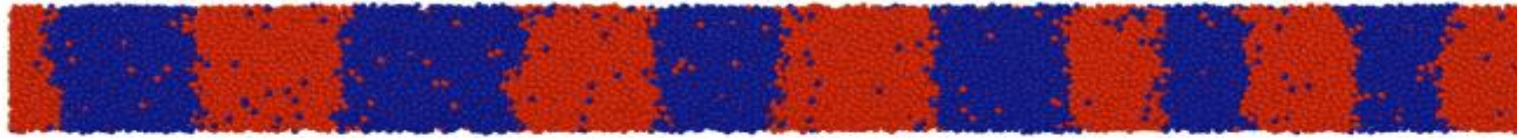
$$\epsilon_w = 0.1$$



$$\epsilon_w = 0.5$$



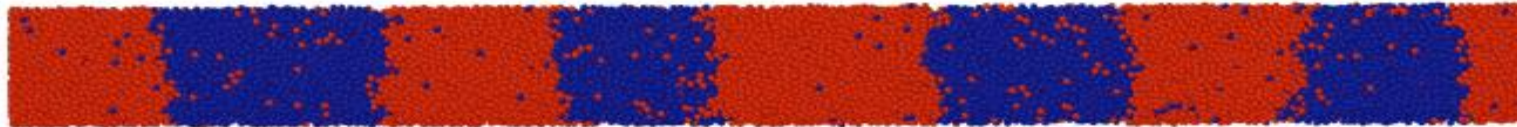
# PW: Different Wetting Strength



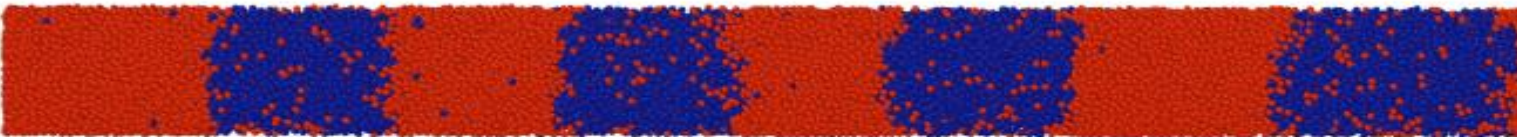
$$\varepsilon_w = 0.1$$



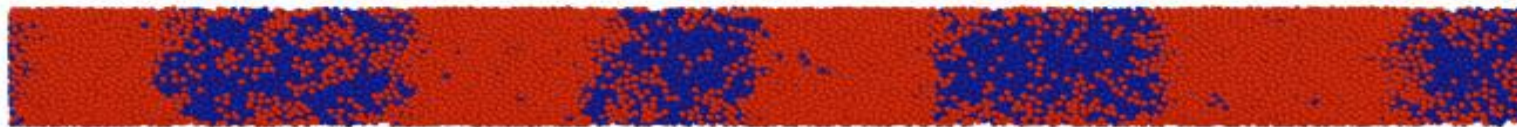
$$\varepsilon_w = 0.2$$



$$\varepsilon_w = 0.3$$



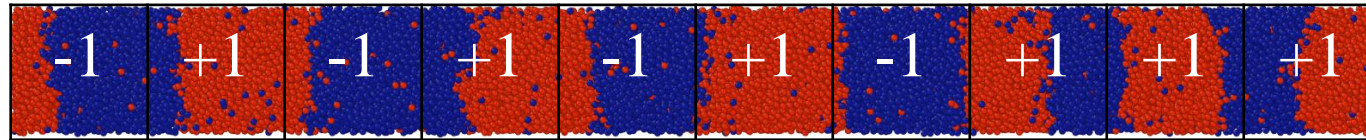
$$\varepsilon_w = 0.4$$



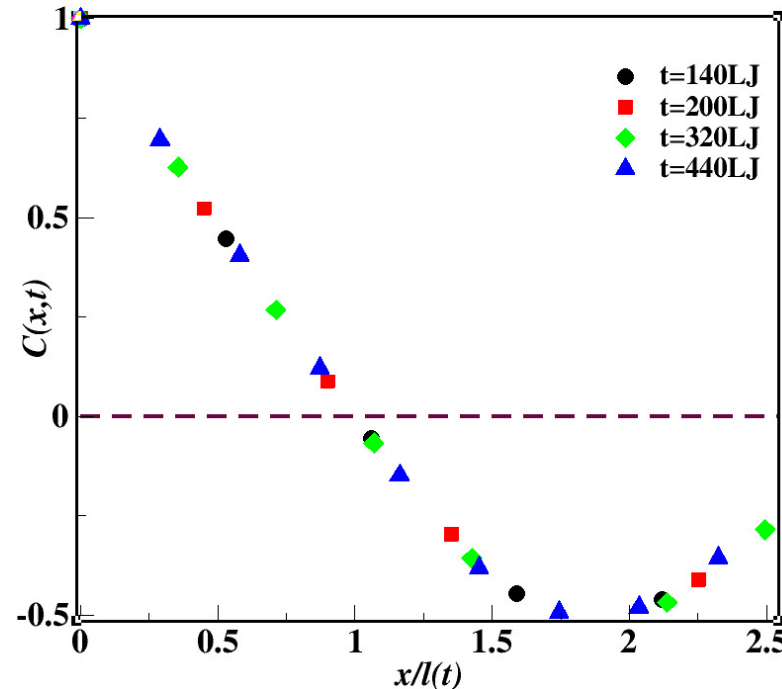
$$\varepsilon_w = 0.5$$

# PW: CORRELATION

Order Parameter and Correlation functions are calculated along the **axis of the cylinder**.



$$C(x, t) = \langle \varphi(0, t) \varphi(x, t) \rangle - \langle \varphi(0, t) \rangle \langle \varphi(x, t) \rangle$$

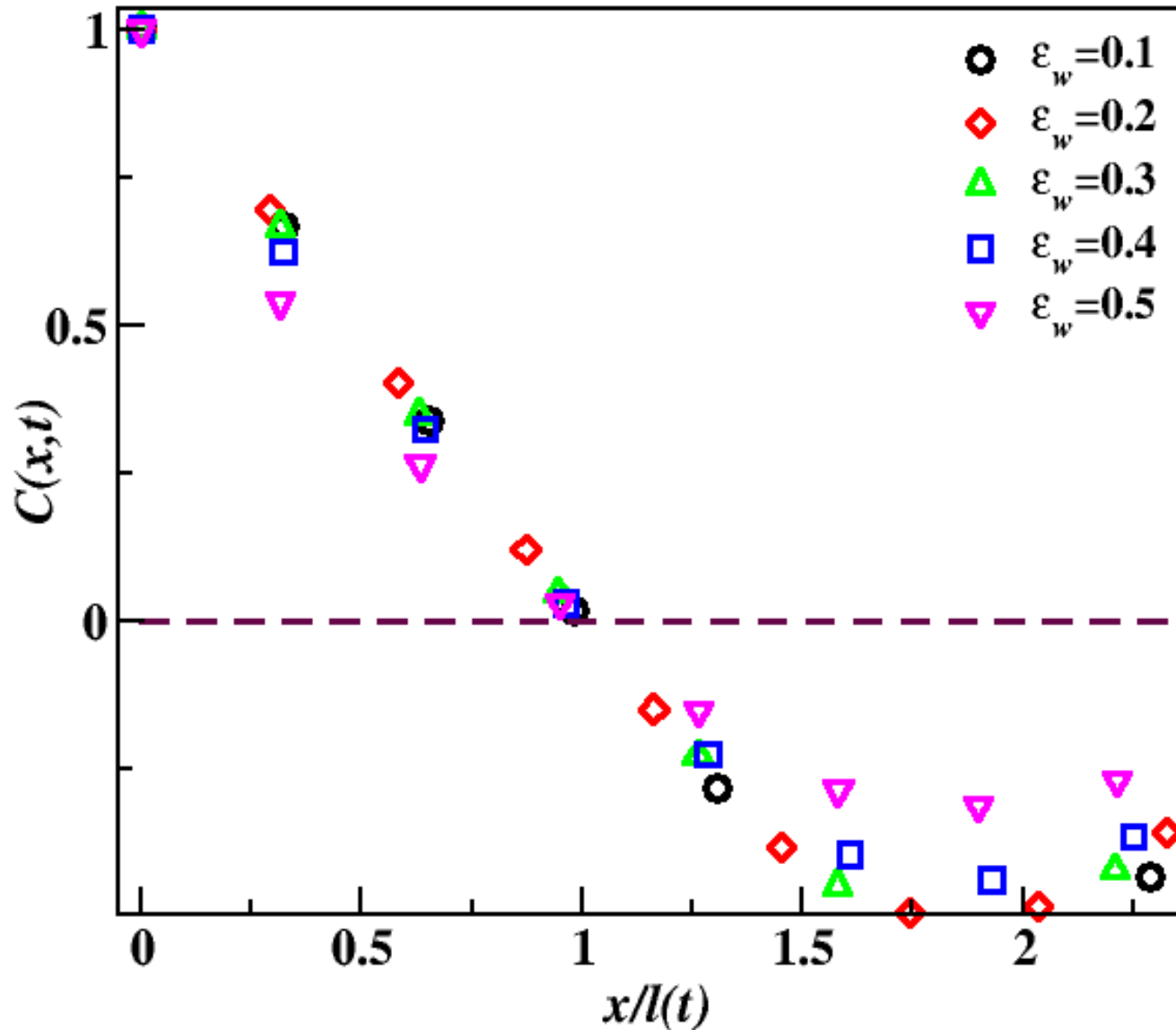


✓ Perfect data Collapse

✓ Self-similar nature of domains



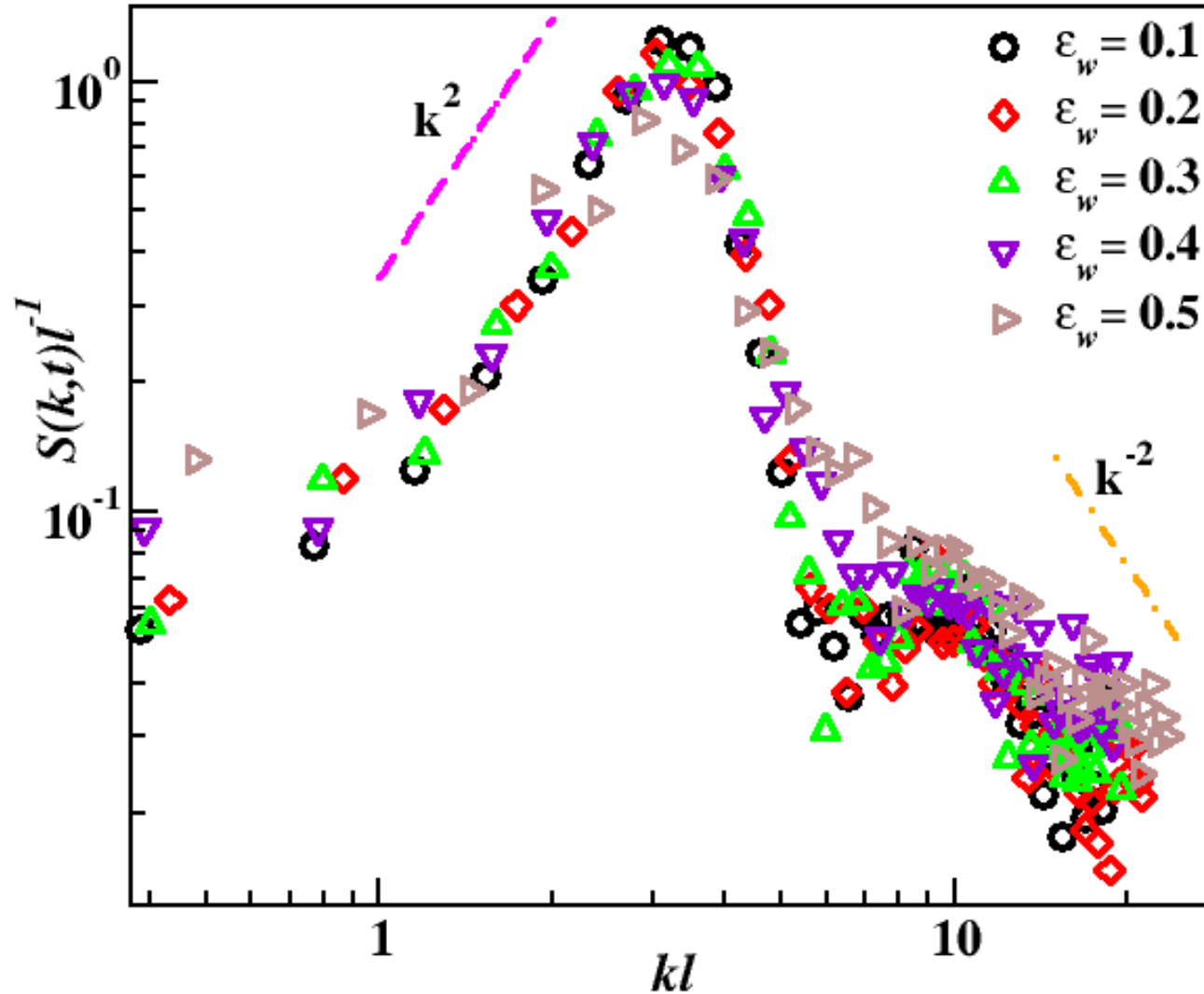
# PW: $C(x,t)$ for different $\epsilon_w$



Scaling behavior violated for higher values of  $\epsilon_w$ .

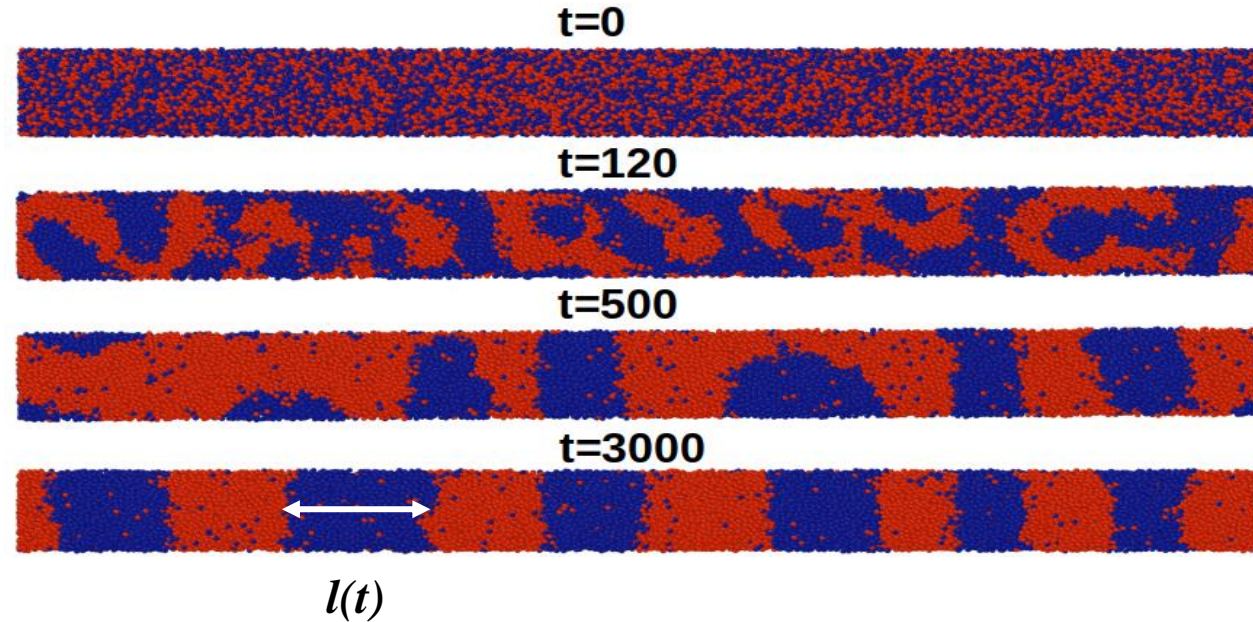
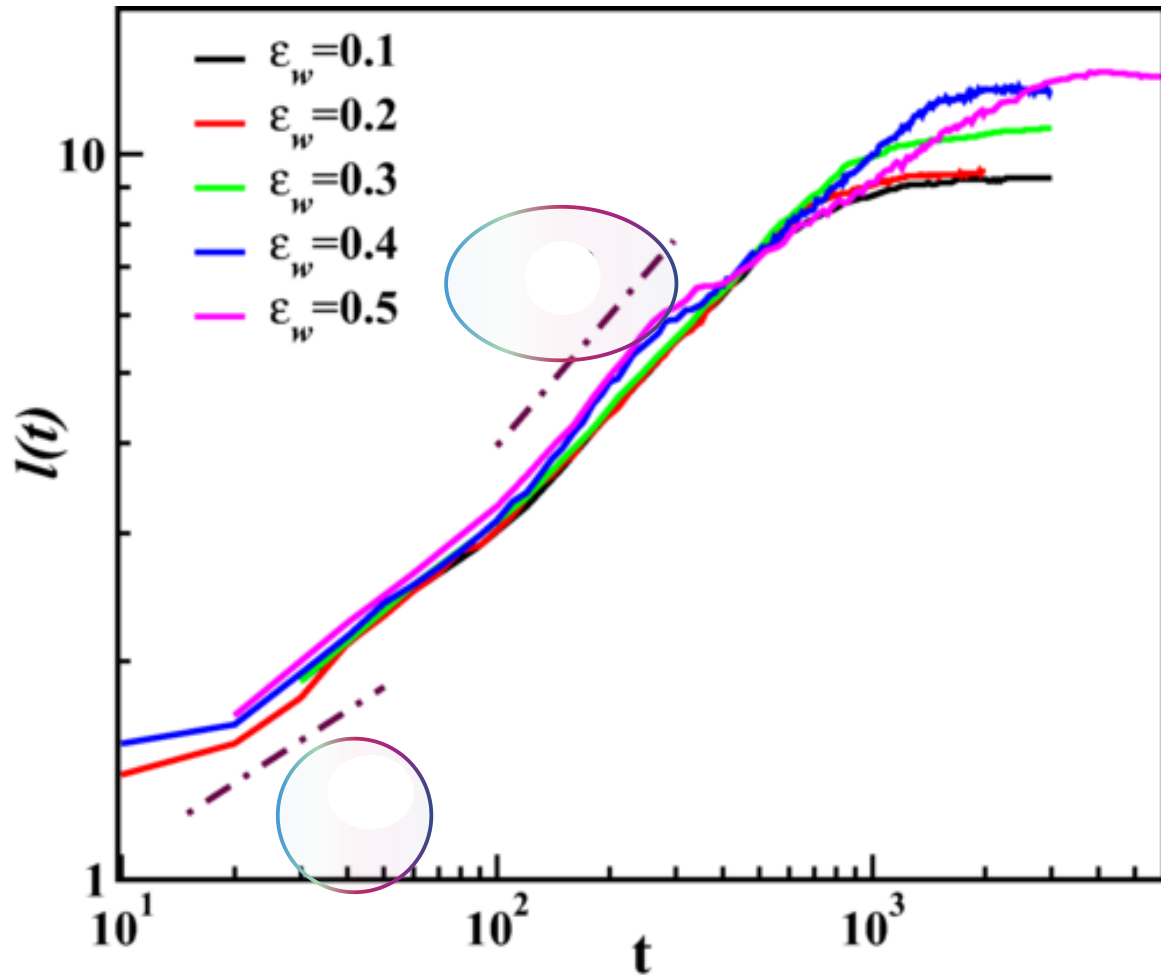
Self similarity nature broken once zero crossed shows the change in domain behavior for different  $\epsilon_w$

# PW: Structure Factor



- ❖  $S(k, t) \approx k^{-(d+1)}$ , here  $d=1$
- ❖ Porod law violated for higher values of  $\epsilon_w$ .
- ❖ Second peak at  $kl \approx 10$  implies sharp domain boundaries.
- ❖ Peak almost vanishes for higher  $\epsilon_w$  ( $\epsilon_w = 0.5$ ).

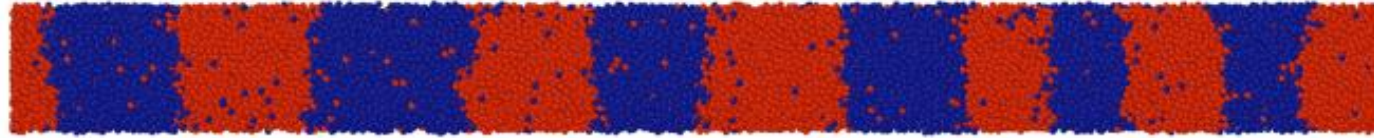
# PW: Growth Dynamics



- ❖ Domain growth with time is represented using the lengthscale  $l(t)$
- ❖ With increasing strength of interaction with wall, the size of domains increases.

# PW: Final Configuration

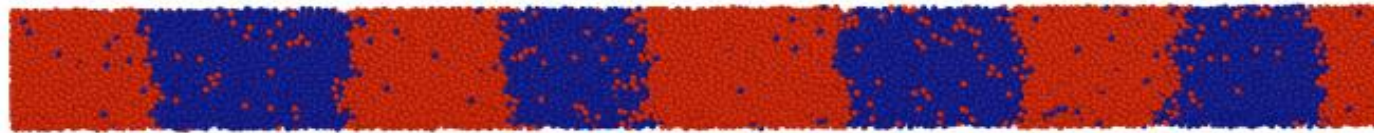
$$\varepsilon_w = 0.1$$



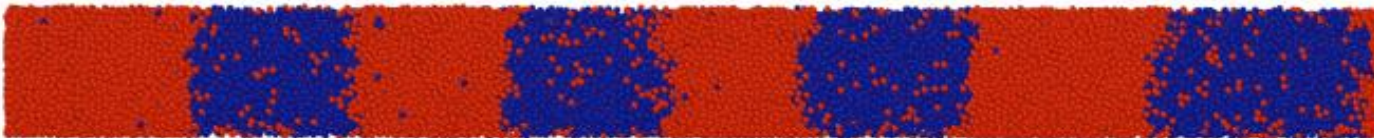
$$\varepsilon_w = 0.2$$



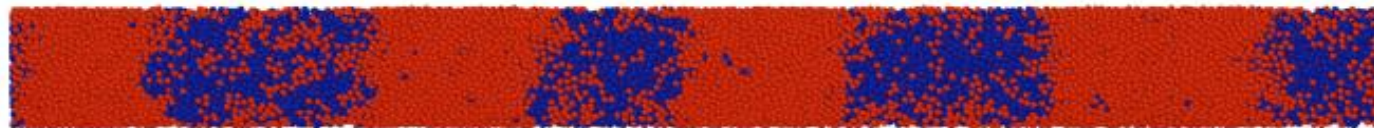
$$\varepsilon_w = 0.3$$



$$\varepsilon_w = 0.4$$



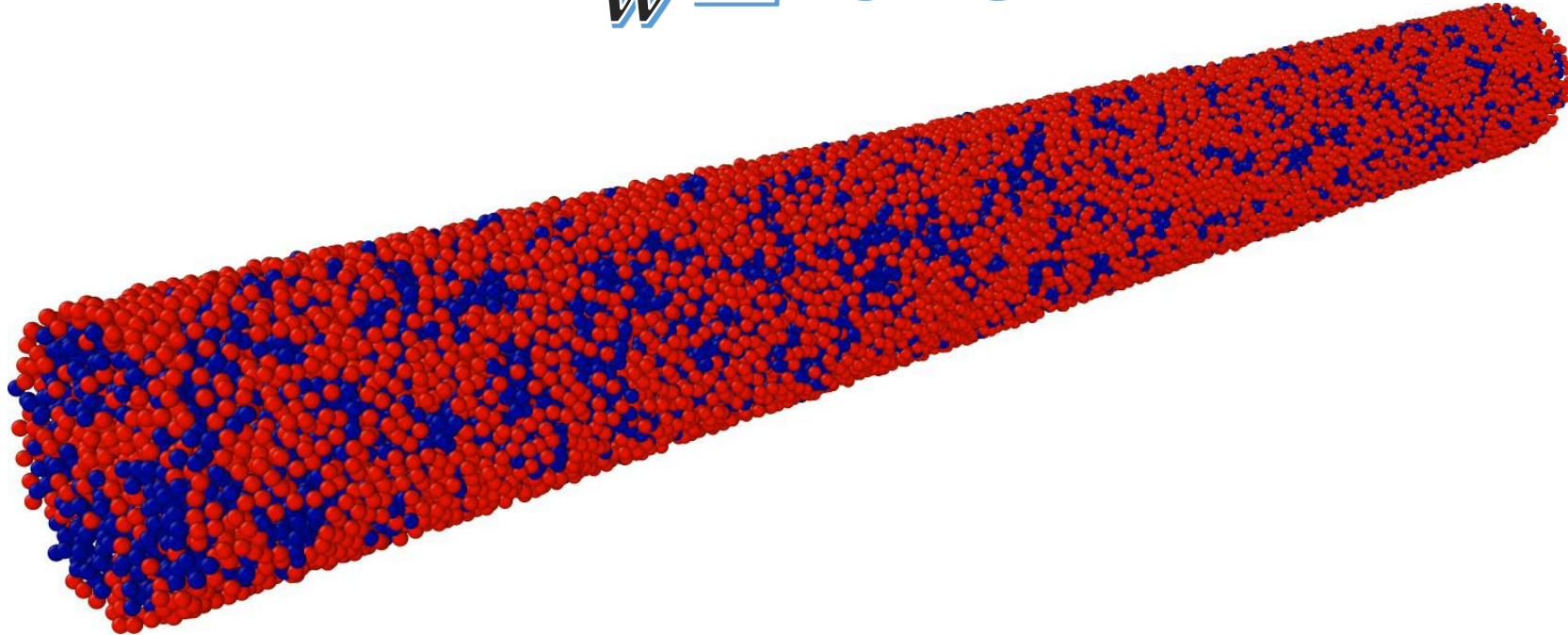
$$\varepsilon_w = 0.5$$





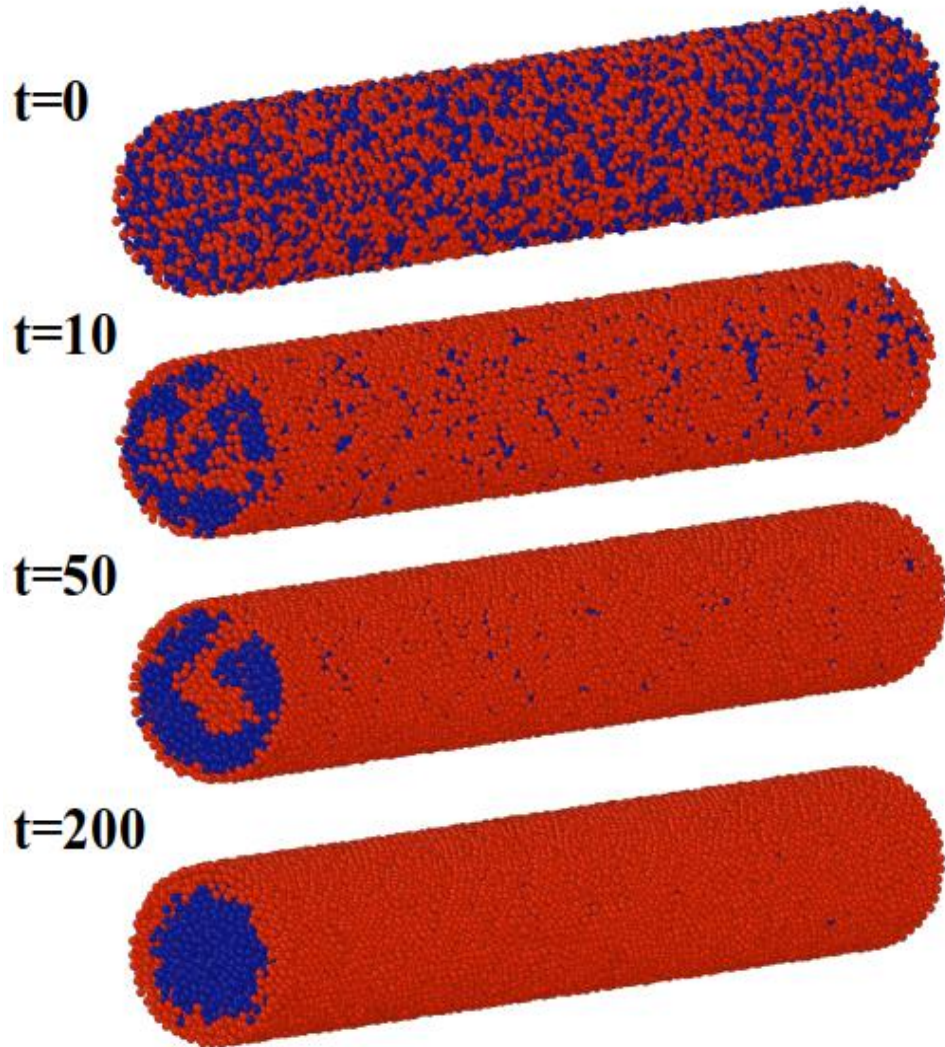
# COMPLETE WETTING (CW)

$$\epsilon_w \geq 0.6$$

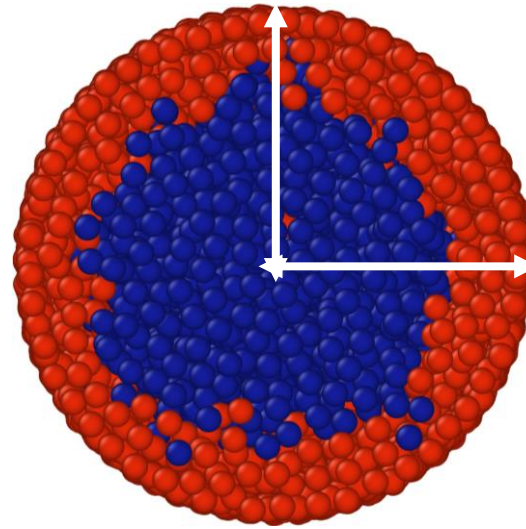


**Metastable state broken and  
complete phase separation obtained**

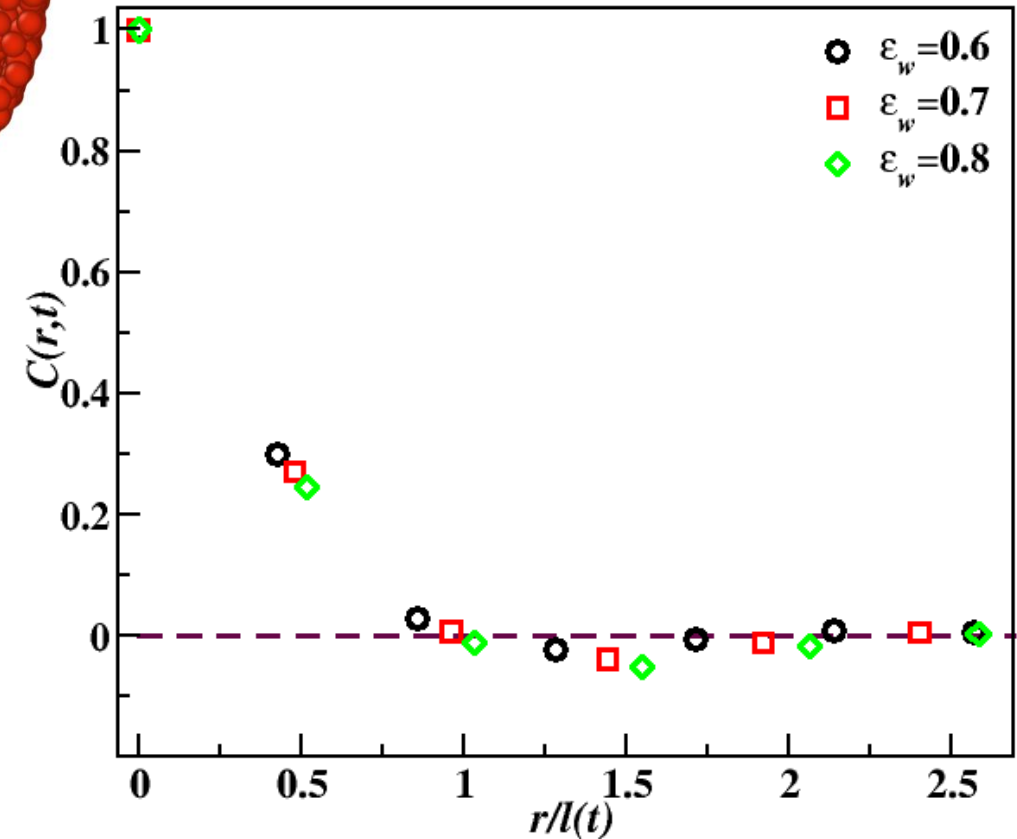
# COMPLETE WETTING (CW)



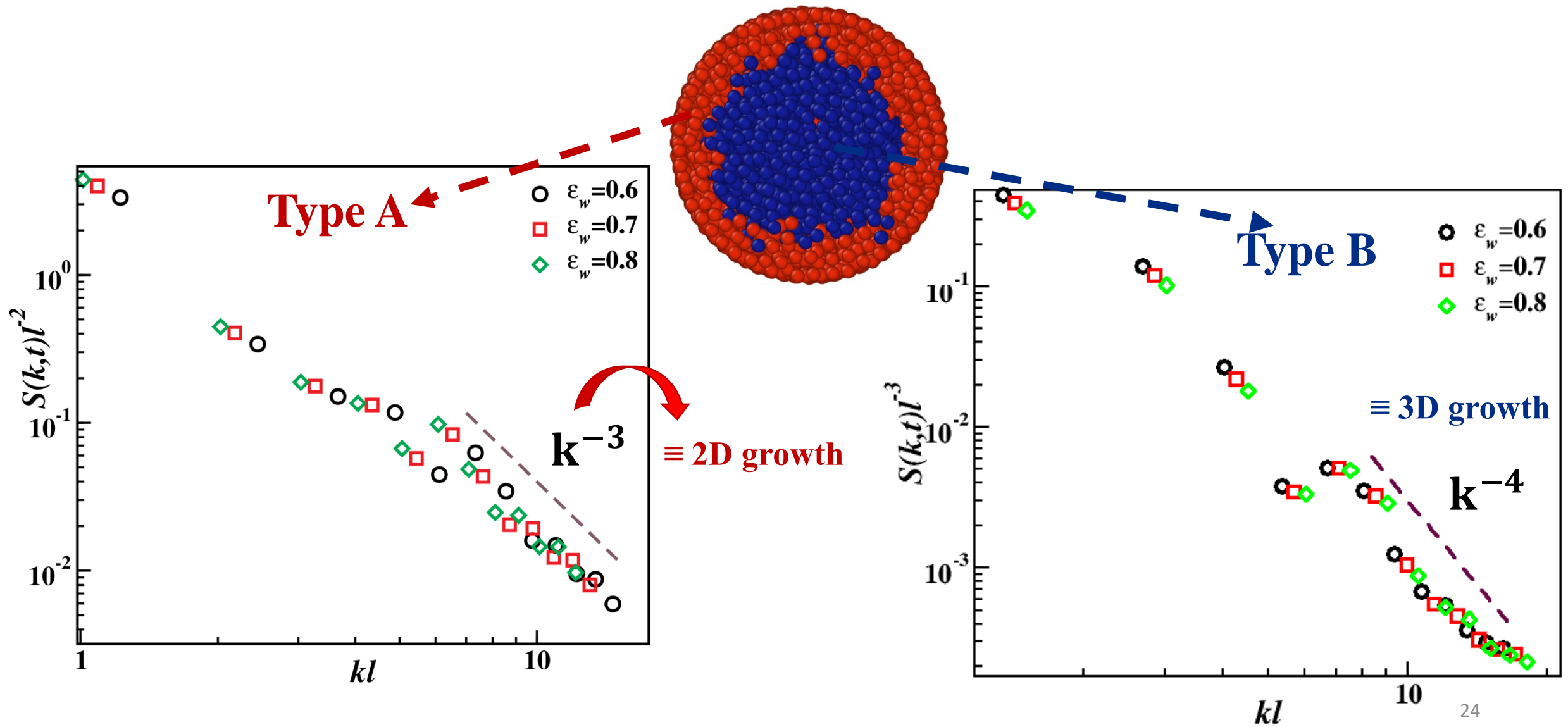
Time evolution of the system



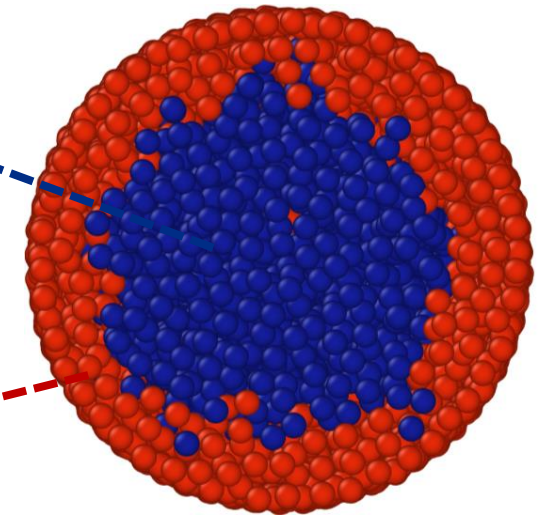
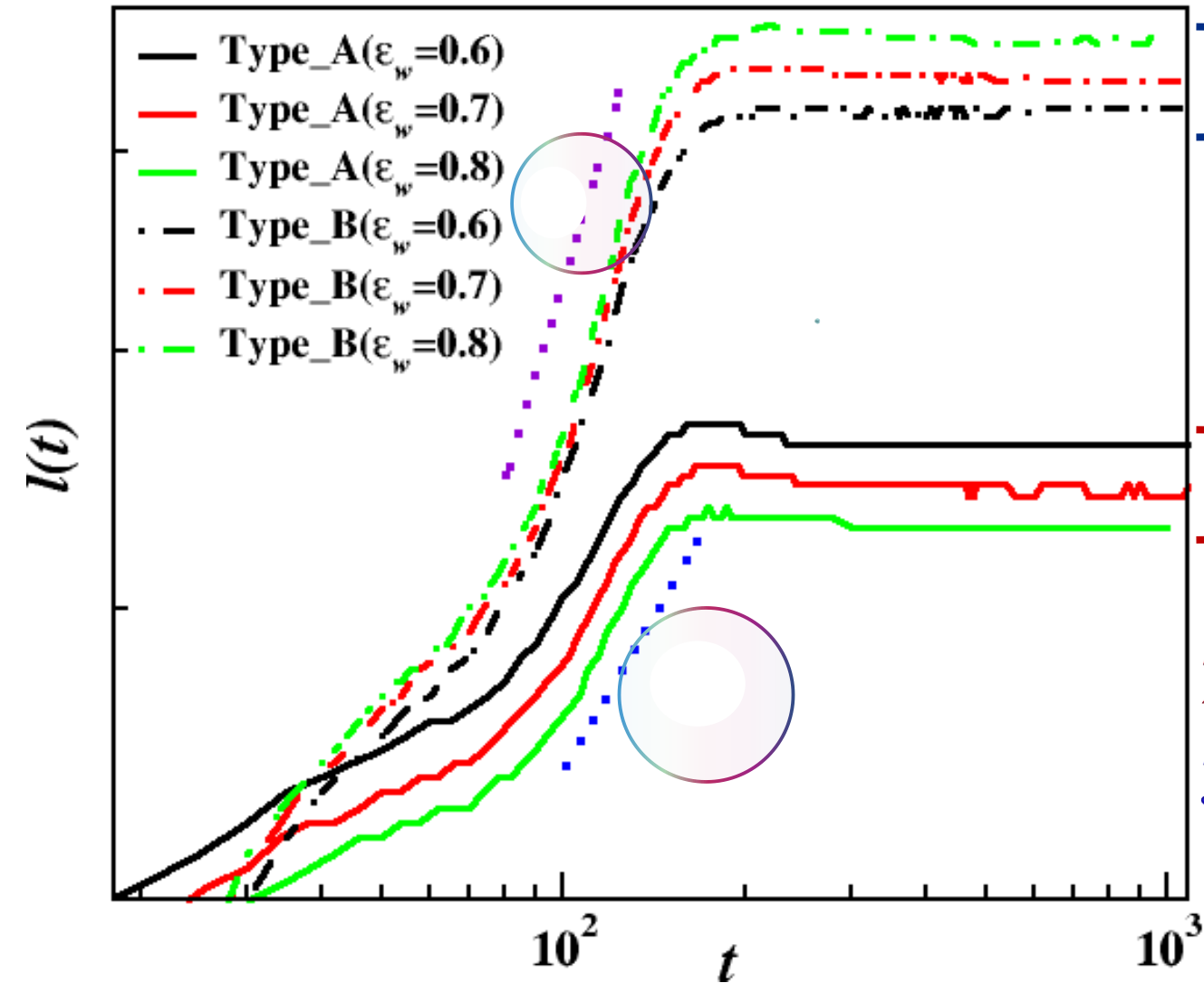
Correlation calculated radially from the center of the cylinder.



# CW: Structure Factor



# CW: Domain Growth



2D Viscous hydrodynamics,  $\alpha=1/2$

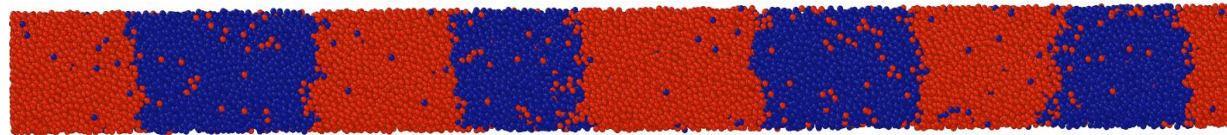
3D Viscous hydrodynamics,  $\alpha=1$



# SUMMARY

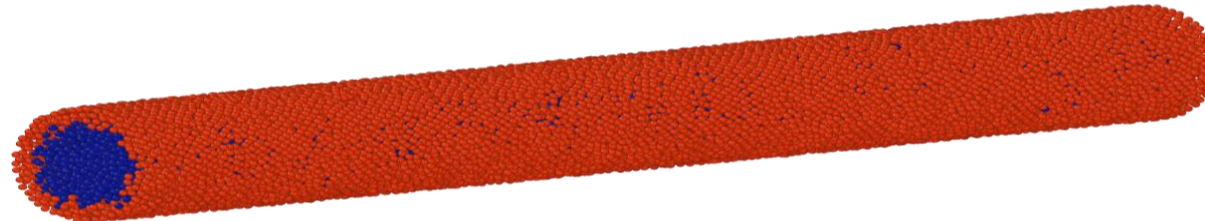
- ❖ Surface-directed spinodal decomposition of binary liquid inside a cylindrical pore is studied
- ❖ Type A particles → wetting interaction and Type B particles → inert to wall.

- ❖ **Partial Wetting** :-



- ✓ Domains → Metastable with increasing domain size w.r.t increasing  $\epsilon_w$
- ✓ Growth laws → Diffusive LS law  $\sim t^{1/3}$ , Inertial hydrodynamic law  $\sim t^{2/3}$

- ❖ **Complete Wetting**:-



- ✓ Domains → Cylindrical or Tube like fully separated domains
- ✓ Growth laws → Viscous hydrodynamic growths:
  - Type A  $\sim t^{1/2}$  ( $\equiv$  2D Growth)
  - Type B  $\sim t$  ( $\equiv$  3D Growth)

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THANK YOU