



(Not just) **Cosmology with pulsar timing arrays.**

Golam Shaifullah

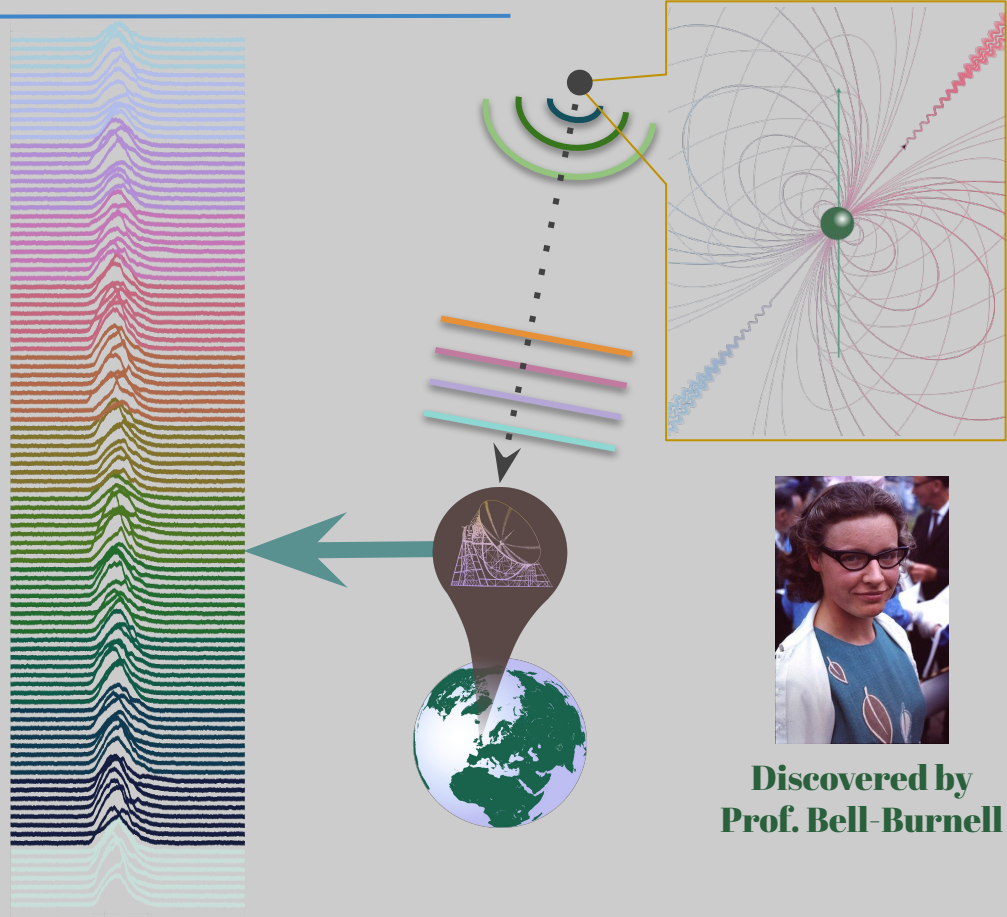
*i do not know what it is about you that closes
and opens; only something in me understands
the voice of your eyes is deeper than all roses
-- E. E. Cummings*



It's not a bird, it's not a plane, definitely not LGM

Pulsars are giant flywheels in space, their compact masses give rise to **incredibly stable rotation**.

On each rotation, the pulsar beam produces a *'pulse'* at Earth, and the photons in that pulse can be assigned a **time-of-arrival (TOA)**.



**Discovered by
Prof. Bell-Burnell**

Models, models, models

TOAs can be predicted using a model with the following (sets of) parameters:

- **astrometric**,
- **pulsar rotation** and
- **binary** (when applicable).

Apart from these pulsar emission is affected by:

- **Dispersive delays due to the intervening *ionised plasma***
- **Red noise (low frequency) processes**

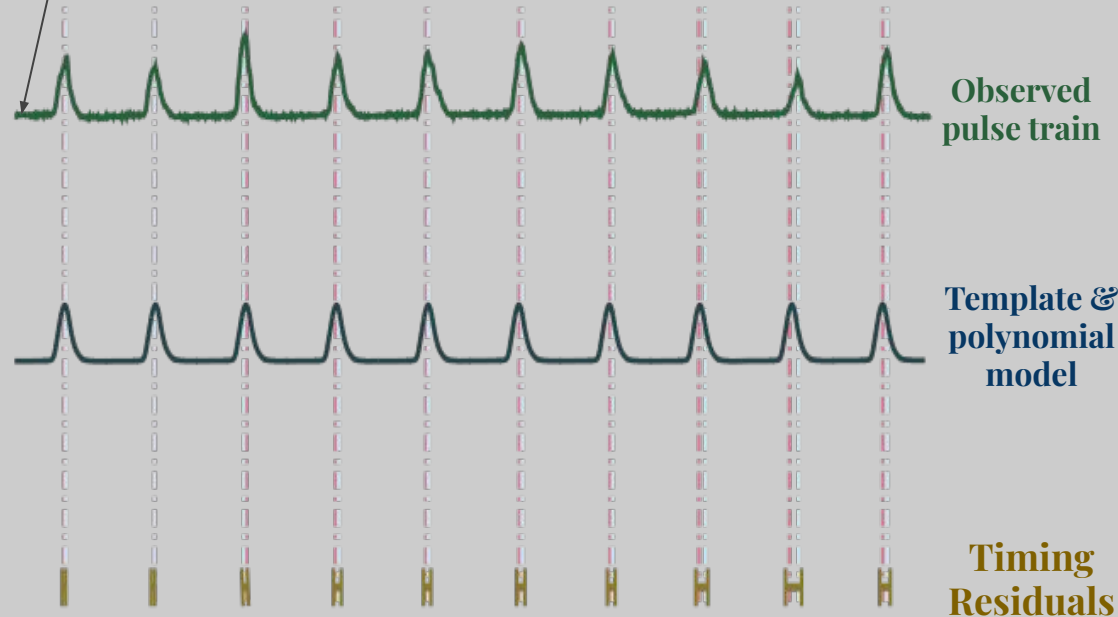


Pulsar timing

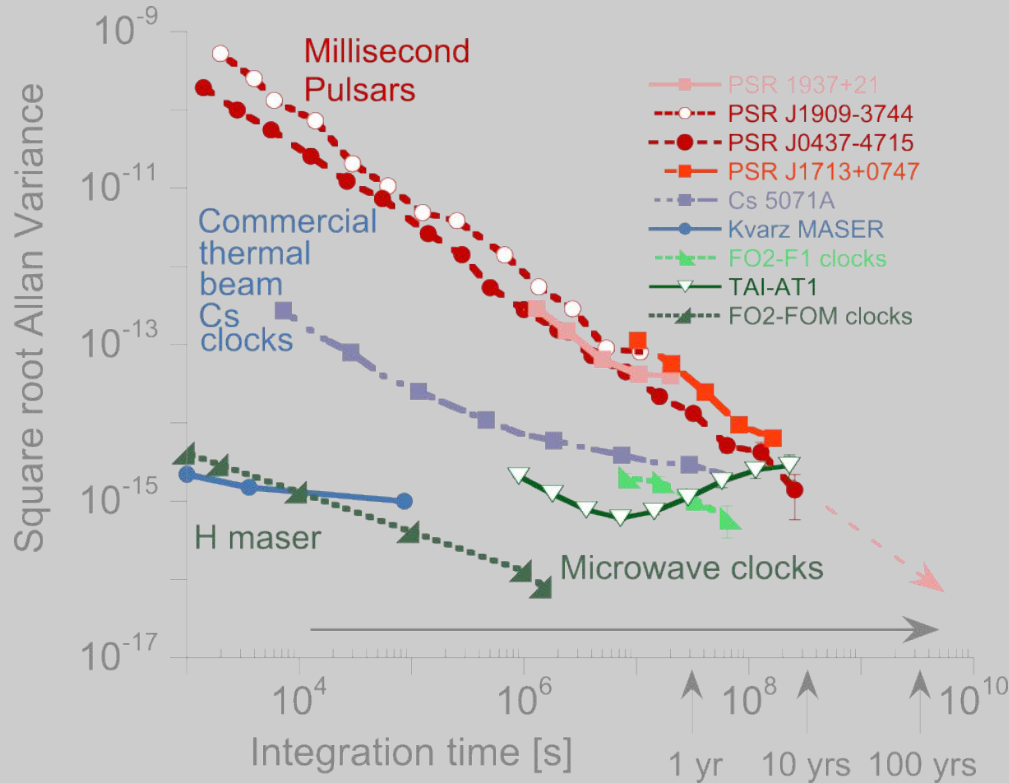
However, once we have estimates of those parameters, we can predict very precisely when the next pulse will arrive. Or the one after 20 million rotations.

When pulses are averaged this precision quickly tends to tens of microseconds to hundreds of nanoseconds.

Time tagged to a precision of picoseconds

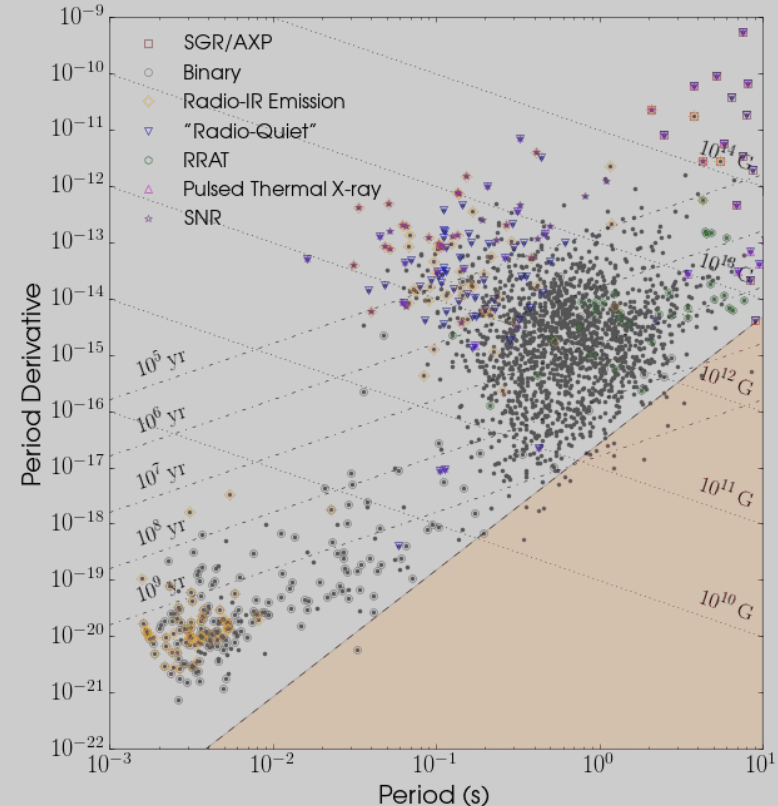


Millisecond pulsars as stable clocks



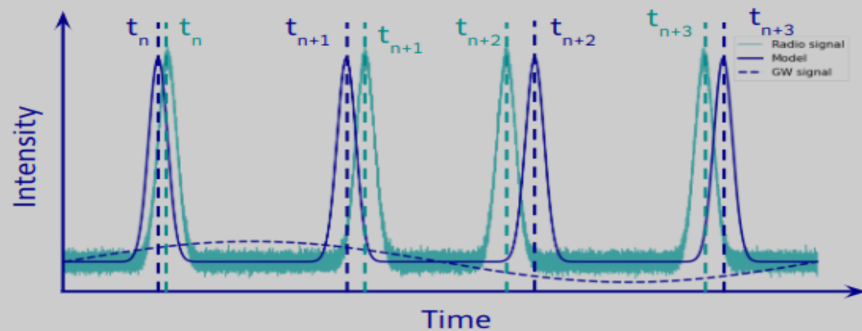
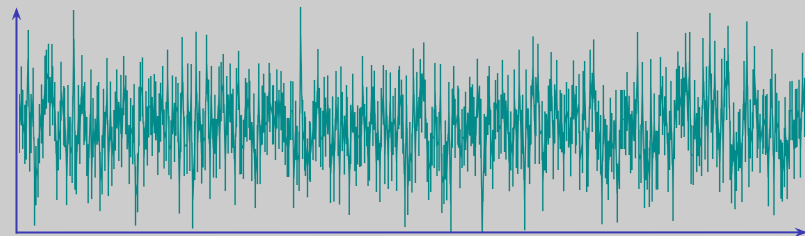
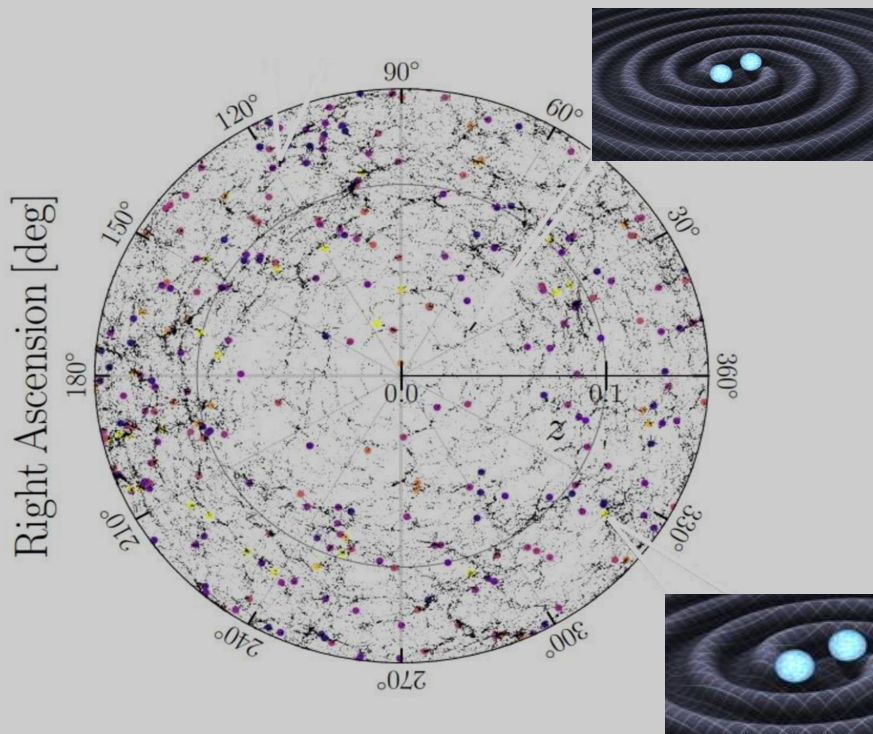
Adapted from Hartnett & Luiten, 2011

See Shannon et al (2016), Lam et al (2018) & others

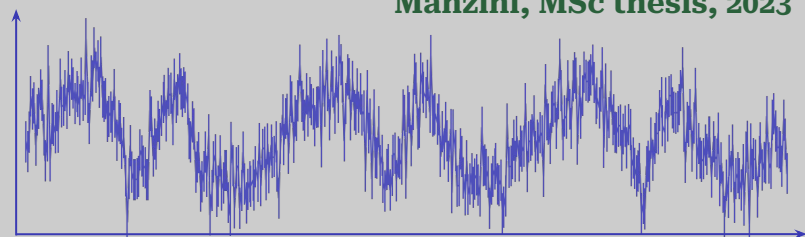


psrppy, (Pitkin, 2011)

All of the light we cannot see



Manzini, MSc thesis, 2023

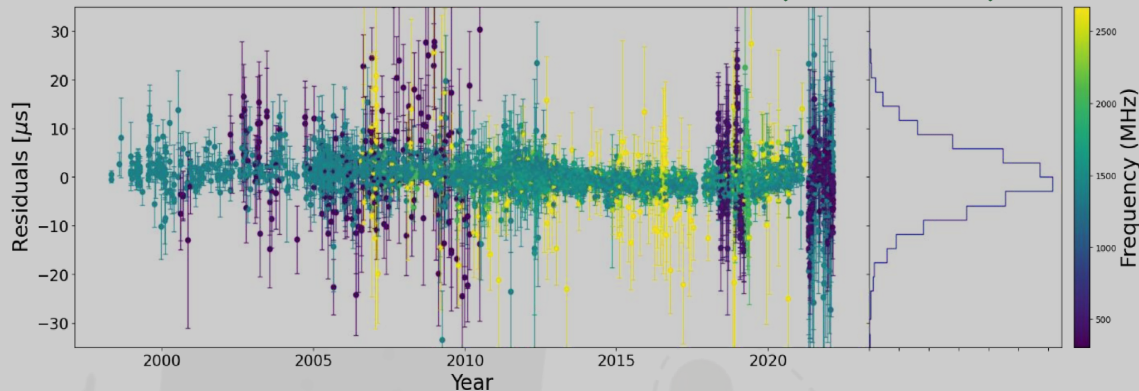


Izquierdo-Villalba et al (2024),
Curylo et al (2023), Bromm & Loeb 2003, Cole et al 2000, Benson (2012)

Pulsar timing arrays

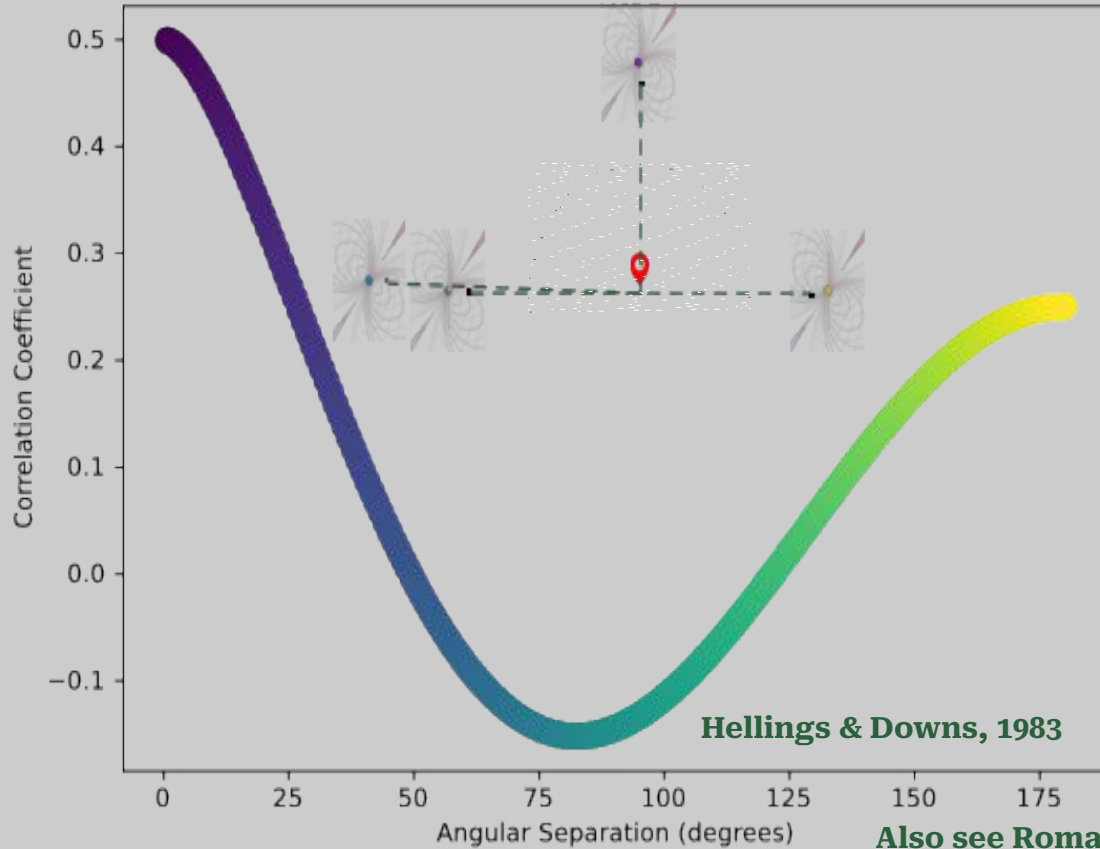
- GWs are expected to induce timing residuals on the order of a few tens of nanoseconds.
- TOA stability scales with number of rotations averaged - use **millisecond pulsars (MSPs)**!
- Single pulsars are 'jittery' and affected by noise, use an **array of MSPs**

Ferranti, MSc thesis, 2023

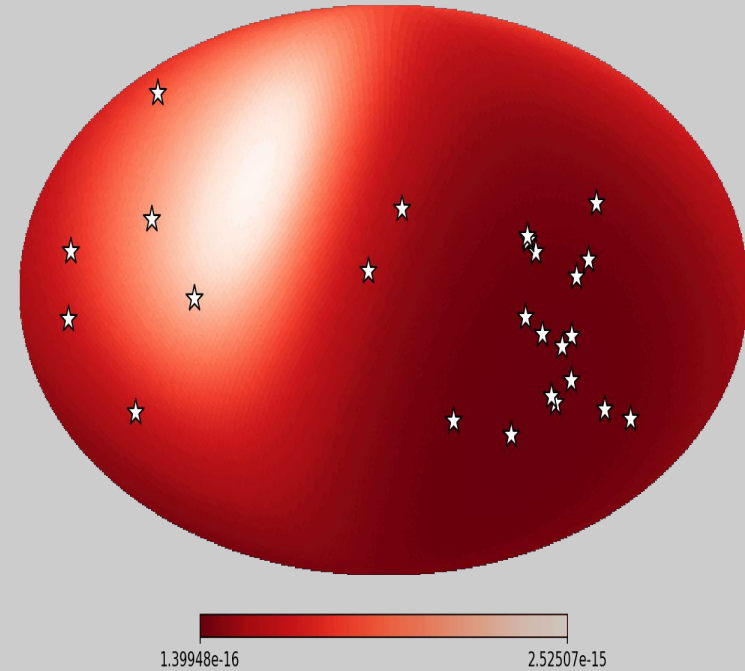


What is the signal PTAs are looking for?

Hellings & Downs Curve



Sky Sensitivity at 1.00e-06 Hz

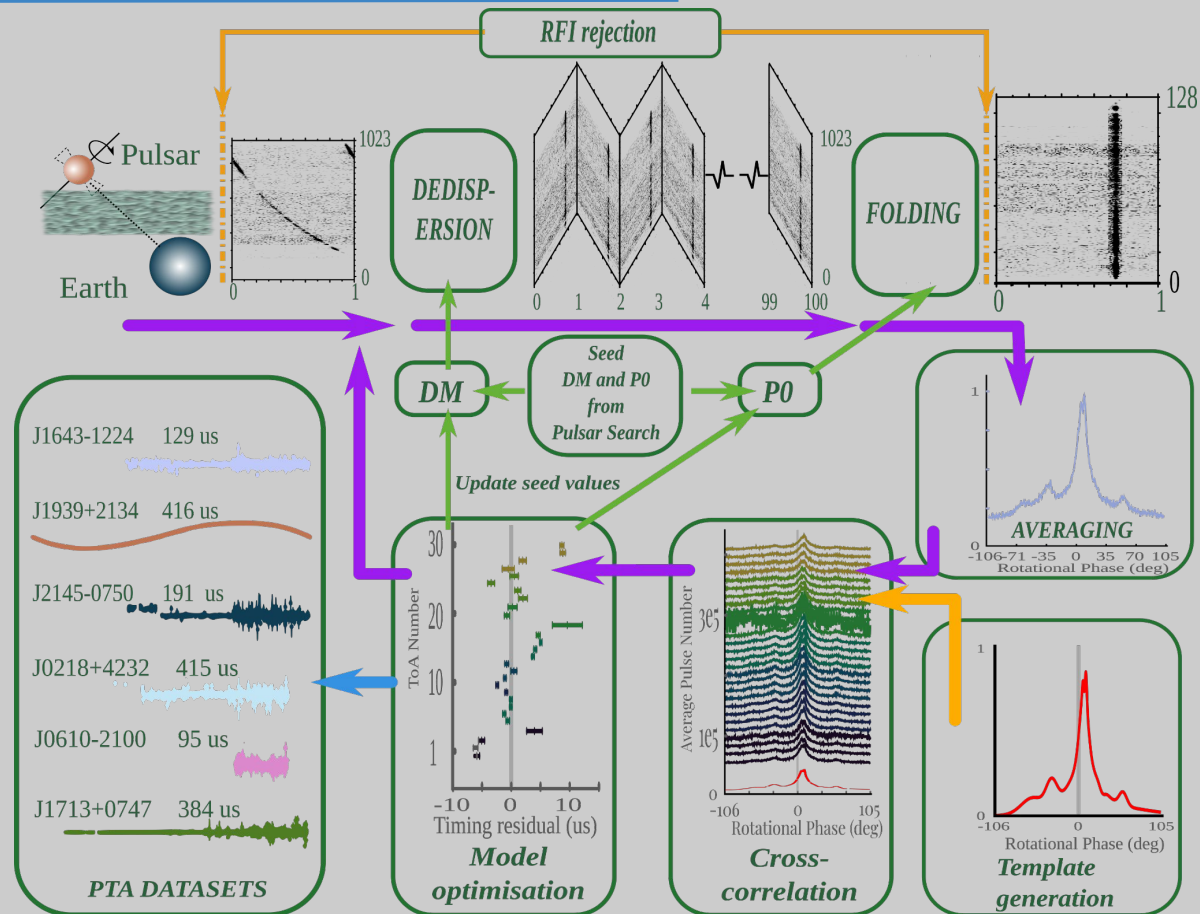


Also see Romano & Allen, arxiv:2308.05847

FreqBayesTM pulsar timing:

- Observe a pulsar
- De-disperse
- Stack
- Average
- Make a template
- Cross-correlate
- Line up your TOAs
- Repeat for another 20 - 100 sources
- Sprinkle post-docs for flavour
- Bake for ~30 years, turning it over once or twice a decade.

Figure from Verbiest & Shaifullah, 2018, CQG

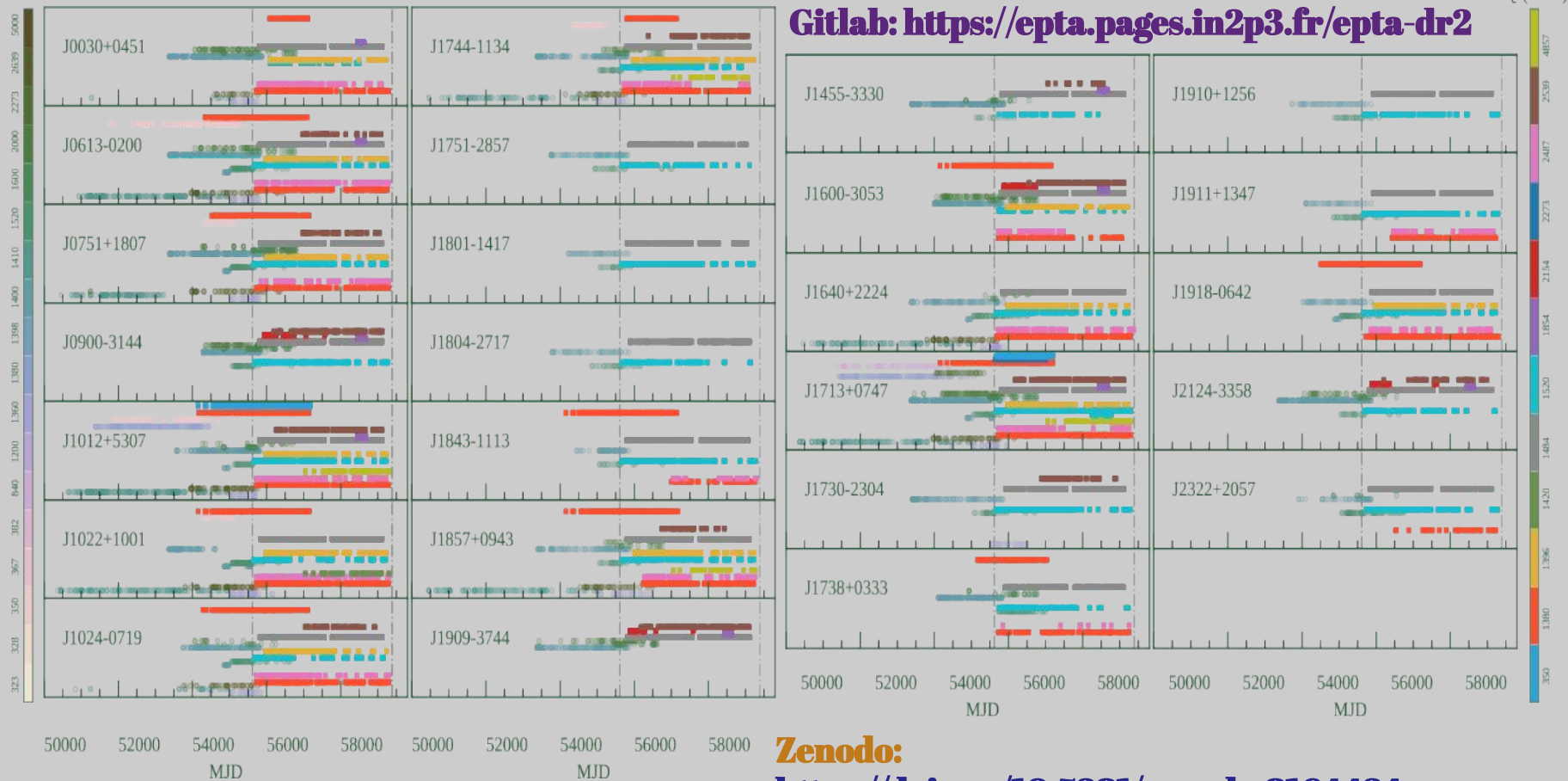


F_c (MHz) ↓ Legacy Backends

EPTA DR2 - Paper I A&A, in press, doi: 10.1051/0004-6361/202346841

Modern Backends ↓ F_c (MHz)

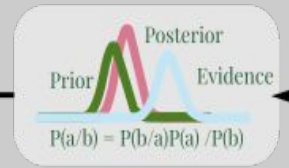
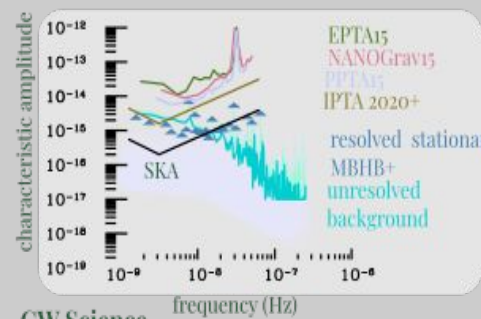
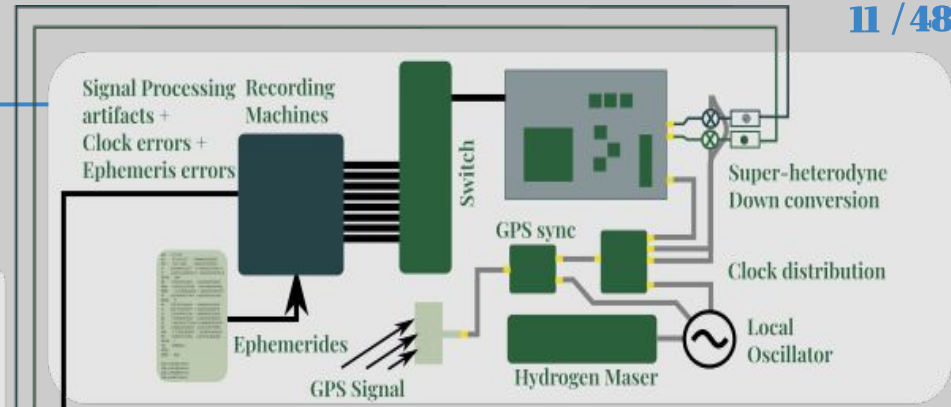
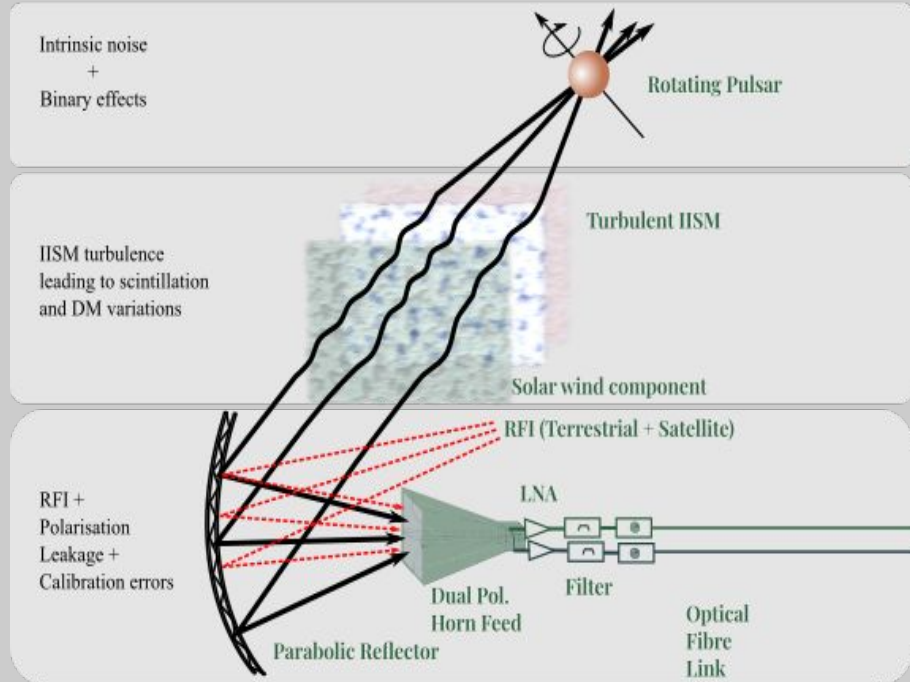
Gitlab: <https://epta.pages.in2p3.fr/epta-dr2>



Zenodo:

11.11.2023 / 10.5291 / 1.0104194

PTA noise sources



Analysis Pipelines

● Figure adapted from Verbiest & Shaifullah, 2018, CQG

GW Science - plot shows part of fig. 33 from Colpi & Sesana, 2017

The detection statistic and search algorithm

- We assume that noise is Gaussian: the likelihood function (likelihood of the signal with given parameters) is

$$P(\vec{\delta t}, \theta) = \{1/\sqrt{(2\pi)^n \det(\mathbf{C})}\} \exp(-\frac{1}{2} (\vec{\delta t} - \vec{s})^T \mathbf{C}^{-1} (\vec{\delta t} - \vec{s}))$$

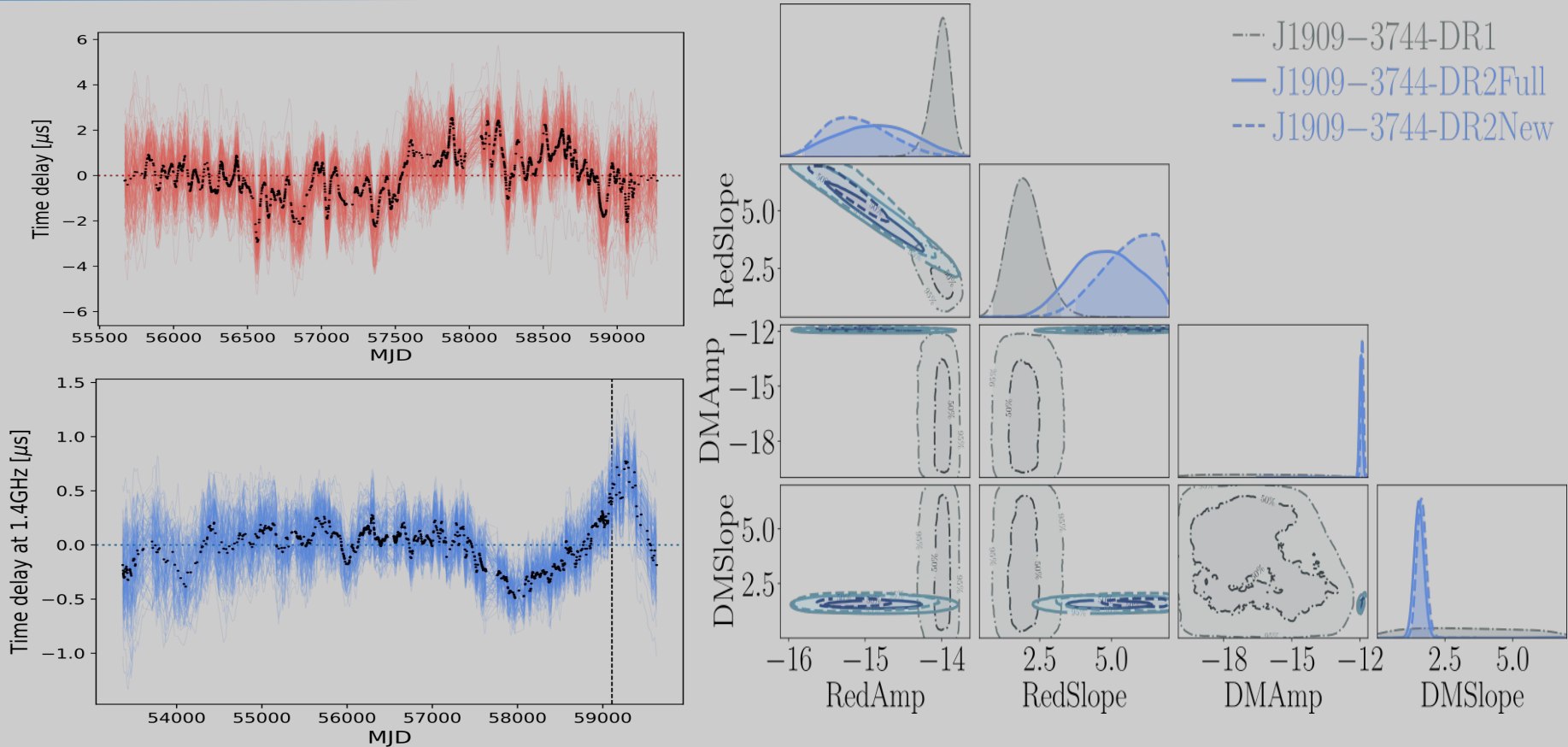
- δt - concatenated residuals from all pulsars in the array: total size n
- s - is a model of deterministic signals (e.g. - GW signals from individually resolvable SMBHBs)
- C is the noise variance-covariance matrix (size $n \times n$);

$$C_{\alpha i, \beta j} = C^{\text{WN}} \delta_{\alpha\beta} \delta_{ij} + C^{\text{RN}}_{ij} \delta_{\alpha\beta} + C^{\text{DM}}_{ij} \delta_{\alpha\beta} + C^{\text{GW}}_{ij} \delta_{\alpha\beta} + \dots$$

white noise
↑
red (spin) noise
↑
dispersion noise
stochastic GW noise

pulsar index
toa index

Noise models & their validity

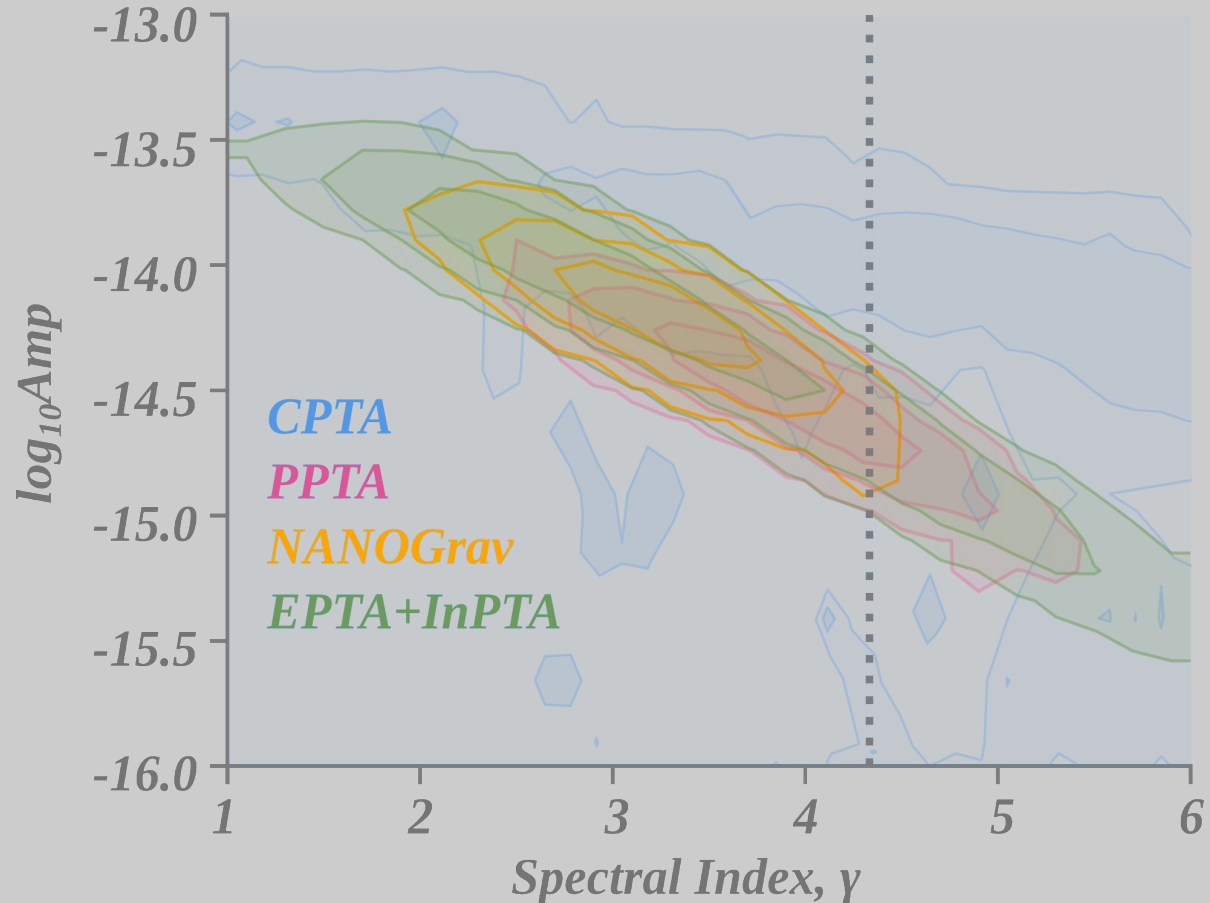


PTAs inching up to the GWB

On June 29, 2023 4 PTAs announced evidence for an HD correlated process in their data.

The significance ranges from ~ 2 to 4.6σ ; below the 5σ detection threshold.

Further this amplitude is **loud** ($\sim 2-3 \times 10^{-15}$) and the spectrum is **flat** (~ 3).



The International Pulsar Timing Array checklist for the detection of nanohertz gravitational waves

Bruce Allen,¹ Sanjeev Dhurandhar,² Yashwant Gupta,³ Maura McLaughlin,⁴
Priyamvada Natarajan,^{5, 6} Ryan M. Shannon,^{7, 8} Eric Thrane,^{9, 10} and Alberto Vecchio¹¹

1 Max Planck Institute for Gravitational Physics, Leibniz Universität Hannover, Callinstrasse 38, D-30167 Hannover, Germany

2 Inter University Centre for Astronomy & Astrophysics, Ganeshkhind, Pune - 411 007, India

3 National Centre for Radio Astrophysics, Pune University Campus, Pune 411007, India

4 West Virginia University Department of Physics and Astronomy, Morgantown, WV, 26501, USA

5 Department of Astronomy, 52 Hillhouse Avenue, New Haven, CT 06511

6 Black Hole Initiative, 20 Garden Street, Cambridge, MA 02138

7 Centre for Astrophysics and Supercomputing, Swinburne University of Technology, Hawthorn, VIC, 3122, Australia

8 OzGrav: The ARC Centre of Excellence for Gravitational Wave Discovery

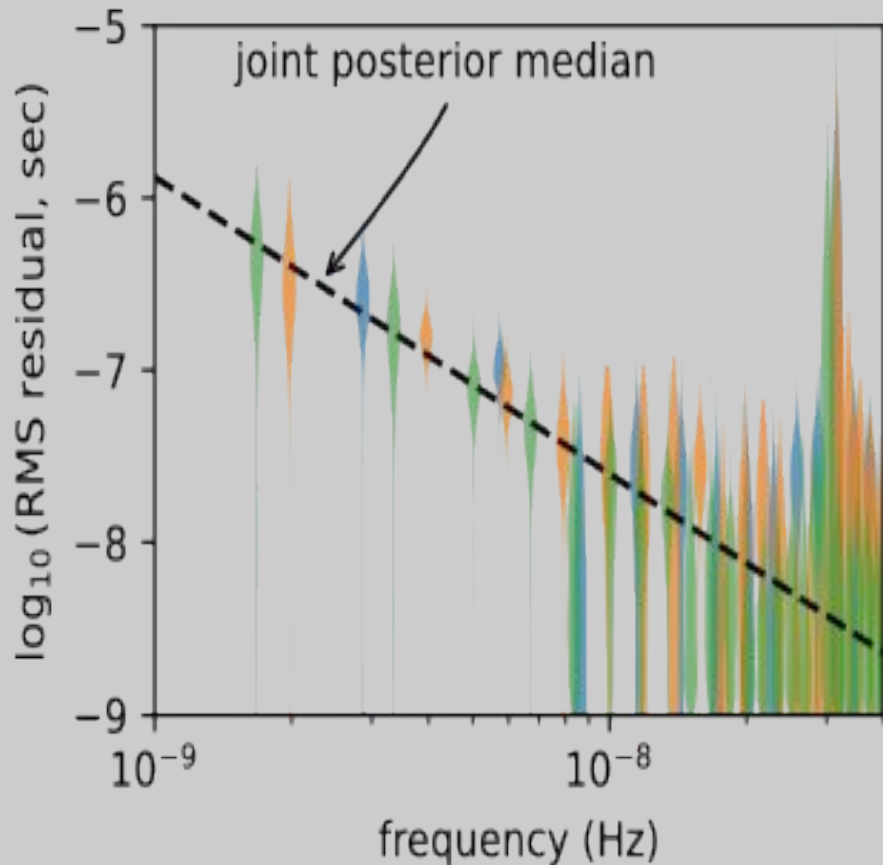
9 School of Physics and Astronomy, Monash University, Clayton VIC 3800, Australia

10 OzGrav: The ARC Centre of Excellence for Gravitational Wave Discovery, Clayton VIC 3800, Australia

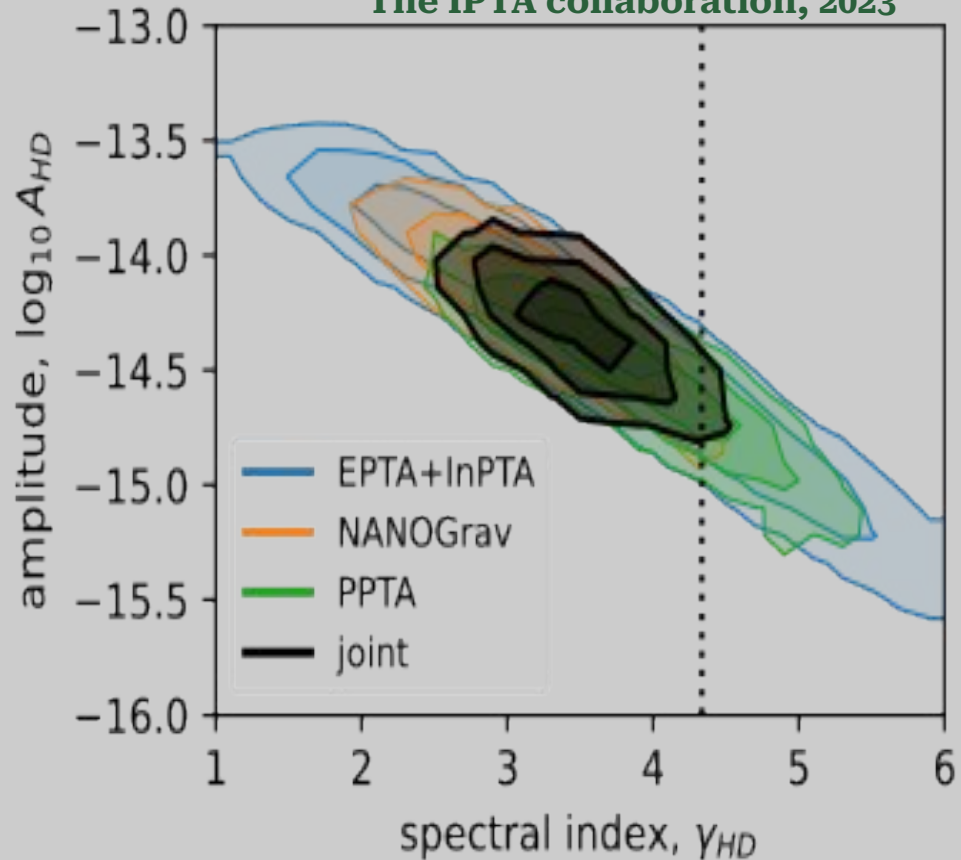
11 School of Physics and Astronomy & Institute for Gravitational Wave Astronomy, University of Birmingham, Birmingham, B15 2TT

“At the present time none of the PTAs have a detection claim.”

Do the PTAs agree?

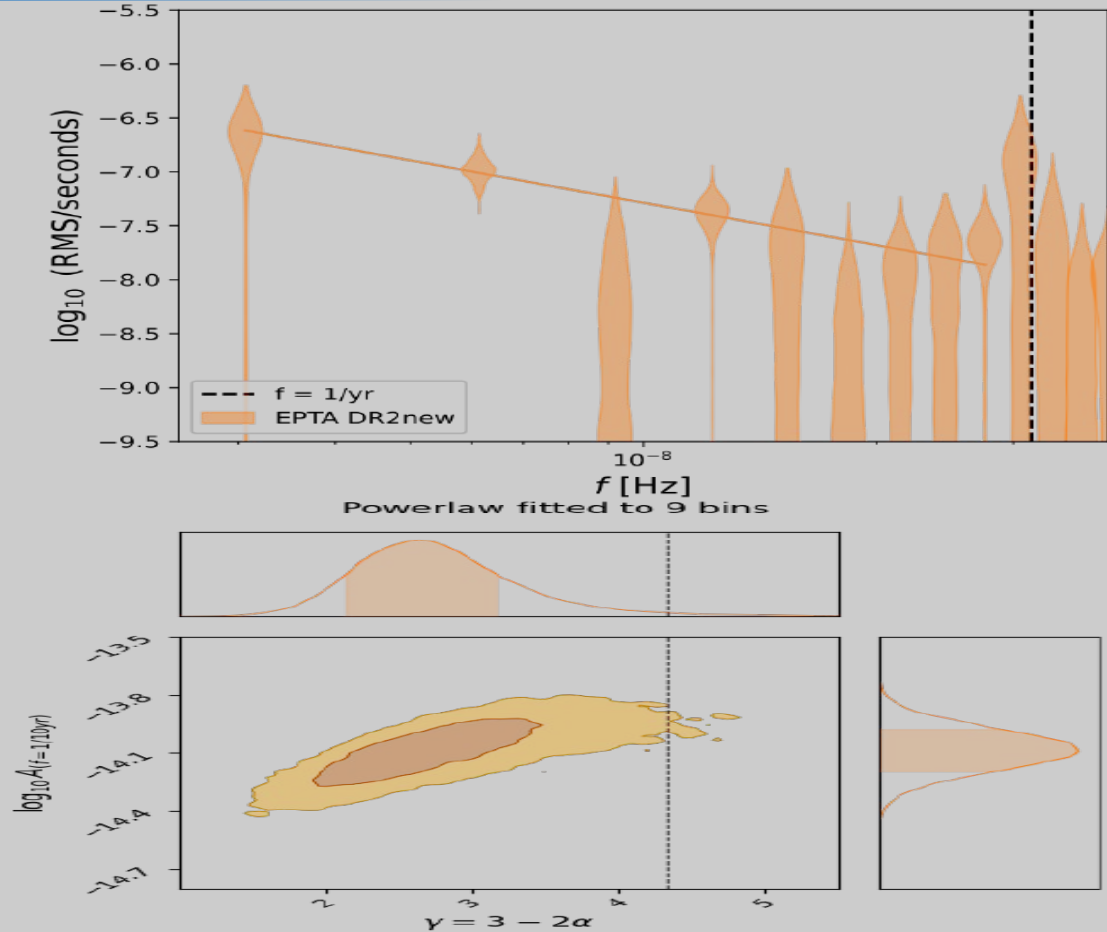


The IPTA collaboration, 2023



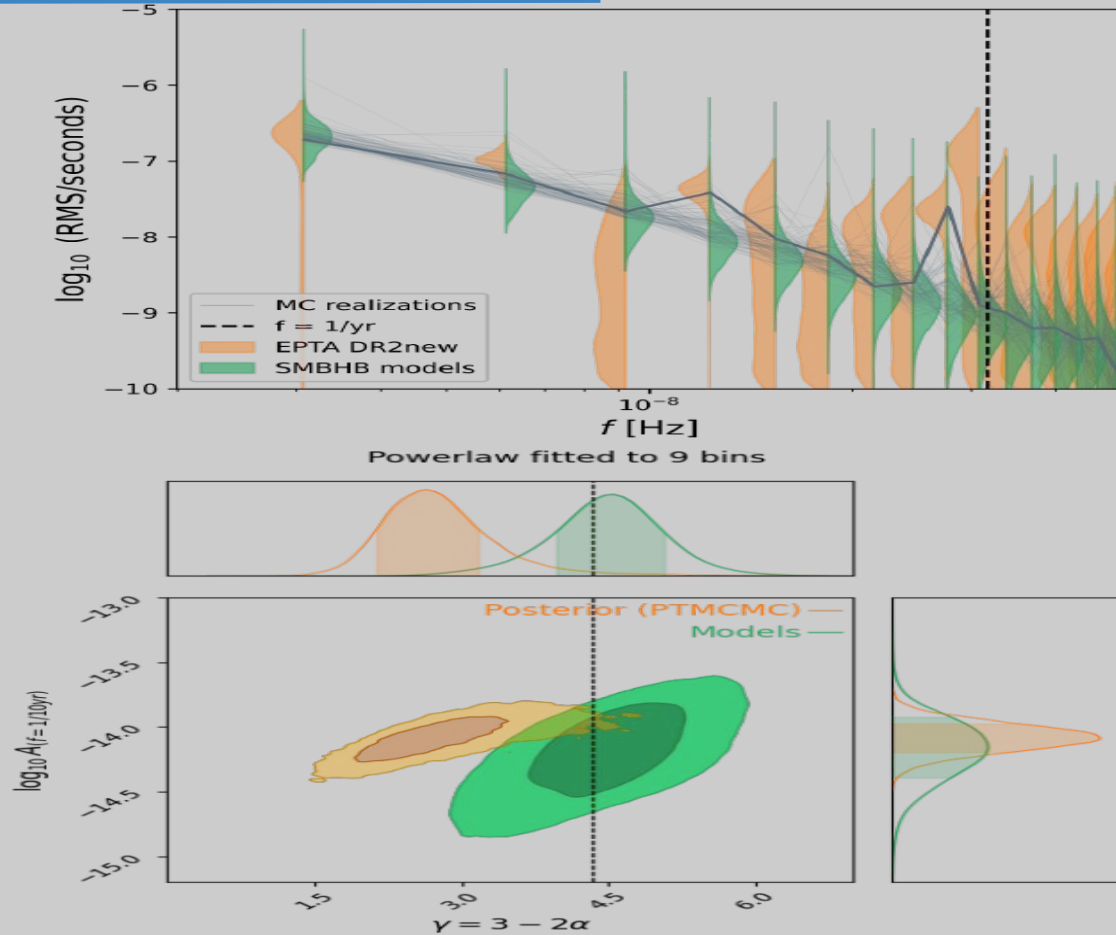
The astrophysical implications

- **The EPTA + InPTA result - a loud background**
- SMBHB generated backgrounds
- Comparisons with Semi-Analytical Models
- Stellar hardening?
- Biased by cosmic variance?
- Inflationary GWB
- Cosmic Strings
- Cosmic turbulence
- Curvature perturbations
- Challenging the ultralight dark matter paradigm



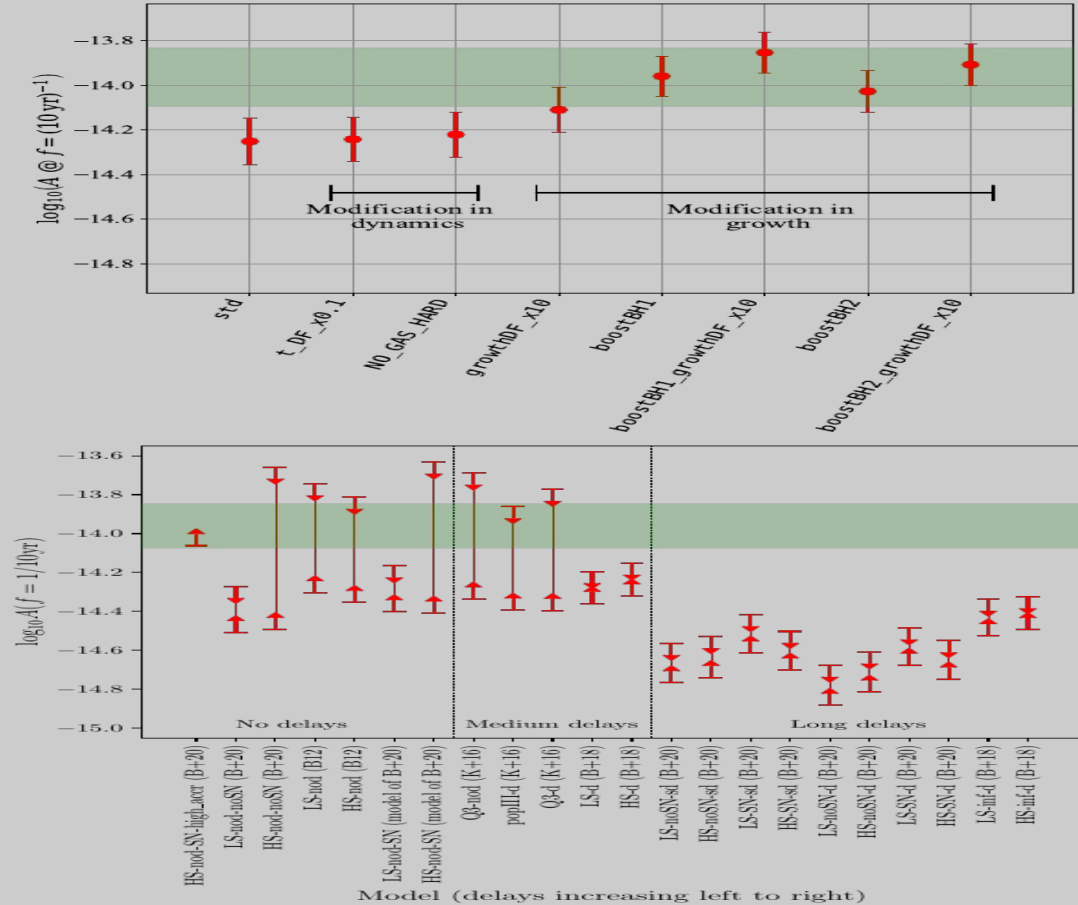
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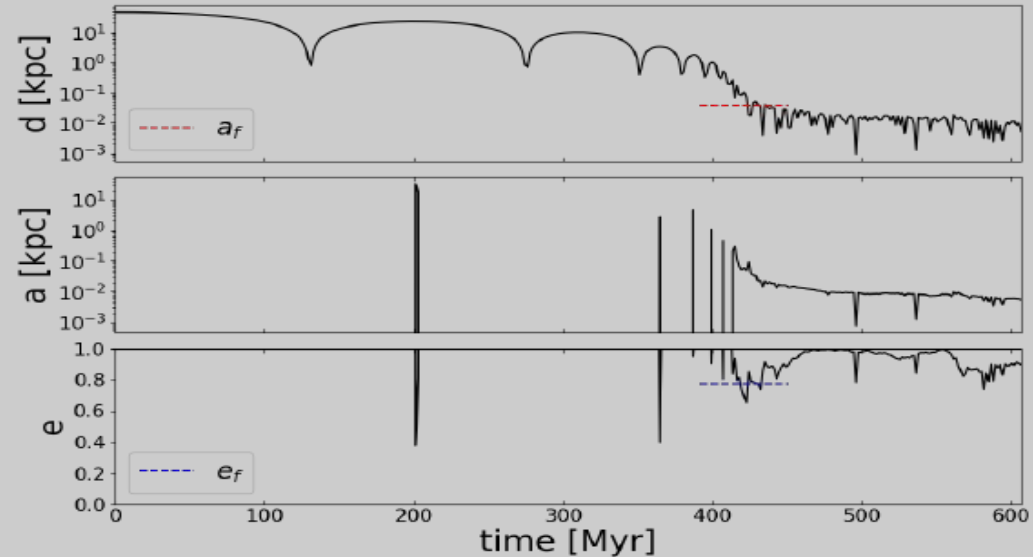
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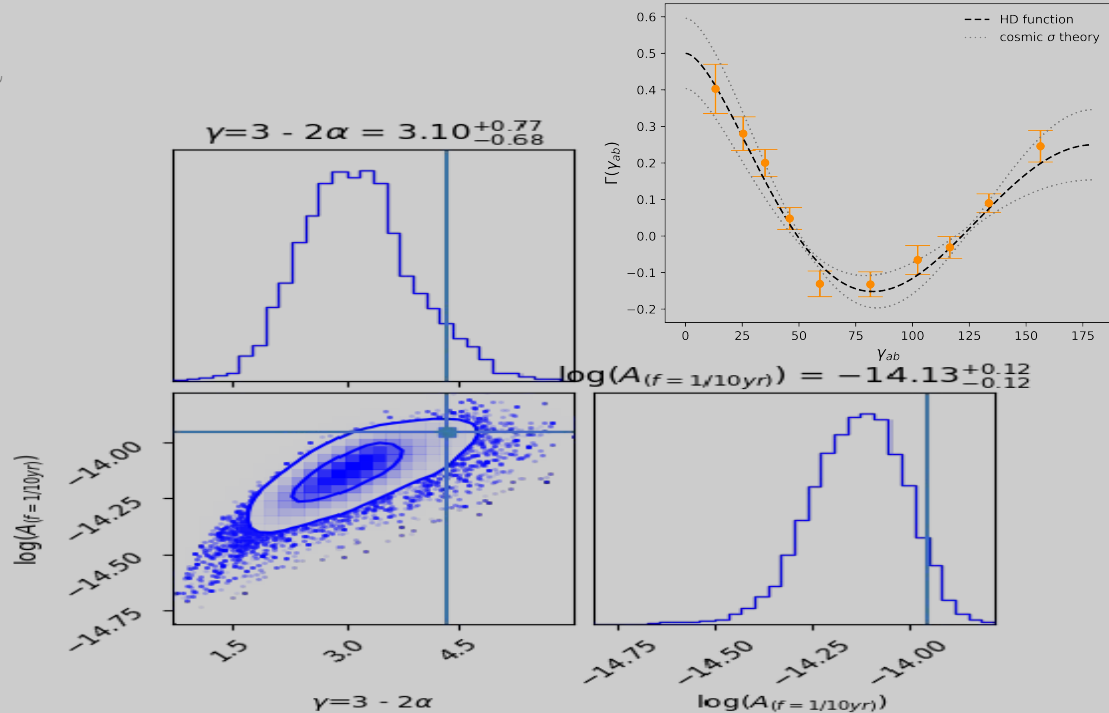
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A GWB generated by stellar hardening-affected SMBHB does NOT explain the PTA result...

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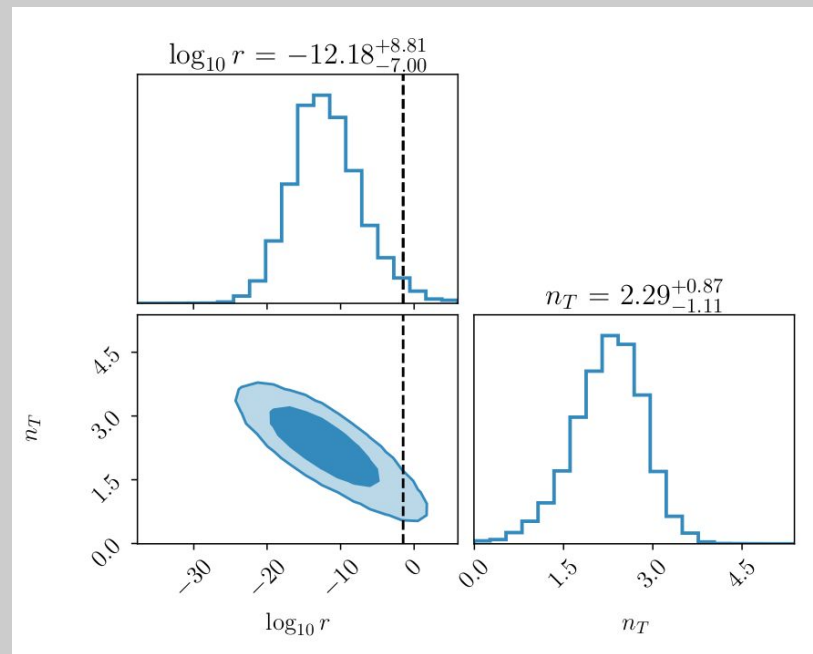
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... but a biased consideration of the uncertainties of the Hellings & Downs curve might.

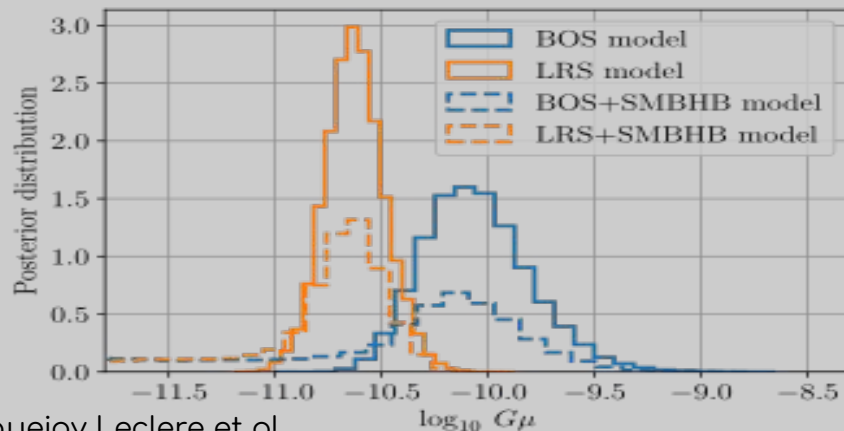
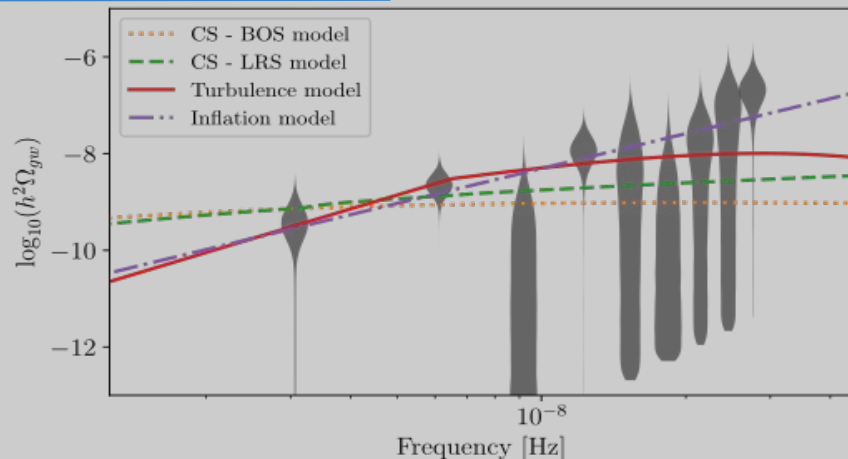
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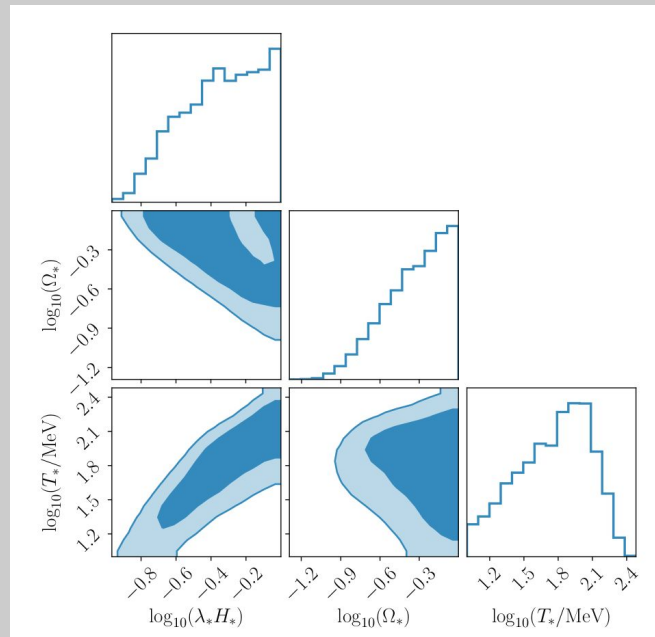
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Just listen Alberto's talk instead!

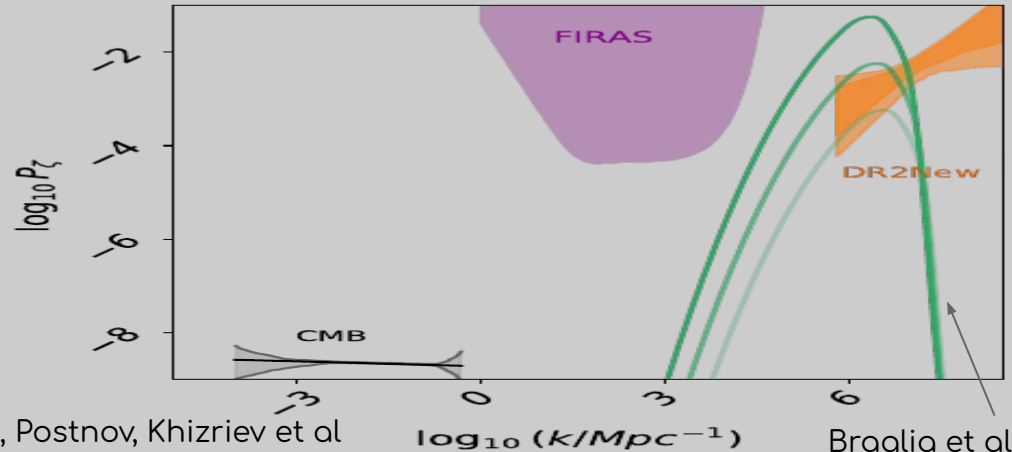
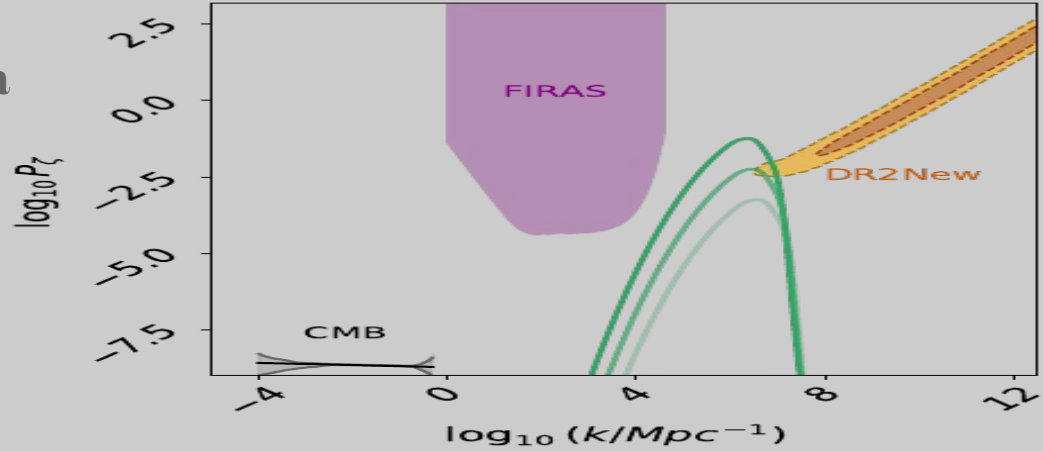


Quelquejey Leclere, Roper Pol et al

The cosmological implications

2nd order scalar induced GWB

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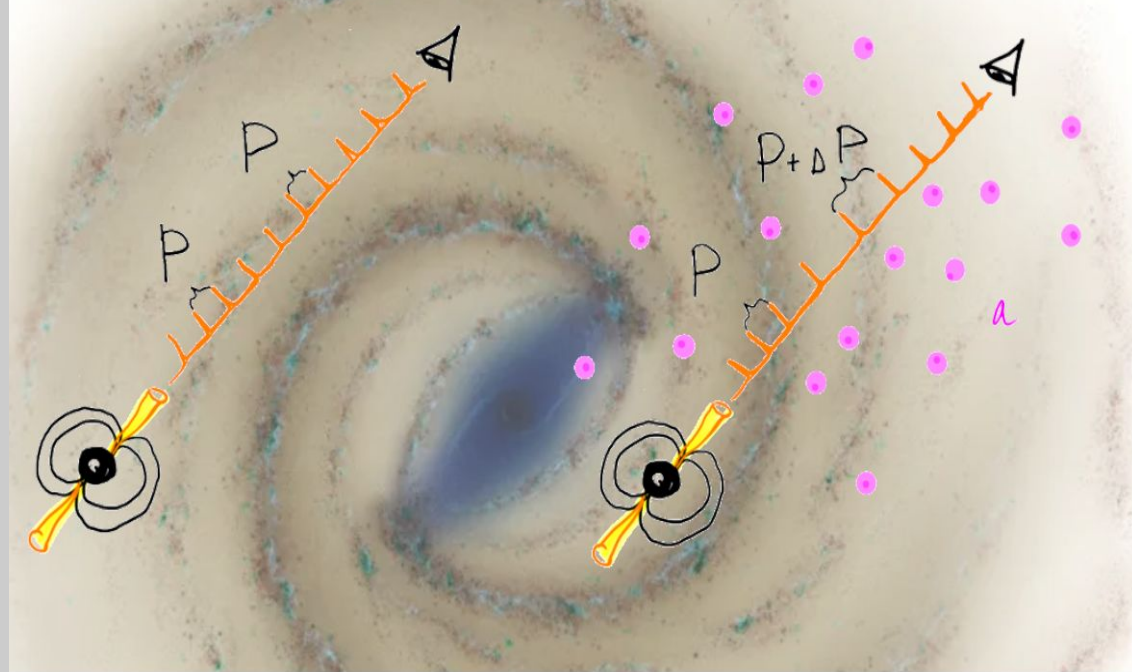
Can we talk about something fun please?

I. ULDM probes through timing data

$$R(t) = r(x_E, t_E) - r(x_p, t_p), \quad r(x_E, t_E) = \frac{\Psi(x_E)}{2\pi f} \kappa(x_E) \sin(2\pi f t_E + \alpha(x_E))$$

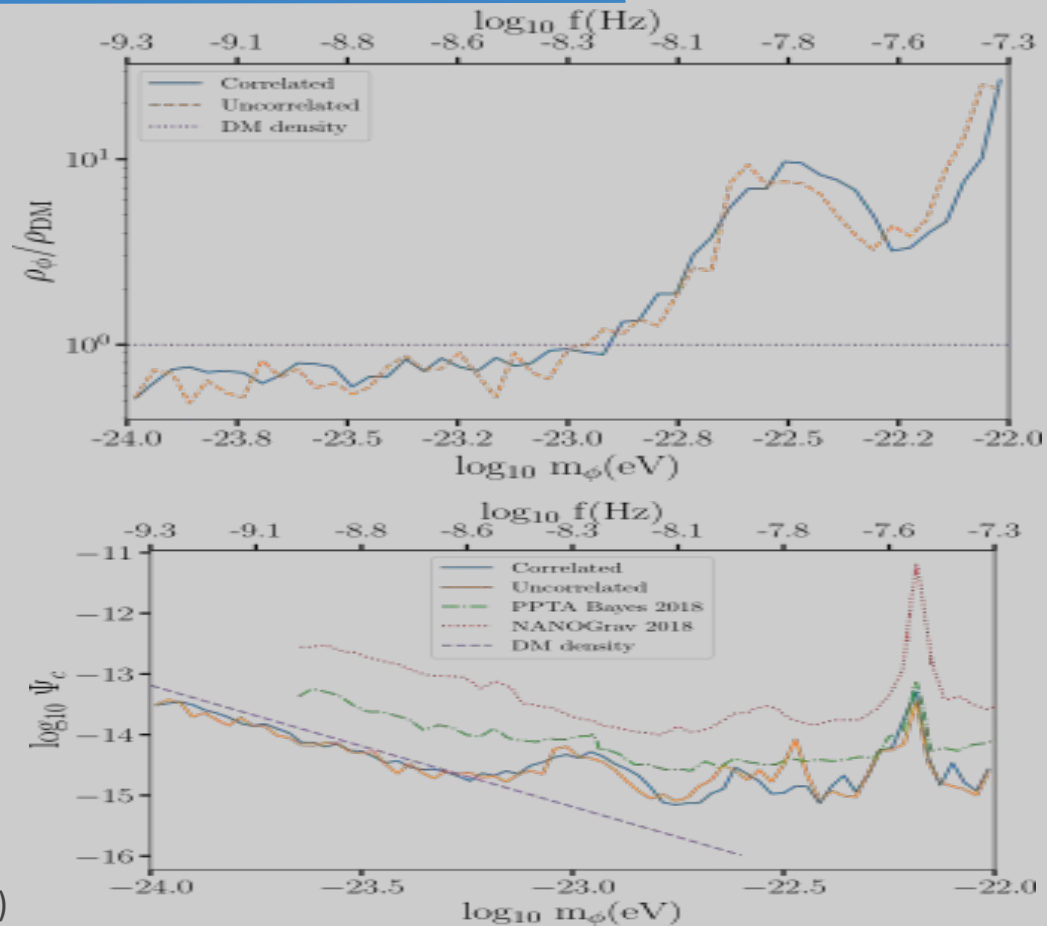
Ultra-light axion dark matter:

1. **Very light axions** with masses ranging between 10^{-23} and 10^{-20} eV
2. **Solve some of the issues of CDM** associated with overproduction of structures at galactic and sub-Galactic scales
3. **Perturb the space-time**, so that the regular flow of pulses deviate from their regular flow

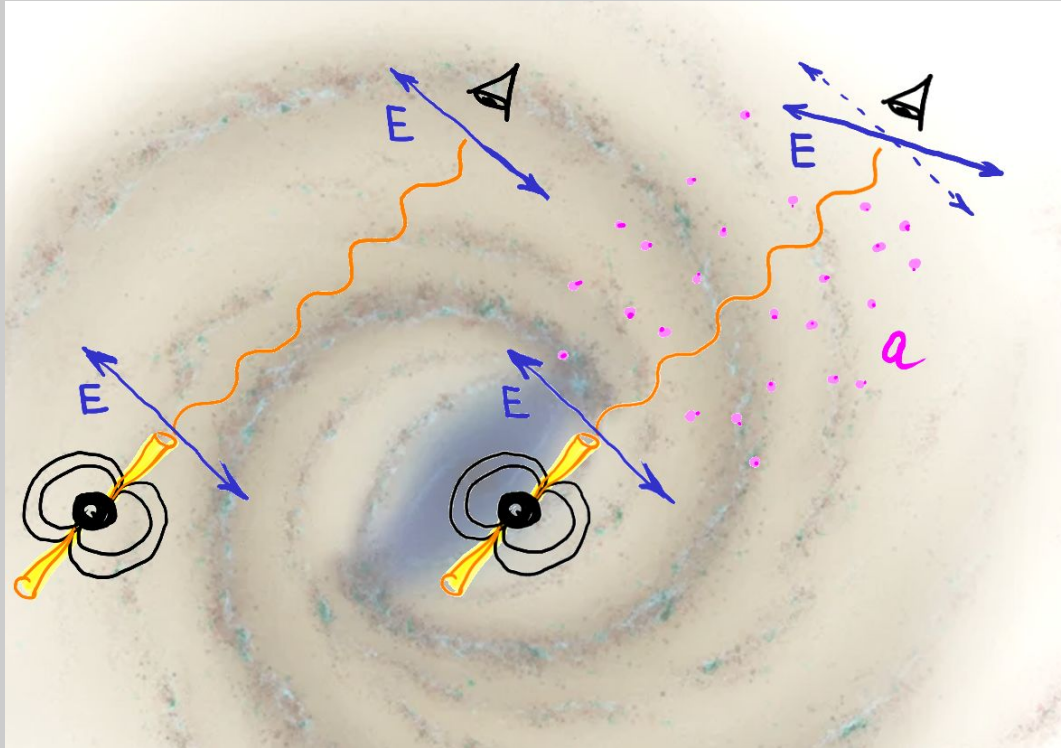


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II. ULDM with pulsar polarimetry



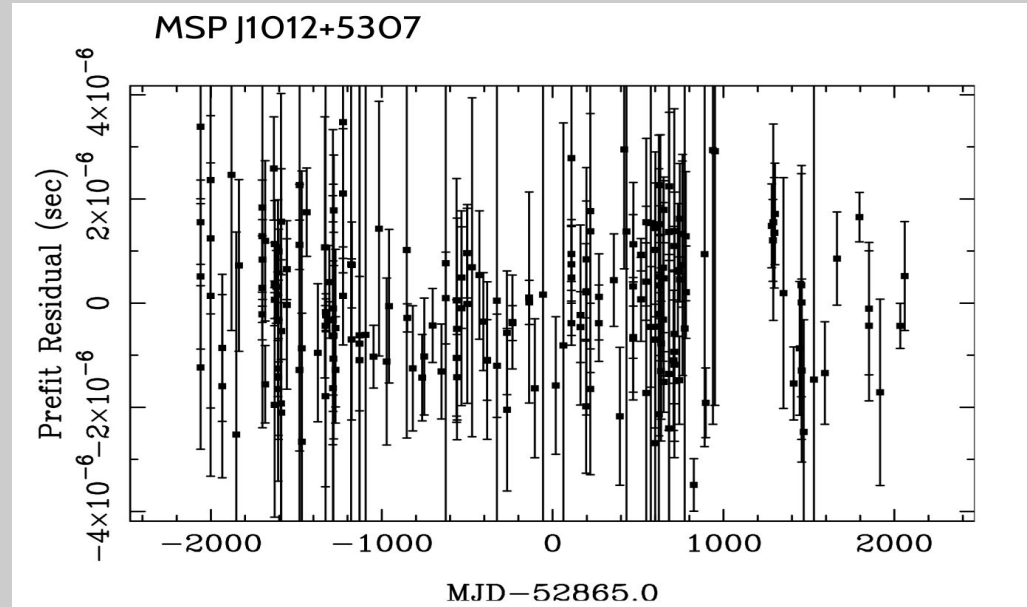
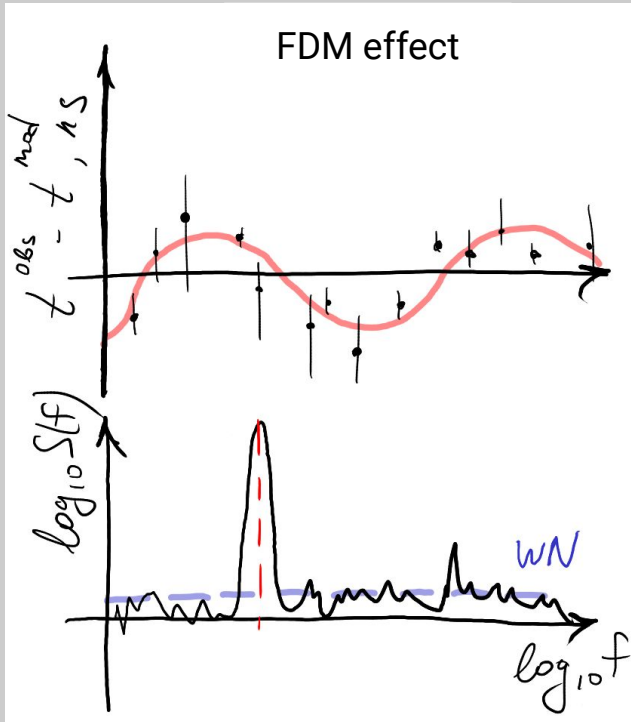
Credit:
NASA/JPL-Caltech

Ultra-light axions in the Milky Way:

1. **Very light axions** with masses ranging between 10^{-23} and 10^{-20} eV
2. When interacting weakly with photons, **rotate the plane** of linearly polarised pulsar light
3. Plane of linear polarisation **oscillates with periods of several years** due to varying pressure

I. ULDM probes through timing data

$$R(t) = r(x_E, t_E) - r(x_p, t_p), \quad r(x_E, t_E) = \frac{\Psi(x_E)}{2\pi f} \kappa(x_E) \sin(2\pi f t_E + \alpha(x_E))$$



II. ULDM with pulsar polarimetry

If we assume non-renormalizable interaction between fuzzy DM particles and photons:

$$\mathcal{L} = \frac{1}{4}F_{\mu\nu}F^{\mu\nu} + \frac{g_{a\gamma}}{4}aF_{\mu\nu}\tilde{F}^{\mu\nu} + \frac{1}{2}(\partial_\mu a\partial^\mu a - m_a^2 a^2)$$

$$(\square + m_a^2)a + \frac{g_{a\gamma}}{4}aF_{\mu\nu}\tilde{F}^{\mu\nu} = 0$$

Polarization properties of light are altered

$$\omega_\pm = k\sqrt{1 \pm g_{a\gamma}\frac{\partial_0 a}{k}} \simeq k \pm \frac{1}{2}g_{a\gamma}\partial_0 a$$

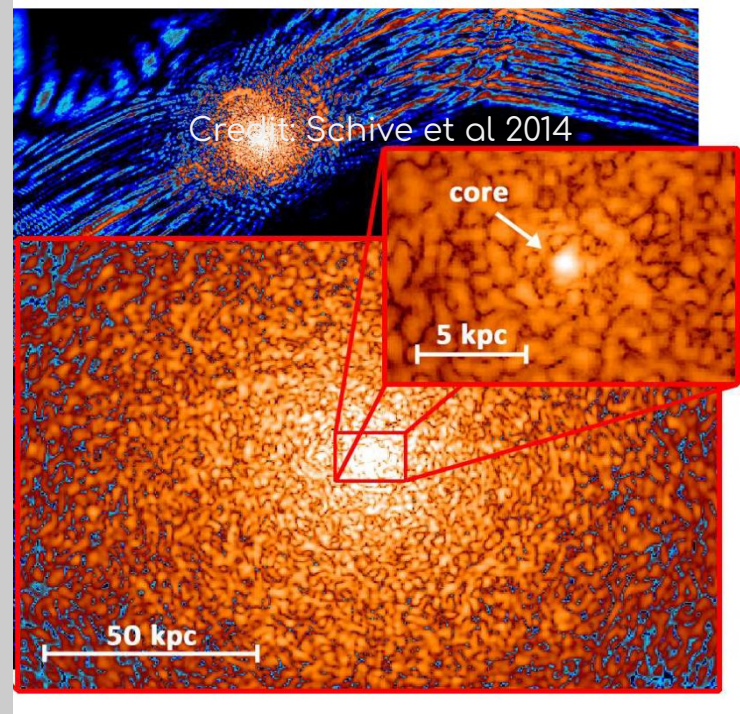
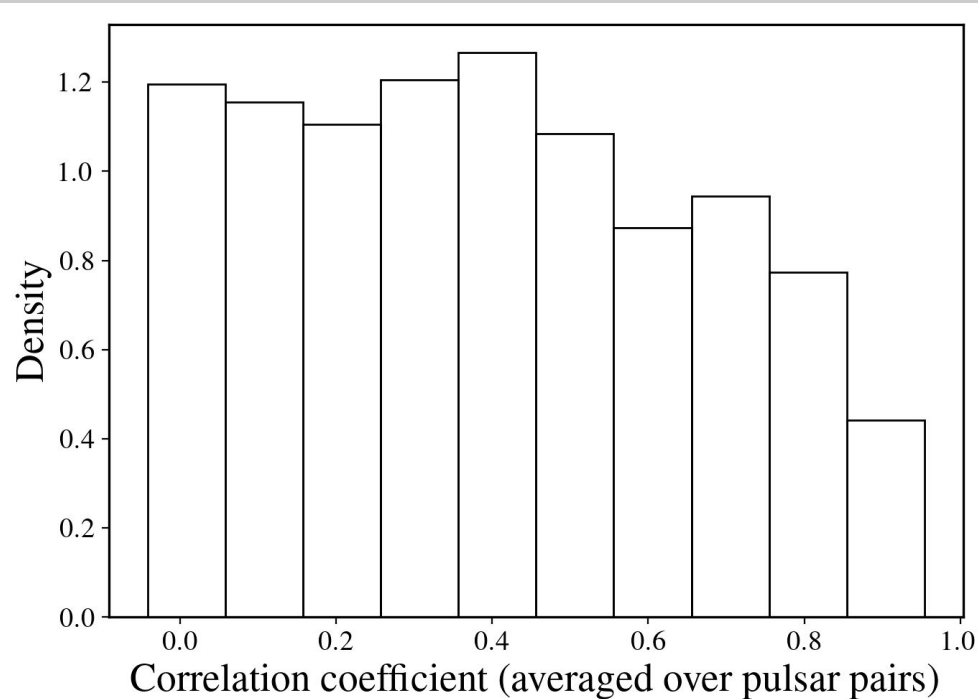
$$\Delta(\text{PA}(t)) = \frac{g_{a\gamma}}{\sqrt{2}m}[\text{p}(t_E, x_E) - \text{p}(t_p, x_p)], \quad \text{p}(t_E, x_E) = \sqrt{\rho_{\text{DM}}}\kappa_E \cos(mt + \phi(x_E))$$



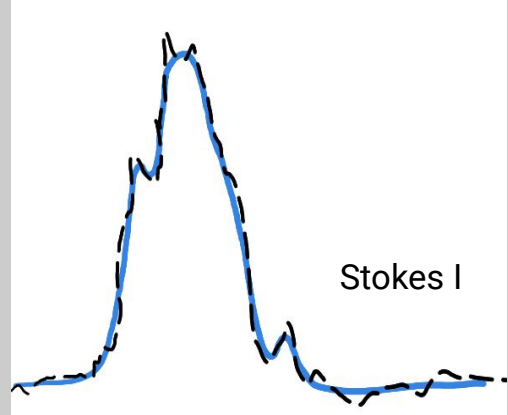
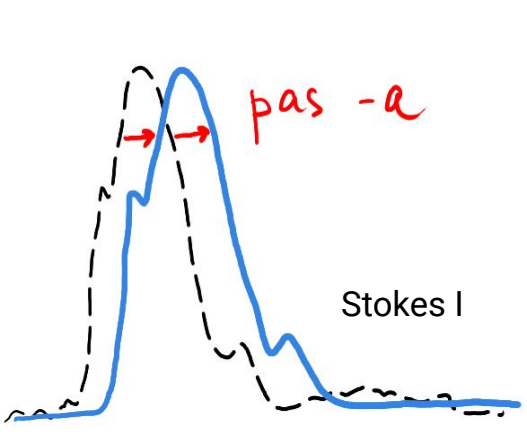
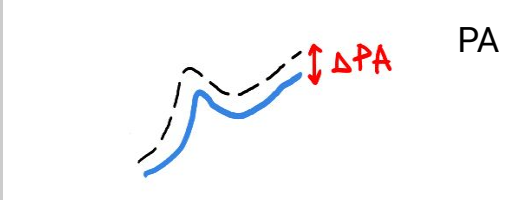
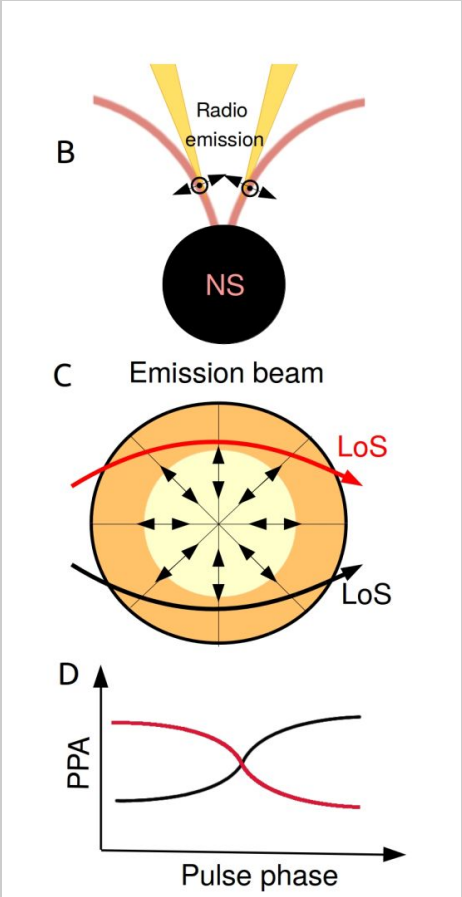
See: Ivanov et al 2018, Castillo et al 2022

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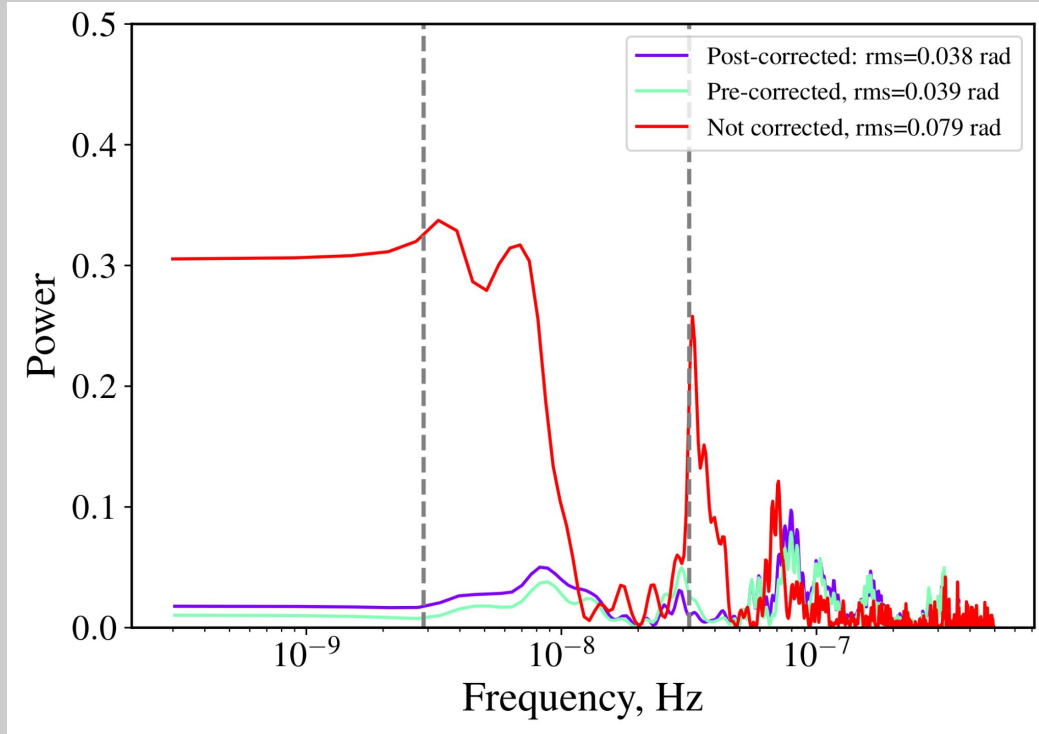


II. ULDM with pulsar polarimetry: data processing



$$\Delta PA = \frac{1}{2} \arcsin\{(U^{\text{obs}} Q^{\text{tmpl}} - Q^{\text{obs}} U^{\text{tmpl}})\}$$

II. ULDM with pulsar polarimetry: systematics



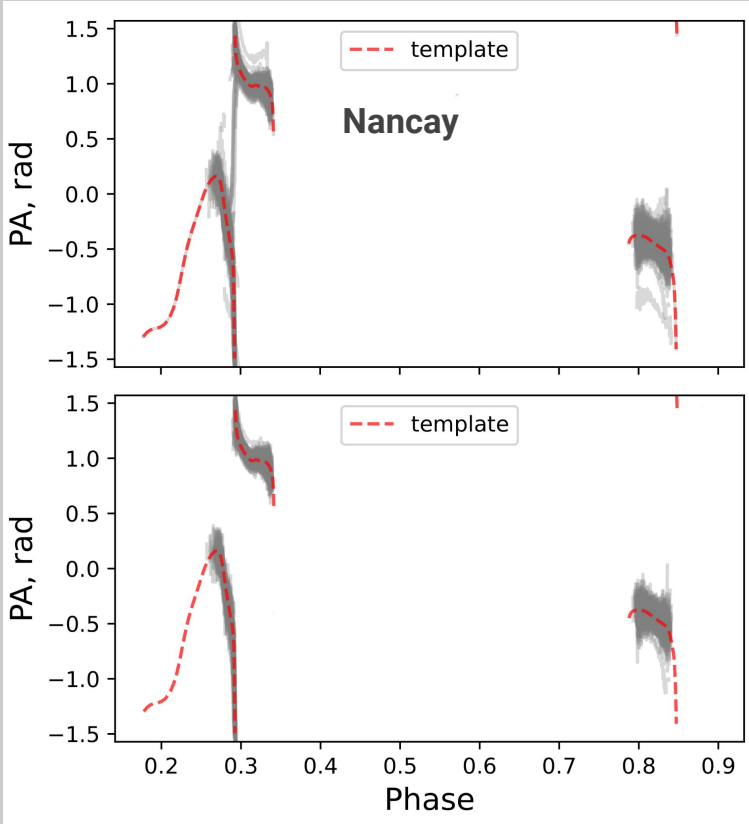
RMextract from Maaijke Mevius:
<https://github.com/lofar-astron/RMextract/tree/master/RMextract>

- i) Ionospheric TEC maps (uqrg)
- +
- ii) Geomagnetic field model (WMM)
- +
- iii) Thin screen approximation

$$\text{RM}_{\text{iono}} = \int n_e \mathbf{B}_{\text{LOS}} d\mathbf{r}$$

$$\text{RM}_{\text{iono}} \sim \text{STEC} \times \mathbf{B}_{\text{IPP}}$$

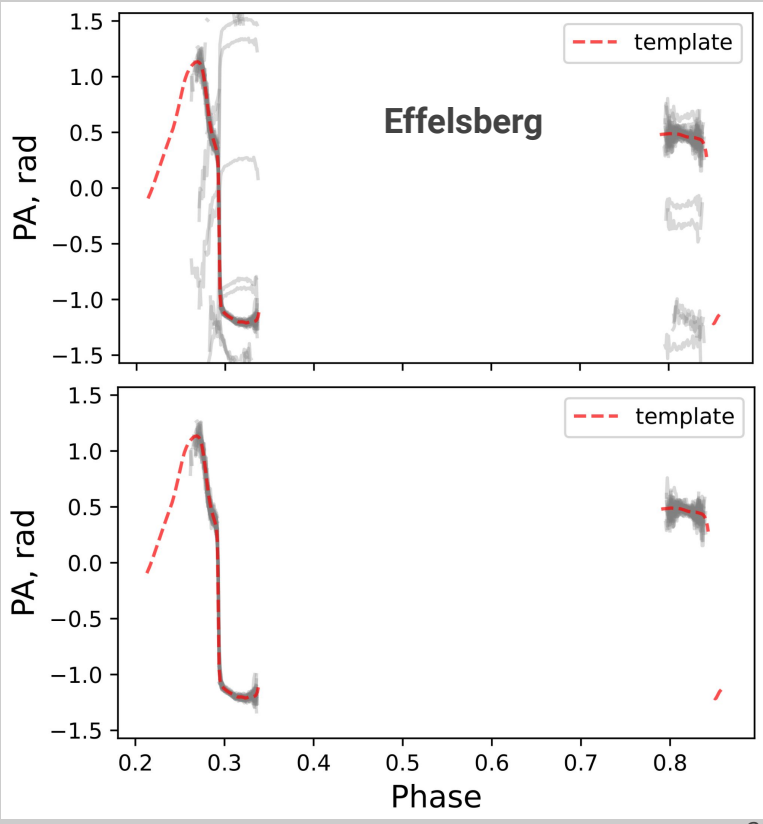
II. ULDM with pulsar polarimetry: challenges



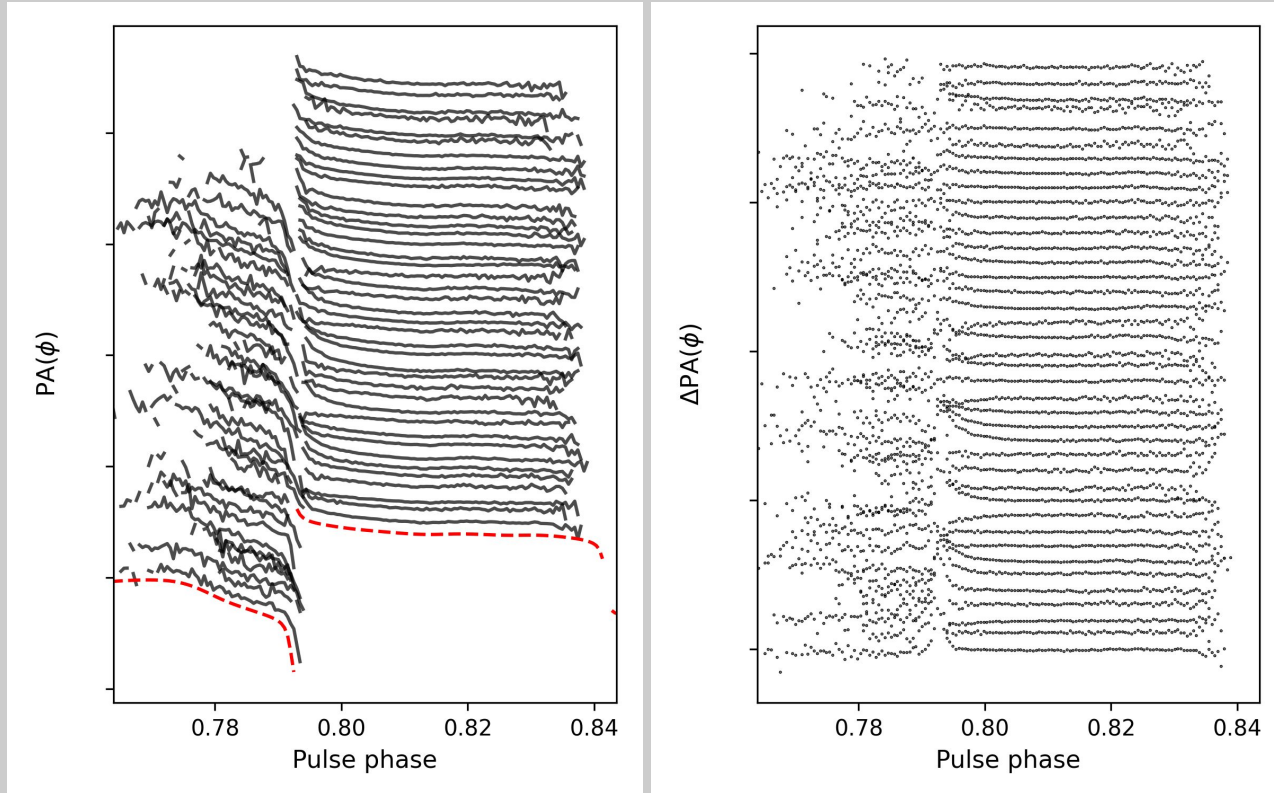
B1937+21

All PA profiles

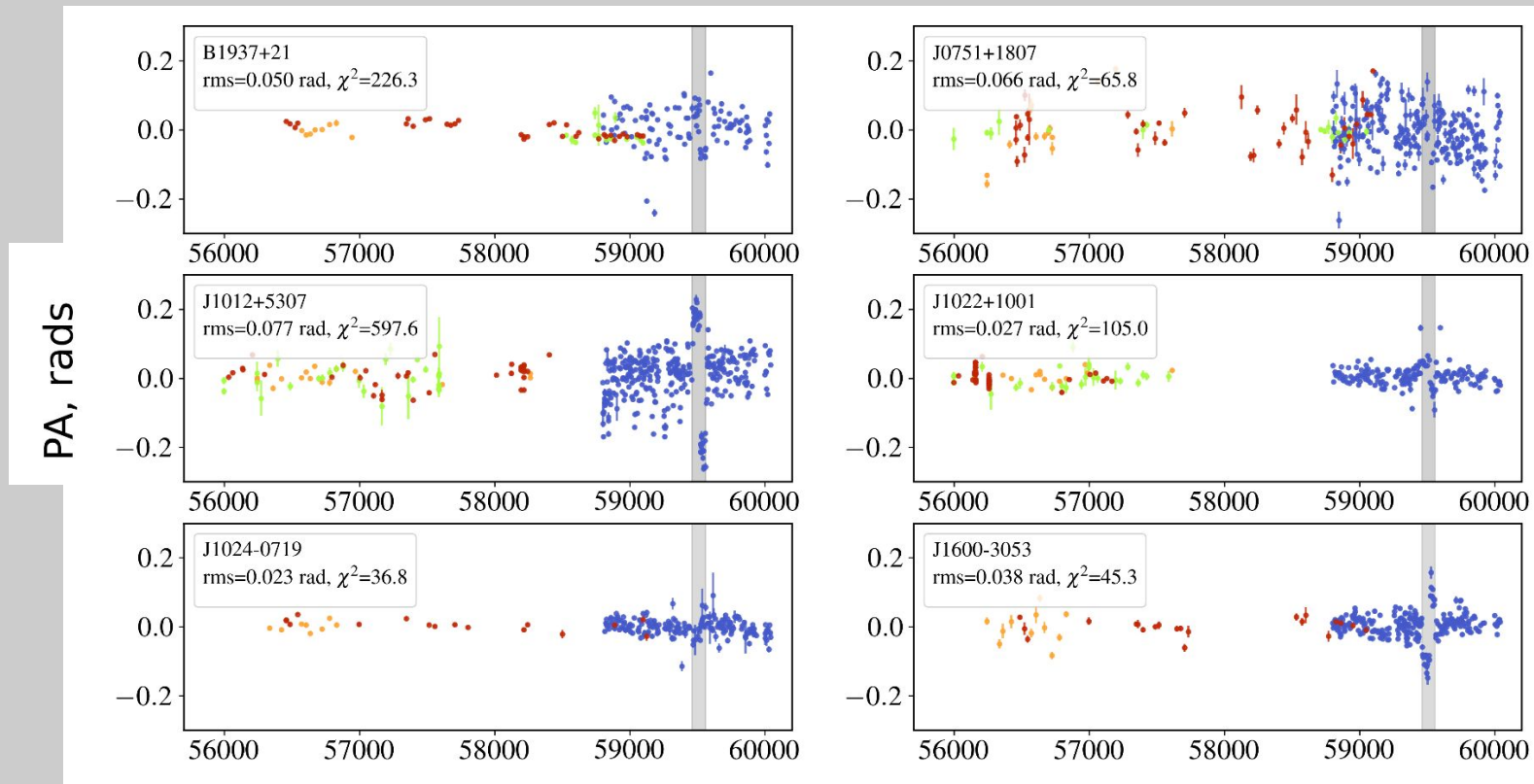
Manually selected
PA profiles



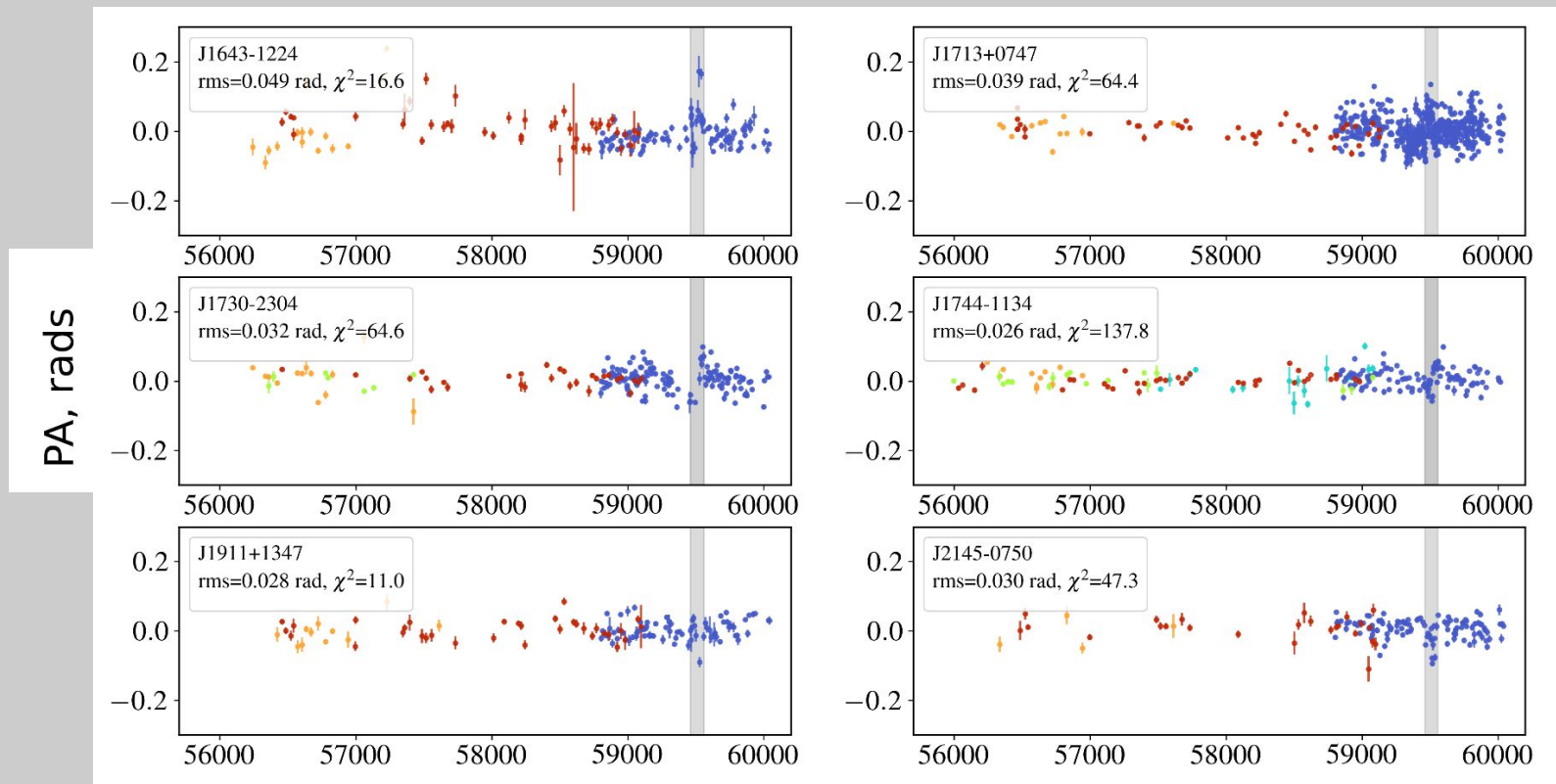
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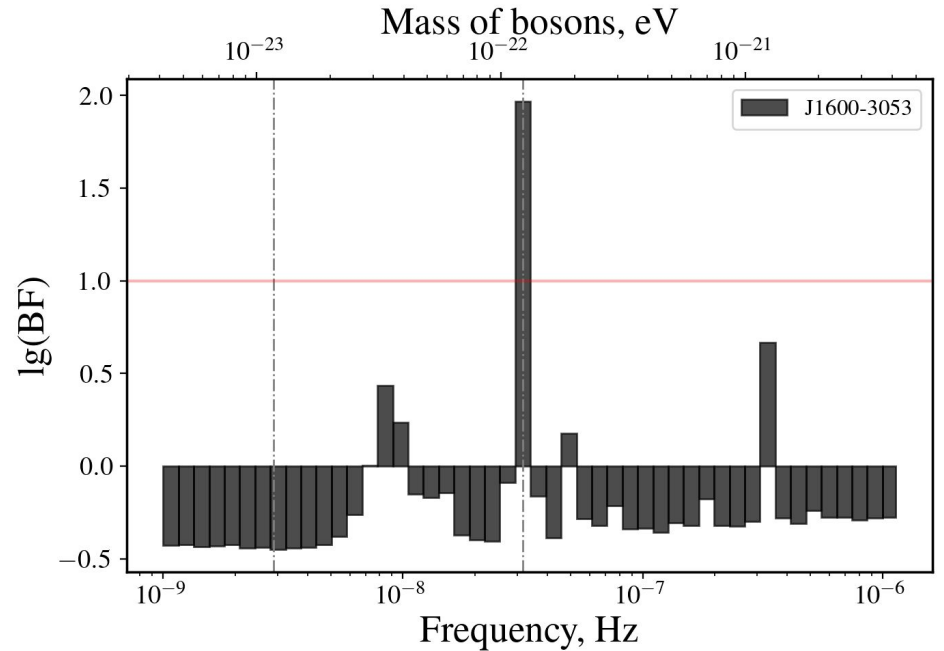
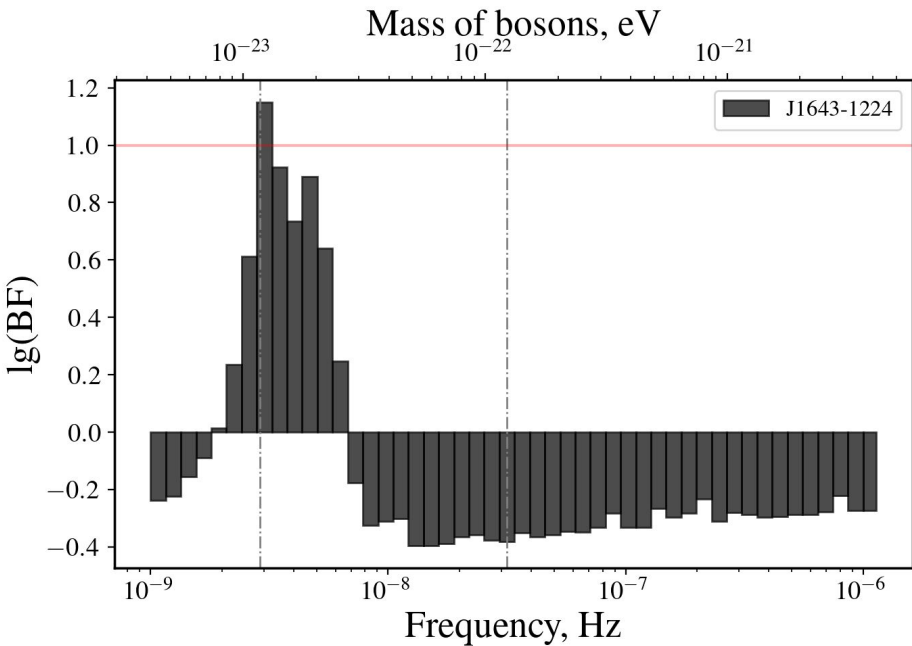
II. ULDM with pulsar polarimetry: dataset



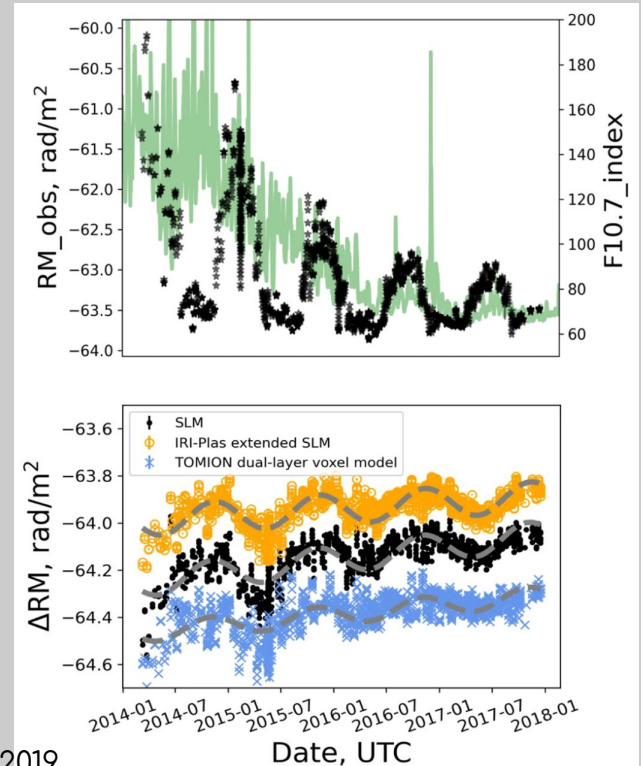
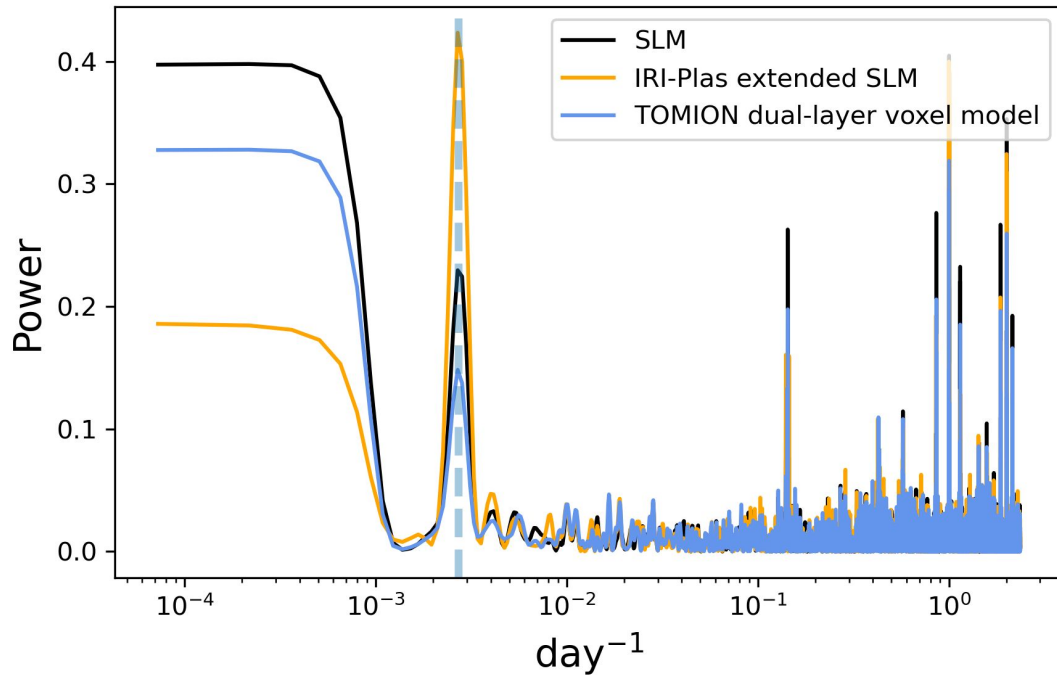
II. ULDM with pulsar polarimetry: dataset



II. ULDM with pulsar polarimetry: back to the ionosphere

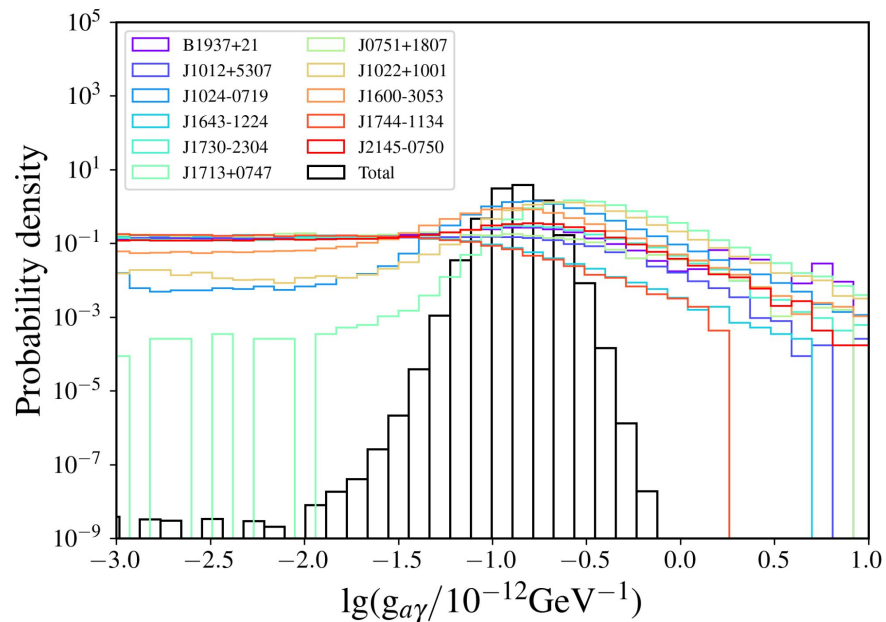
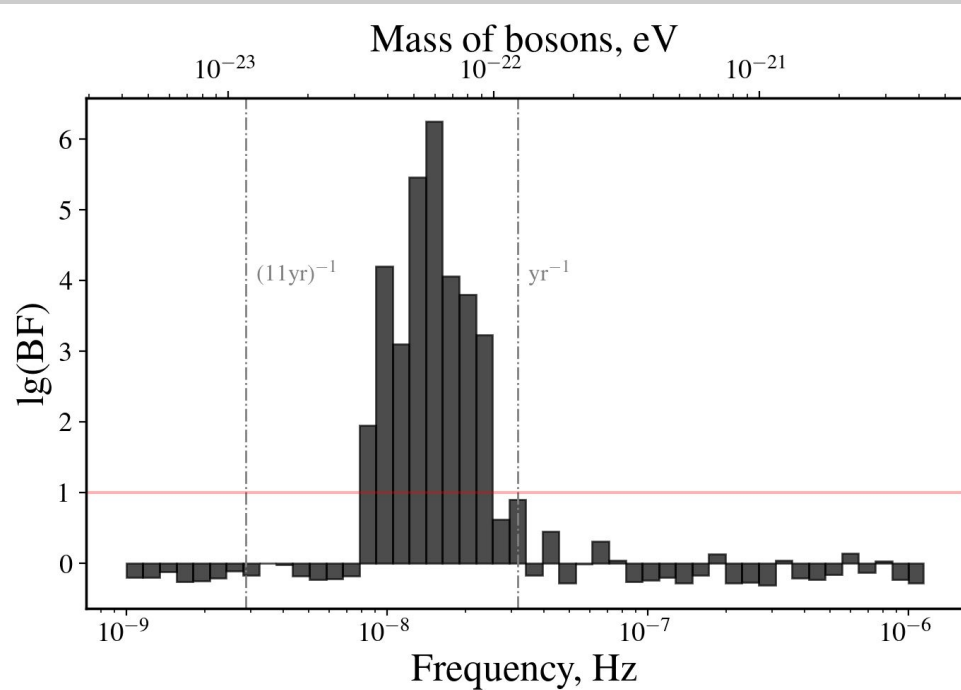


II. ULDM with pulsar polarimetry: back to the ionosphere

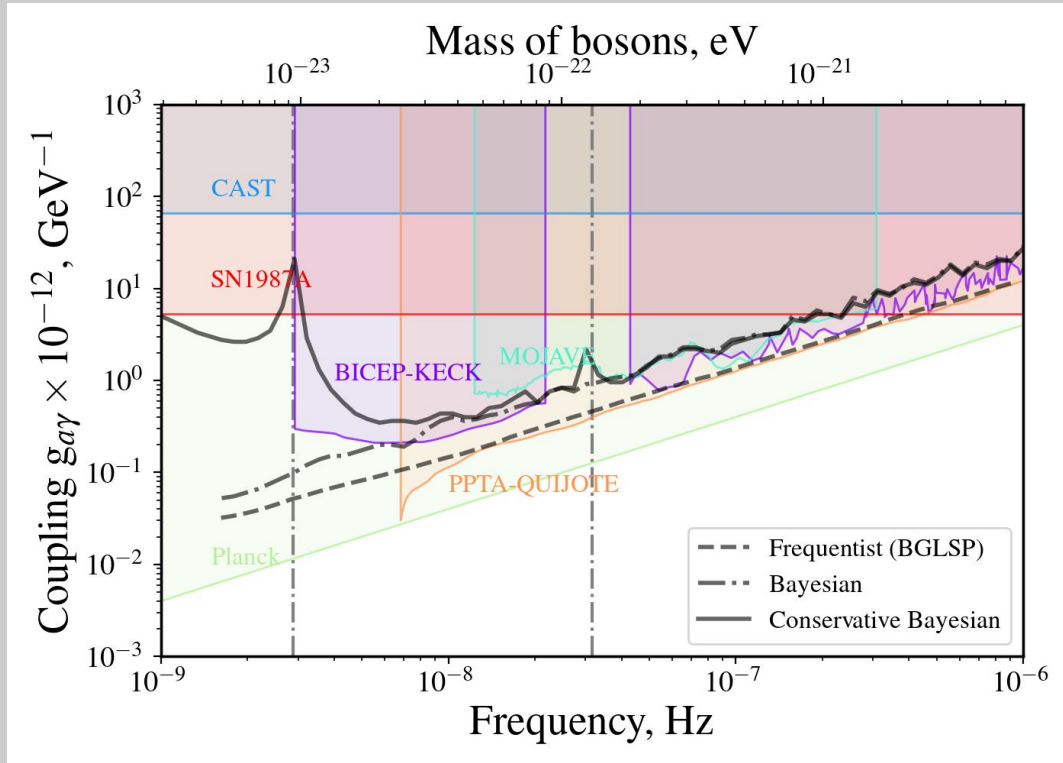


Porayko et al 2019,
Porayko et al 2023

Factorised upper limits and BFs



III. ULDM with pulsar polarimetry: first results



Ultra-light axions in the Milky Way:

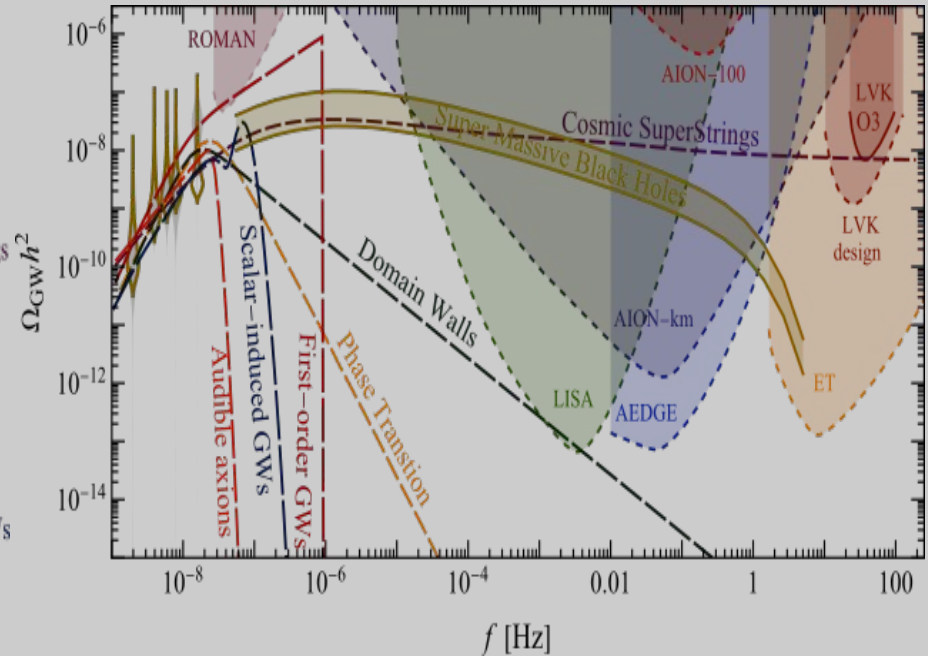
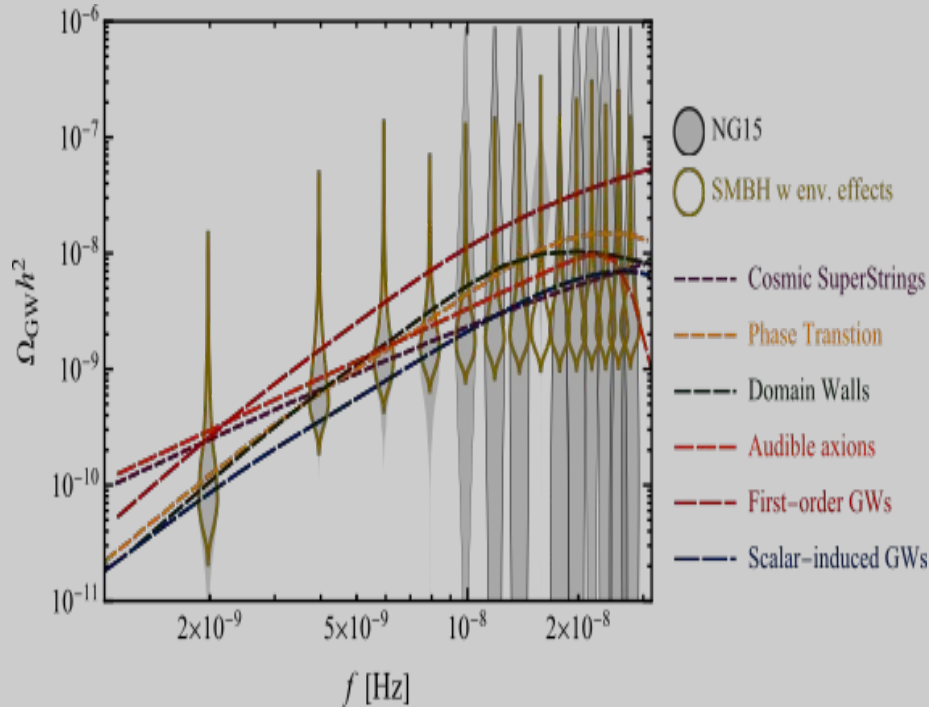
3. The **effect is achromatic**, so can be distinguished from chromatic Faraday rotation

4. **Terrestrial ionosphere** is the main source of noise, when searching for ultra-light axions in pulsar polarimetry

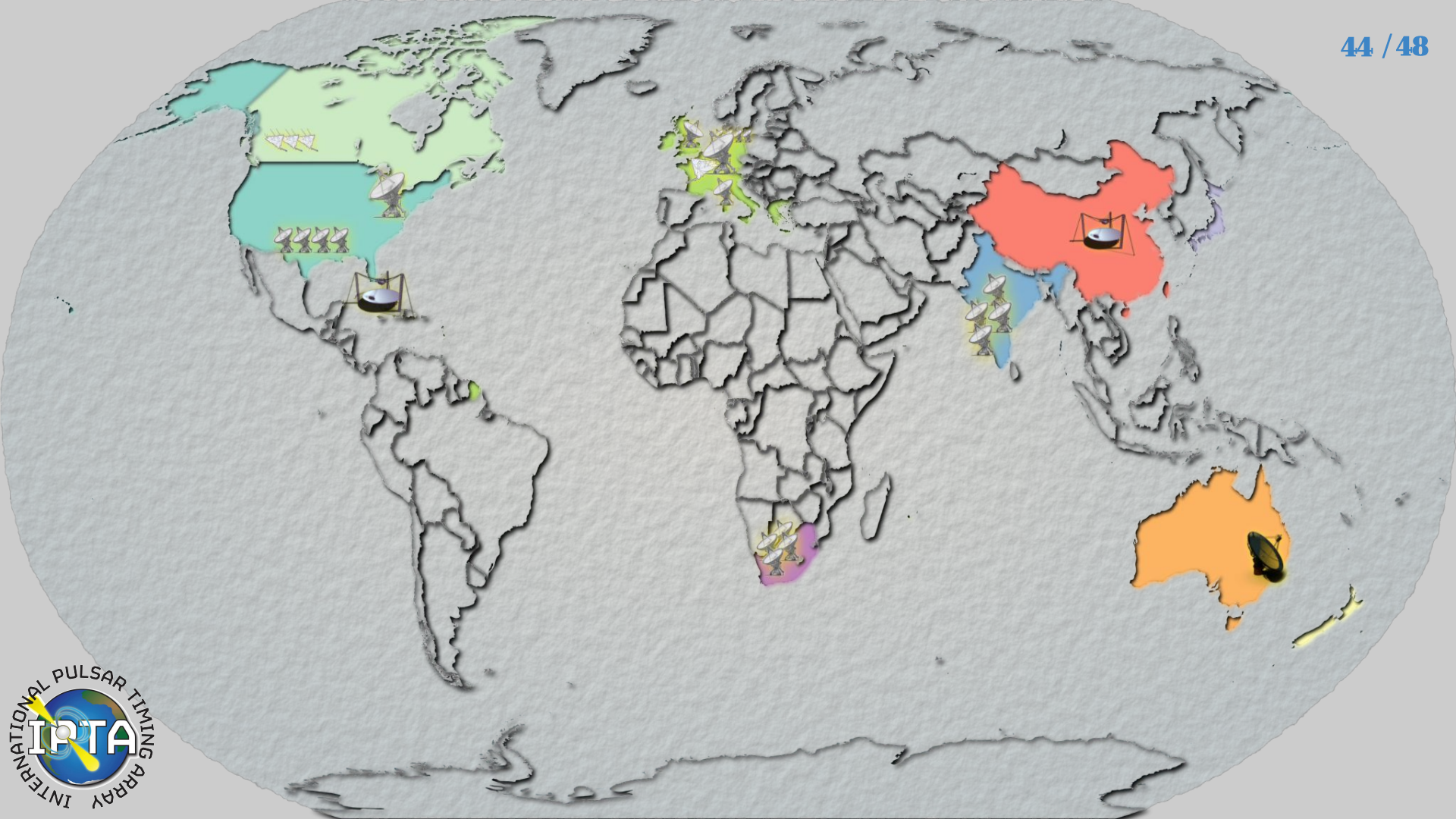
5. We plan to incorporate **low-frequency data** from LOFAR(2.0) to independently mitigate ionospheric Faraday rotation

The true picture & a wider landscape

So we are tantalisingly close to *detecting* the GWB, but what is the true nature of this signal?



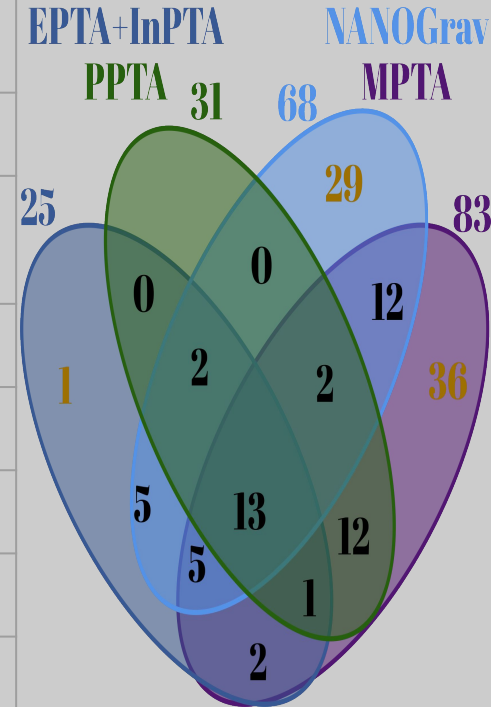
Ellis et al (2023; 2308.08546)



IPTA DR3 dimensions

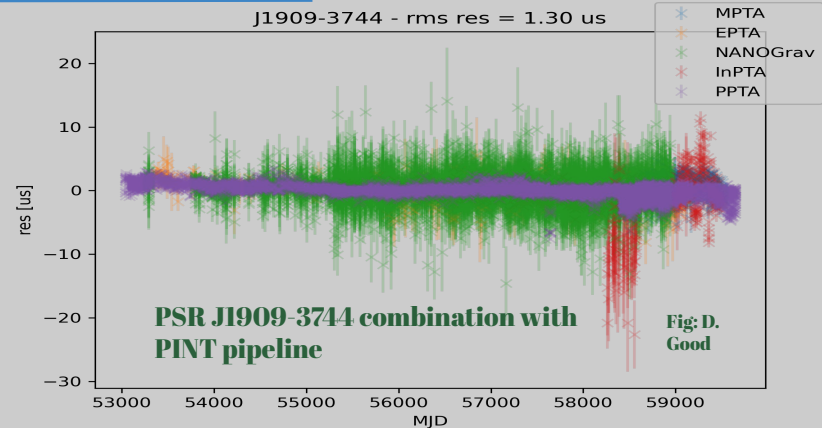


PTA	Dataset	PSRs	Tspan (years)	$f_{\text{GW,low}}$ (nHz)	f_{radio} (MHz)
EPTA	DR2 / DR3	25 / +35	24.5	1.29	283 - 5107
	LOFAR + NENUFAR	17	9.6	-	30 - 190
NANOGrav v	15-yr	68	15.9	1.99	302 - 3988
	CHIME	11	2.5		400 - 800
PPTA	DR3	24	18.1	1.75	704 - 4032
InPTA	DR1	15	3.5	9.05	300 - 1460
MeerKAT	DR2	88	4.5	7.04	856 - 1412
IPTA	DR3	121	~25/40	1.29/0.79	30 - 5107

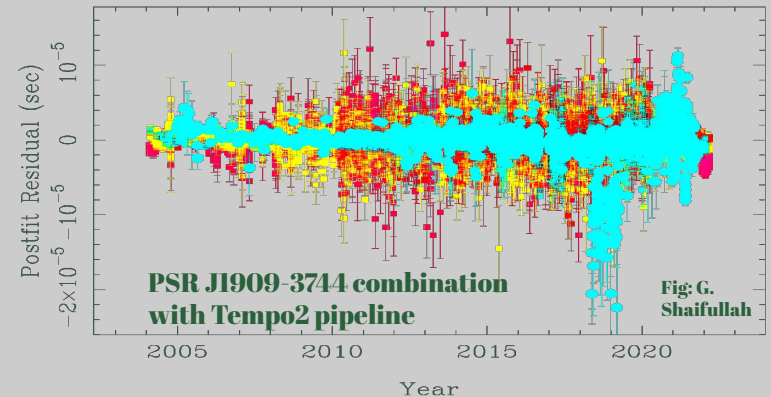


The IPTA DR3

- Add data from 5+ PTAs:
 - EPTA (+ LOFAR, NENUFAR)
 - NANOGrav (+ CHIME)
 - PPTA
 - InPTA
 - MPTA (MeerKAT)
- **2+ independent data combination pipelines**
- **121 pulsars, down to <100 ns for a few pulsars**
- Greater sky coverage!
- More pulsar pairs for angular correlation searches.
- **Lots of TOAs**
- **Loads of compute**
- July, 2024 - “Early Data Release” (eDR3), which includes the 20 best/longest-timed pulsars
- Dec, 2024 ~80 pulsars have been combined, first noise runs too!



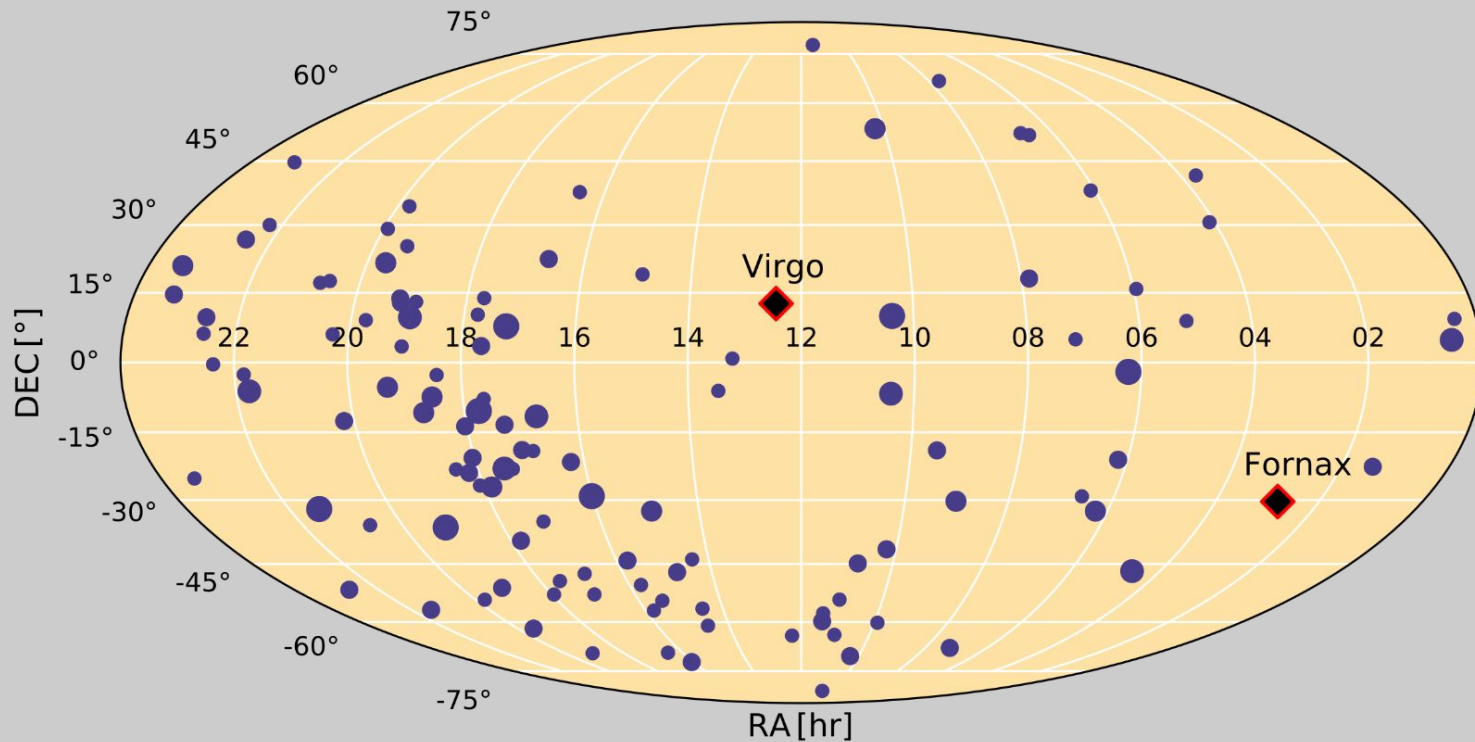
J1909-3744 ($W_{\text{rms}} = 0.631 \mu\text{s}$) post-fit



IPTA DR3 dimensions



- In total **121** pulsars in full DR3;
 - The biggest / most sensitive PTA dataset ever made !!



GWECs Coordination Office

Secretary General



Golam Shaifullah

Coordination Generals



Elisa Maggio



Mikhail Korobko



Gravitational-Wave Early Career Scientists



Former council members



Elisa Maggio



Graeme McChee



Huy-Tuong Cao



Martina Muratore



Michael Katz



Miquel Miravet



Monica Seglar



Nicola Tamanini



Simone Mastrogiovanni



Stefano Rinaldi

GWECs Council

LECS



Deborah Ferguson



Florentina Pisan



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Jishnu Suresh



Lucia Papalini

LAAC



Jessica Steinlechner



Mikhail Korobko



PTA



Golam Shaifullah

Einstein Telescope

Anna Green

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