

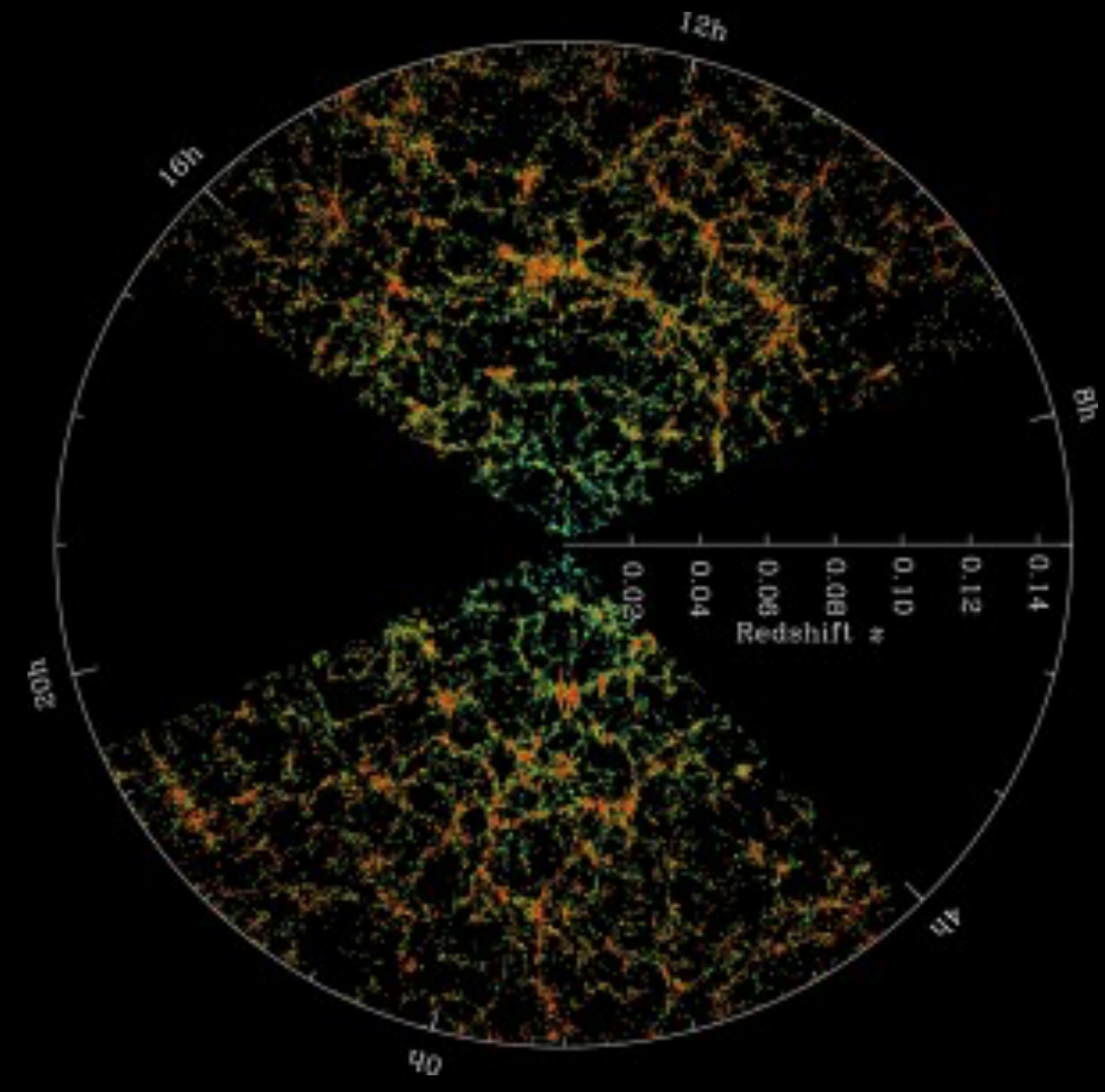
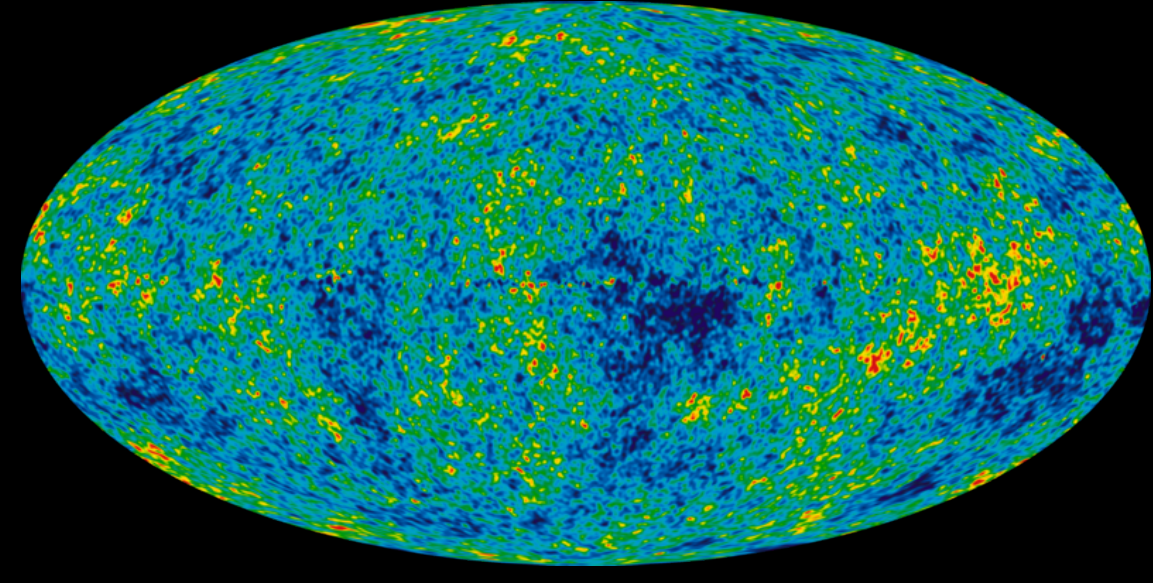
Seeing highly anisotropic gravitational wave backgrounds from the early universe

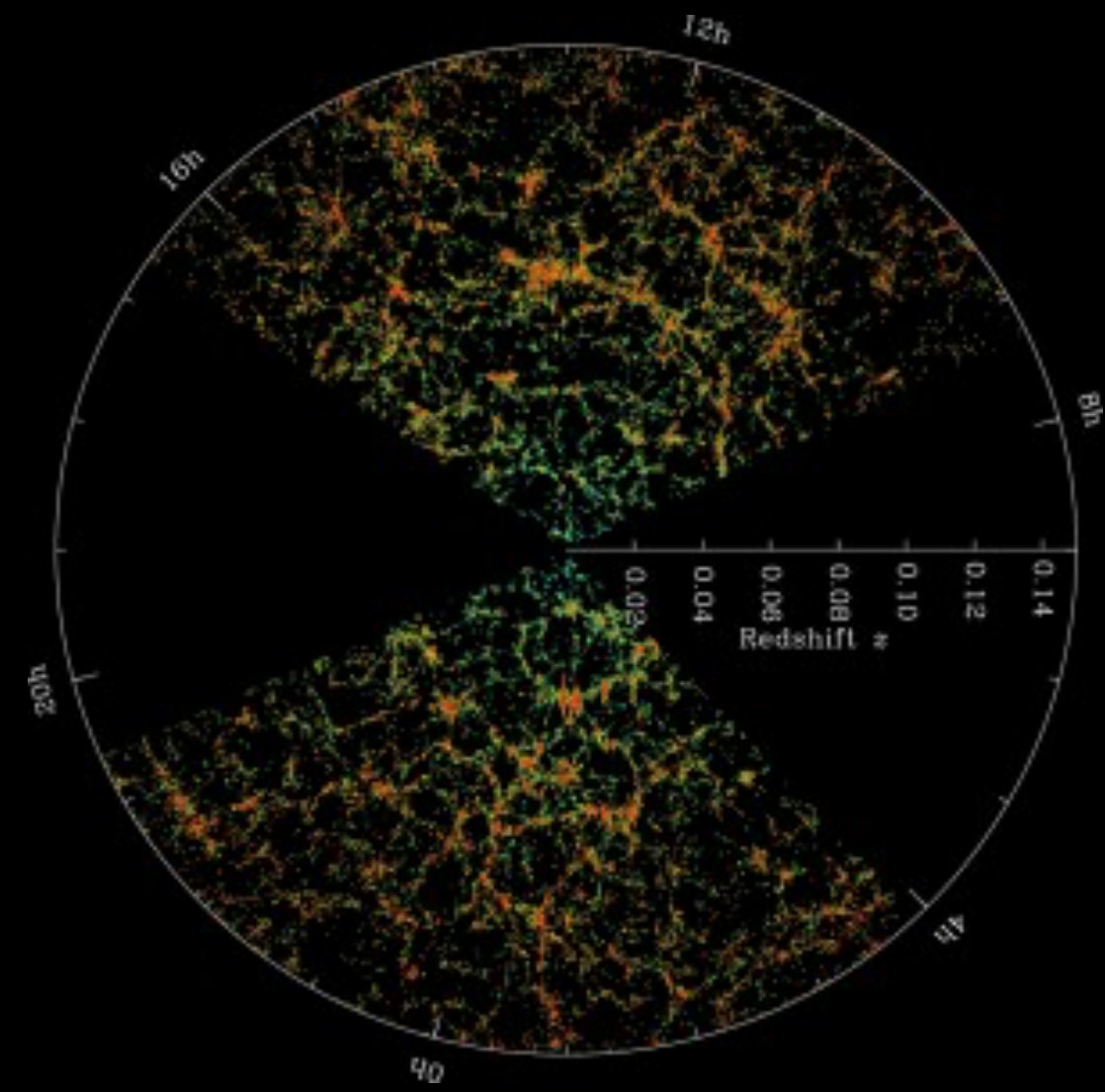
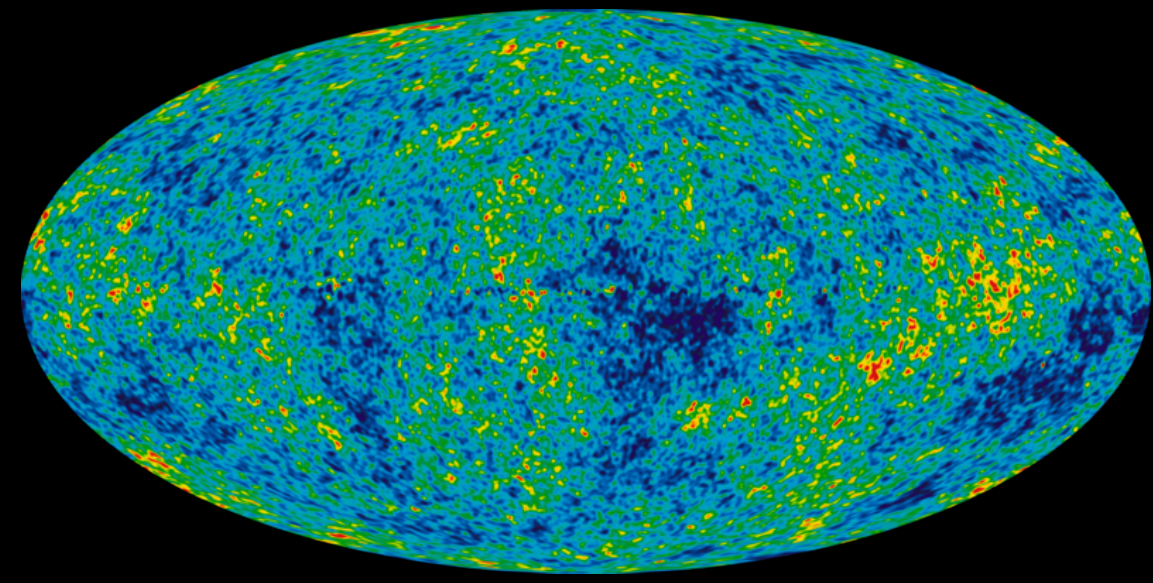
Arushi Bodas

Postdoc @ U.Chicago & Fermilab

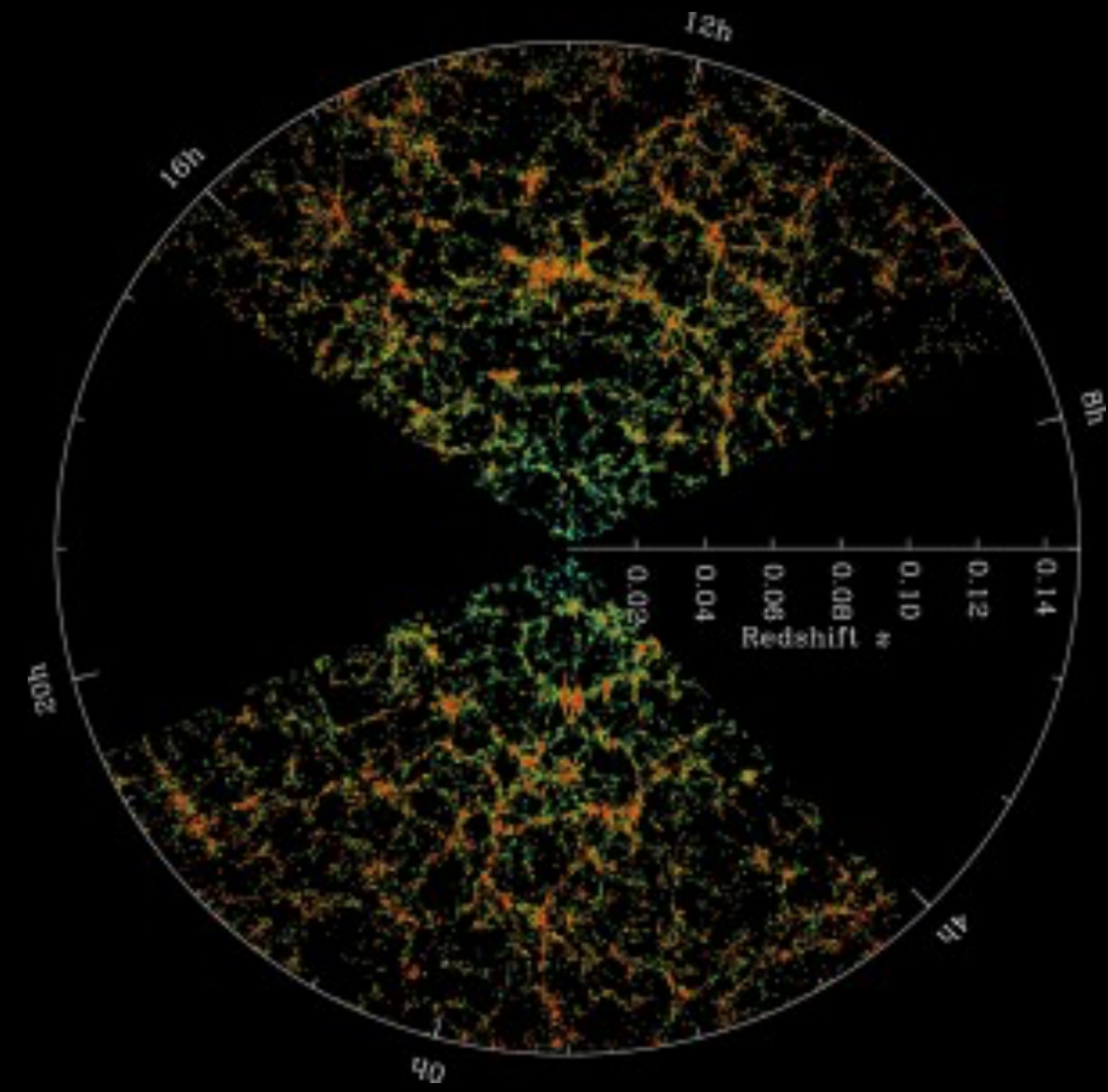
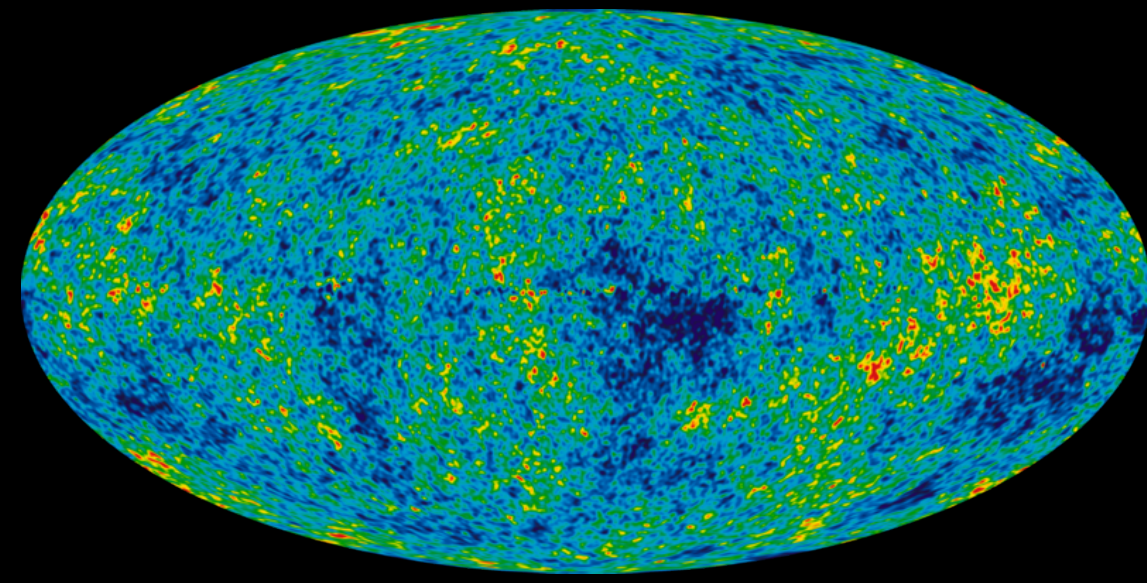
AB, R. Sundrum: *JHEP* 06 (2023) 029

AB, K. Harigaya, K. Inomata, T. Terada, L-T Wang: Ongoing work





Quantum fluctuations of a scalar field + inflation



Quantum fluctuations of a scalar field + inflation

Anisotropy maps are unique windows into inflationary physics

Common origin of known datasets

- Current observations tell us that density perturbations in all Standard Model (SM) species and Dark Matter (DM) originate from the same inflationary fluctuation (e.g. the inflaton).
[Planck, 1807.06211](#)
- Current observations (CMB) already constrain the prospect of seeing new inflationary physics in future datasets based on SM and DM species (line-intensity, large scale structure).
- Can we think of a fluctuation map that could be very different from the CMB?

What's the messenger?

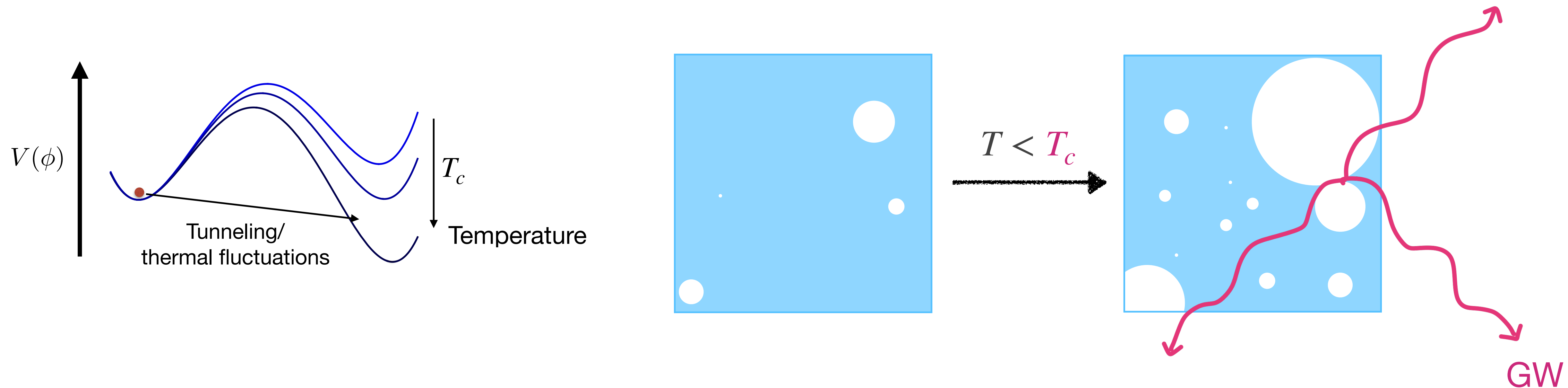
- Copiously produced in the early universe
- Free-streaming (does not thermalize with SM and DM)
- Could be detectable with the technology that we have today

What's the messenger?

- Copiously produced in the early universe
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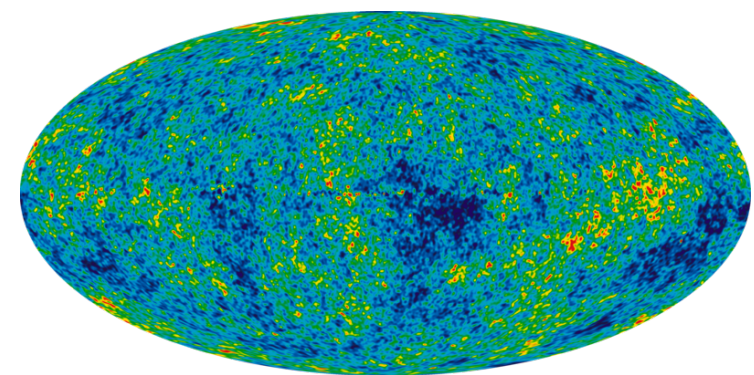
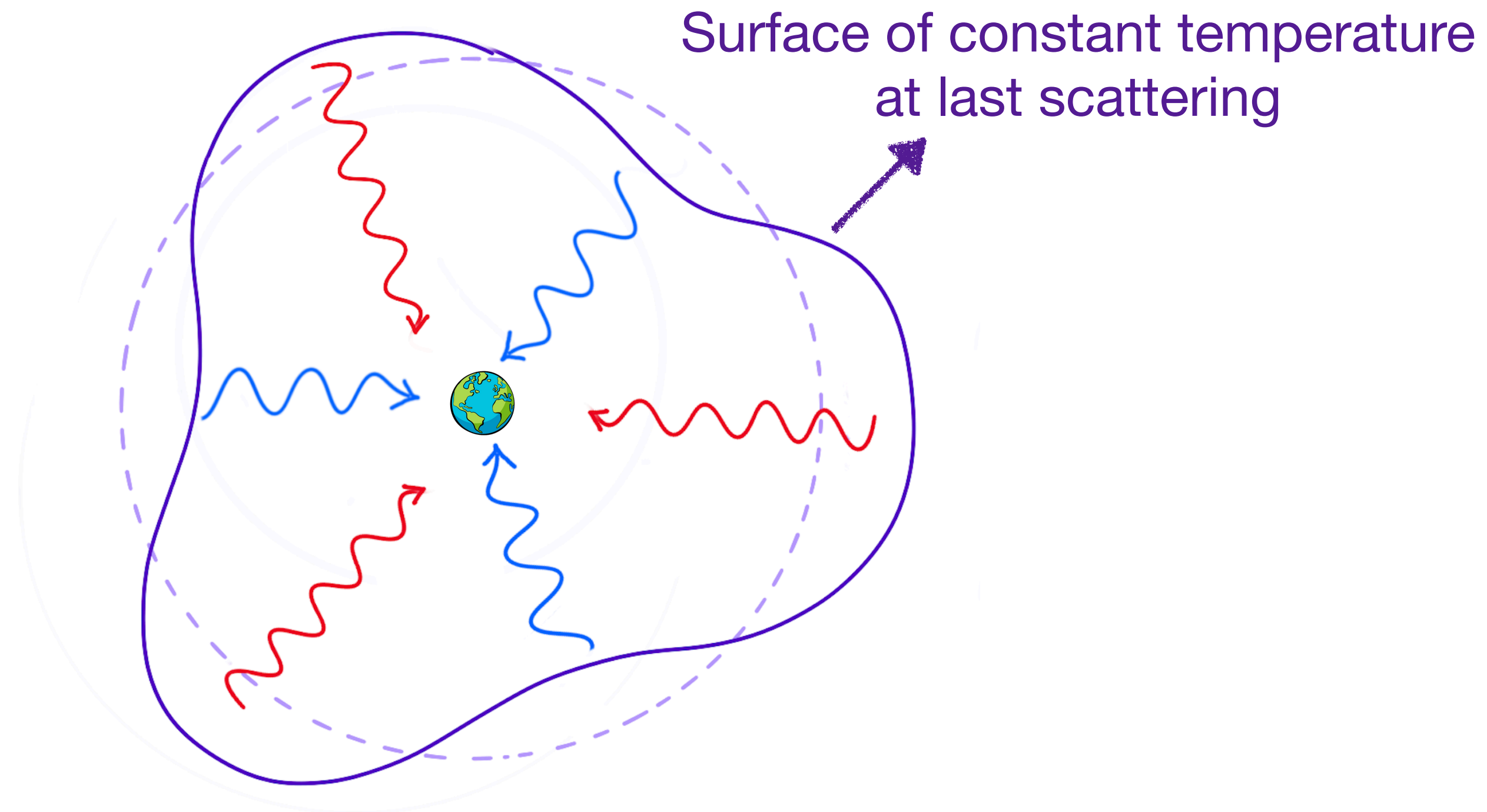
Gravitational waves!

Case 1: Gravitational waves from a phase transition



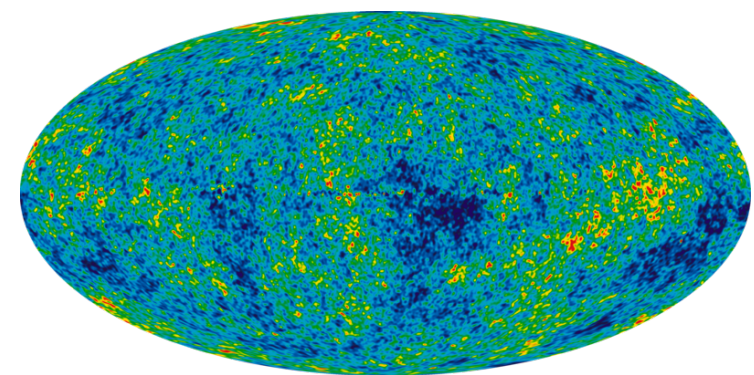
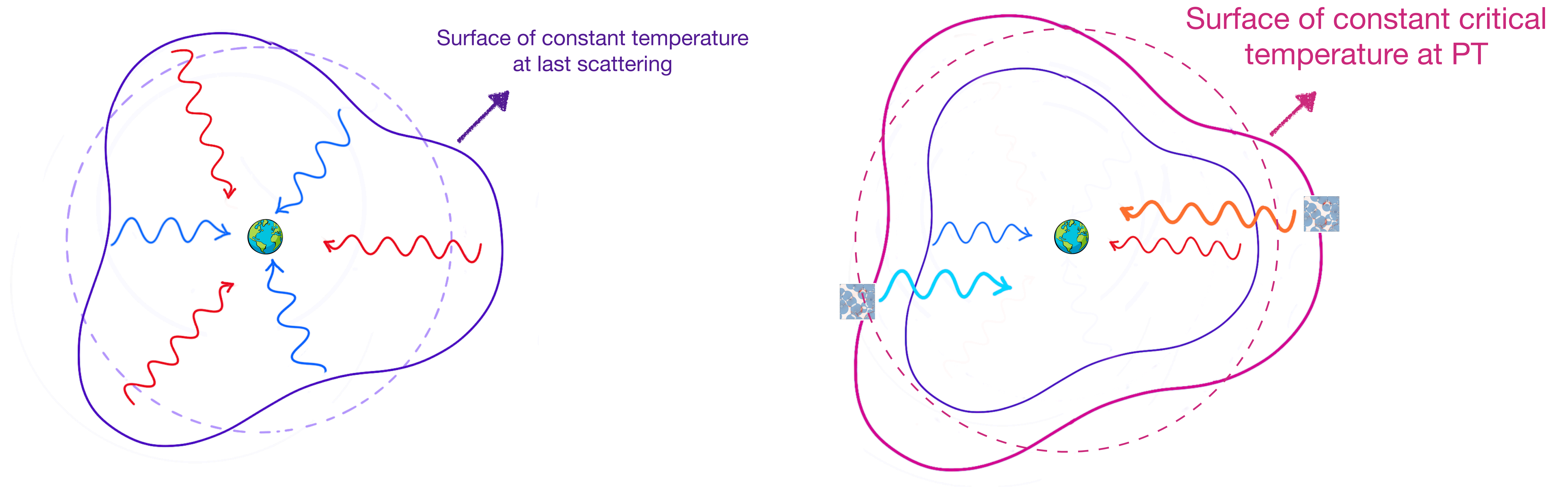
Extensions of SM have PTs at $T_c \sim 1 - 1000 \text{ TeV}$. Frequency of GW from such PTs would be redshifted to $10^{-4} - 10^{-1} \text{ Hz}$ today, which is the target frequency range of many proposed space-based experiments such as LISA, BBO, etc.

Recap: CMB anisotropies

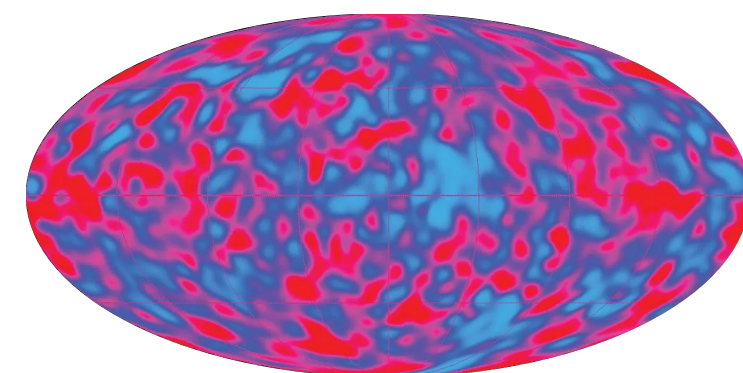


$$\delta_{\text{CMB}} \equiv \frac{\Delta T}{\bar{T}} \sim 10^{-5}$$

GWB anisotropies

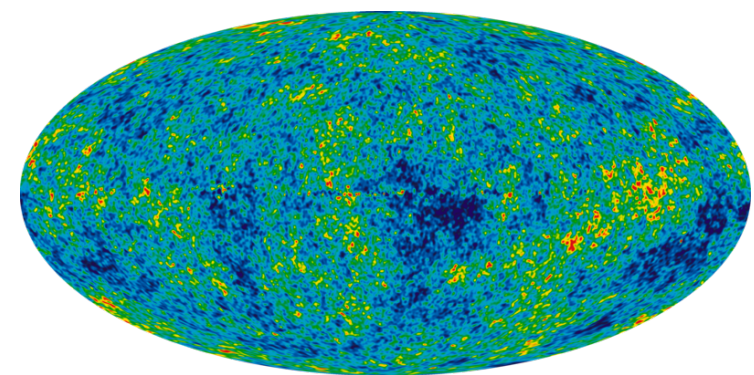
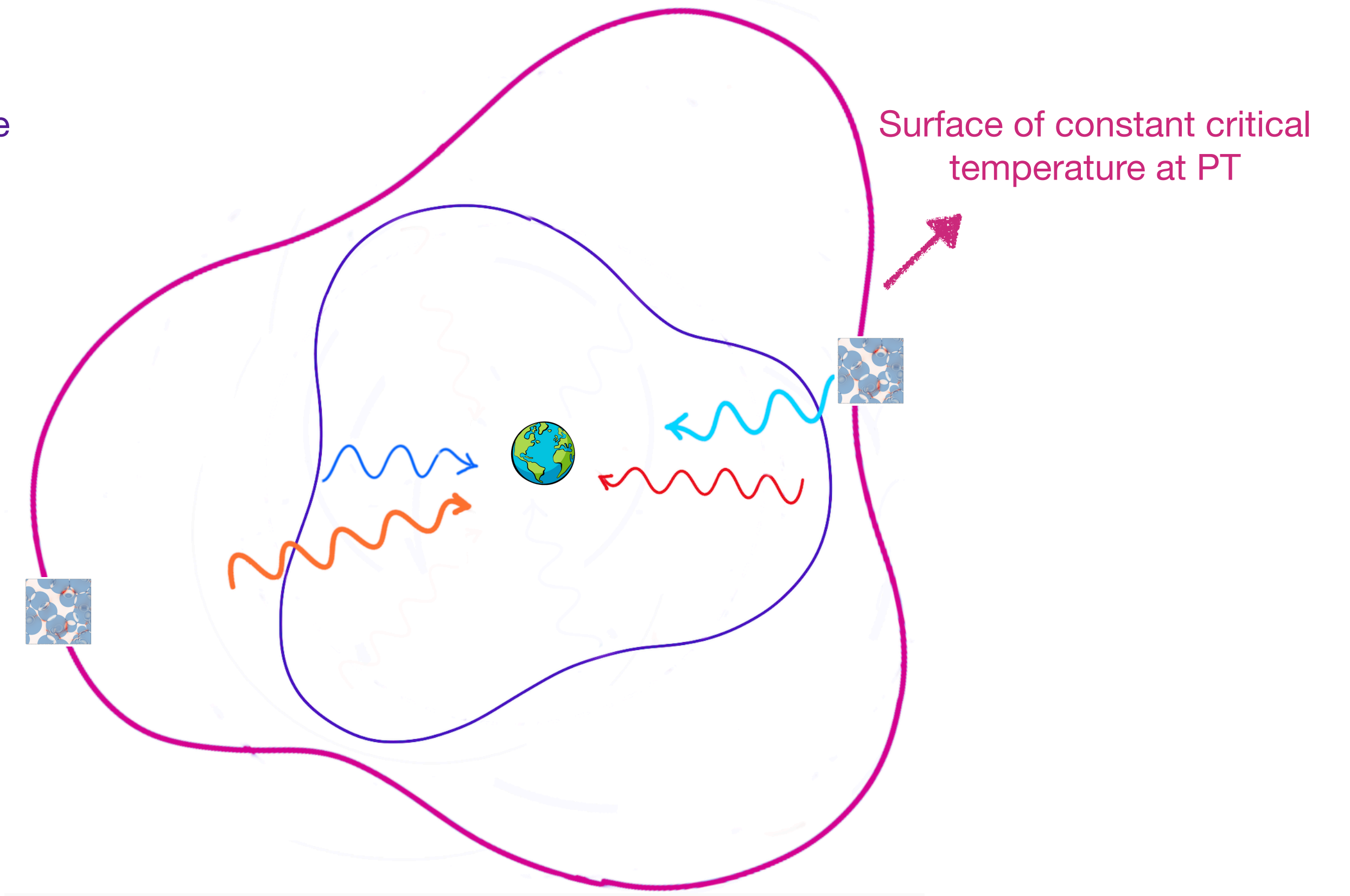
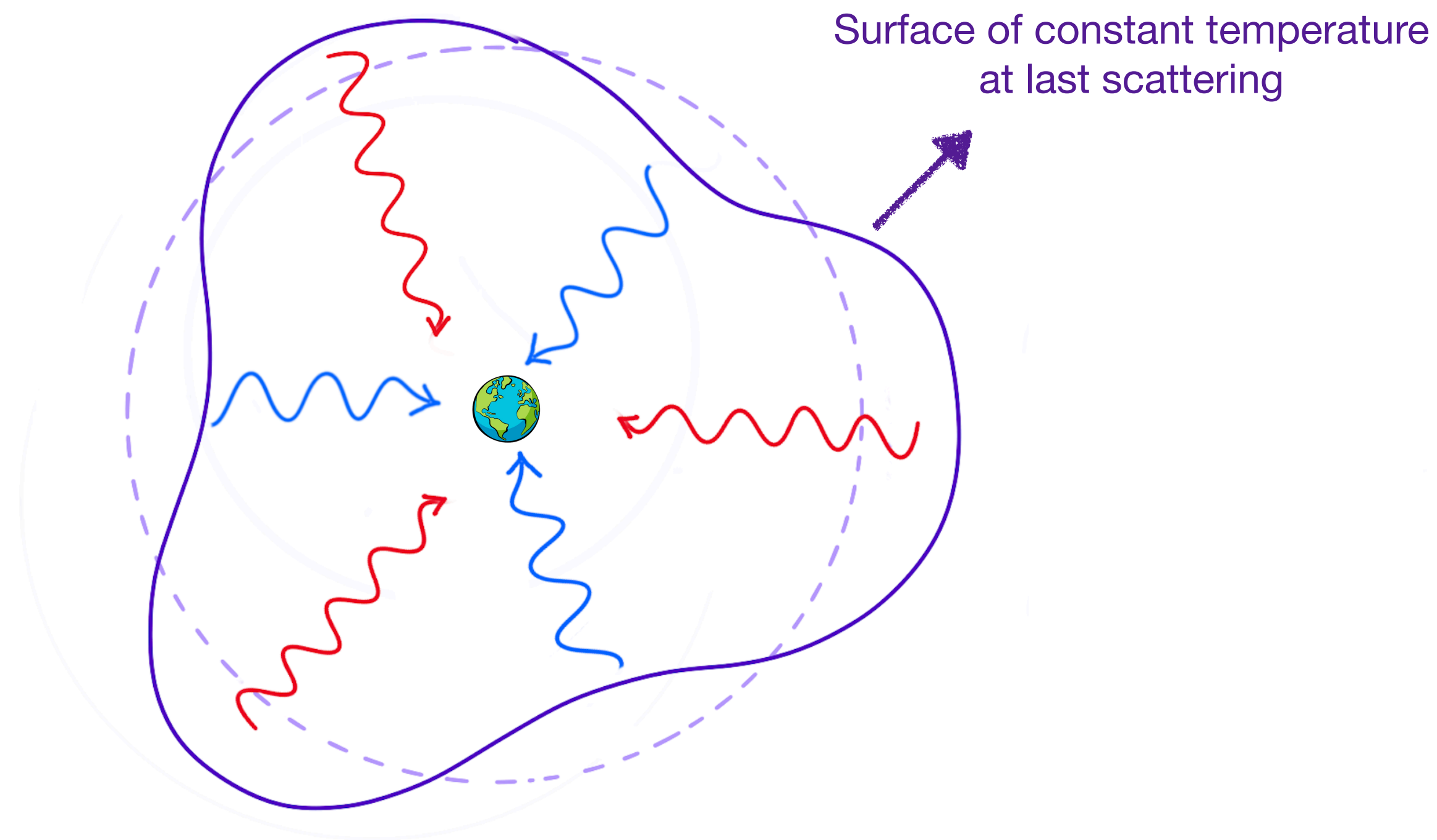


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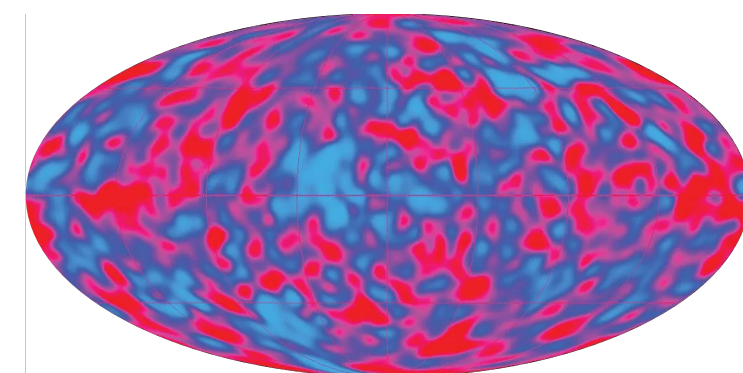


$$\delta_{\text{GWB}} \equiv \frac{\Delta \rho_{\text{GWB}}}{\bar{\rho}_{\text{GWB}}} \sim 10^{-5}$$

Isocurvature GWB anisotropy

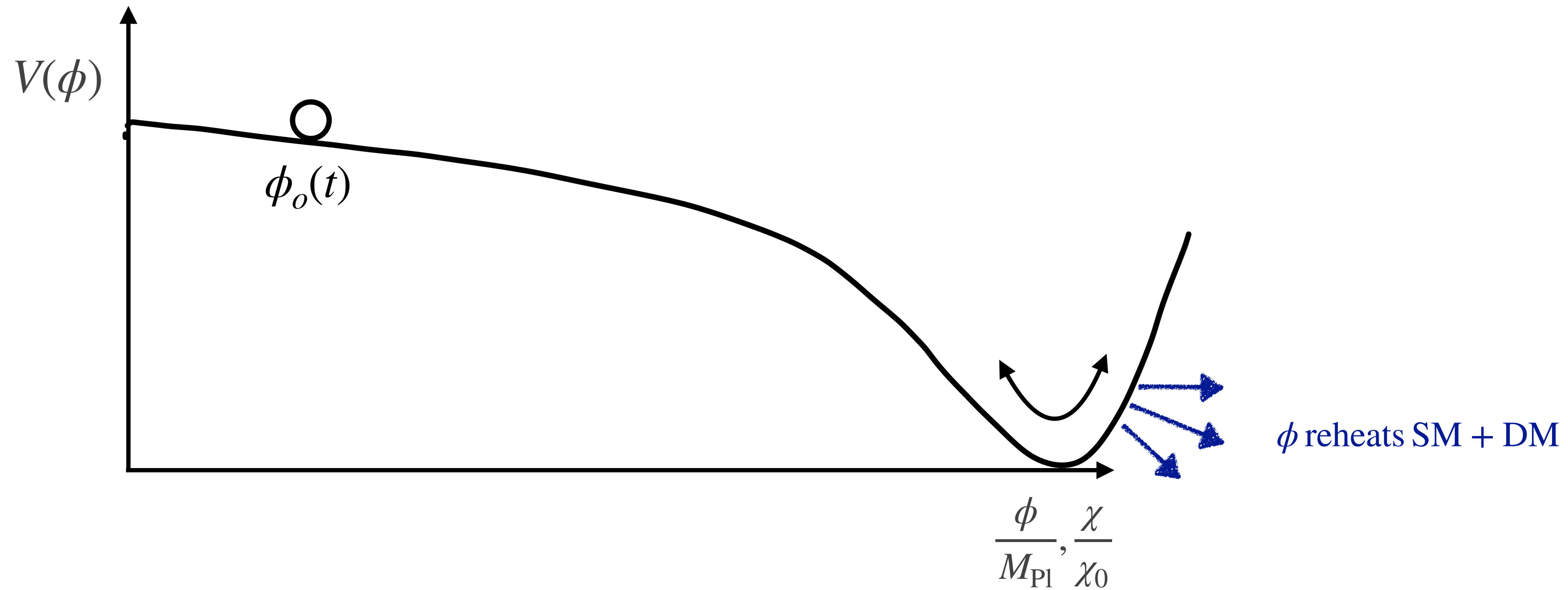


$$\delta_{\text{CMB}} \equiv \frac{\Delta T}{\bar{T}} \sim 10^{-5}$$

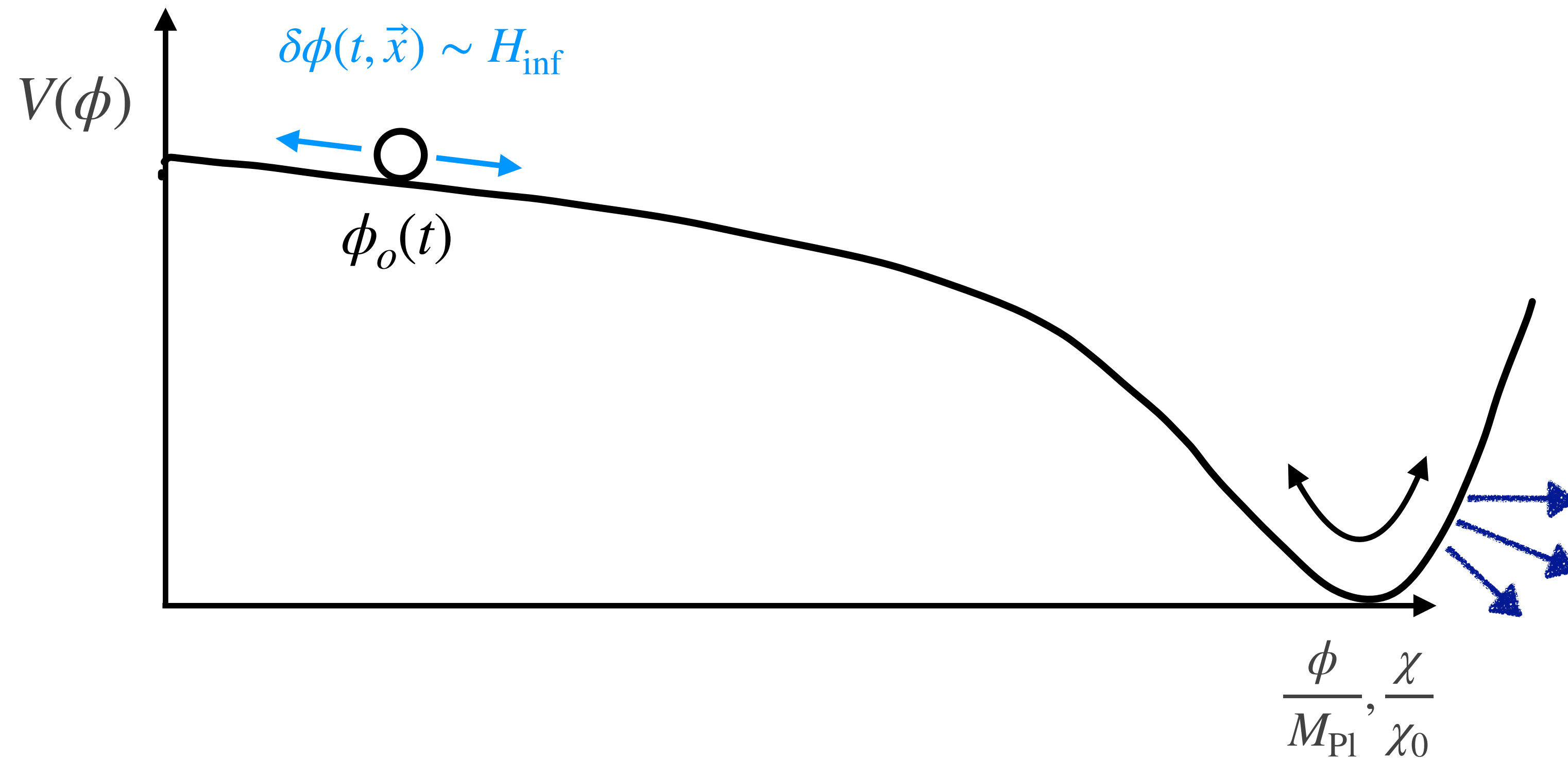


$$\delta_{\text{GW}} \equiv \frac{\Delta \rho_{\text{GW}}}{\bar{\rho}_{\text{GW}}} \neq 10^{-5}$$

Multi-field inflation: Inflaton + ALP (χ)



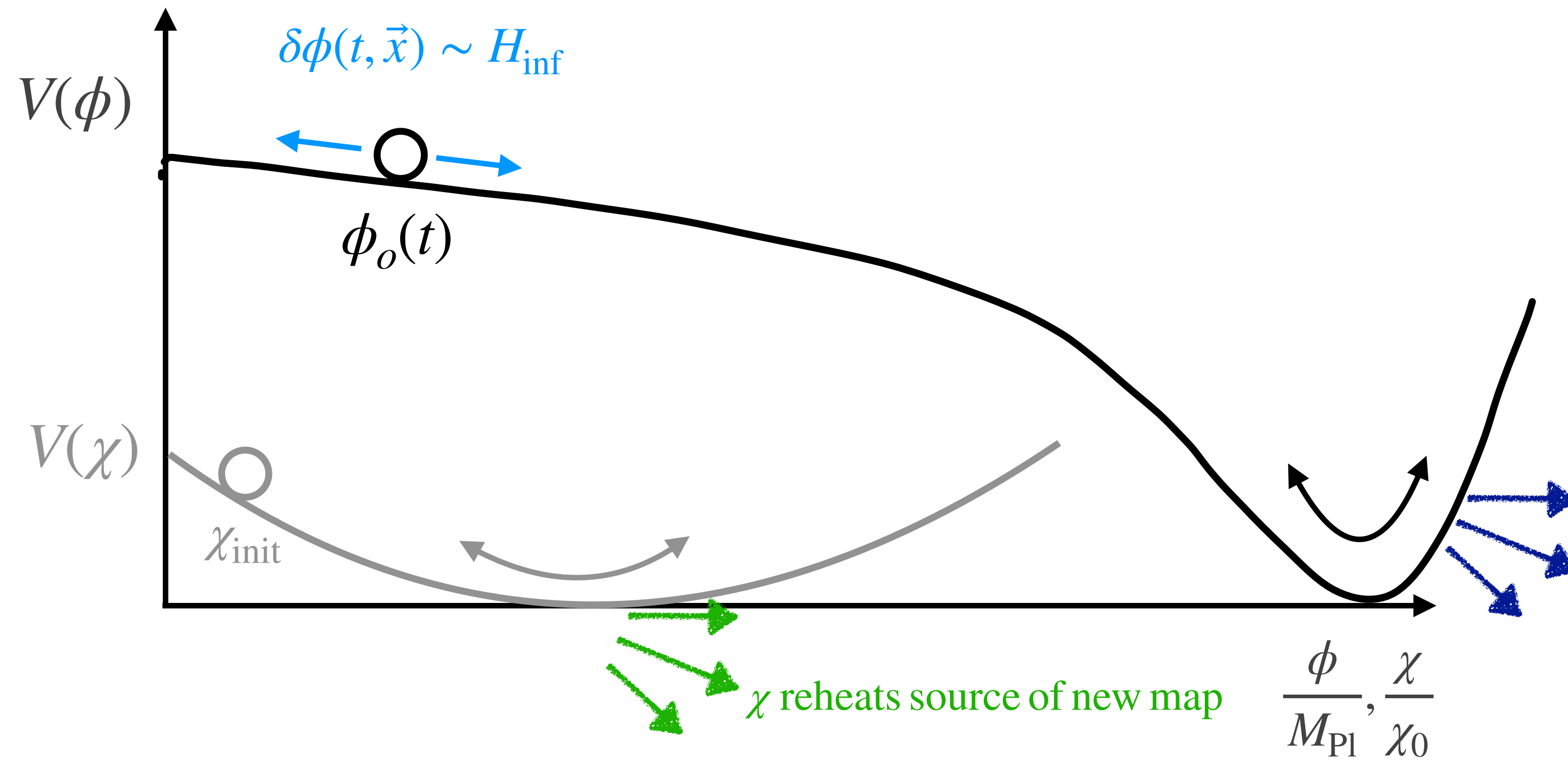
Multi-field inflation: Inflaton + ALP (χ)



ϕ reheats SM + DM

$$\delta_{\text{SM}} \equiv \frac{\Delta V}{V} \Big|_{\phi} \sim \frac{H_{\text{inf}} \delta\phi}{\dot{\phi}_0}$$

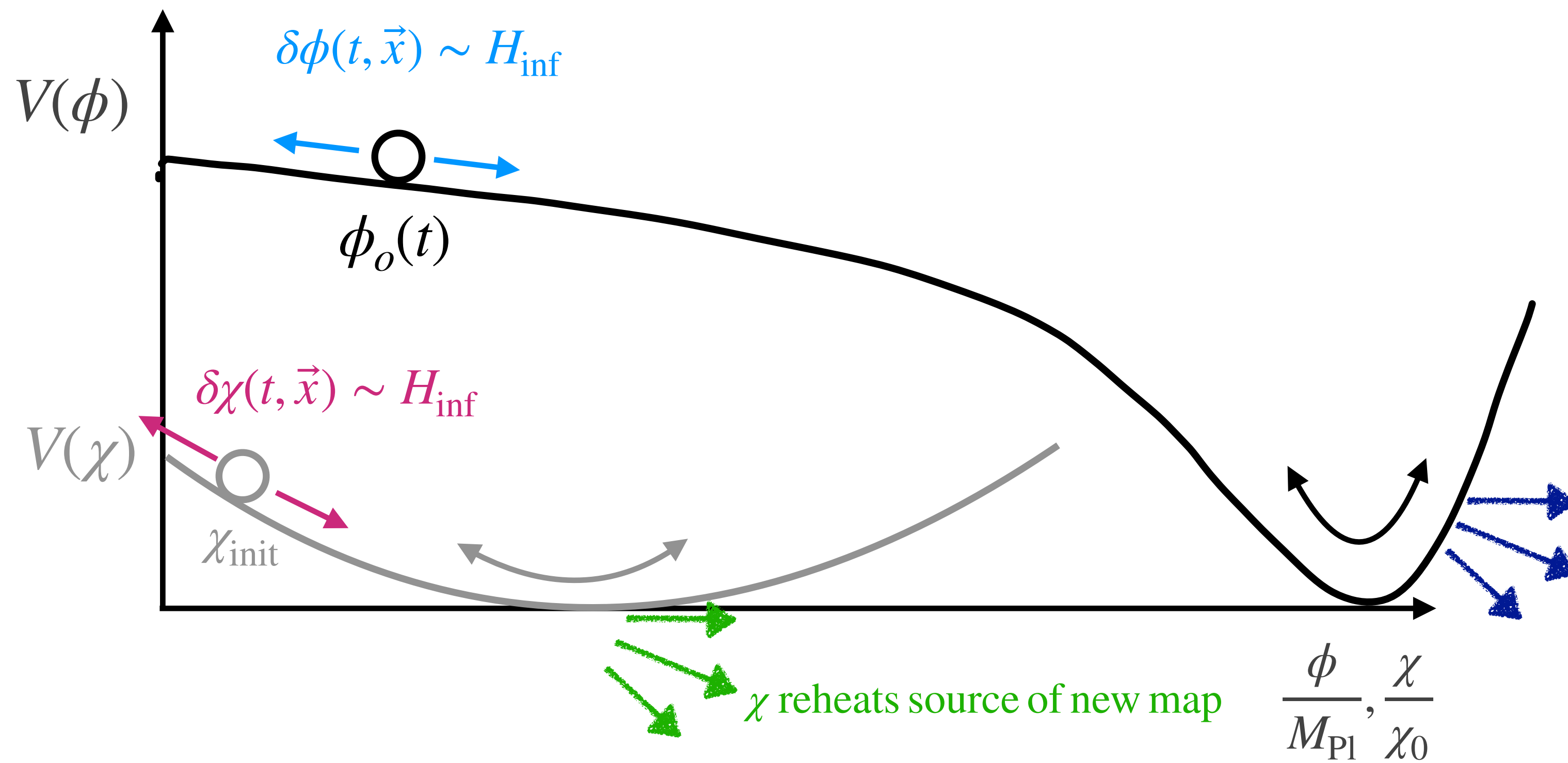
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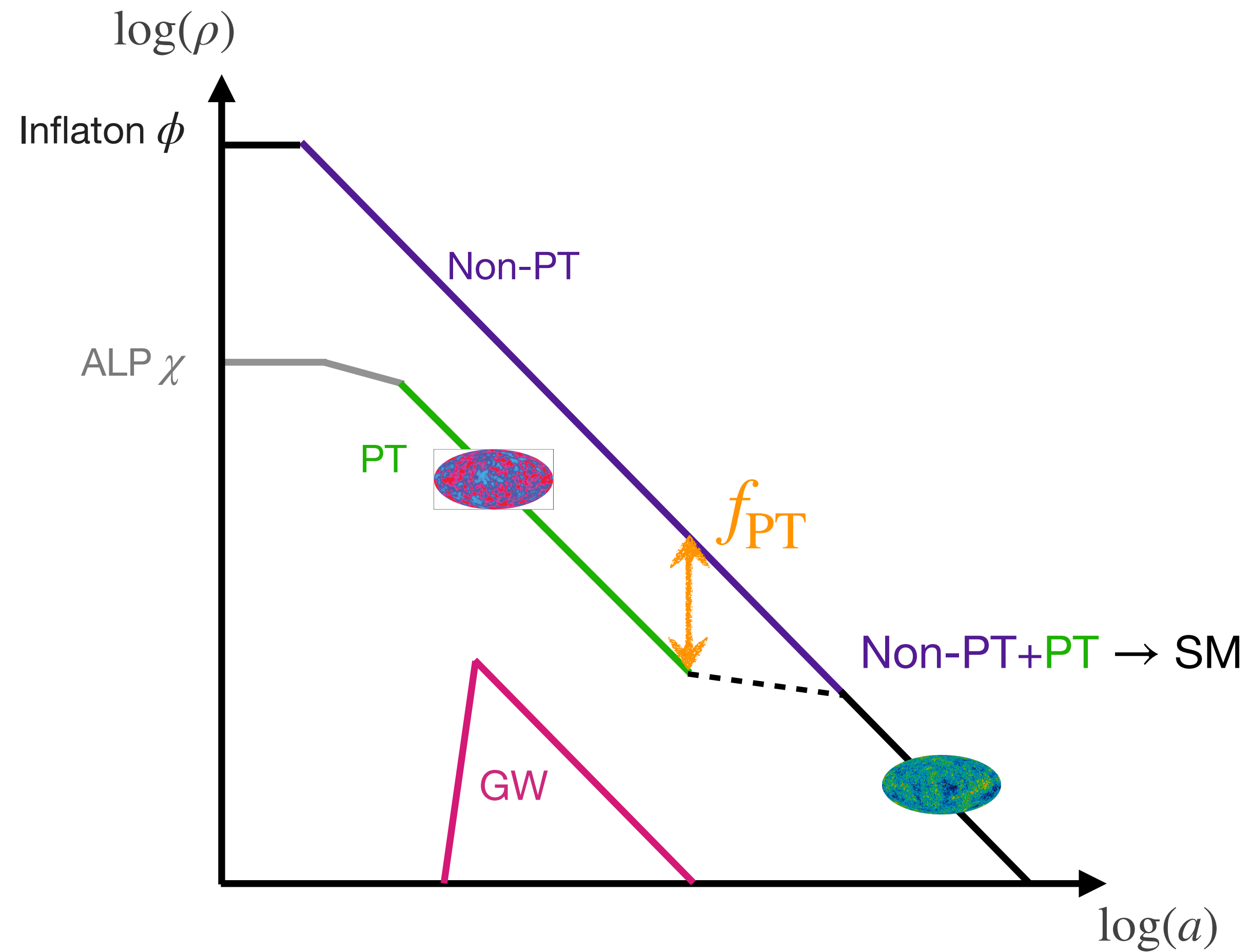
ϕ reheats SM + DM

$$\delta_{\text{SM}} \equiv \left. \frac{\Delta V}{V} \right|_{\phi} \sim \frac{H_{\text{inf}} \delta\phi}{\dot{\phi}_0}$$

$$\delta_{\text{new}} \equiv \left. \frac{\Delta V}{V} \right|_{\chi} \sim \frac{\delta\chi}{\chi_{\text{init}}}$$

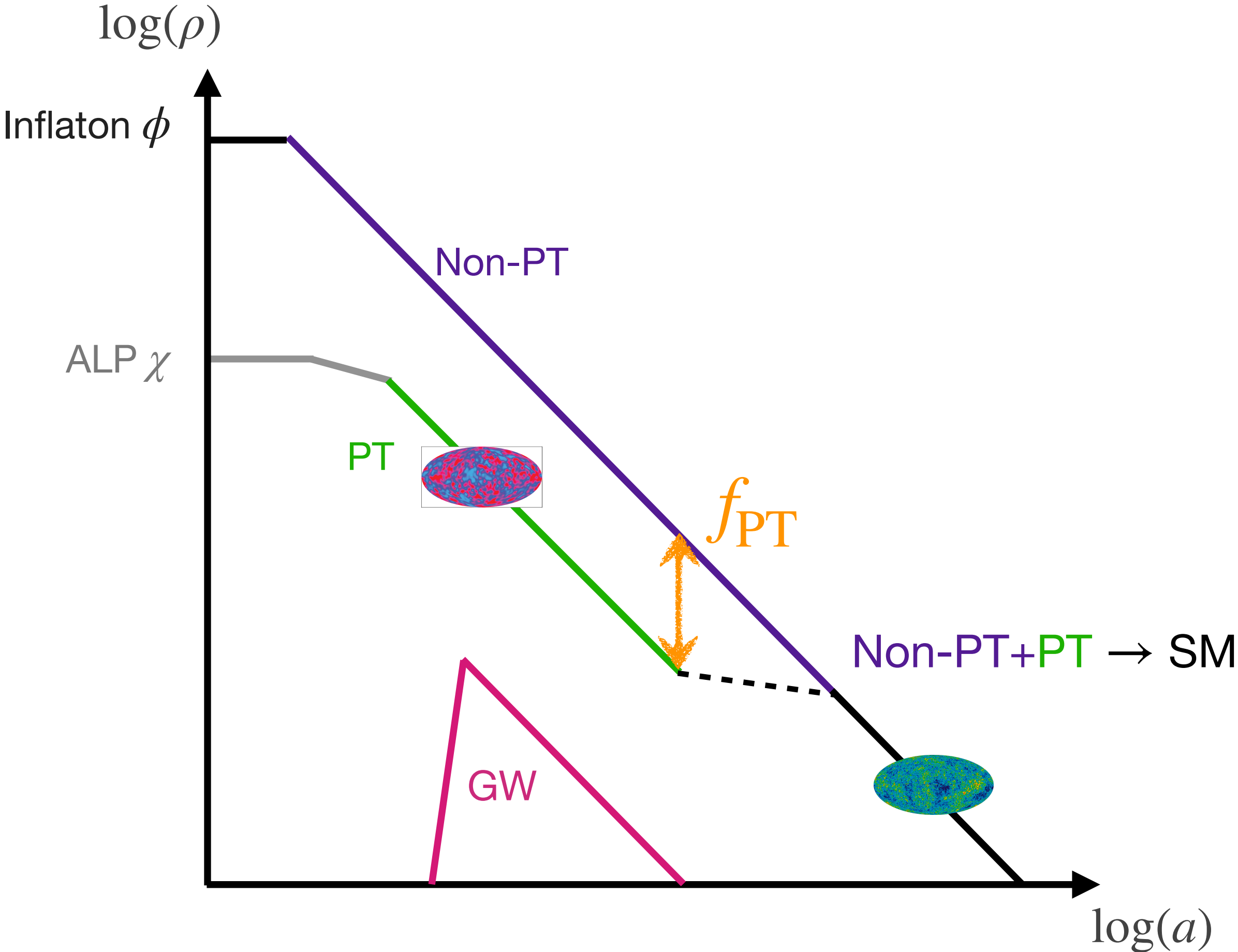
A model of isocurvature GWB

Geller, Hook, Sundrum, Tsai 1803.10780



A model of isocurvature GWB

Geller, Hook, Sundrum, Tsai 1803.10780



$$\delta_{\text{GW}} \sim \delta_{\chi} + \delta_{\phi}$$

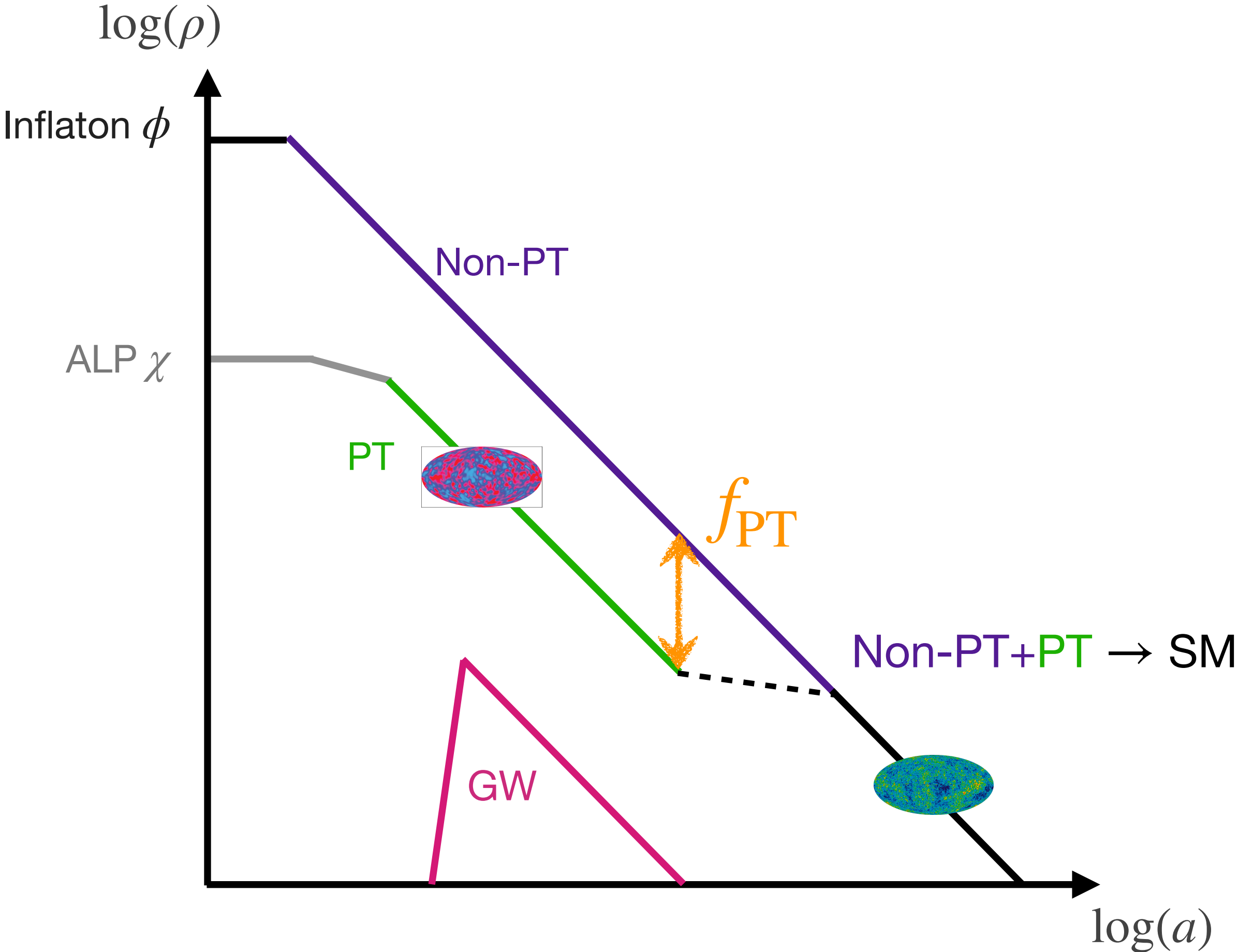
Sachs-Wolfe contribution $\sim 10^{-5}$

$$\delta_{\text{CMB}} \sim \delta_{\phi} + f_{\text{PT}} \delta_{\chi} \sim 10^{-5}$$

$$f_{\text{PT}} = \frac{\rho_{\text{PT}}}{\rho_{\text{total}}} \ll 1$$

A model of isocurvature GWB

Geller, Hook, Sundrum, Tsai 1803.10780



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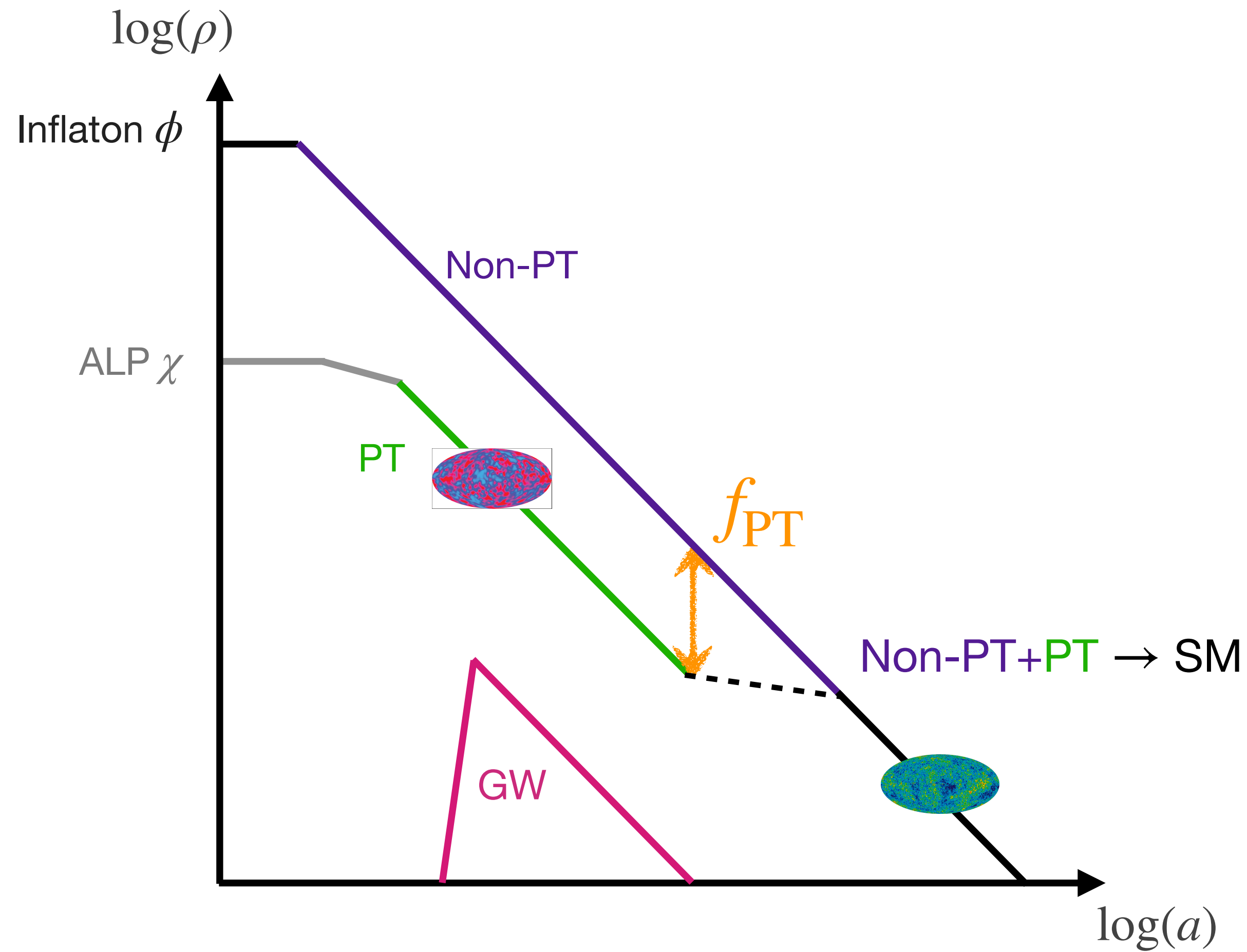
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$$f_{\text{PT}} = \frac{\rho_{\text{PT}}}{\rho_{\text{total}}} \ll 1$$

$\delta_{\chi} \gg \delta_{\phi}$

The tradeoff



$$\delta_{\text{GW}} \sim \delta_{\chi} + \delta_{\phi}$$

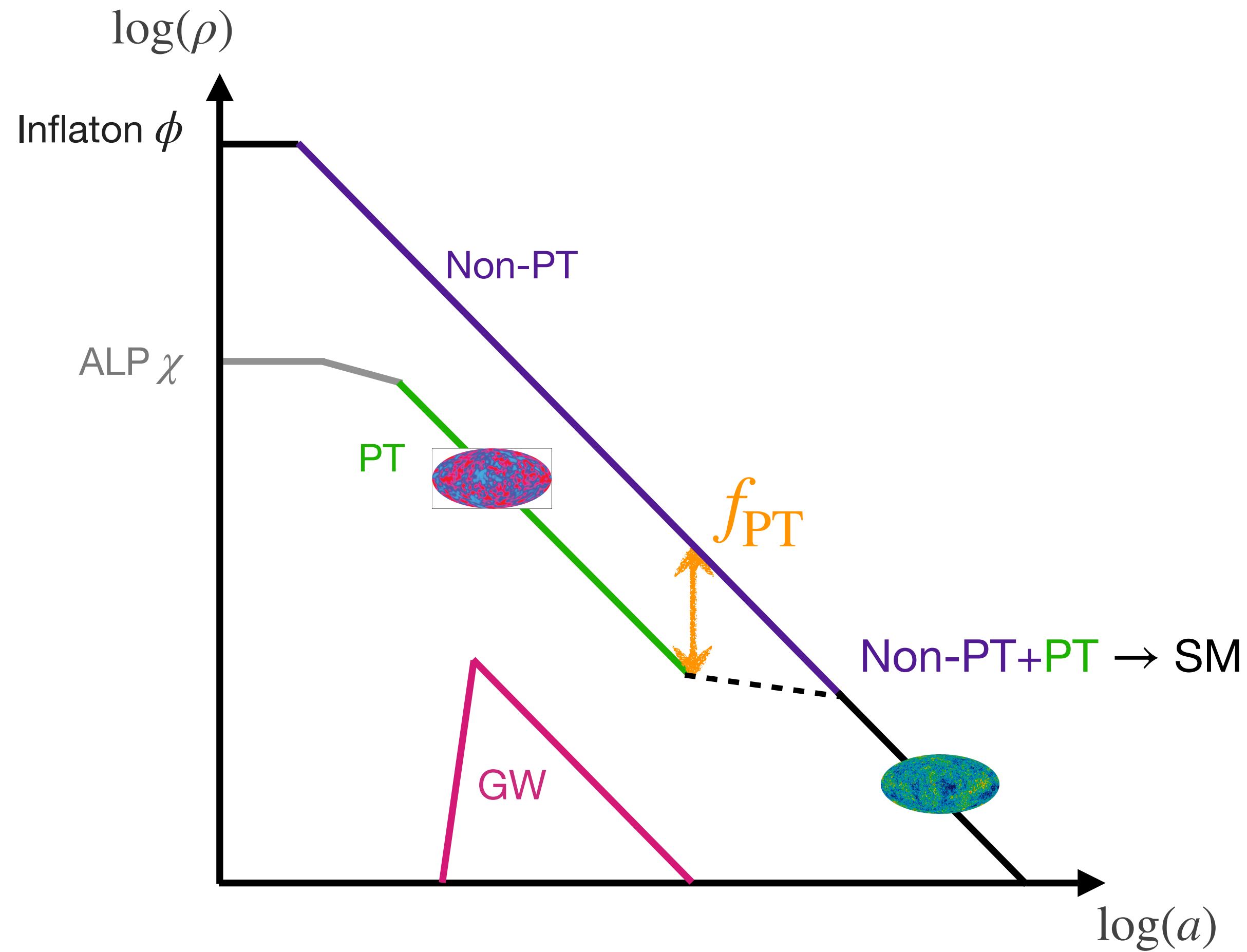
$$\delta_{\text{CMB}} \sim \delta_{\phi} + f_{\text{PT}} \delta_{\chi} \sim 10^{-5}$$

$$\Omega_{\text{GW}} := \frac{\rho_{\text{GW}}}{\rho_{\text{total}}} \propto f_{\text{PT}}^2$$

$$h^{\text{TT}} \propto \rho_{\text{PT}}$$

$$\rho_{\text{GW}} \propto (h^{\text{TT}})^2 \propto \rho_{\text{PT}}^2$$

The tradeoff



$$\delta_{GW} \sim \delta_\chi + \delta_\phi$$

$$\delta_{CMB} \sim \delta_\phi + f_{PT} \delta_\chi \sim 10^{-5}$$

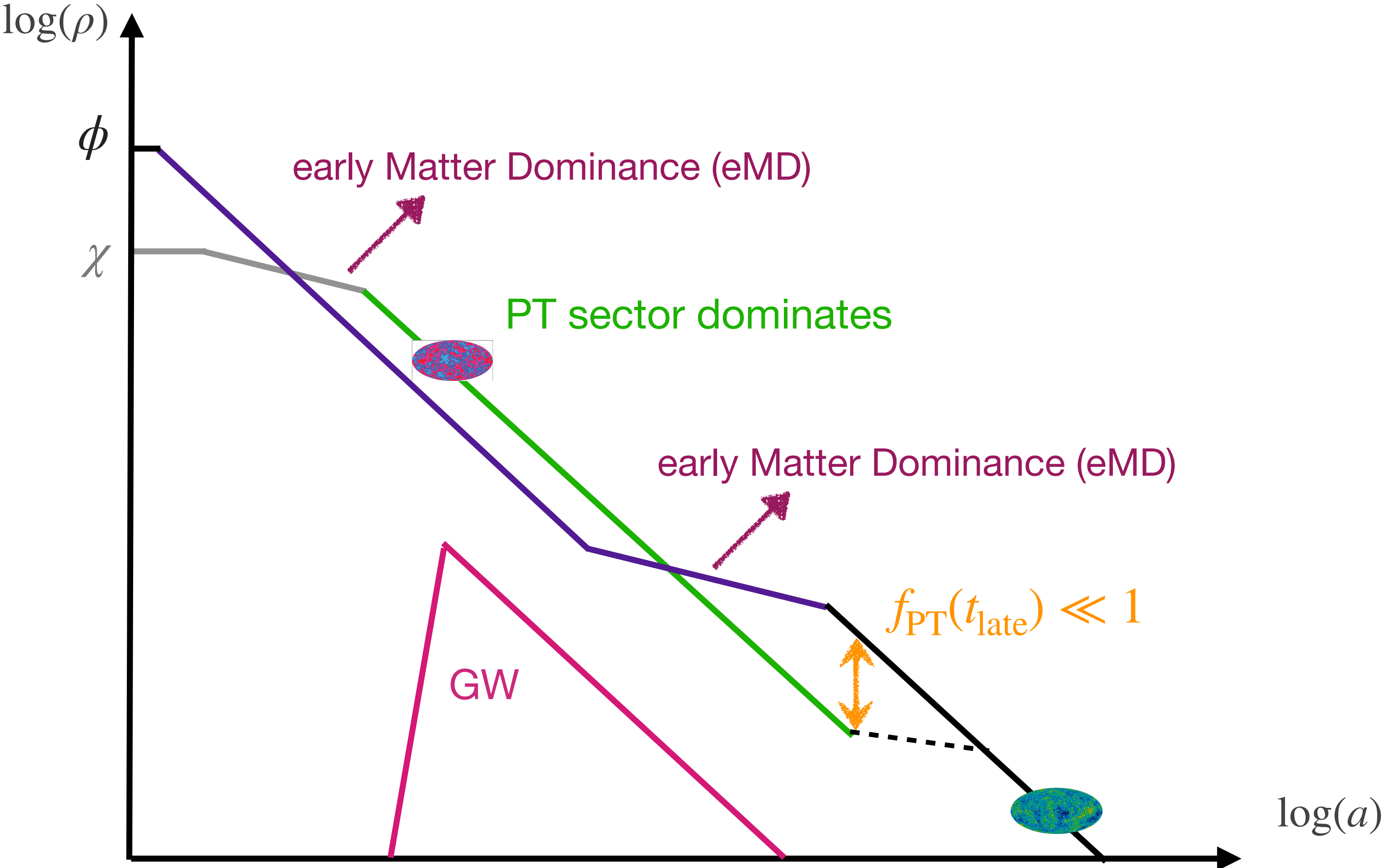
$$\Omega_{GW} := \frac{\rho_{GW}}{\rho_{total}} \propto f_{PT}^2$$

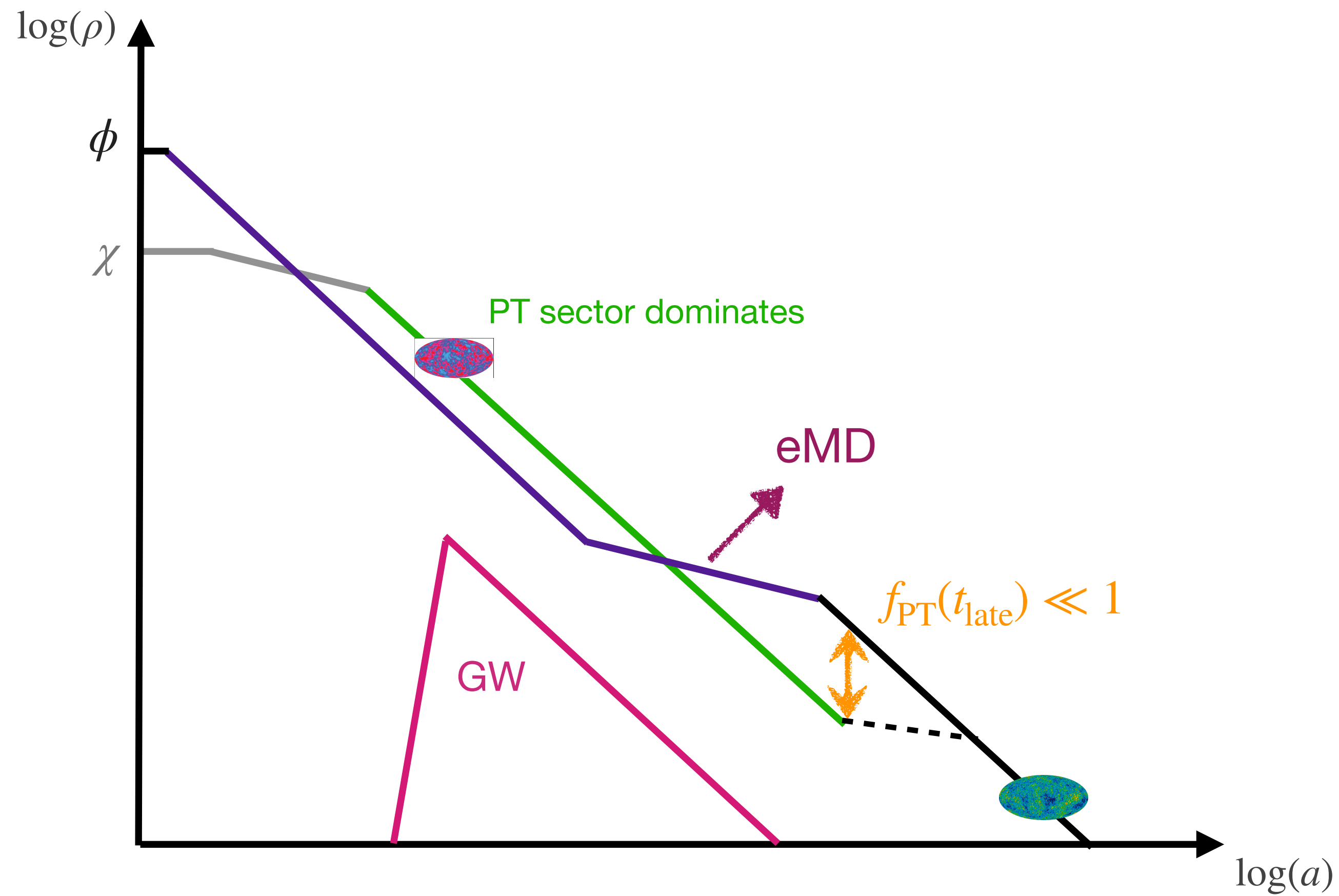
$$h^{TT} \propto \rho_{PT}$$

$$\rho_{GW} \propto (h^{TT})^2 \propto \rho_{PT}^2$$

Can the PT sector be dominant during phase transition?

AB, R. Sundrum: JHEP 06 (2023) 029



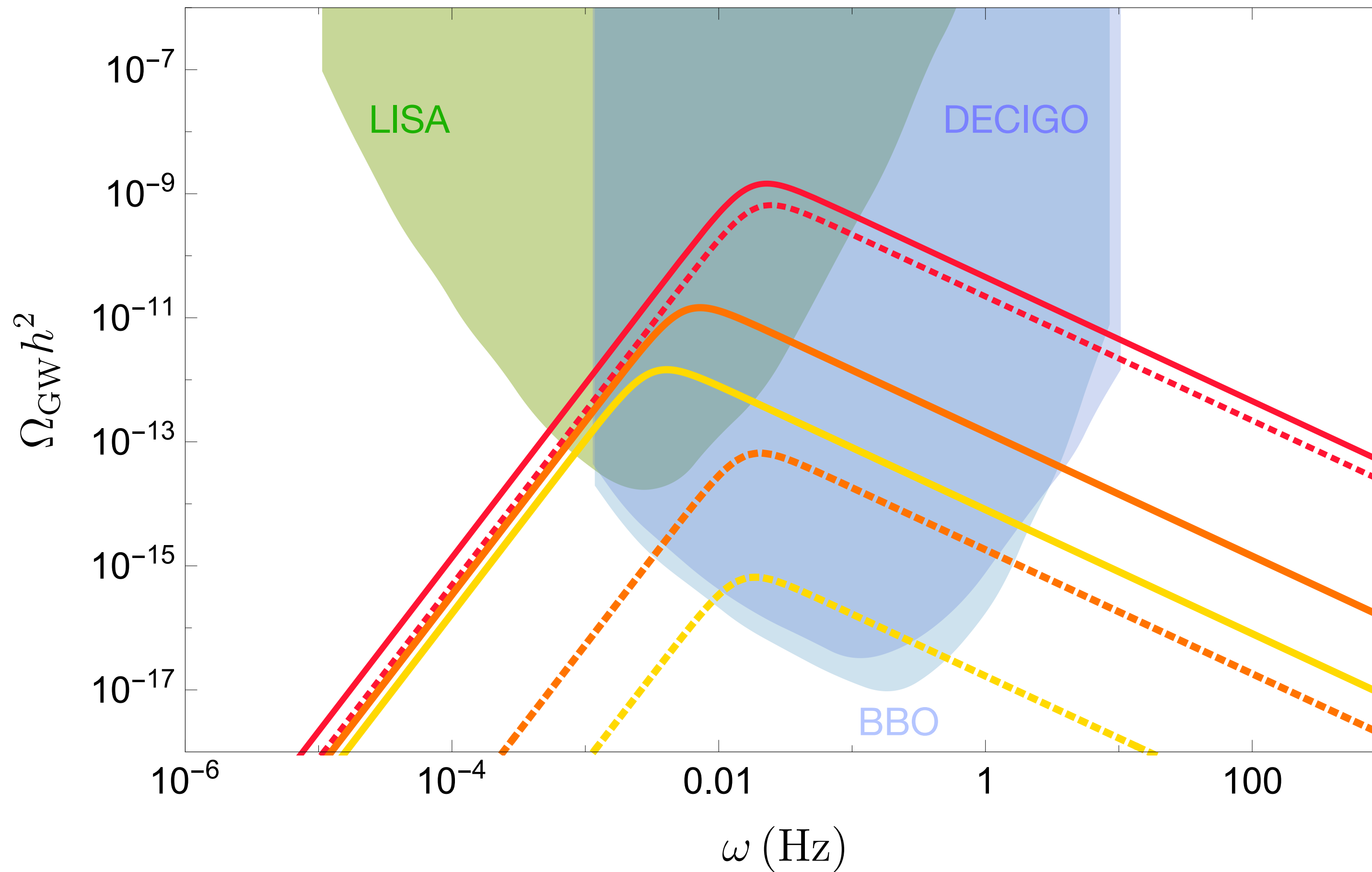


No suppression at production

Relative dilution from eMD

$$\Omega_{GW}^{\text{today}} \propto f_{PT} \text{ instead of } f_{PT}^2$$

Improvement in the GWB signal



Dashed lines: Simple model

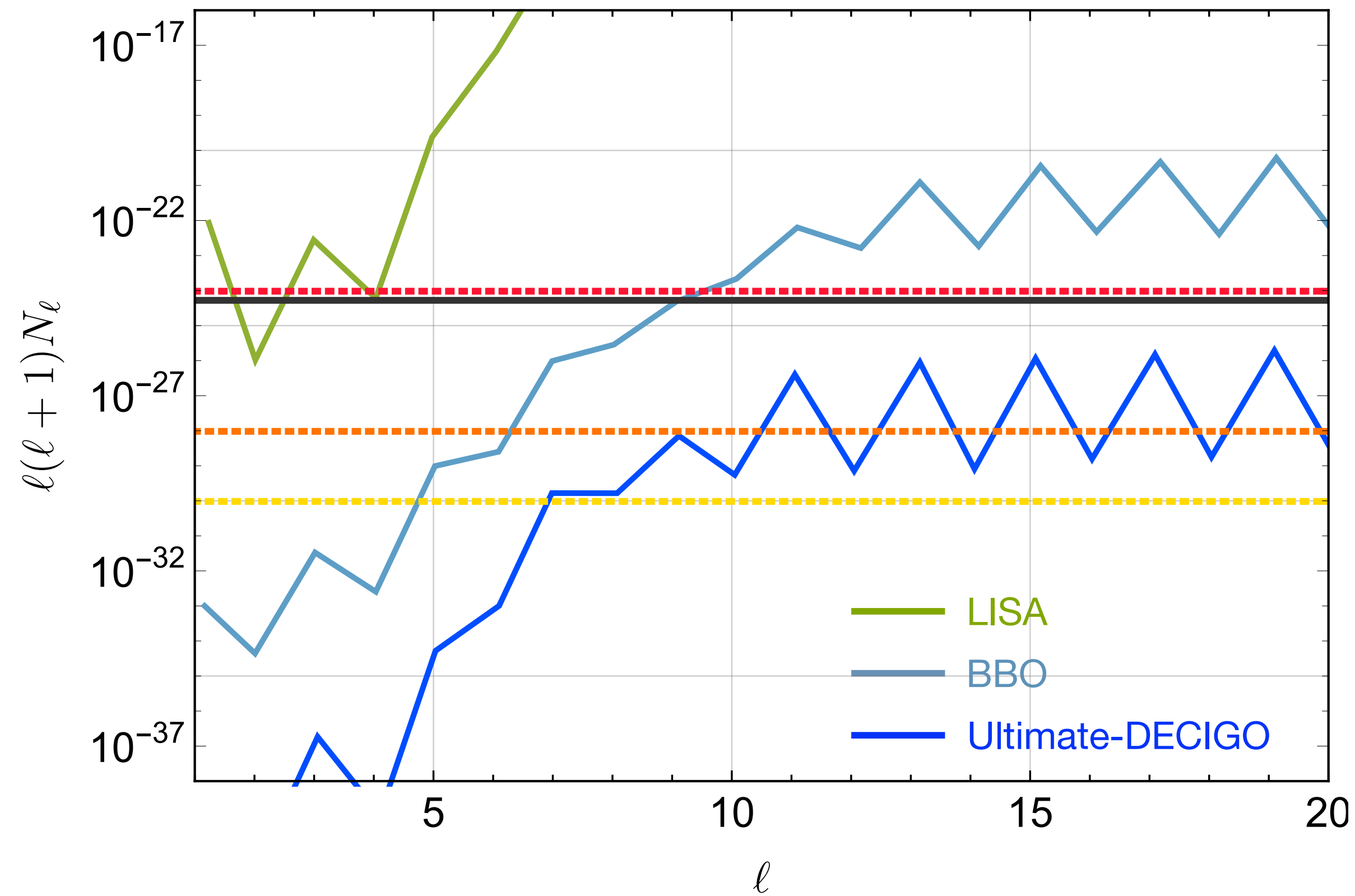
Solid lines: eMD model

— $\delta_{\text{GW}} \sim 10^{-4}, f_{\text{PT}} \sim 10^{-1}$

— $\delta_{\text{GW}} \sim 10^{-2}, f_{\text{PT}} \sim 10^{-3}$

— $\delta_{\text{GW}} \sim 10^{-1}, f_{\text{PT}} \sim 10^{-4}$

Detectability of large anisotropy



Dashed lines: Simple model

Solid lines: eMD model

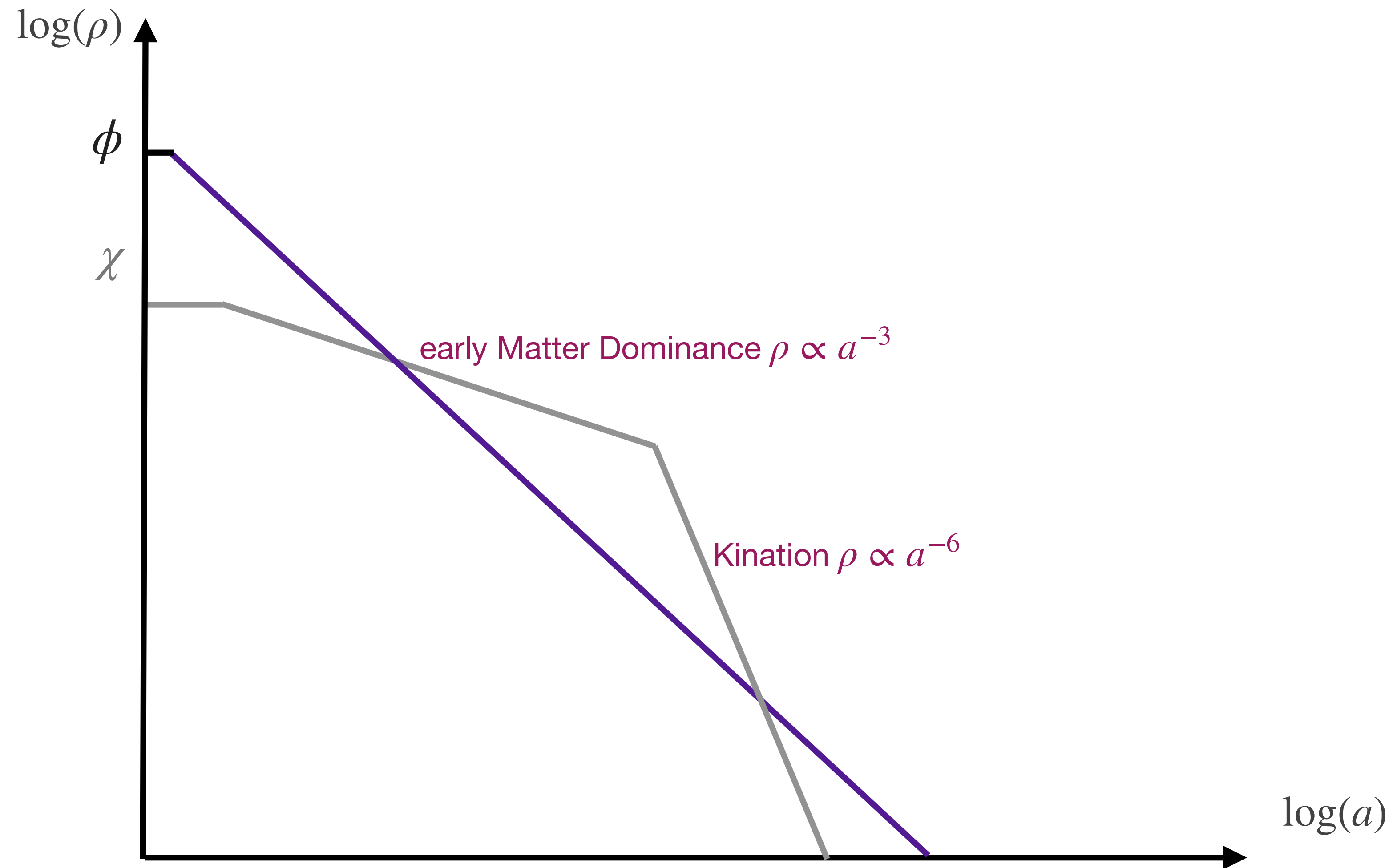
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— $\delta_{\text{GW}} \sim 10^{-1}, f_{\text{PT}} \sim 10^{-4}$

Another possibility

Matter domination followed by a period of kination: rotating ALP field
Induced gravitational waves from large scalar perturbations at small scales



Rotating ALP field

K. Harigaya, R. Co 1910.02080

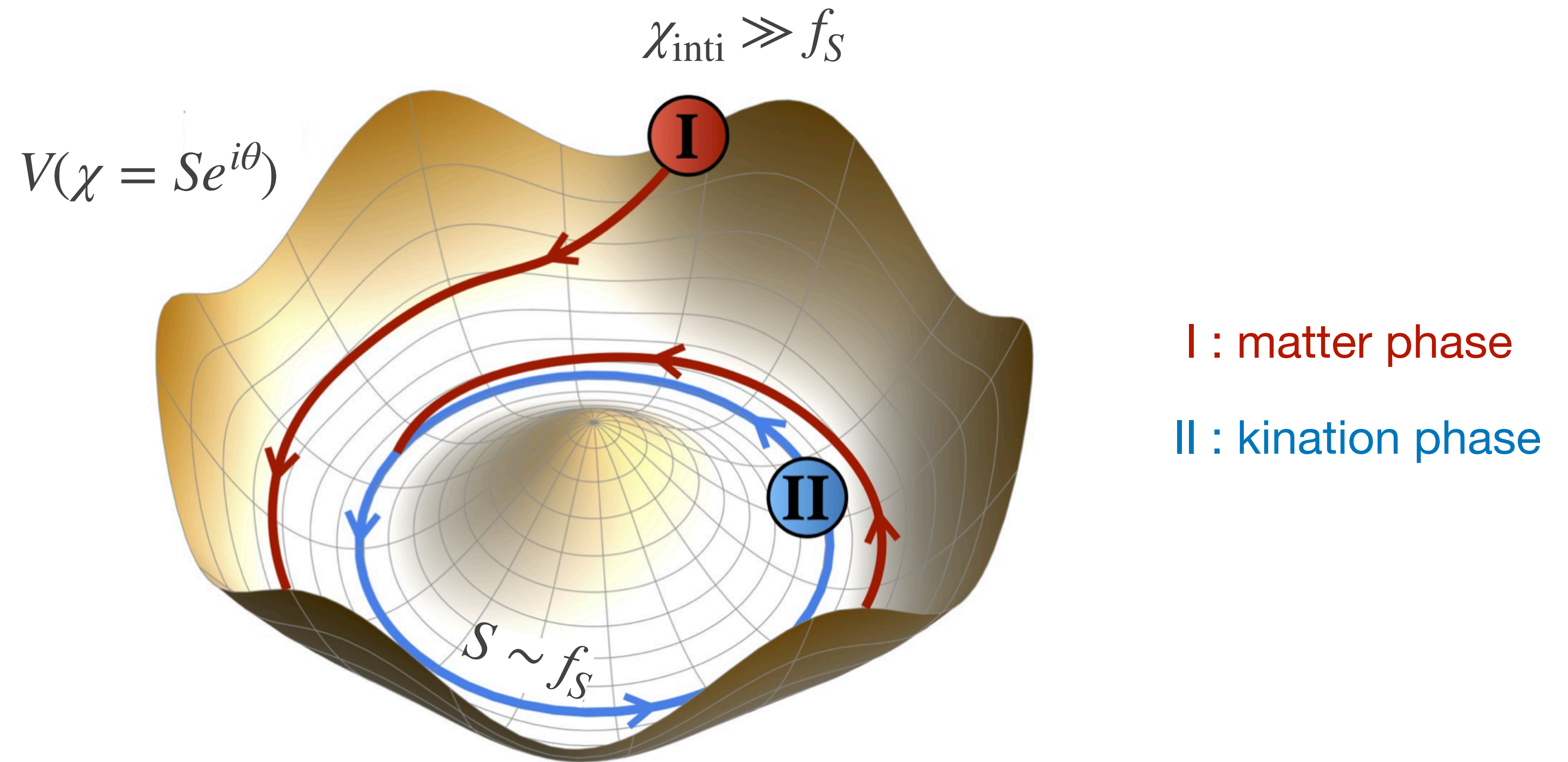
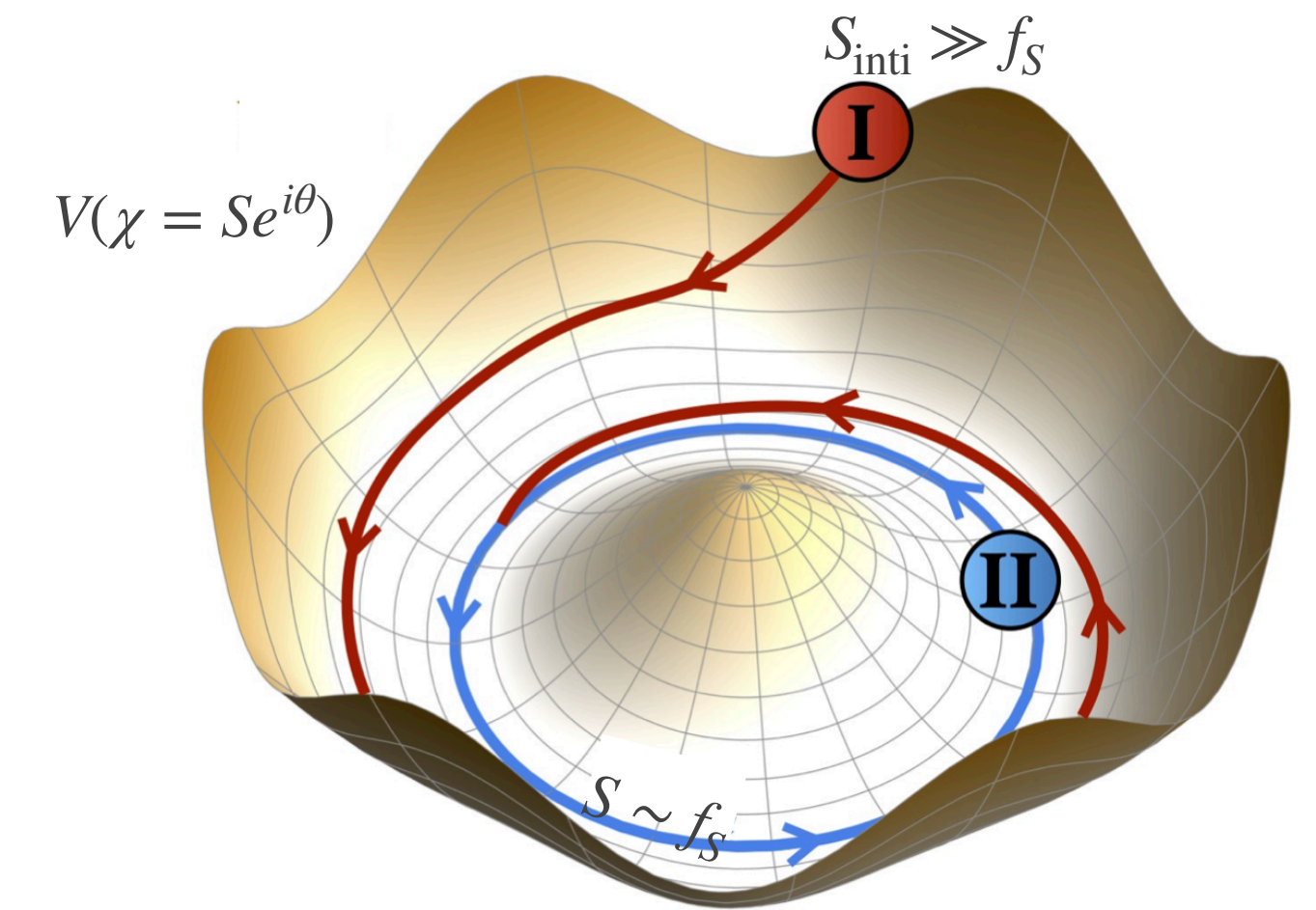
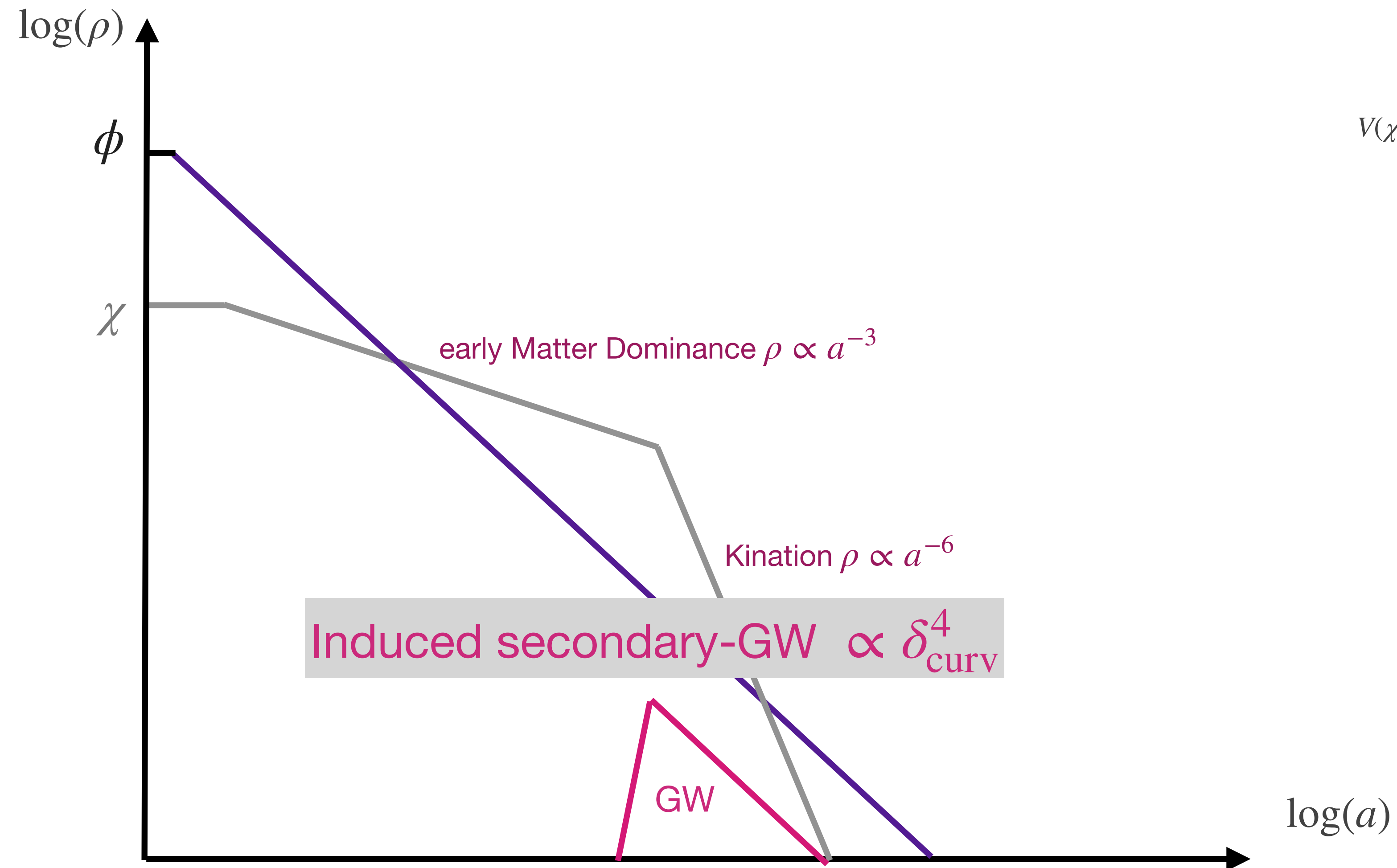


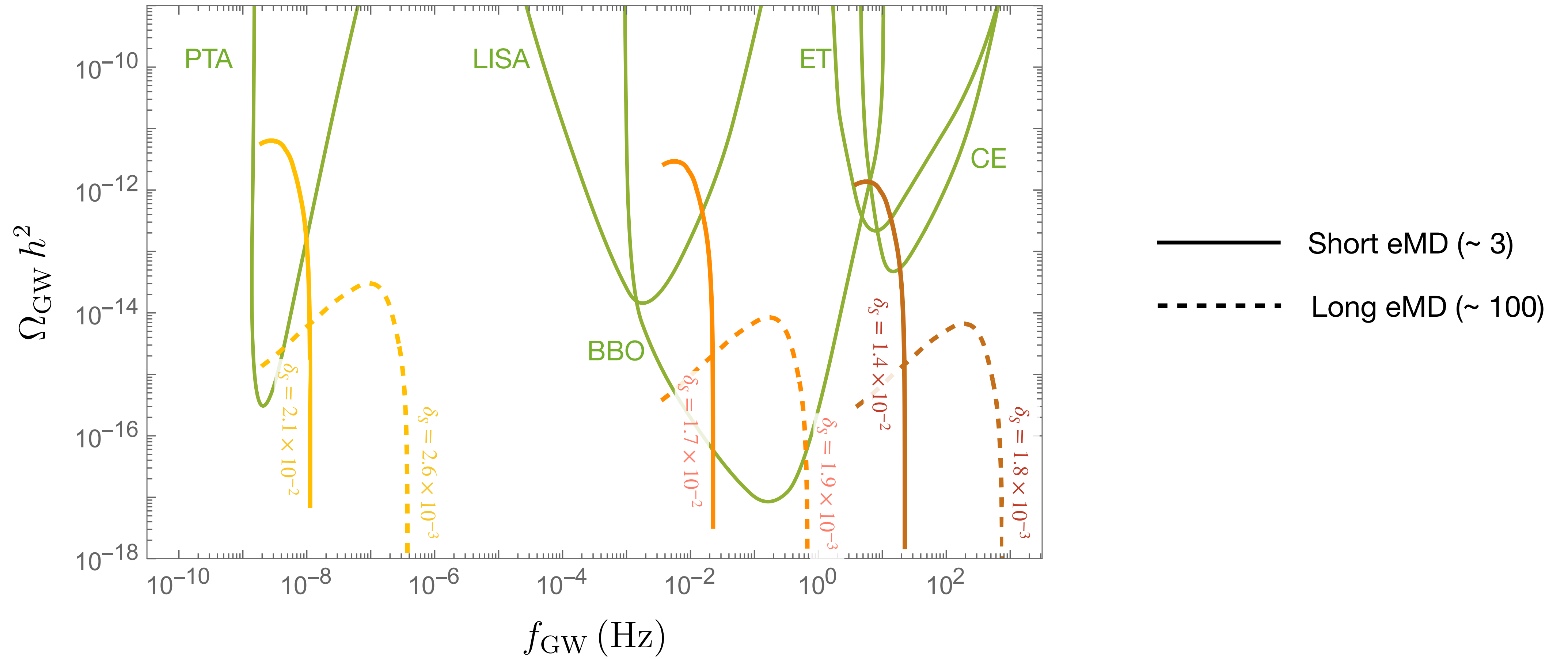
Fig. from Y. Gouttenoire et al. 2111.01150

Case 2: Induced secondary-GW

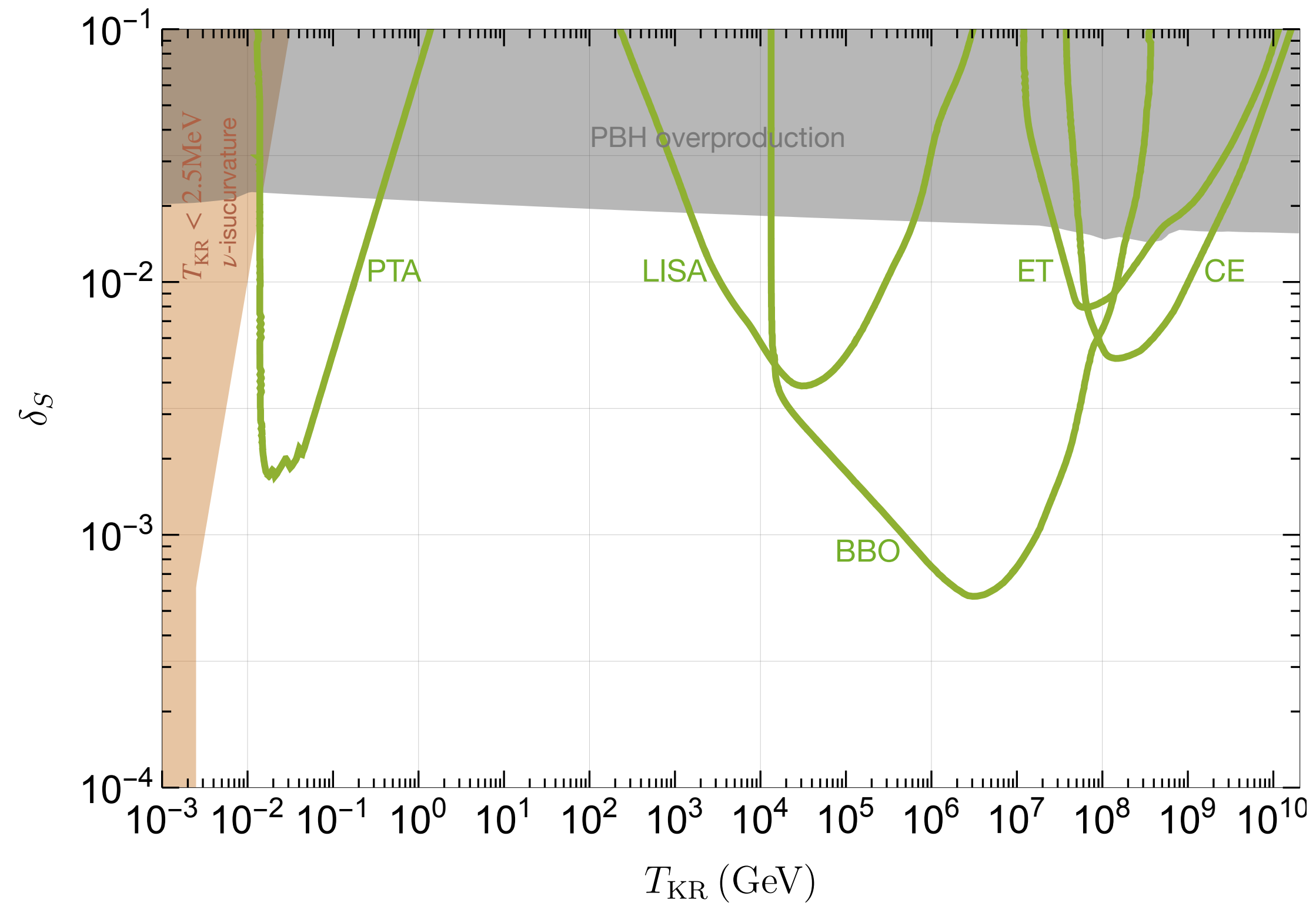
Matter domination followed by a period of kination: rotating ALP field



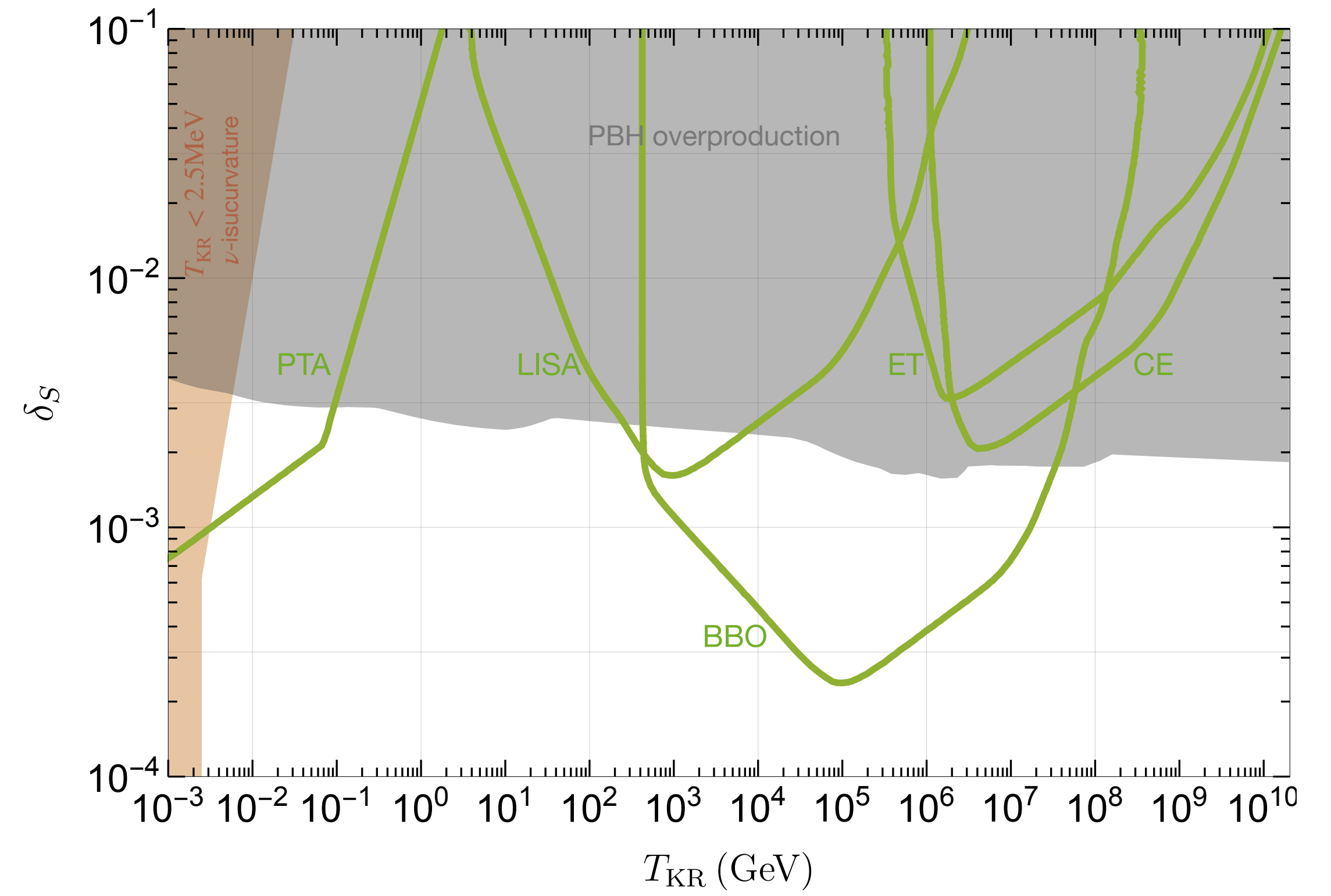
In progress...



In progress...



Short eMD ~ 3



Long eMD ~ 100

Summary

- There can be new cosmological fluctuation maps significantly different from CMB.
- Such maps can be realized in GWB (first-order phase transition, induced secondary-GW).
- GWB with large (large scale) fluctuations are interesting both experimentally and theoretically.
- Modified post-inflationary cosmologies play an important role in the observability of these highly anisotropic GWB.

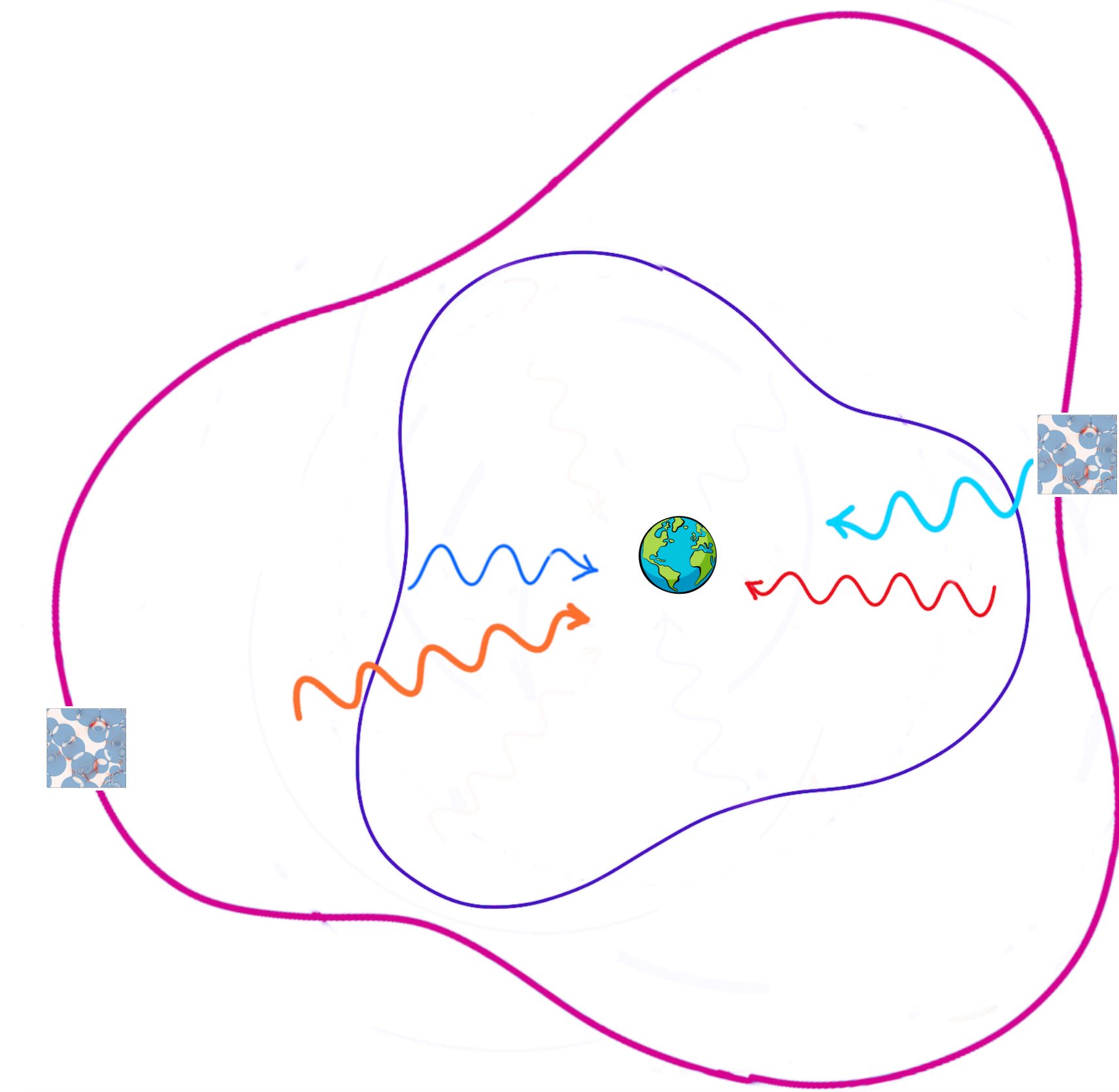
Summary

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Thank you!

Back-up slides

Bubbles are unresolvable

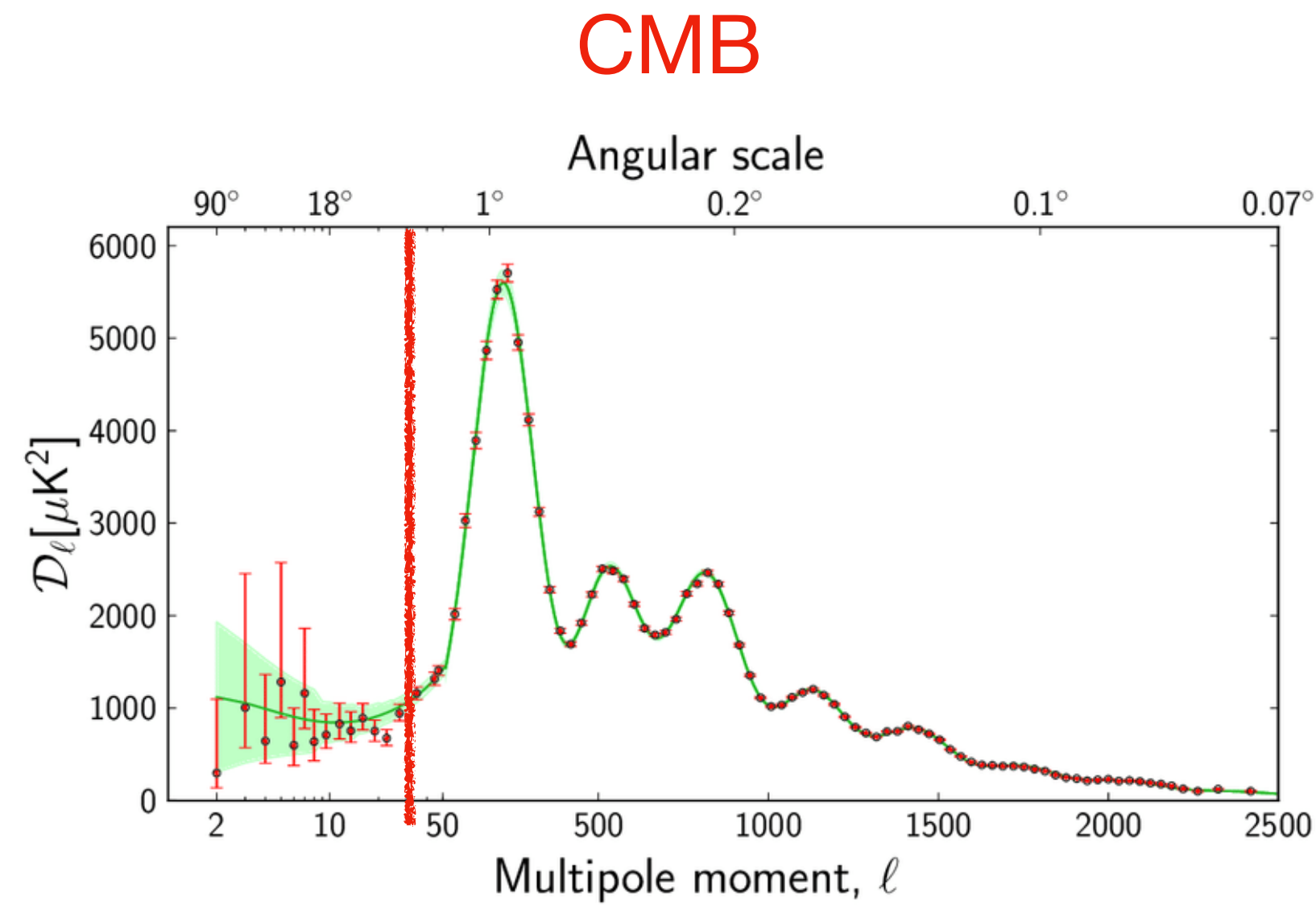


Caution: Zoomed in!

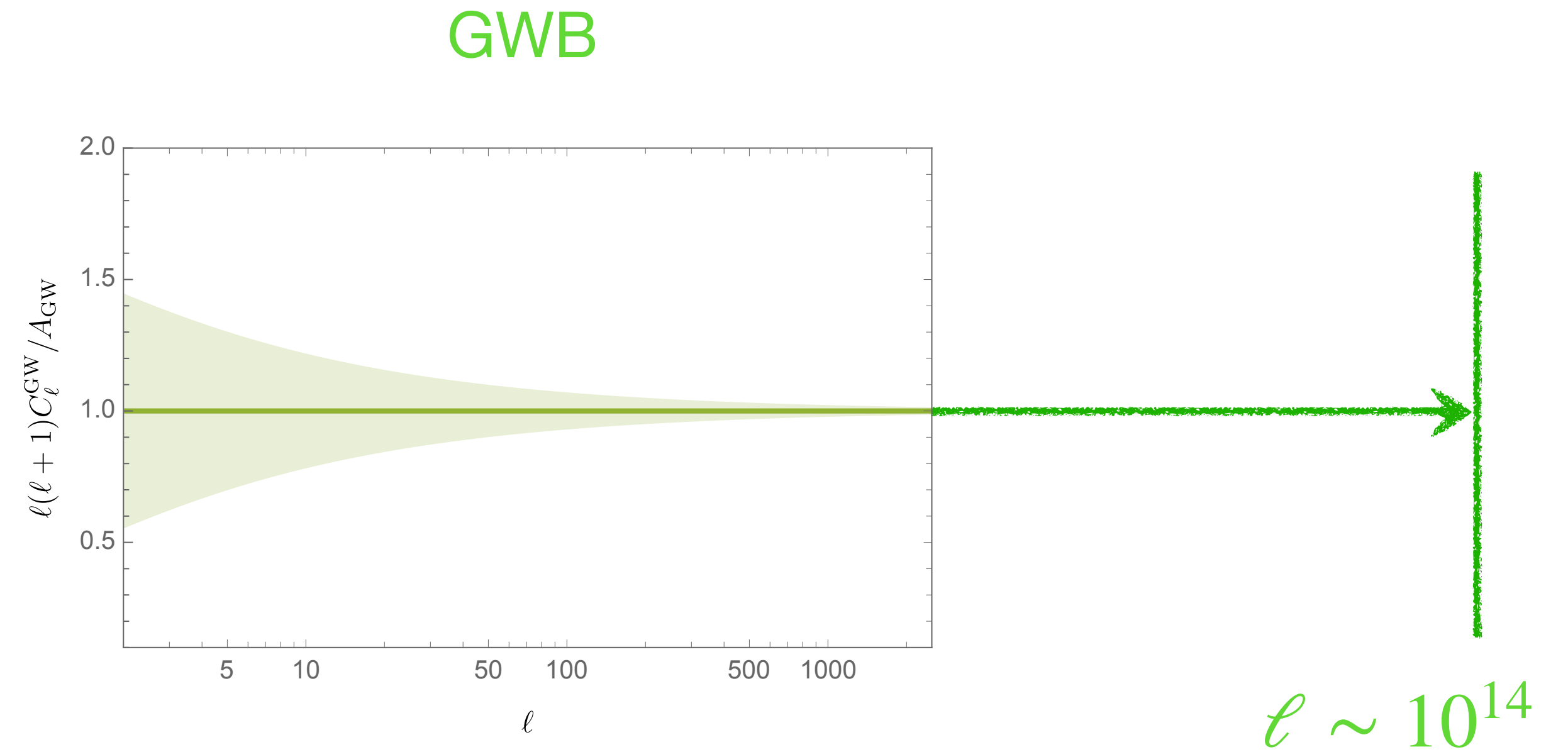
$> 10^{18}$ bubble collisions/arcsec²
 \implies Bubbles are unresolvable
sources : getting a course
grained picture of GWB

GWB is a “pristine” map

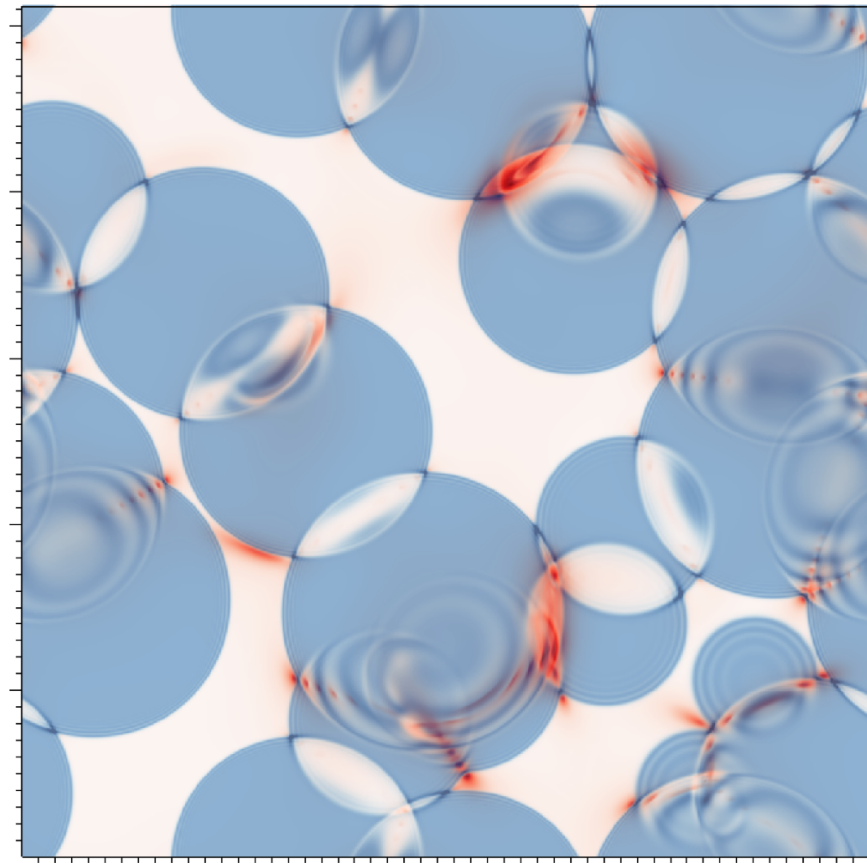
Earlier production + free-streaming of GW \rightarrow large range of scales is unaltered by sub-horizon physics



Planck



Energy density in GWB from PT (2)



Power released in bubble collision

$$\frac{dE_{\text{GW}}}{dt} \sim G_N \left(\frac{d^3 Q}{dt^3} \right)^2$$

Quadrupole moment

$$Q \sim \rho_{\text{lat}} r^5 \rightarrow \frac{d^3 Q}{dt^3} \sim \rho_{\text{lat}} \frac{r^5}{(\Delta t_{\text{PT}})^3}$$

Typical time scale /length scale (Duration of the PT)

$$r \sim \Delta t_{\text{PT}} \equiv \beta^{-1}$$

GW energy density released in bubble collision

$$\rho_{\text{GW}} \sim \frac{dE_{\text{GW}}}{dt} \frac{\Delta t_{\text{PT}}}{r^3} \sim \frac{G_N \rho_{\text{lat}}^2}{\beta^2}$$

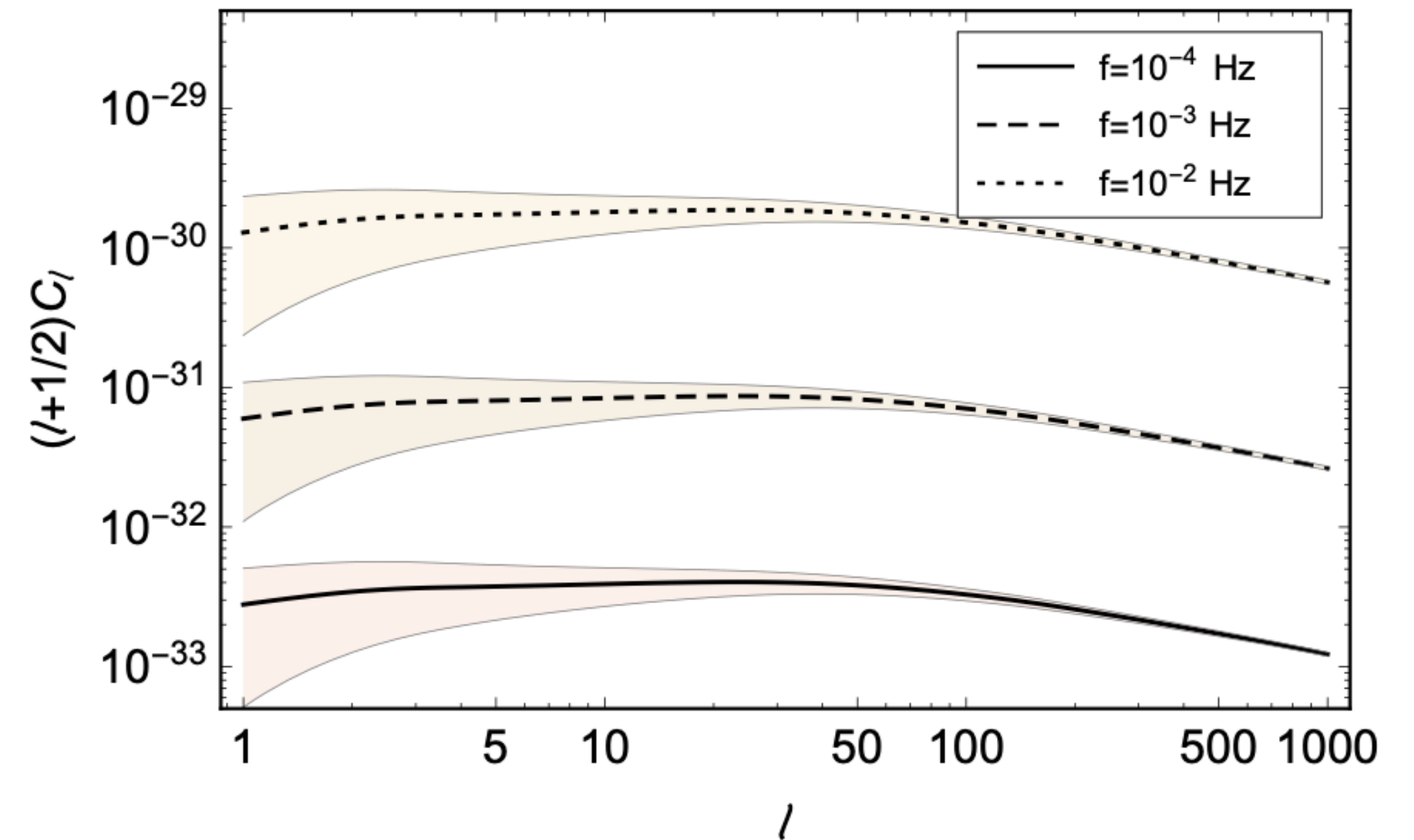
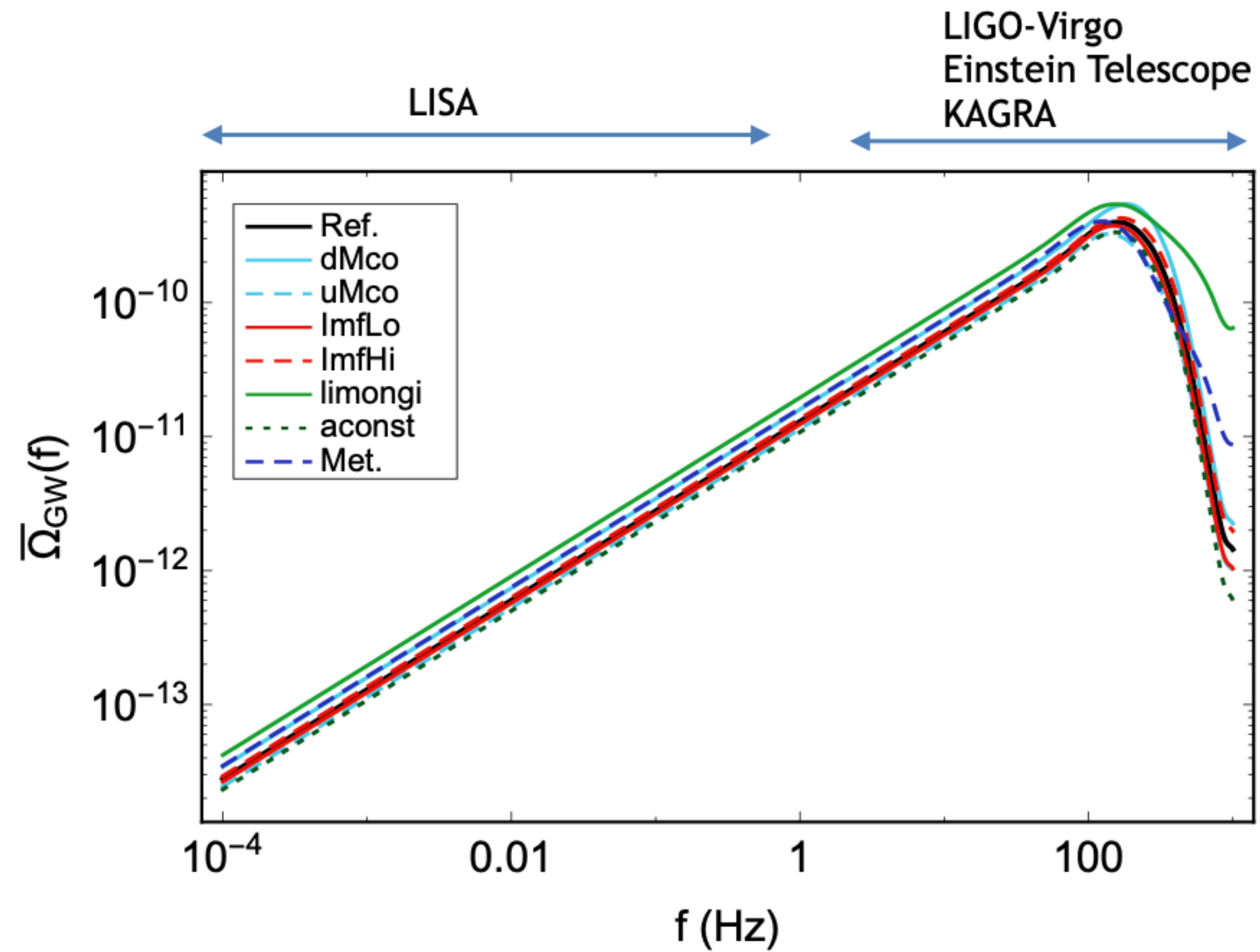
$$G_N \rho_{\text{total}} \sim H^2$$

→

$$\rho_{\text{GW}} \sim \left(\frac{H}{\beta} \right)^2 \left(\frac{\rho_{\text{lat}}}{\rho_{\text{total}}} \right)^2 \rho_{\text{total}}$$

Astrophysical foregrounds in mHz range

Inspiring stellar-mass BH



Giulia Cusin, Irina Dvorkin, Cyril Pitrou, Jean-Philippe Uzan: 1904.07757v2

Also see: 2201.08782v from LISA working group