

Introduction

*Gravitational waves from first-order phase transitions:
model distinction from sound-wave and free-streaming sources*

*GWs from
sound-wave
sources*

Ryusuke Jinno (Kobe Univ.)

*w/ Chiara Caprini, Thomas Konstandin, Alberto Roper Pol, Henrique Rubira,
Bibhushan Shakya, Isak Stomberg, Jorinde van de Vis*

Hearing BSM with Cosmic Sources of GWs @ICTS, 2024/12/31

*GWs from
free-streaming
sources*

Summary



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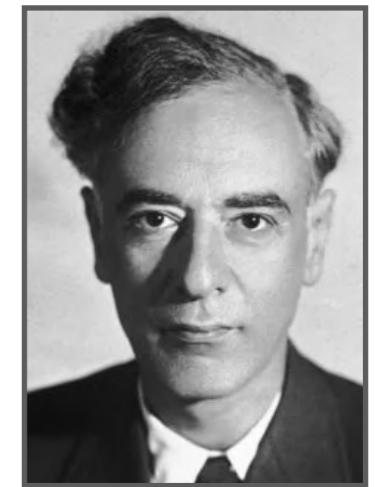
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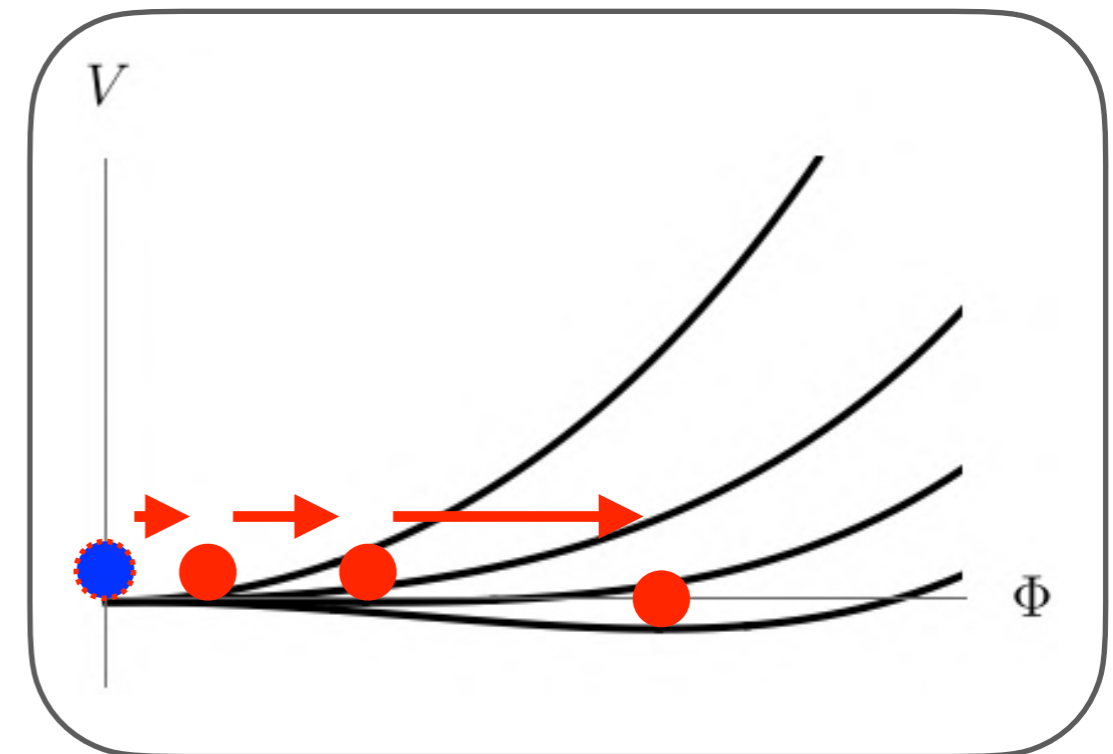
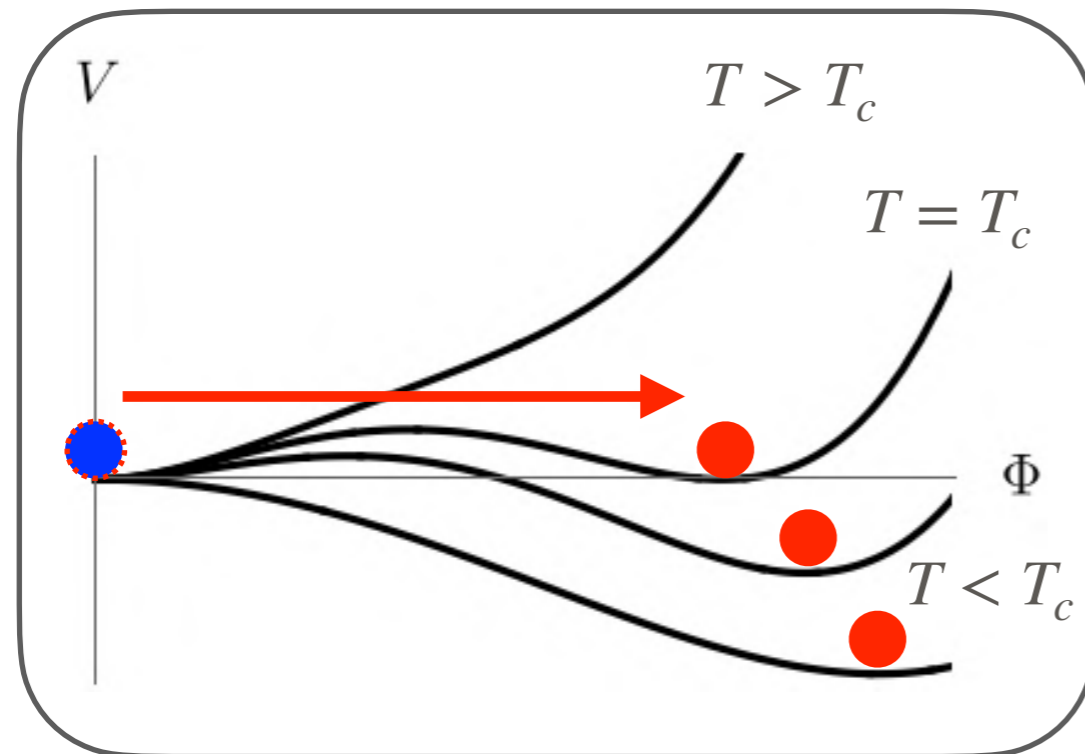
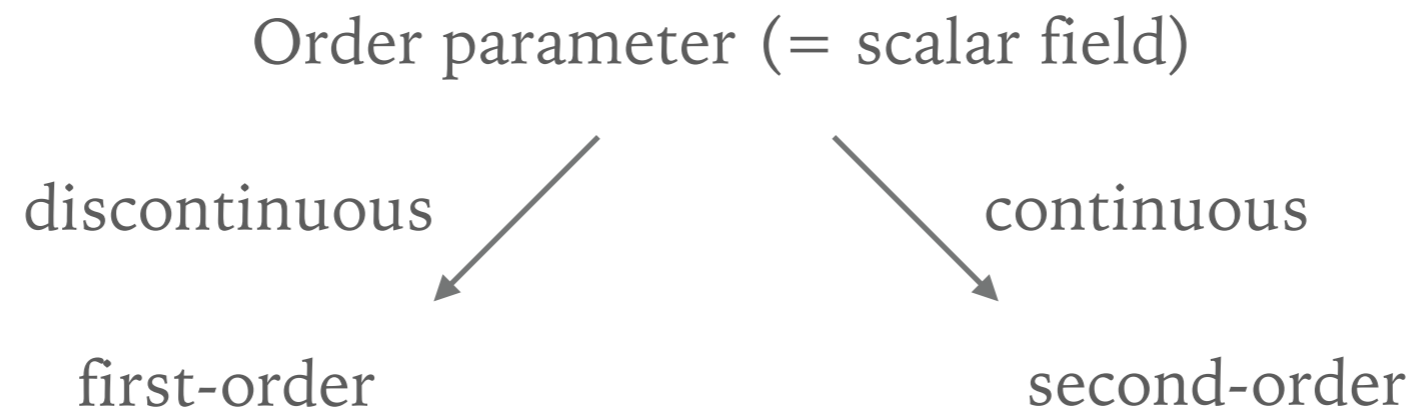


PHASE TRANSITIONS

► Classification of phase transitions (a la Landau)



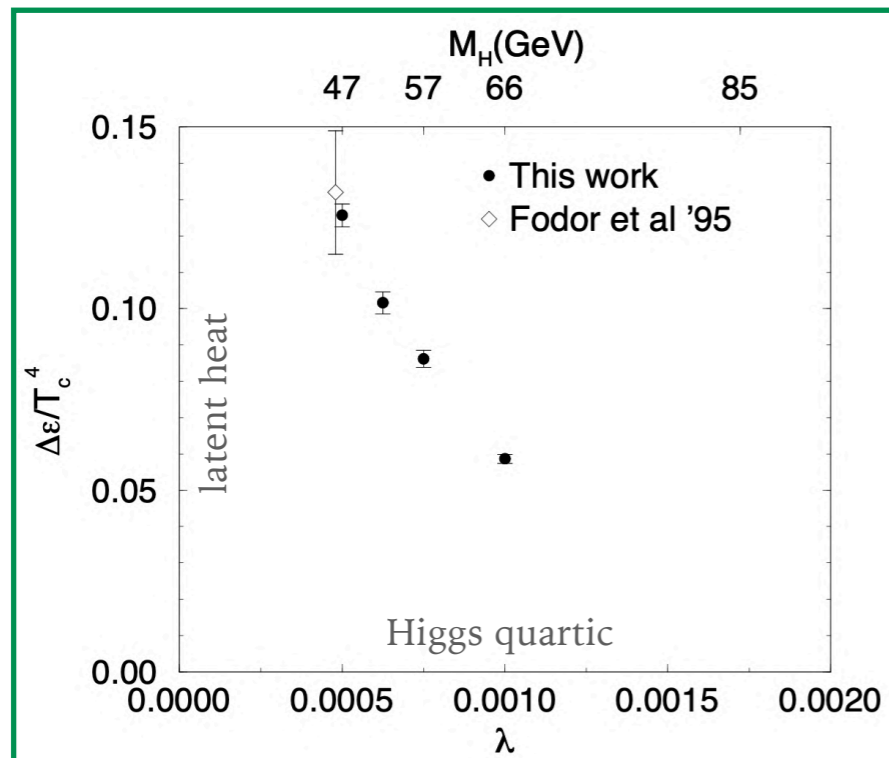
[Landau, from Wikipedia]



THERMAL HISTORY OF THE UNIVERSE

- ▶ Two candidates for FOPTs in the Standard Model (SM)

Electroweak phase transition & QCD phase transition

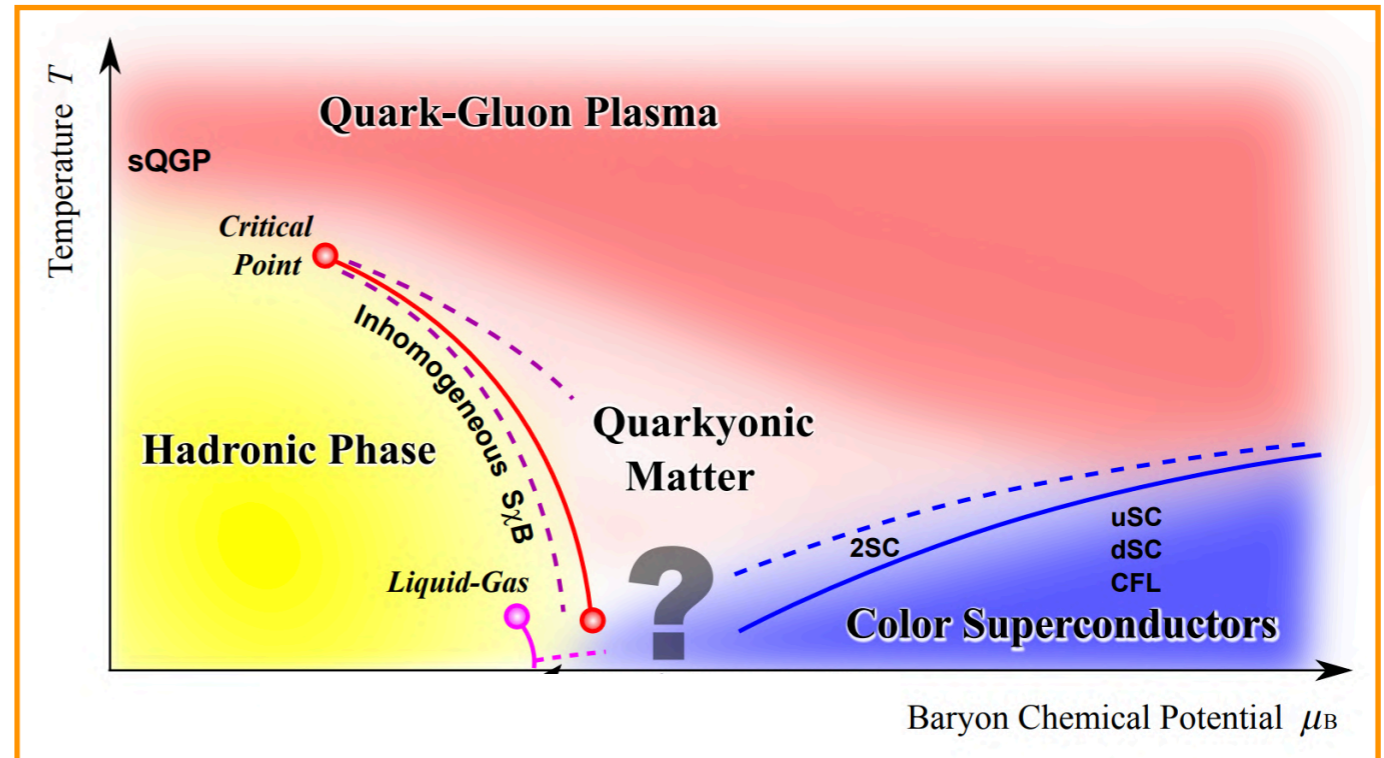


[Aoki '97]

see also

[Kajantie, Laine, Rummukainen, Shaposhnikov '96]

[Karsch, Neuhaus, Patkós, Rank '97]



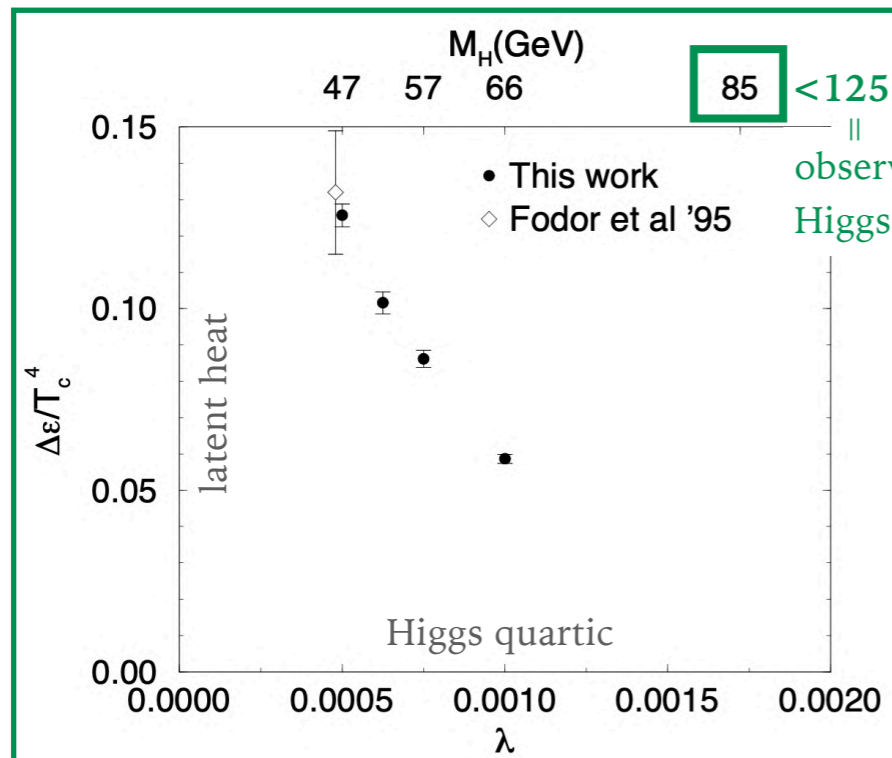
[Fukushima, Hatsuda '11]

→ Unfortunately both are crossover

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Electroweak phase transition & QCD phase transition

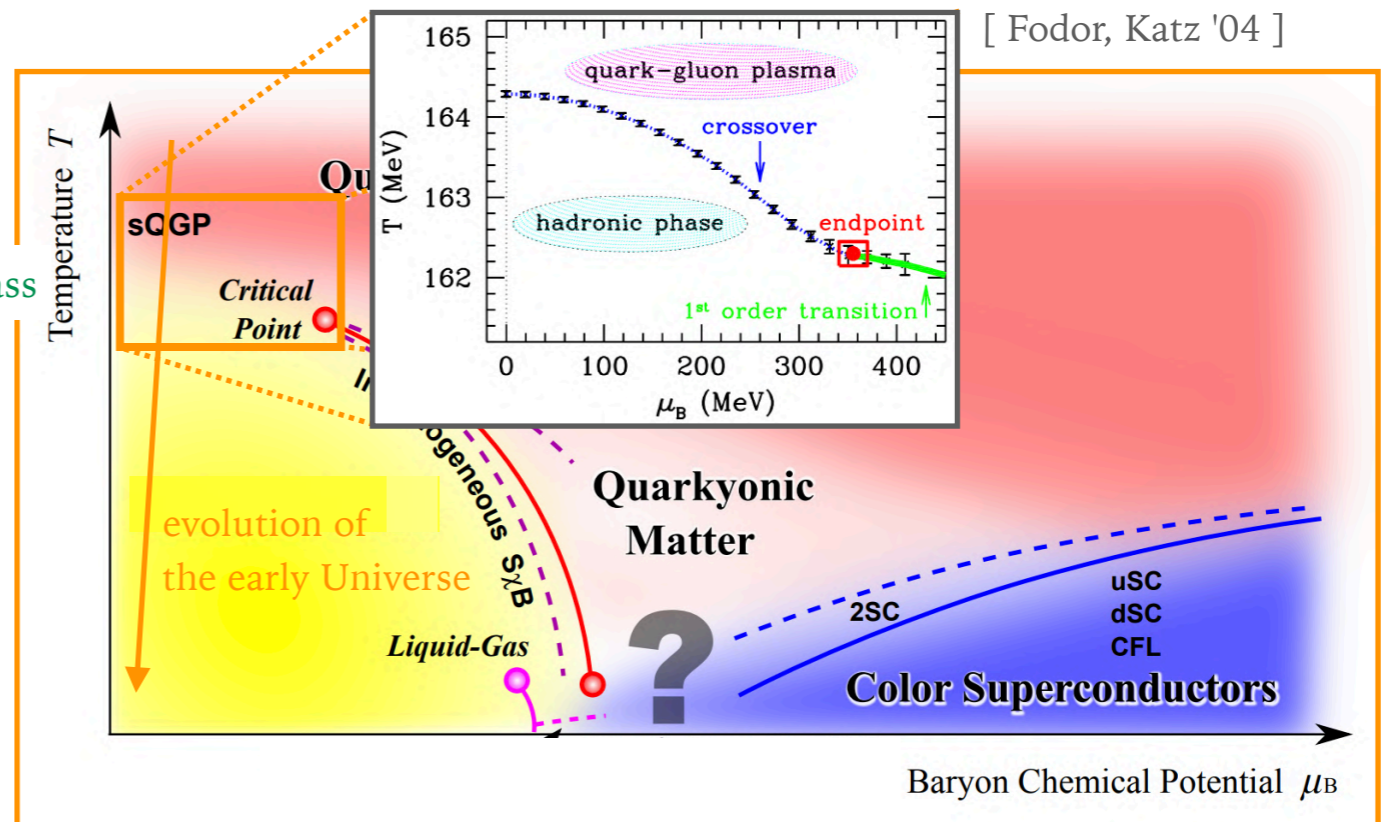


[Aoki '97]

see also

[Kajantie, Laine, Rummukainen, Shaposhnikov '96]

[Karsch, Neuhaus, Patkós, Rank '97]



[Fodor, Katz '04]

[Fukushima, Hatsuda '11]

→ Unfortunately both are crossover

WHY DO WE CONSIDER FIRST-ORDER PHASE TRANSITIONS?

- The vast energy scale the Universe might have experienced from inflation ($\lesssim 10^{15}\text{GeV}$) to the present ($\sim 10^{-4}\text{eV}$)
- Spontaneous symmetry breaking that might have happened
 - Breaking of the GUT group
 - Breaking of Peccei-Quinn symmetry $U(1)_{\text{PQ}}$
 - Breaking of B-L symmetry $U(1)_{\text{B-L}}$
 - Breaking of dark groups ...
- Testable in the coming 10-20 yrs with GWs

OVERVIEW

microphysics

Dynamics of bubbles

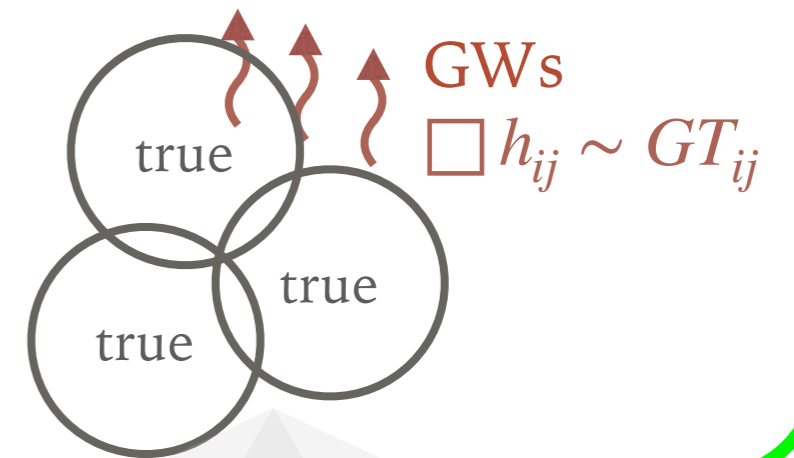
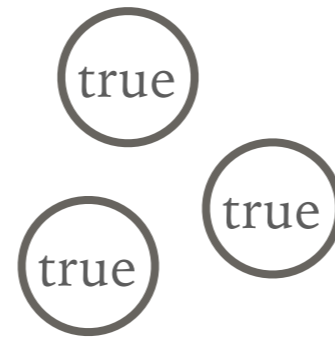
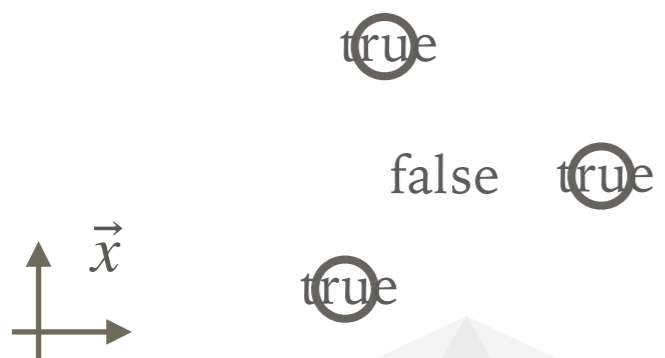
macrophysics

time or scale →

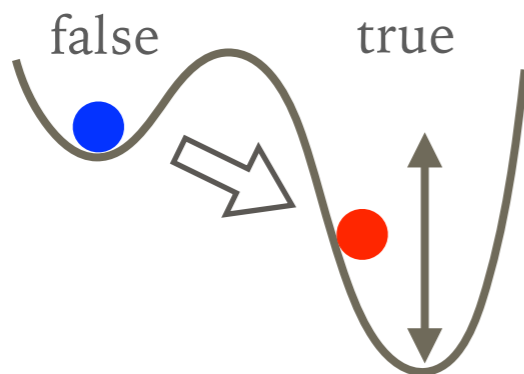
(1) nucleation (核生成)

(2) expansion (拡大)

(3) collision (衝突)



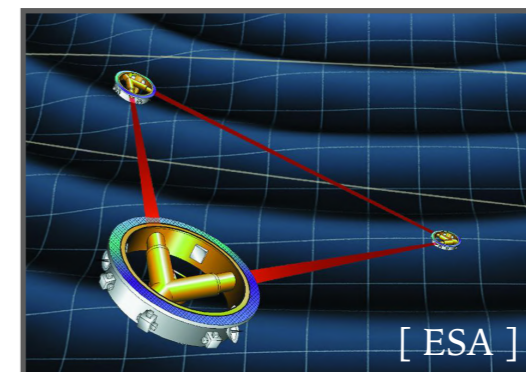
Physics of the Higgs sector



FOPTs in BSM

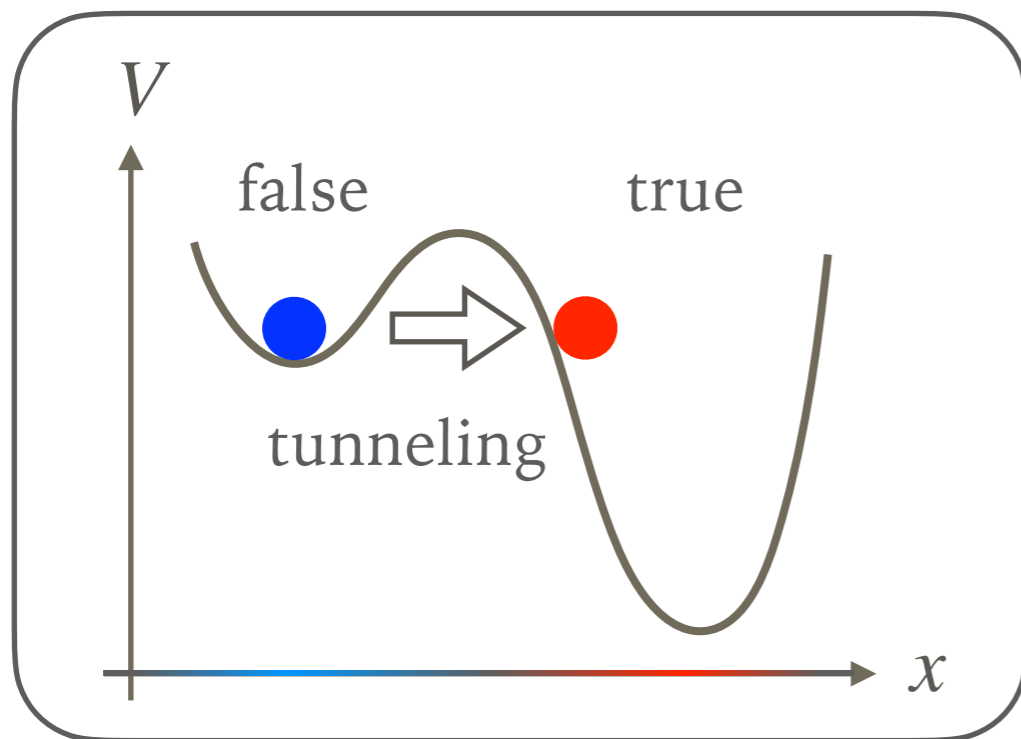
GWs

GW observations

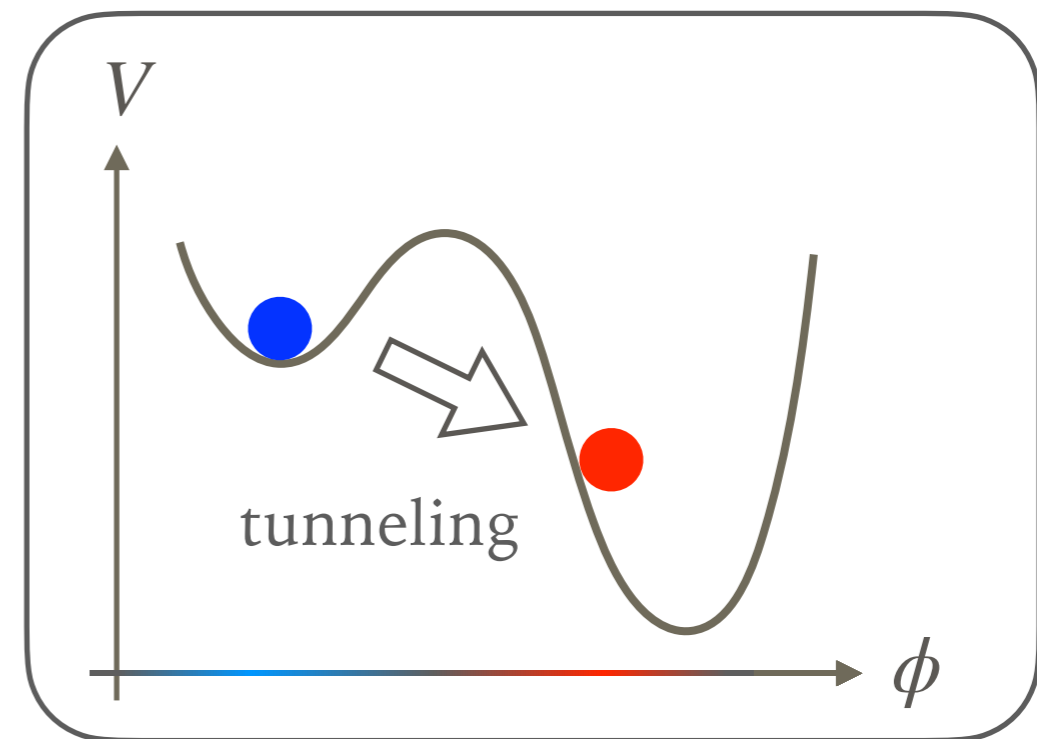


TUNNELING IN QUANTUM MECHANICS AND QFT

Quantum mechanics

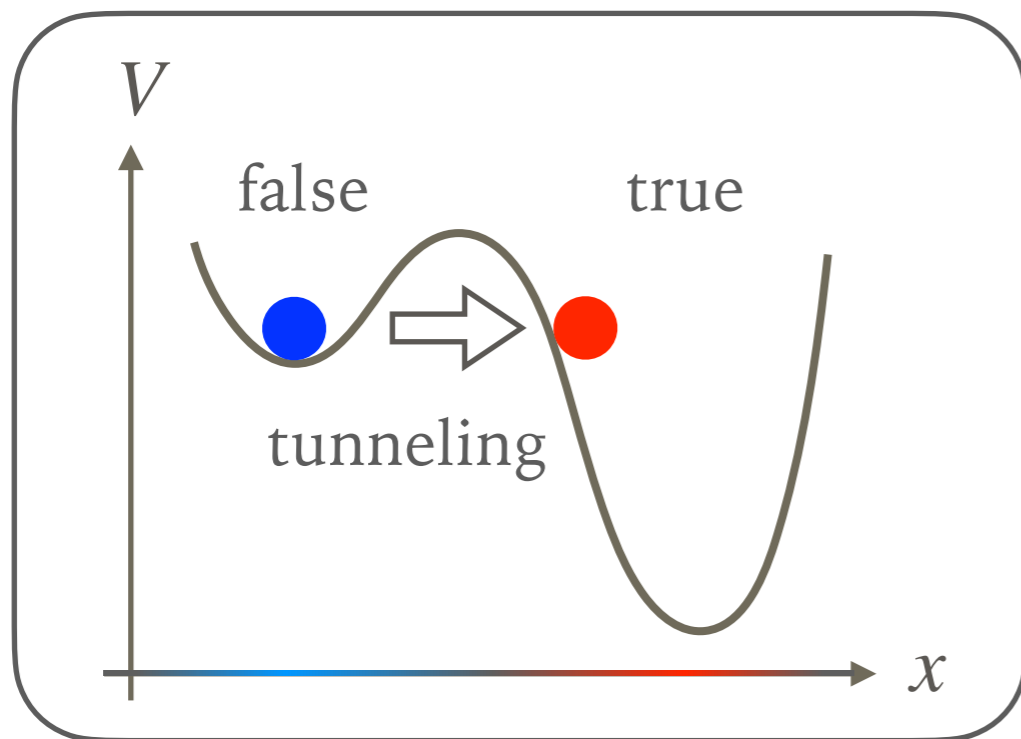


Quantum field theory

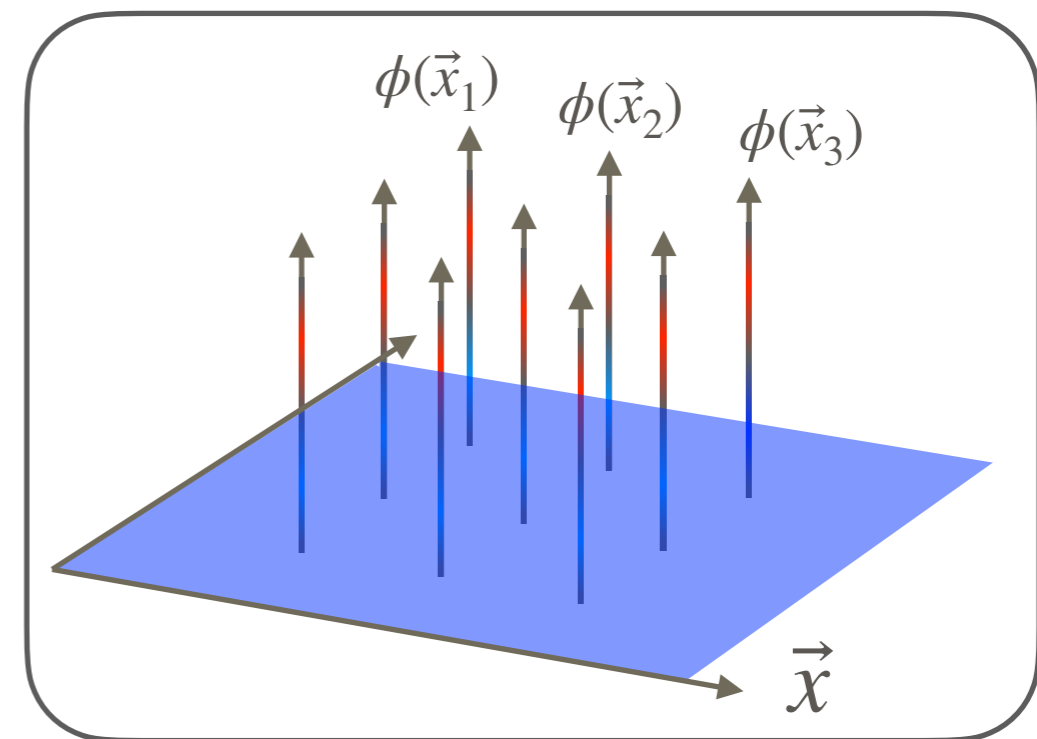


TUNNELING IN QUANTUM MECHANICS AND QFT

Quantum mechanics

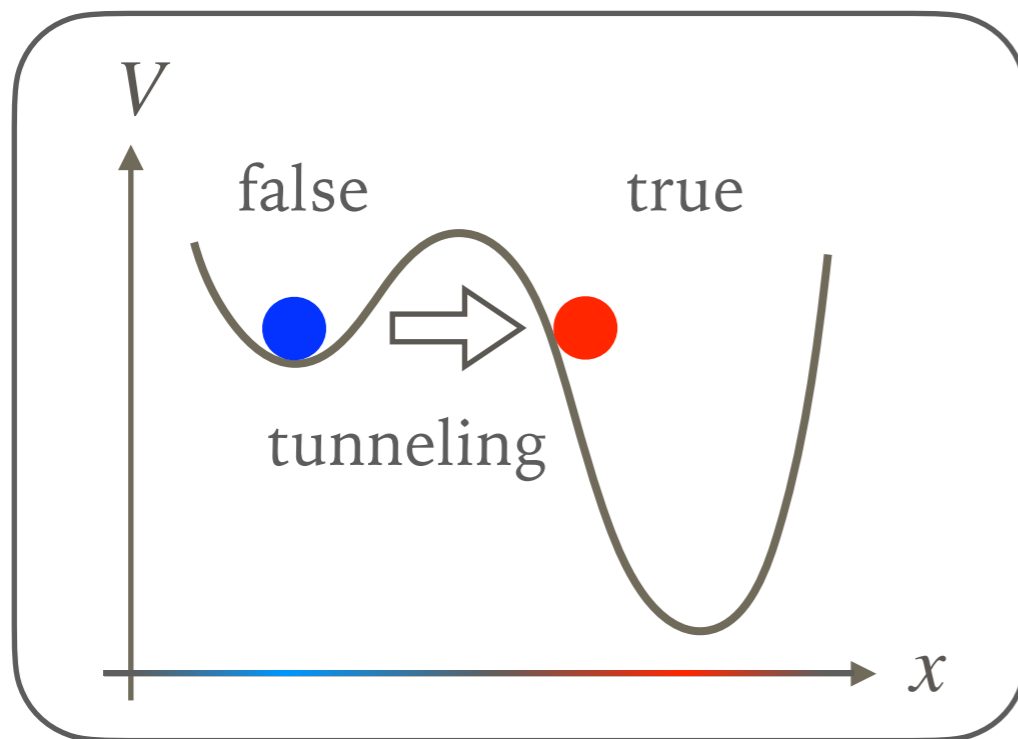


Quantum field theory

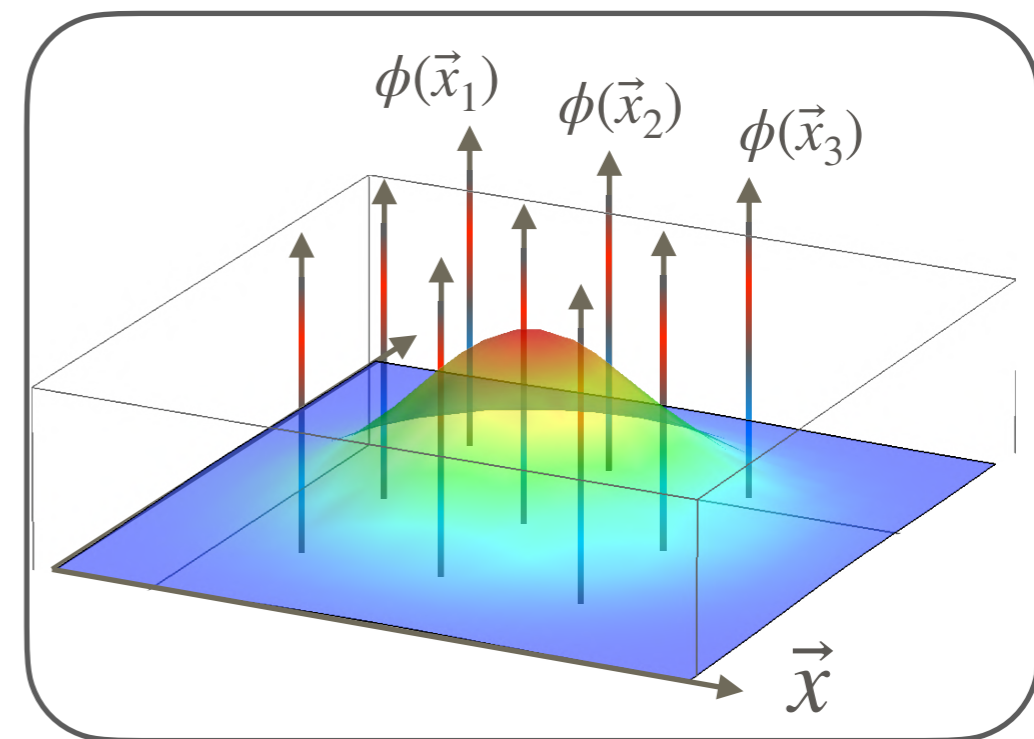


TUNNELING IN QUANTUM MECHANICS AND QFT

Quantum mechanics

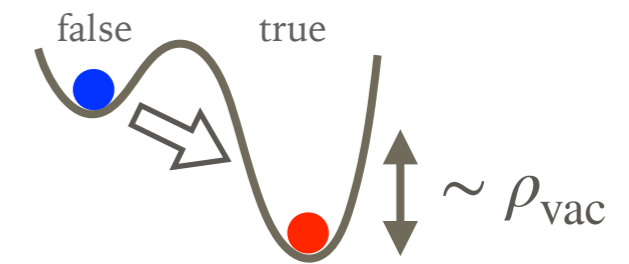


Quantum field theory



tunneling (nucleation, 核生成)

BUBBLE EXPANSION



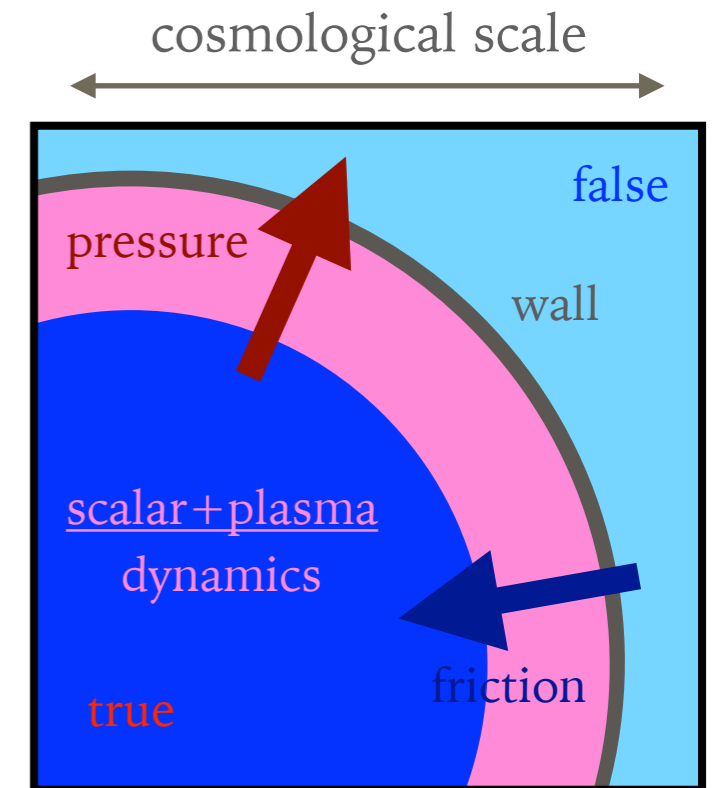
► "Pressure vs. Friction" determines the behavior:

(1) **Pressure**: wall is pushed by the released energy

Determined by $\alpha \equiv \rho_{\text{vac}}/\rho_{\text{plasma}}$

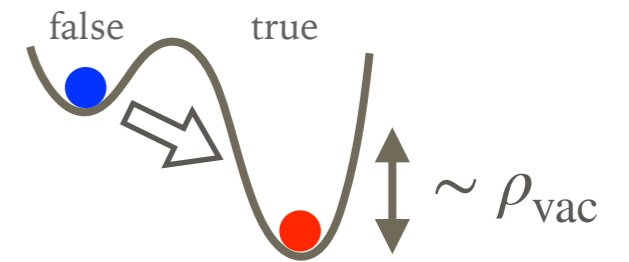
see e.g. [Espinosa et al. '10,
Hindmarsh et al. '15,
Giese et al. '20]

(2) **Friction**: wall is pushed back by plasma particles

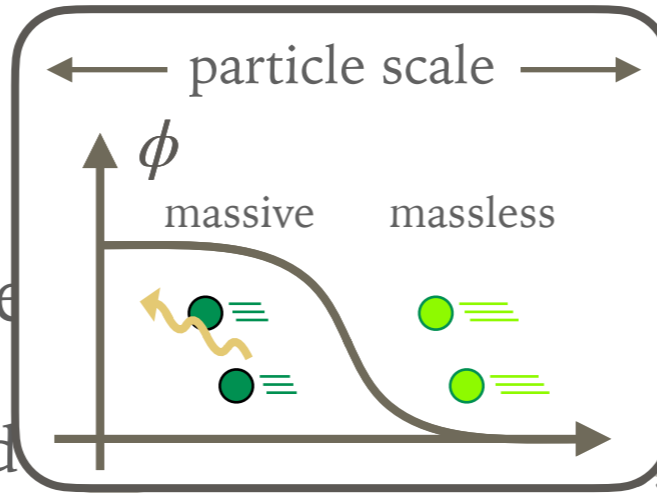


BUBBLE EXPANSION

[See Andrew's talk]



► "Pressure vs. Friction" depends on:



on:

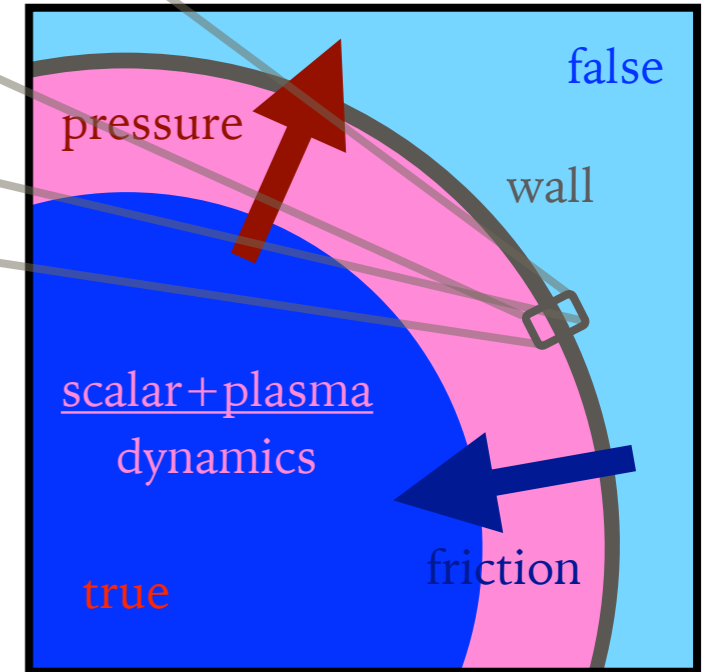
cosmological scale

(1) Pressure: wall is pushed forward

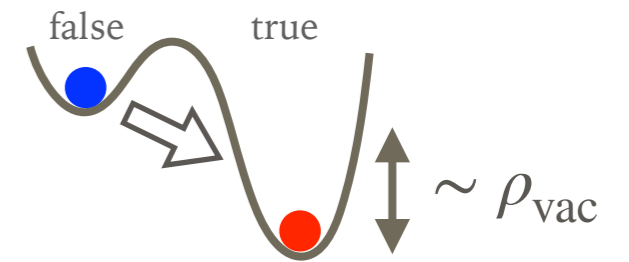
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(2) Friction: wall is pushed back by plasma particles



BUBBLE EXPANSION



➤ "Pressure vs. Friction" determines the behavior:

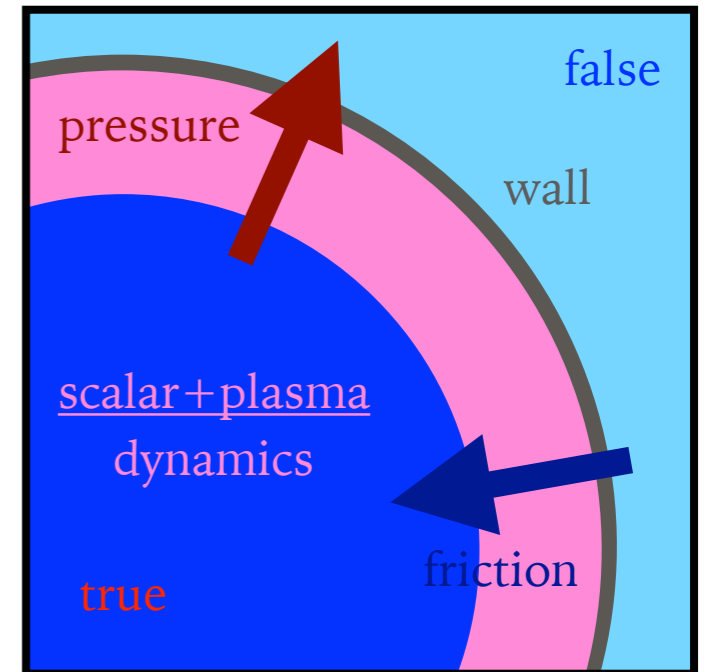
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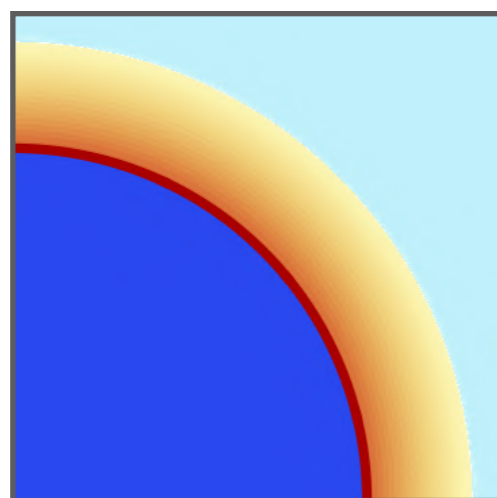
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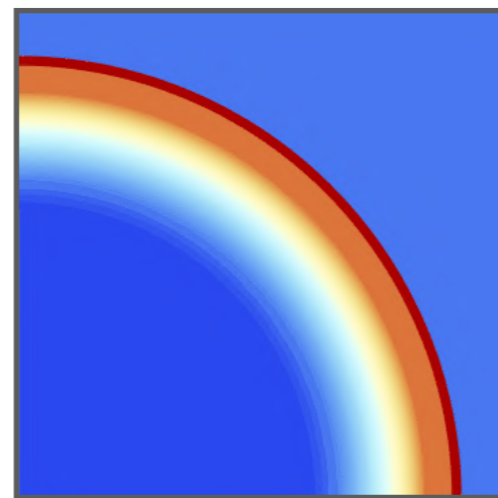
cosmological scale



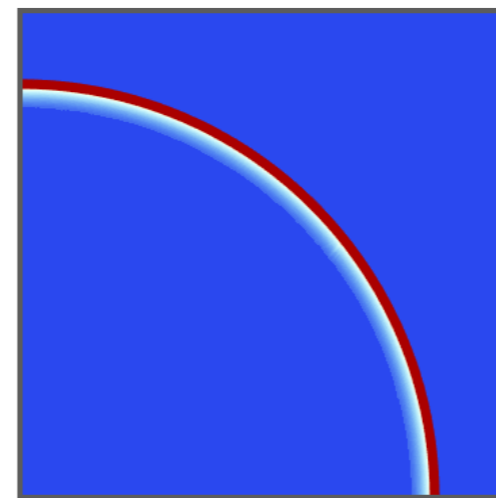
➤ Different types of bubble expansion



deflagration



detonation



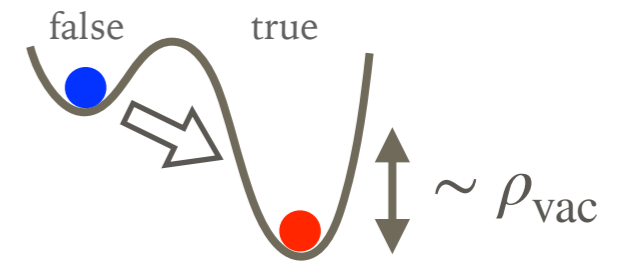
~ 1 relativistic detonation $\gg 1$



runaway

α

BUBBLE EXPANSION

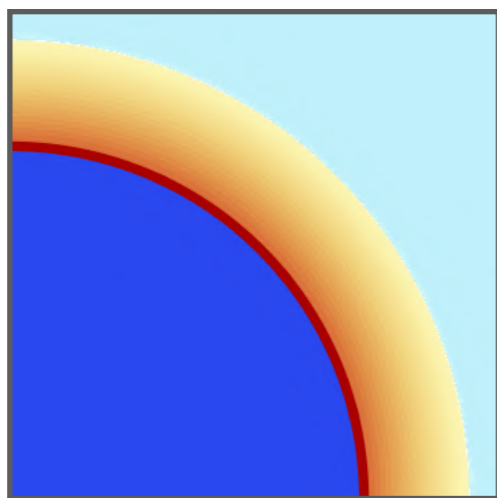
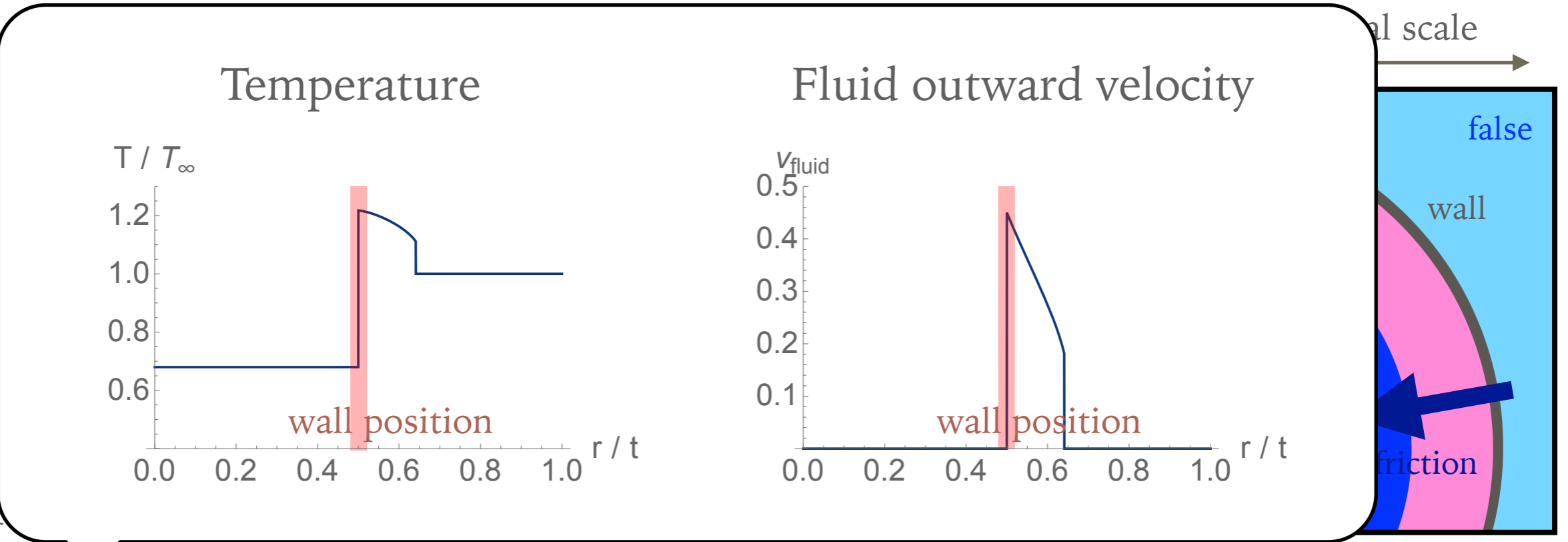


➤ "Pr"

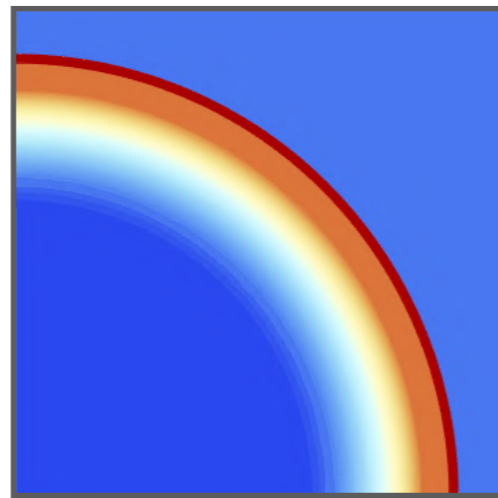
(1)

(2)

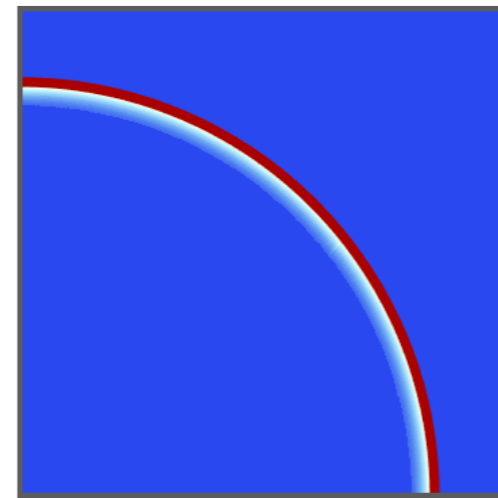
➤ Dis



deflagration



detonation



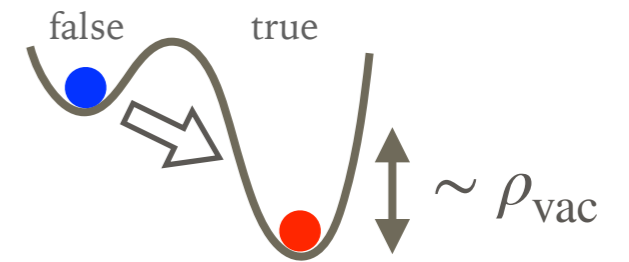
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runaway



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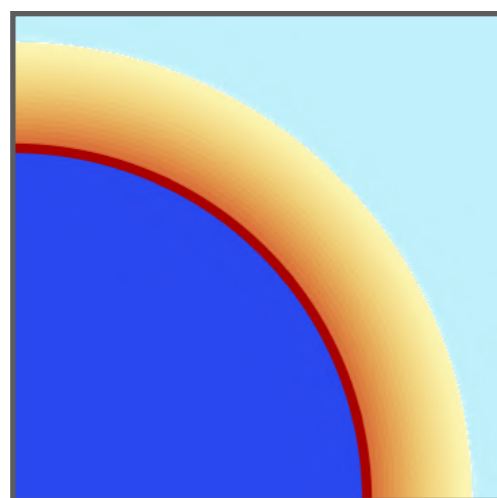
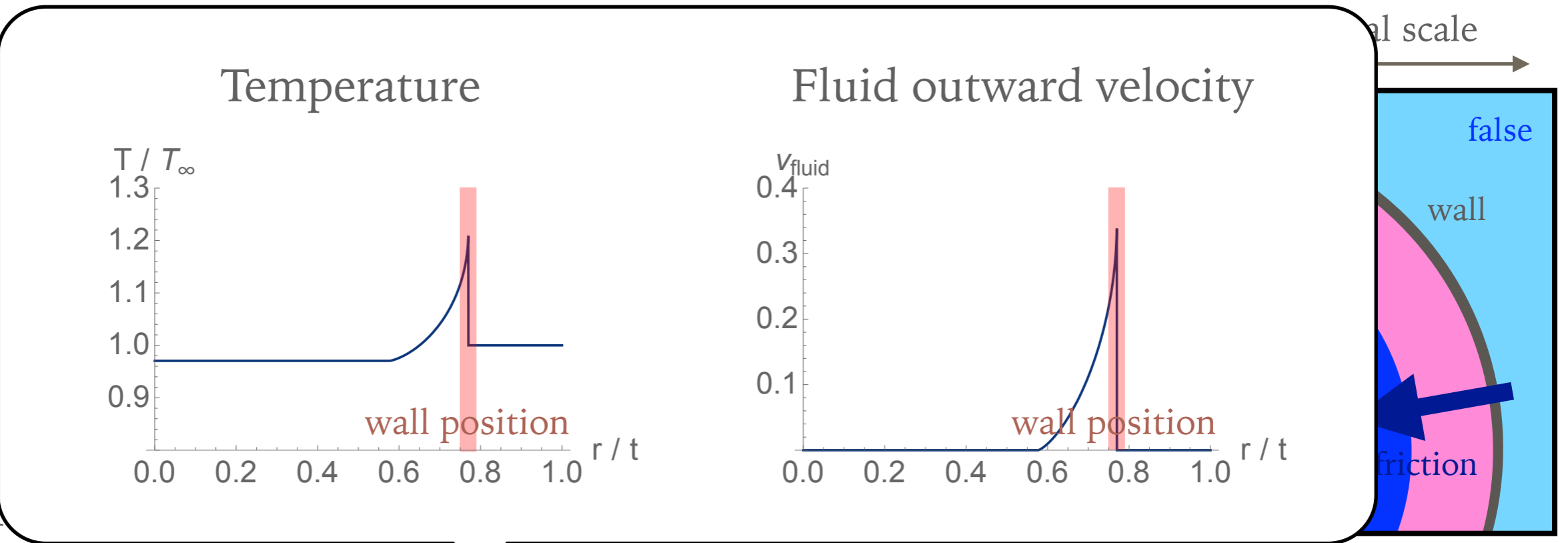


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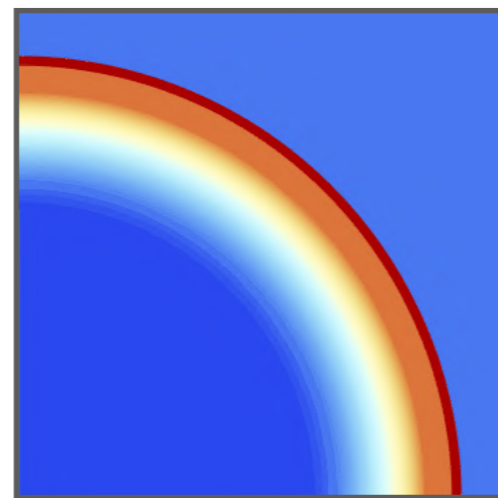
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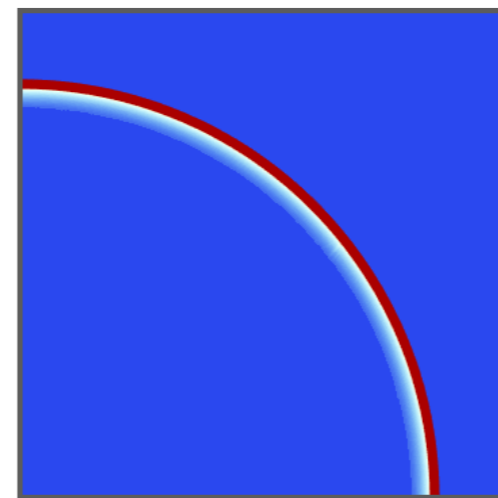
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deflagration



detonation



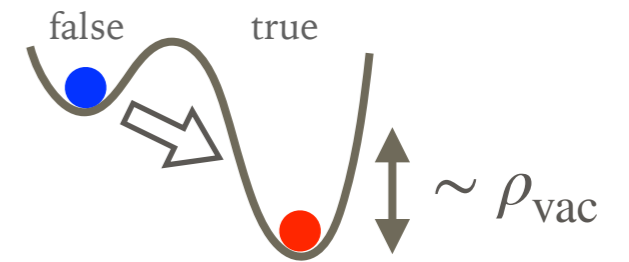
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runaway



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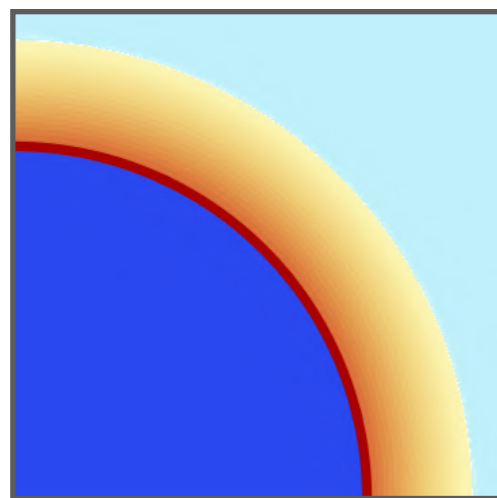
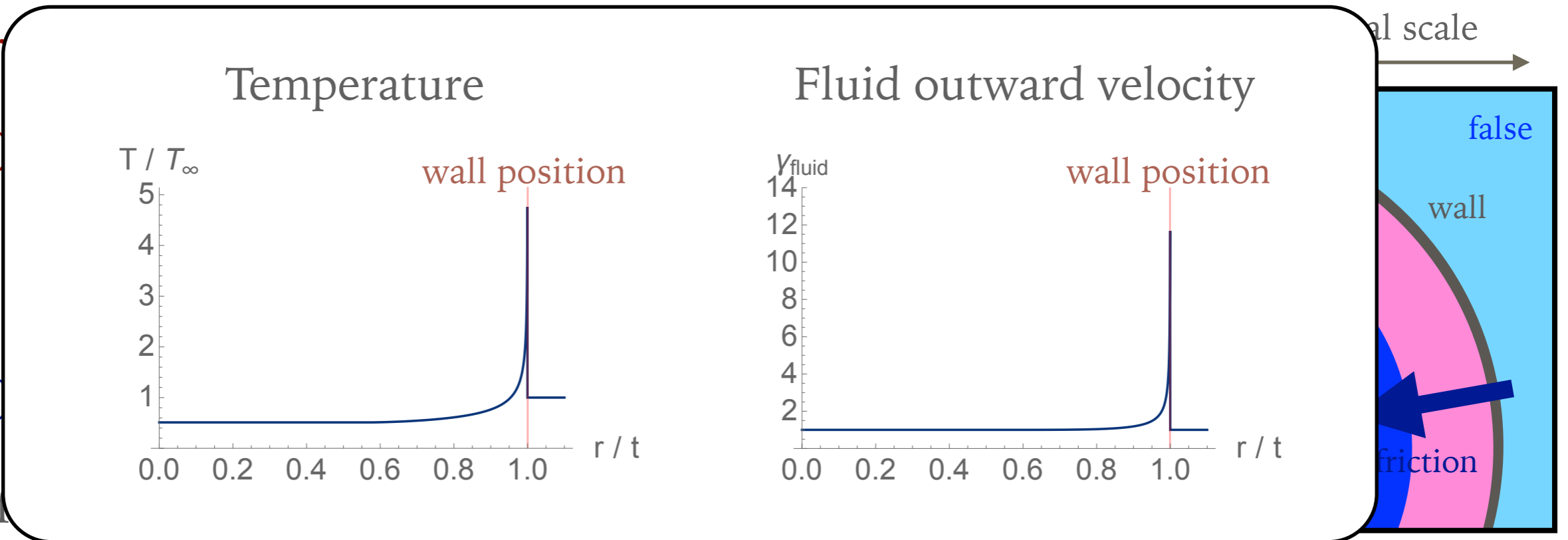


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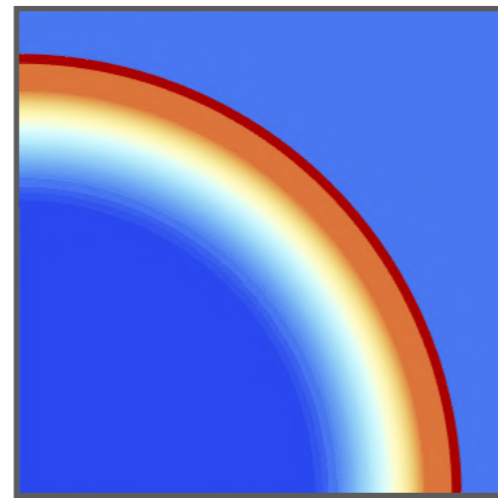
(1)

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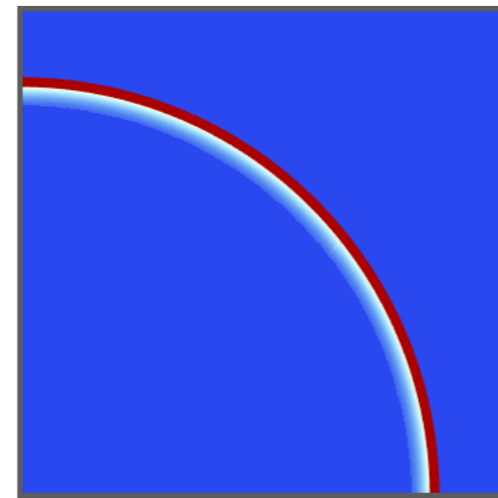
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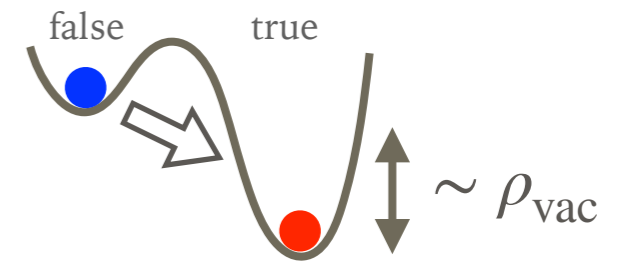
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runaway



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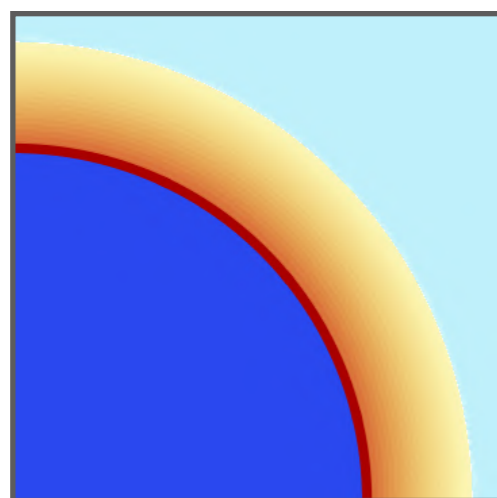
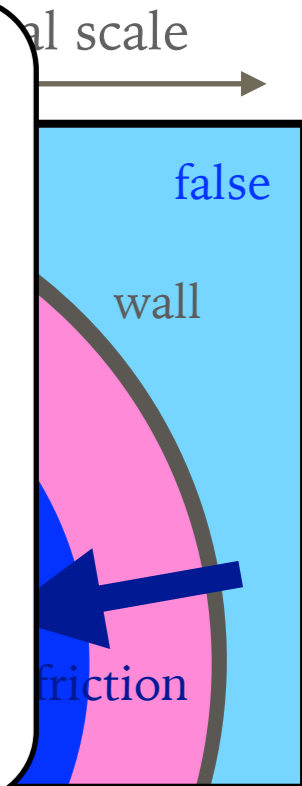
(1)

Plasma particles cannot stop the acceleration of the walls:
walls continue to accelerate until they collide with others

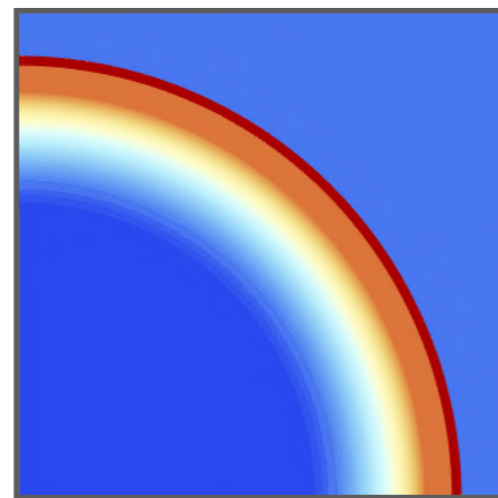
(2)

[Bodeker & Moore '09, '17]

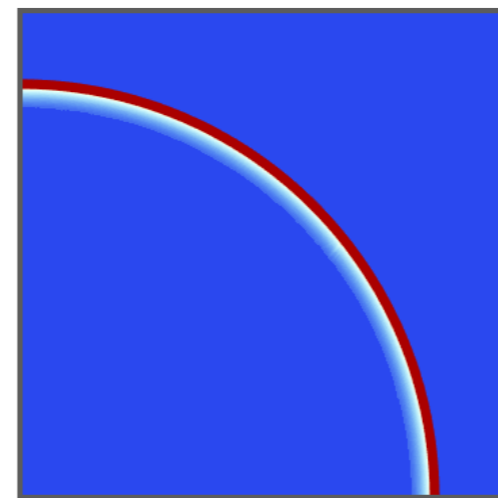
➤ Dis



deflagration



detonation



~ 1 relativistic detonation $\gg 1$



runaway



Youtube "Explosions: 100 ton test detonation"



GRAVITATIONAL WAVES: A NEW PROBE TO THE UNIVERSE

[See Subhendra's lecture]

- Einstein equation:

$$R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} = 8\pi GT_{\mu\nu}$$

"Spacetime tells **matter** how to move. **Matter** tells spacetime how to curve."

- Gravitational waves: transverse-traceless part of the **metric**

$$ds^2 = -dt^2 + a^2(\delta_{ij} + h_{ij})dx^i dx^j \quad \partial_i h_{ij} = h_{ii} = 0$$


- After expanding the Einstein equation,

GWs obey a wave equation sourced by **energy-momentum tensor**

$$\square h_{ij} = 16\pi G \Lambda_{ij,kl} T_{kl}$$

- LIGO/Virgo detected GWs from binary black holes for the first time in 2015

PRL 116, 061102 (2016) Selected for a **Viewpoint** in *Physics* week ending 12 FEBRUARY 2016
PHYSICAL REVIEW LETTERS


Observation of Gravitational Waves from a Binary Black Hole Merger
B. P. Abbott *et al.**
(LIGO Scientific Collaboration and Virgo Collaboration)
(Received 21 January 2016; published 11 February 2016)

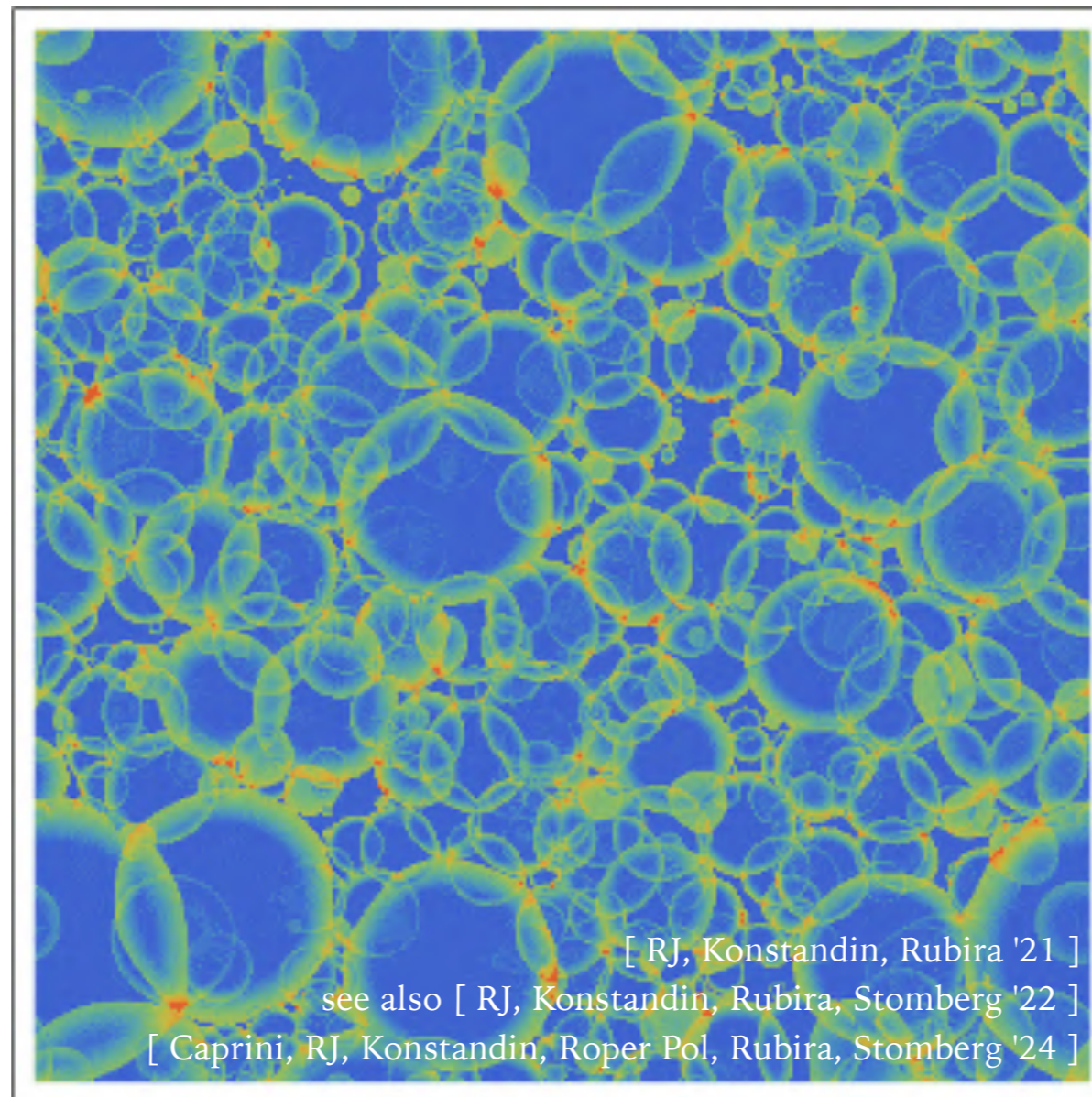
$$36M_{\odot} + 29M_{\odot} \rightarrow 62M_{\odot} + 3M_{\odot} \text{ (GWs)}$$

BUBBLE COLLISION & FLUID DYNAMICS

► Bubbles collide, and fluid dynamics sets in (example for



)



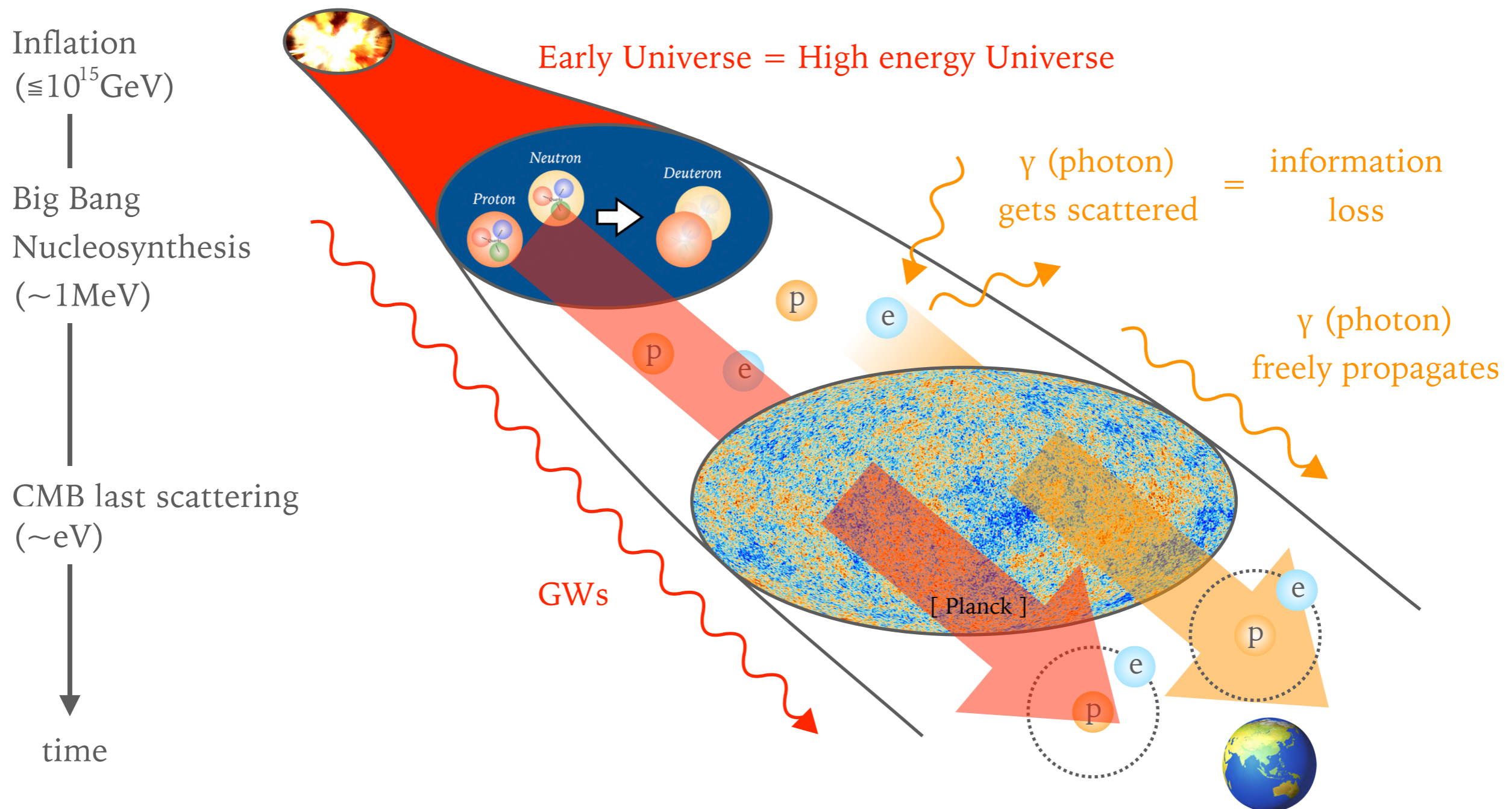
[RJ, Konstandin, Rubira '21]

see also [RJ, Konstandin, Rubira, Stomberg '22]

[Caprini, RJ, Konstandin, Roper Pol, Rubira, Stomberg '24]

GWS AS A PROBE OF THE EARLY UNIVERSE

► Cosmic Microwave Background (CMB) vs. Gravitational Waves (GWs)



PRESENT & FUTURE OBSERVATIONS

Pulsar timing
arrays

$\sim 10^{-8}$ Hz

Space-borne
interferometers

\sim mHz – Hz

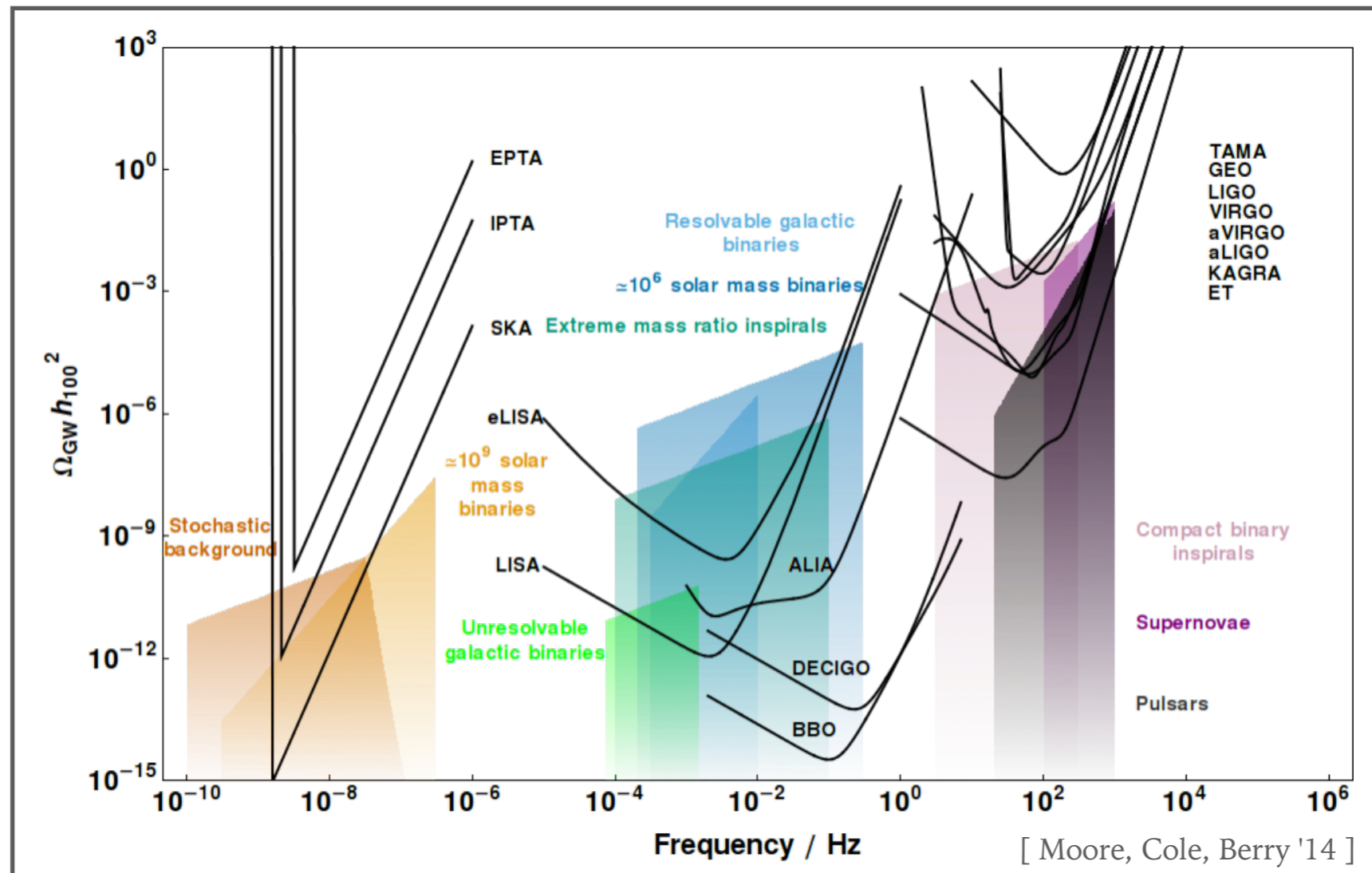
Ground-based
interferometers

~ 100 Hz

[Sriramkumar's lecture]

GW energy density per unit log freq.

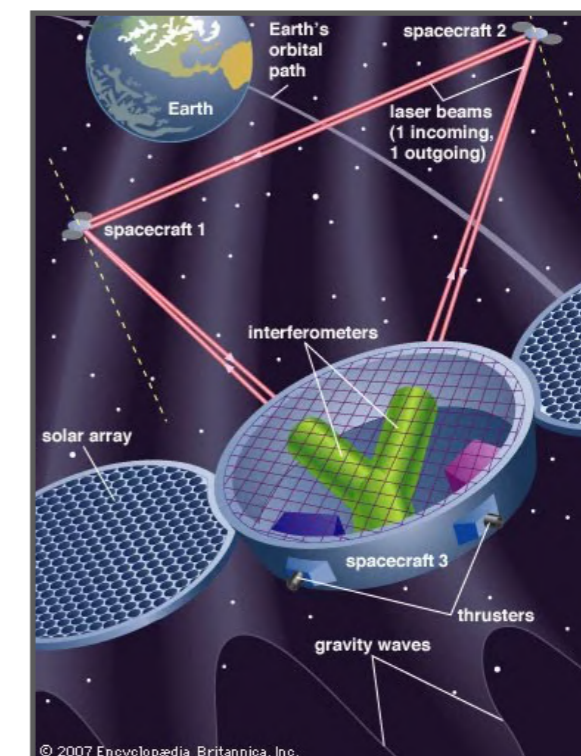
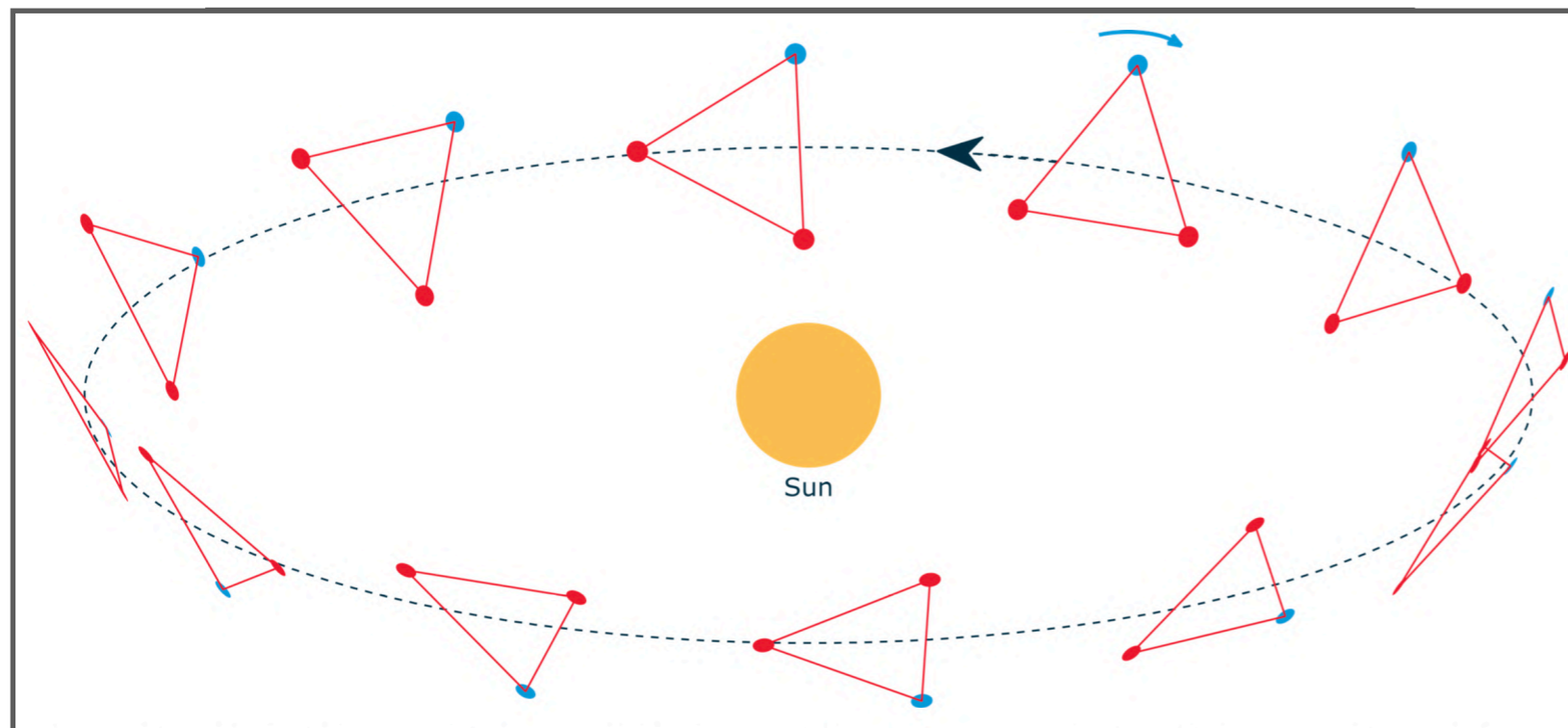
total energy density of the Universe



LISA (LASER INTERFEROMETER SPACE ANTENNA)

[LISA Mission L3 Proposal, https://www.elisascience.org/files/publications/LISA_L3_20170120.pdf] [Auclair et al. '22]

- Mission led by *ESA* and *NASA*
- Launch is planned *in the mid 2030's*
- *3 satellites* forming an equilateral triangle in an Earth-trailing orbit
- Distance between satellites = 2.5×10^6 km
- Nominal mission of *4.5 years*, with a duty cycle of *82%*



[LISA Red book] [<https://www.britannica.com/science/physics-science/The-study-of-gravitation>]



Introduction

*GWs from
sound-wave
sources*

*GWs from
free-streaming
sources*

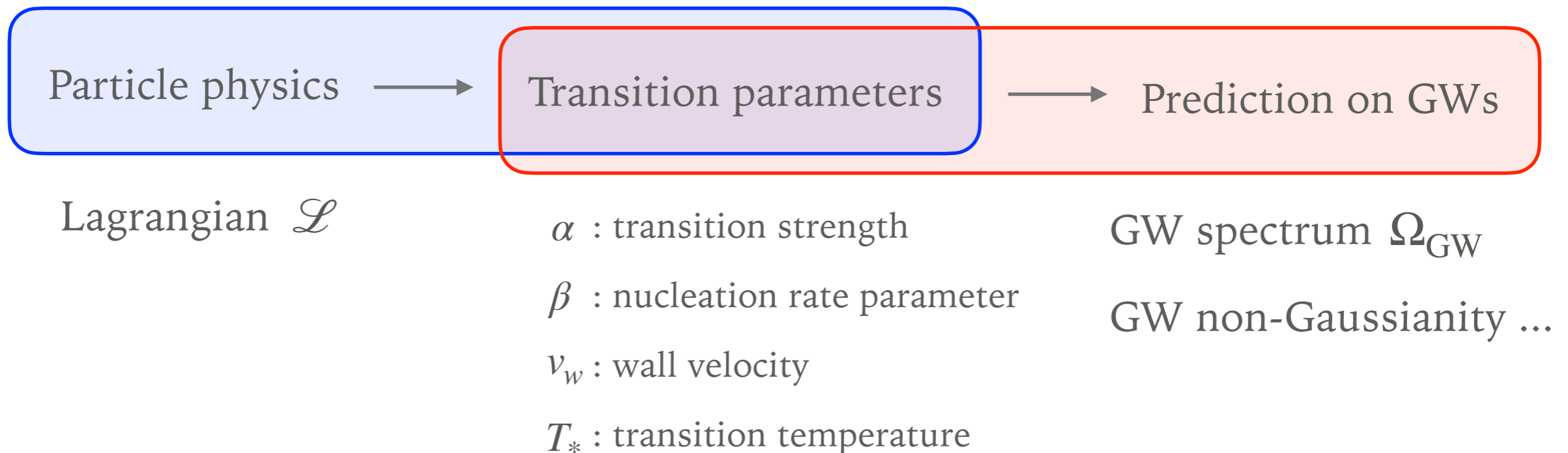
Summary

TRANSITION (\doteq THERMODYNAMIC) PARAMETERS

- Remind the spirit of thermodynamics
 - Only a few parameters determine macroscopic properties

TRANSITION (\doteq THERMODYNAMIC) PARAMETERS

- Remind the spirit of thermodynamics
 - Only a few parameters determine macroscopic properties
- What are parameters that describe the present macroscopic system?



TRANSITION (\doteq THERMODYNAMIC) PARAMETERS

see e.g. [Caprini et al. '16]

[Caprini et al. '20]

► Transition strength $\alpha \equiv \rho_{\text{vac}}/\rho_{\text{plasma}}$

- How much energy (= latent heat) is released in comparison to the plasma energy

- The numerator $\rho_{\text{vac}} = \rho_{\text{vac,false}} - \rho_{\text{vac,true}}$ is calculated from the Helmholtz

free energy, through the relation $U = F + TS = F - T \left(\frac{\partial F}{\partial T} \right)_V$ as

$$\rho_{\text{vac,true}} = V_{\text{eff}}(\phi_{\text{true}}, T) - T \left(\frac{\partial V_{\text{eff}}(\phi_{\text{true}}, T)}{\partial T} \right)$$

$$\rho_{\text{vac,false}} = V_{\text{eff}}(\phi_{\text{false}}, T) - T \left(\frac{\partial V_{\text{eff}}(\phi_{\text{false}}, T)}{\partial T} \right)$$

TRANSITION (\doteq THERMODYNAMIC) PARAMETERS

see e.g. [Caprini et al. '16]

[Caprini et al. '20]

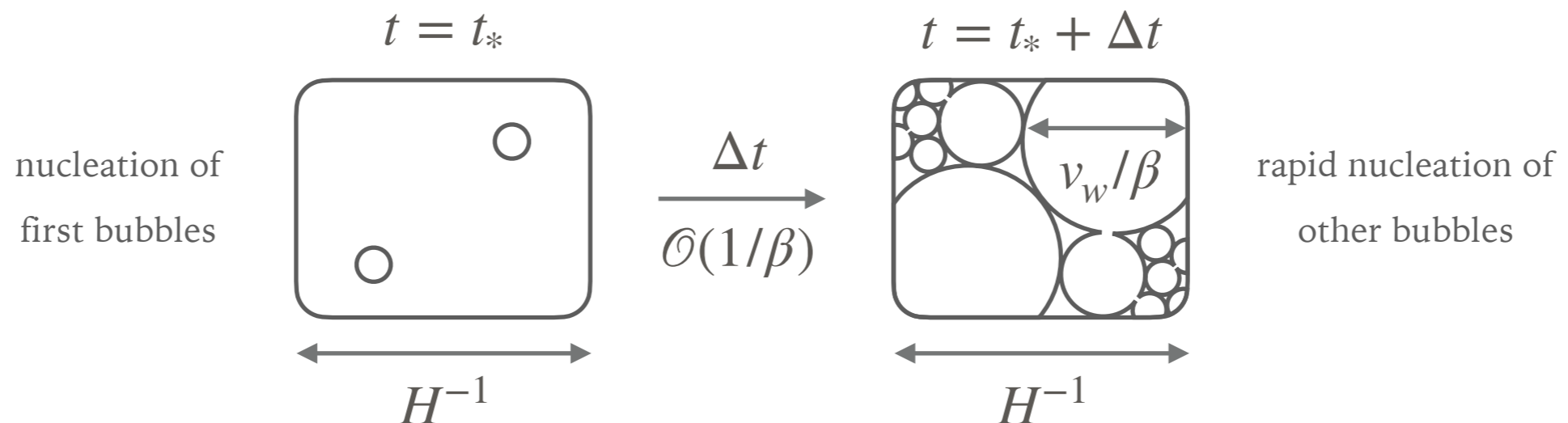
► Nucleation rate parameter β

- Taylor-expansion coefficient of the exponent of nucleation rate $\Gamma(t) \propto e^{\beta(t-t_*)+\dots}$

(per unit time & vol.) around the typical transition time $t = t_*$

- Thermal field theory is used to calculate $\Gamma(T)$, which is then converted into $\Gamma(t)$

- Its inverse (precisely, v_w/β) gives the typical bubble size at the time of collision



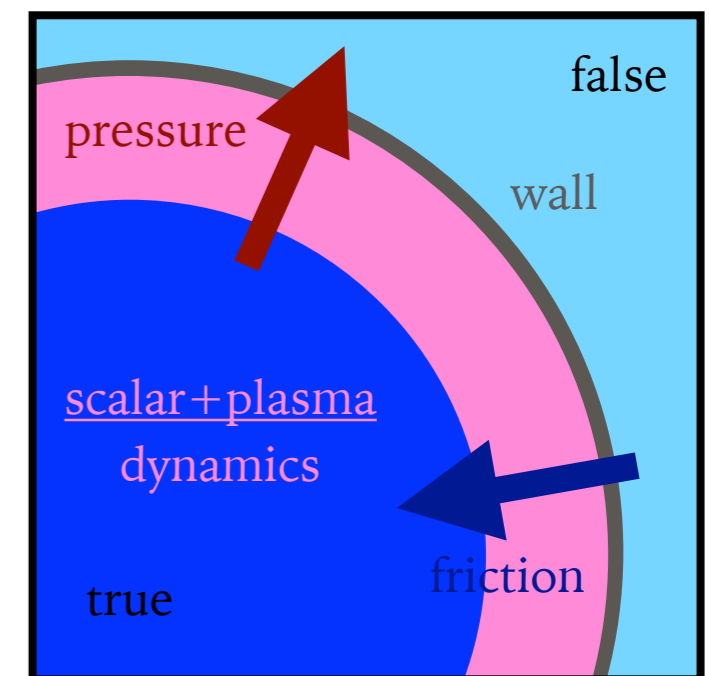
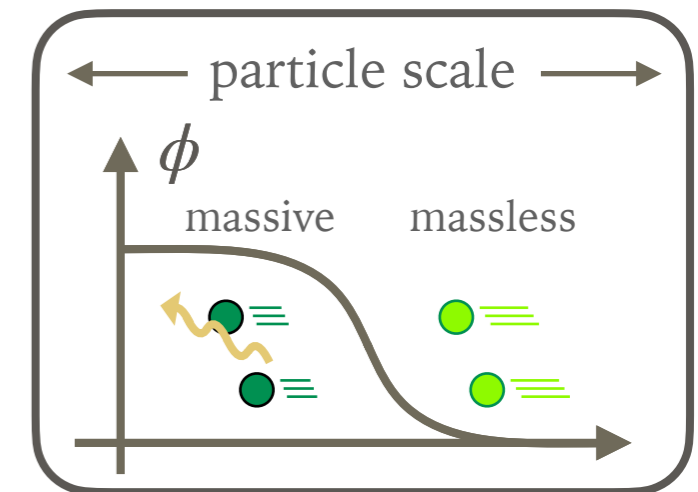
TRANSITION (\doteq THERMODYNAMIC) PARAMETERS

see e.g. [Caprini et al. '16]
[Caprini et al. '20]

[See Andrew's talk]

➤ Wall velocity v_w

- Determined from "pressure vs. friction"
- Should in principle be obtained from Boltzmann eq.,
but in reality often put by hand
(regarded as trade-off btwn. coupling \Leftrightarrow velocity)

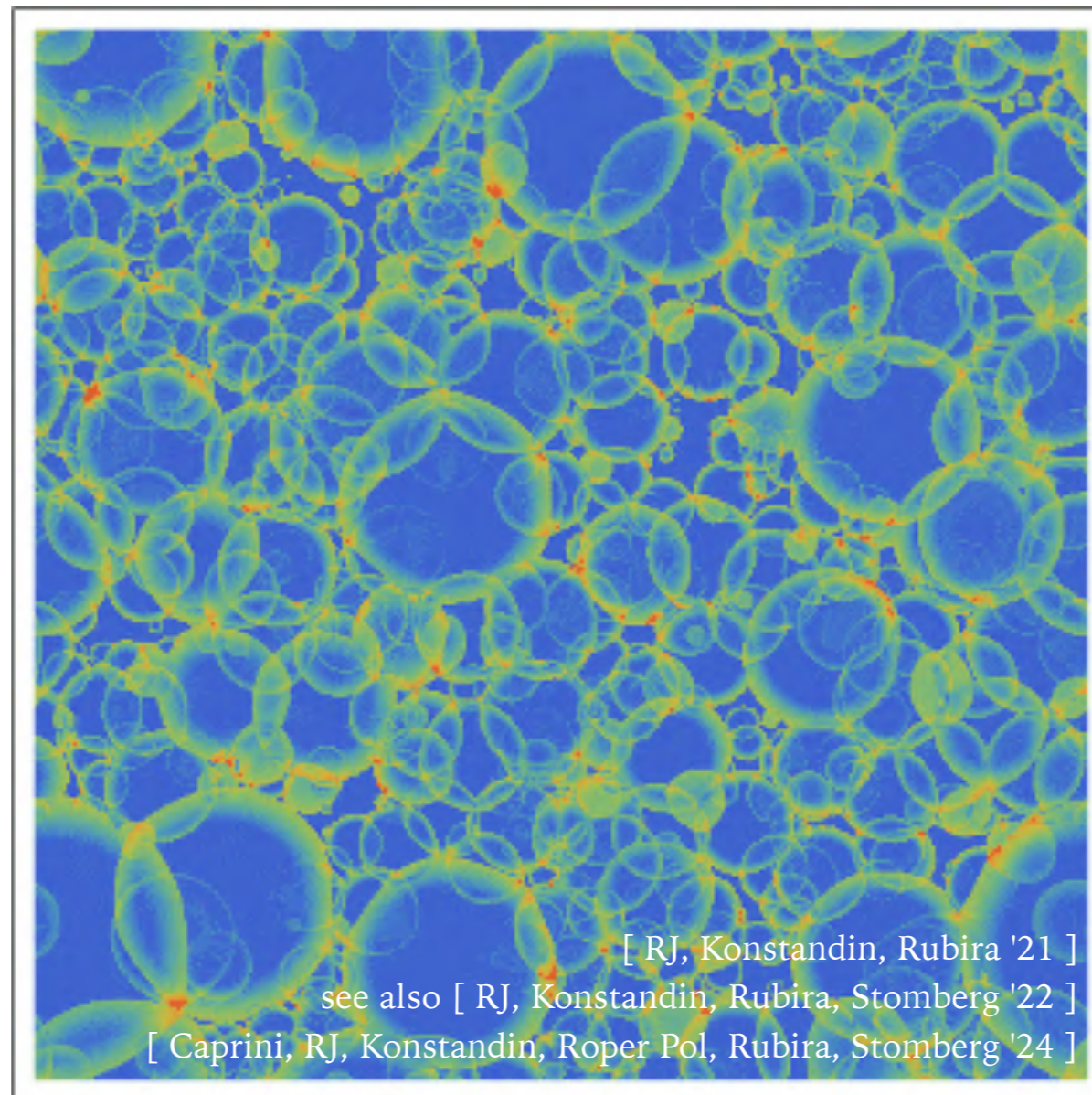


➤ Transition temperature T_*

- Determined from your microphysical theory

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► Bubbles collide, and fluid dynamics sets in (example for



GRAVITATIONAL WAVE SOURCES

[Kosowsky, Turner, Watkins '92]
[Kosowsky, Turner '92]
[Kamionkowski, Kosowsky, Turner '93]
and e.g. [Caprini et al. '16] [Caprini et al. '20]

► Bubble collision

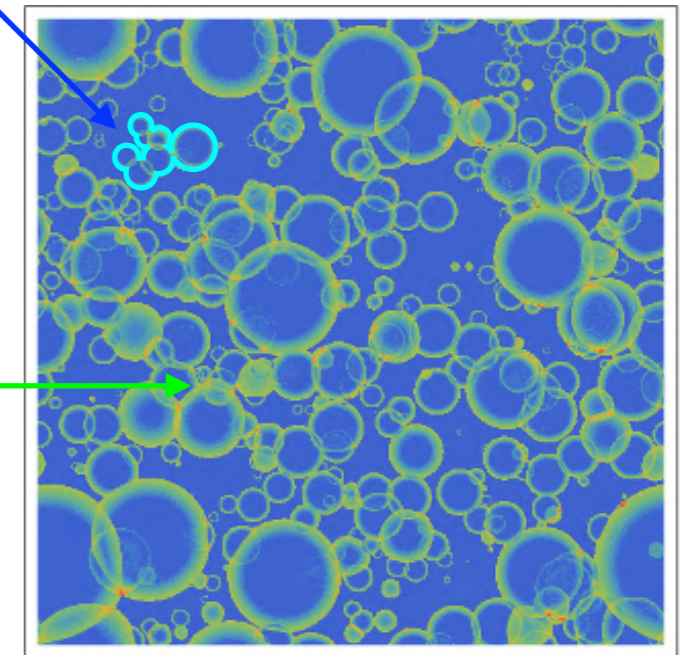
- Kinetic & gradient energy of the scalar field
(= order parameter field)
- Dominant when the transition is extremely strong
and the walls runaway

► Sound waves

- Compression mode of the fluid motion
- Dominant unless the transition is extremely strong

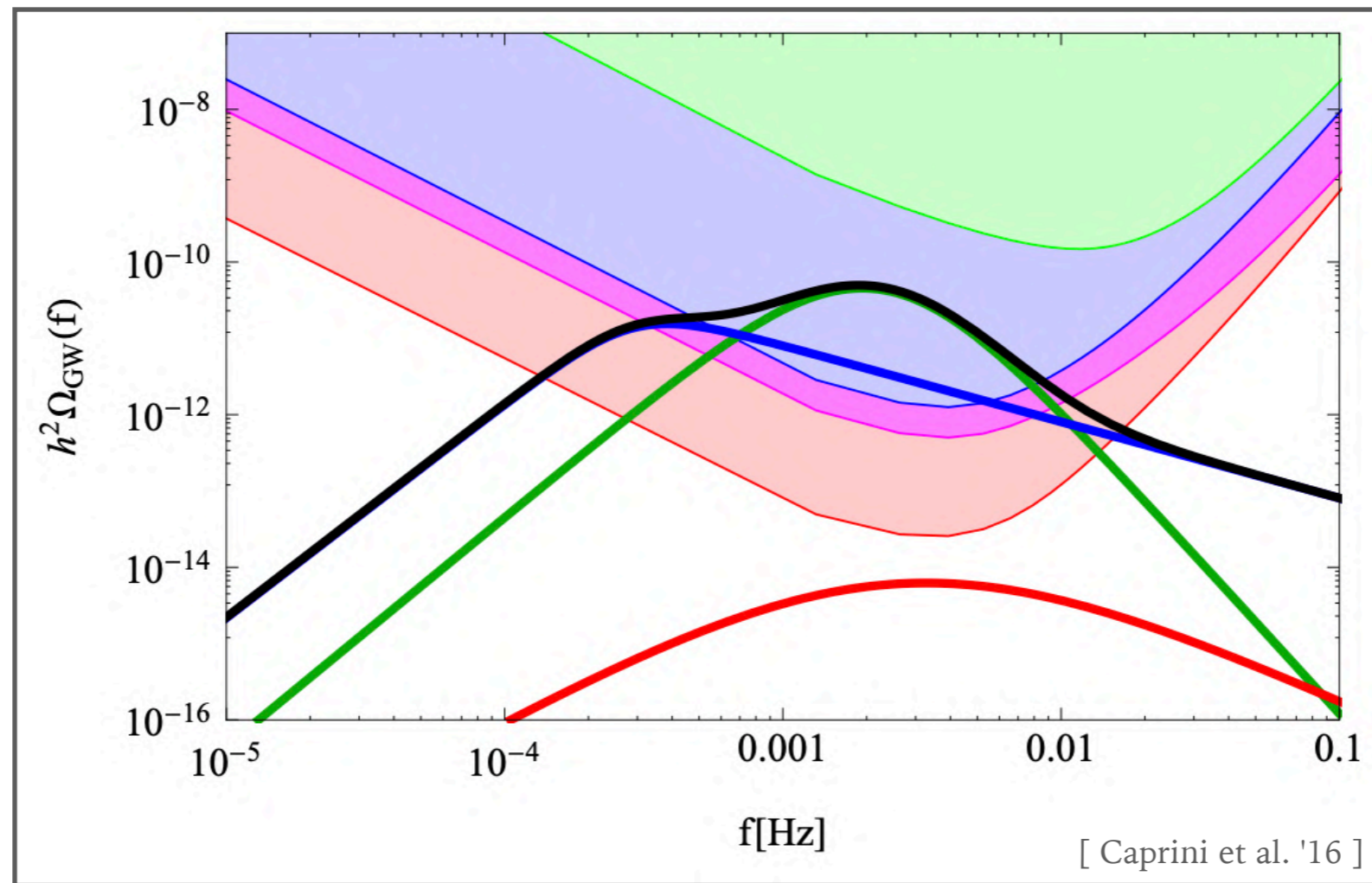
► Turbulence [See Alberto's talk]

- Turbulent motion caused by fluid nonlinearity
- Expected to develop at a later stage



important at later stage

GRAVITATIONAL WAVE SPECTRUM



ROUGH ESTIMATE ON GW PRODUCTION

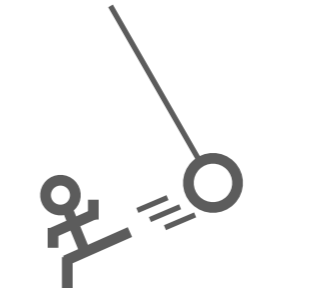
[See Subhendra's lecture]

► Big & relativistic objects radiate more GWs

- Integrate the GW equation of motion over the sourcing time Δt

$$\square h_{ij} \sim GT_{ij} \xrightarrow[\text{sourcing time } \Delta t]{\text{integration over}} \dot{h}_{ij} \sim GT_{ij}\Delta t$$

oscillator



kicked oscillator

The diagram shows a stick figure on the left kicking a circular oscillator on the right. A line connects the top of the oscillator to the $\dot{h}_{ij} \sim GT_{ij}\Delta t$ term in the equation above.

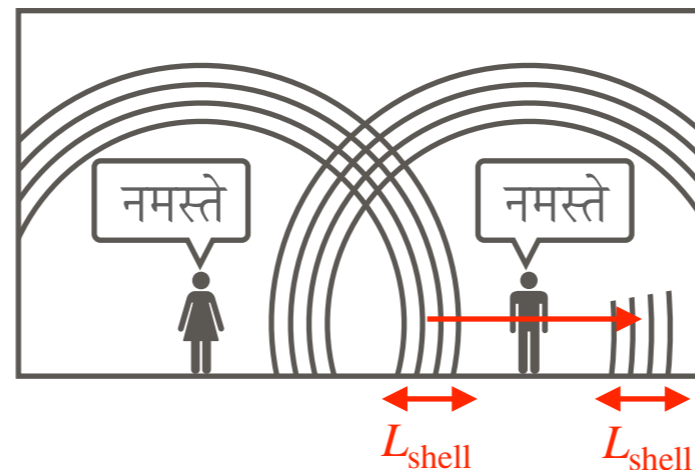
- GW energy density $\rho_{\text{GW}} \sim G^{-1} \dot{h}_{ij}^2 \propto T_{ij}^2 \Delta t^2$ Note but: GWs from sound waves behave differently

1. Relativistic objects have larger $T_{ij} \propto \alpha$

2. Big bubbles typically have longer sourcing time $\Delta t \propto \beta^{-1}$

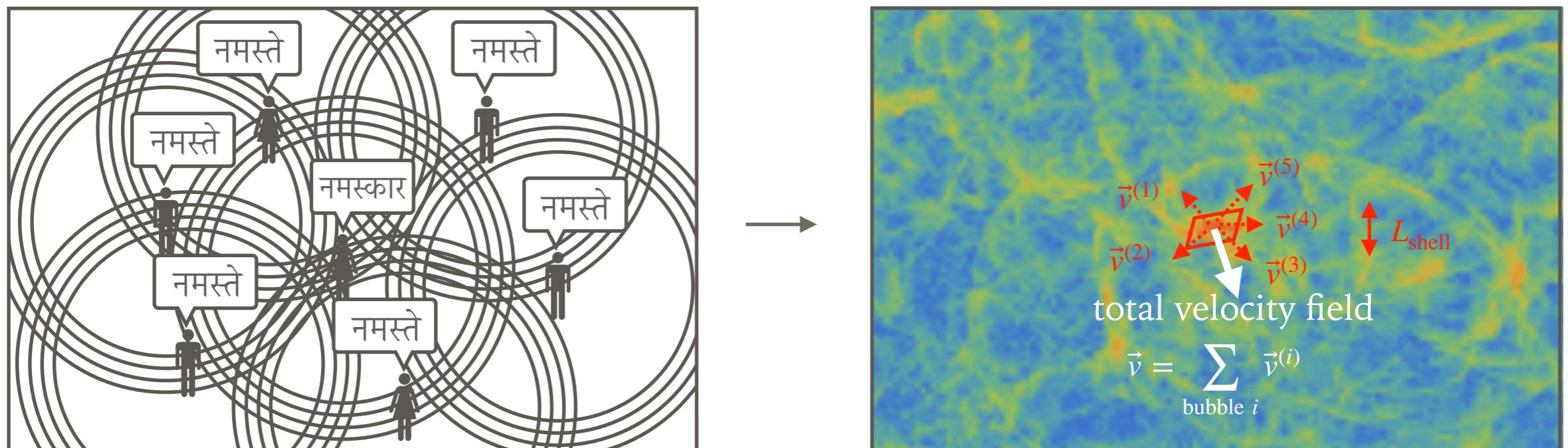
GRAVITATIONAL WAVES FROM SOUND WAVES

- ▶ Sound shells continue to propagate inside other bubbles



- ▶ Shell overlap creates random velocity fields, continuously sourcing GWs

[Hindmarsh, Huber, Rummukainen, Weir '14, '15, '17] [Hindmarsh '15, +Hijazi '19]



SOUND WAVE SIMULATIONS

➤ Fluid 3d simulation is a bit hard

- Shock waves

- Numerical viscosity

- Computational resources

→ currently 2 groups working on

sound wave & GW production simulations

➤ Our proposal: the Higgsless scheme [Thomas's talk]

[RJ, Konstandin, Rubira '21] [RJ, Konstandin, Rubira, Stomberg '22]

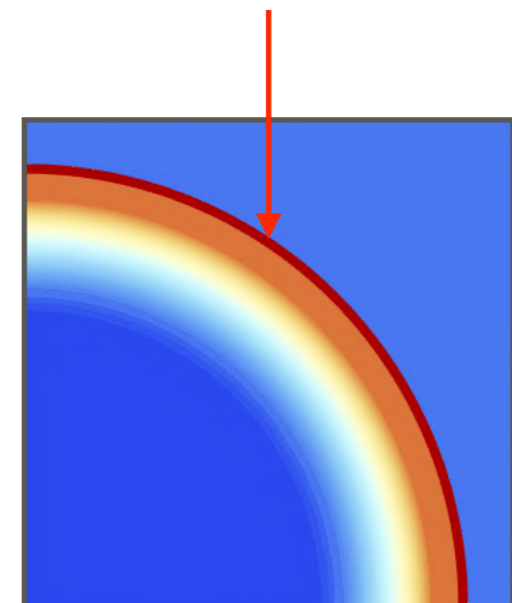
[Caprini, RJ, Konstandin, Roper Pol, Rubira, Stomberg '24]

- We do *not* solve both the scalar field and fluid

but rather "integrate out" the scalar field

(= treat the scalar field as non-dynamical boundary)

non-dynamical energy-injecting boundary for fluid



HOW TO "INTEGRATE OUT" THE HIGGS

► The fluid evolution is determined from

① Energy-momentum conservation of the fluid $\partial_\mu T^{\mu\nu} = 0$

② Energy injection at the wall, parametrized by $\epsilon_{\text{vac}} = \begin{cases} \epsilon_f & (\text{false vac.}) \\ \epsilon_t & (\text{true vac.}) \end{cases}$

► How to implement fluid evolution in simulations

① Assume relativistic perfect fluid $T^{\mu\nu} = (\epsilon + p)u^\mu u^\nu - g^{\mu\nu} p$

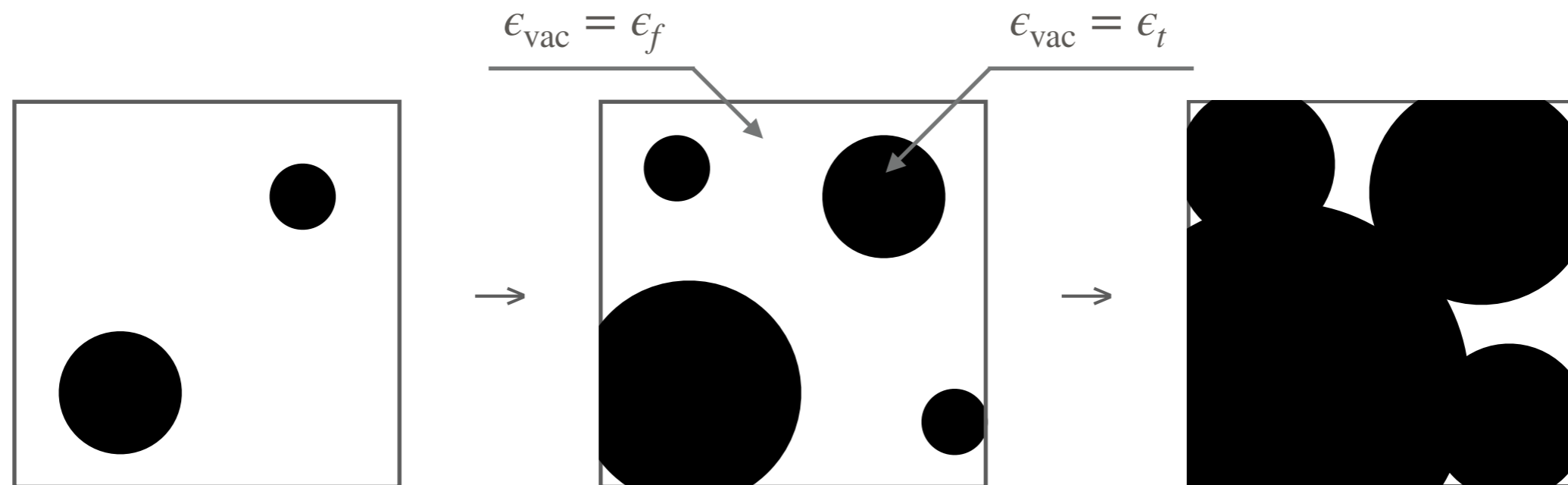
② Define $K^\mu \equiv T^{\mu 0}$, then $\partial_\mu T^{\mu\nu} = 0$ reduces to $\begin{cases} \partial_0 K^0 + \partial_i K^i = 0 \\ \partial_0 K^i + \partial_j T^{ij}(K^0, K^i) = 0 \end{cases}$

③ The effect of energy injection appears in $T^{ij}(K^0, K^i)$

$$T^{ij}(K^0, K^i) = \frac{3}{2} \frac{K^i K^j}{(K^0 - \epsilon_{\text{vac}}) + \sqrt{(K^0 - \epsilon_{\text{vac}})^2 - \frac{3}{4} K^i K^i}}$$

RECIPE FOR THE HIGGSLESS SIMULATION

- ▶ We first numerically generate nucleation points, and determine the false-true boundary of the bubbles

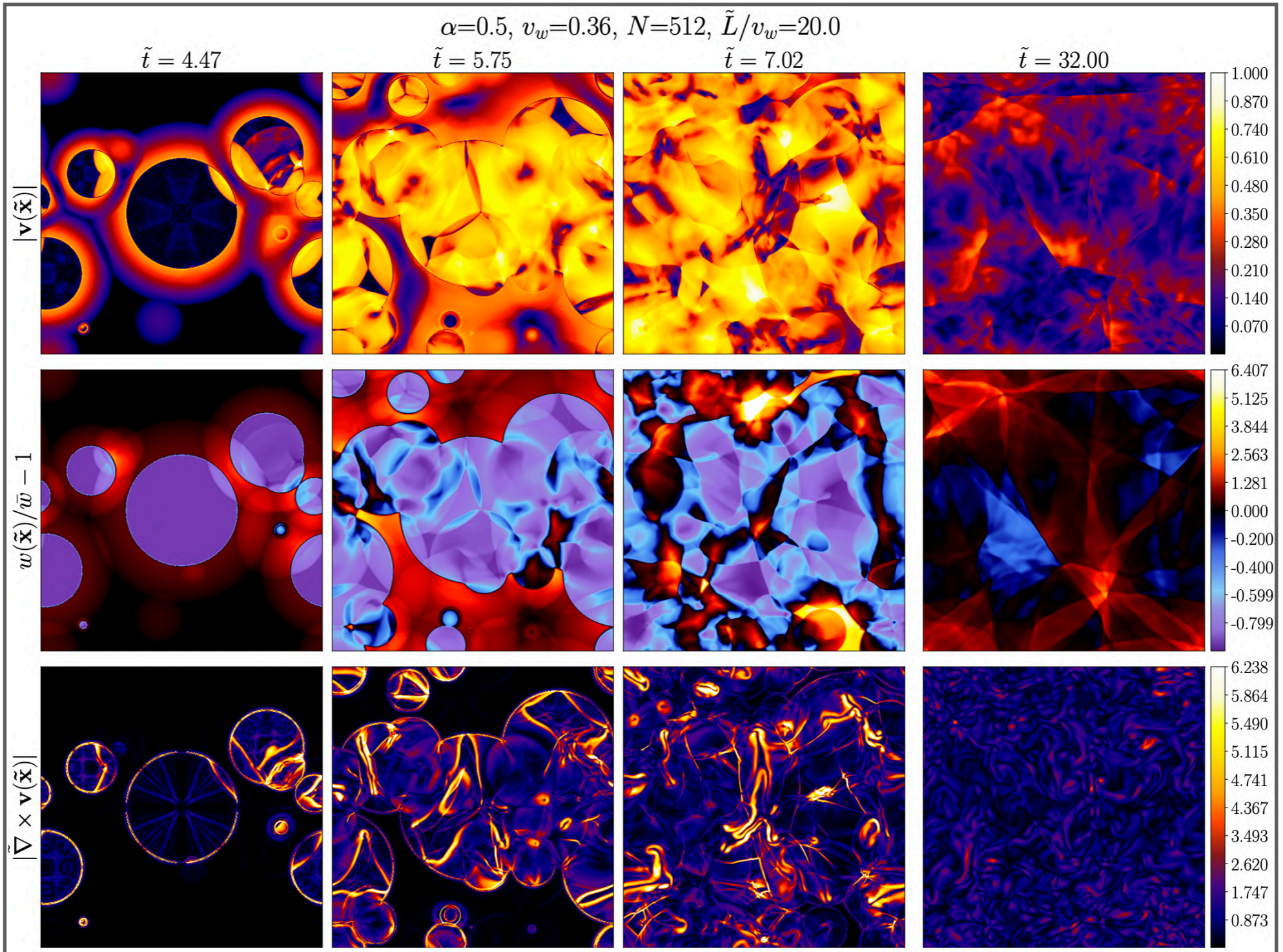


- ▶ We then evolve the fluid in this box according to
$$\begin{cases} \partial_0 K^0 + \partial_i K^i = 0 \\ \partial_0 K^i + \partial_j T^{ij}(K^0, K^i) = 0 \end{cases}$$

→ Fluid automatically develops profiles

RECIPE FOR THE HIGGSLESS SIMULATION

fluid velocity



enthalpy

vorticity

RECIPE FOR THE HIGGSLESS SIMULATION

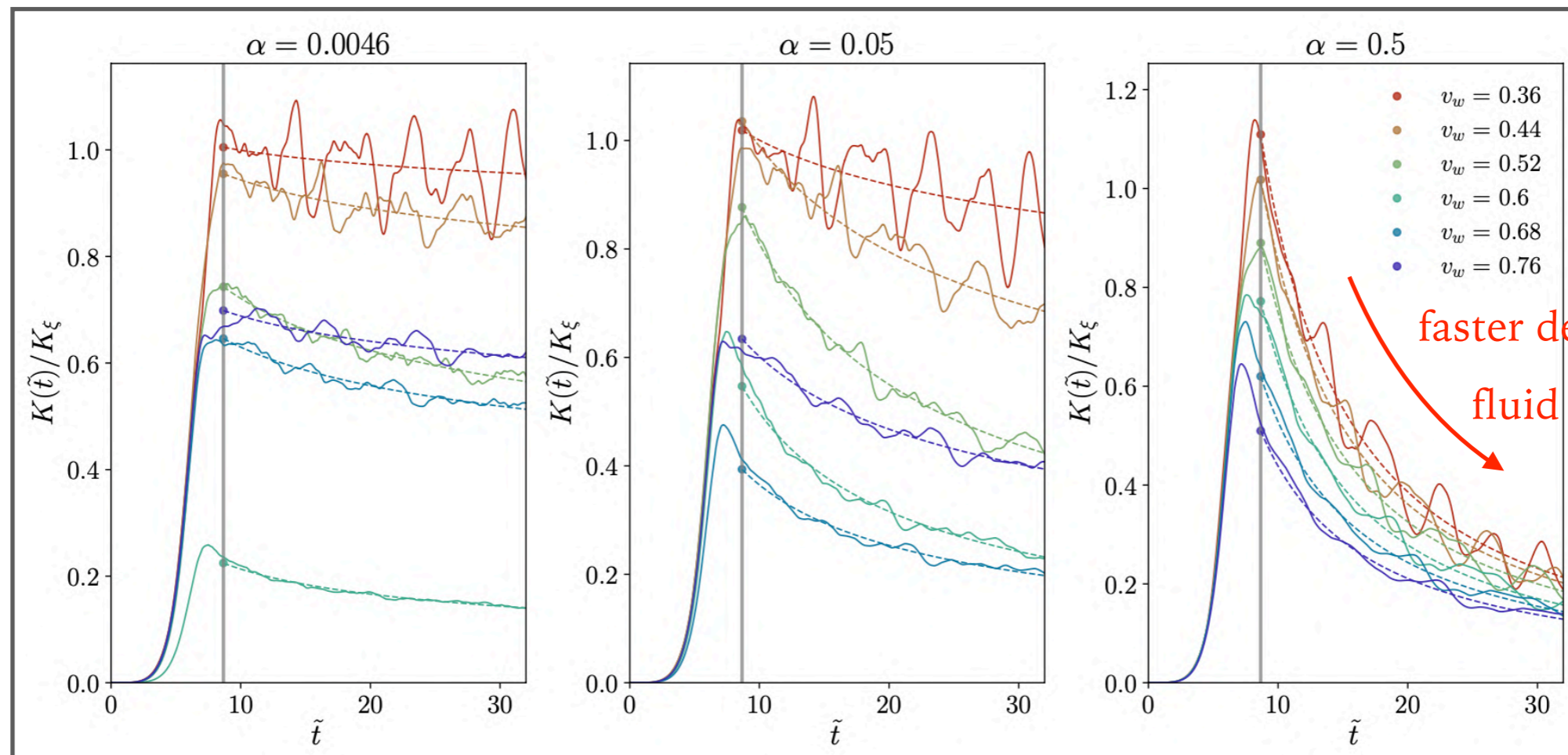
fluid kinetic energy



weak

intermediate

strong



time

SUMMARY (PART 1)

- The Higgsless simulation is now one of the largest simulations
(spatial resolution: $N^3 = 256^3$ or 512^3 grids; simulation time: $T = 32/\beta$)
- We are now able to simulate the strong transition regime $\alpha \sim 1$,
which was previously difficult due to shocks and numerical viscosities
- Numerical data suggest that we might be observing sound waves
developing into turbulence



Introduction

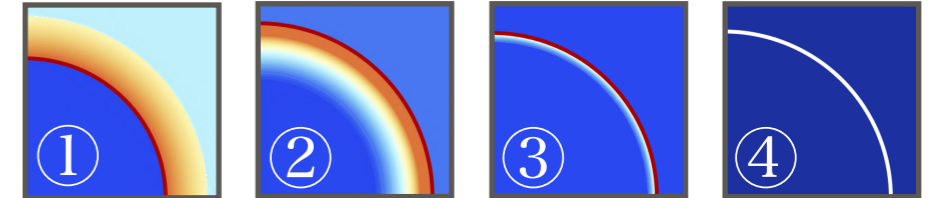
*GWs from
sound-wave
sources*

*GWs from
free-streaming
sources*

Summary

GW PRODUCTION: THE STANDARD LORE & BEYOND

➤ GW sources



Bubble walls (dominant in case ④)

Energy released accumulates in the walls (= scalar field kinetic & gradient).

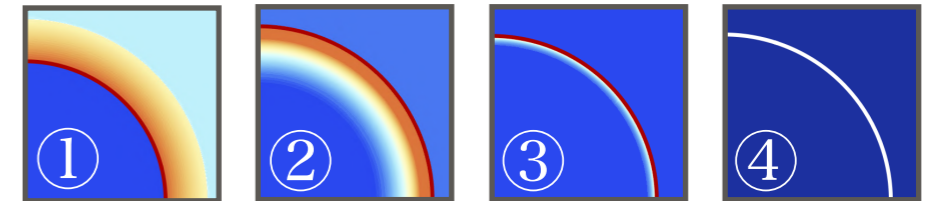
Fluid (dominant in case ①②③) = Sound waves & Turbulence

Particles in the broken phase frequently interact and can be described by fluid picture.

Aren't we missing one possibility?

GW PRODUCTION: THE STANDARD LORE & BEYOND

➤ GW sources



Bubble walls (dominant in case ④)

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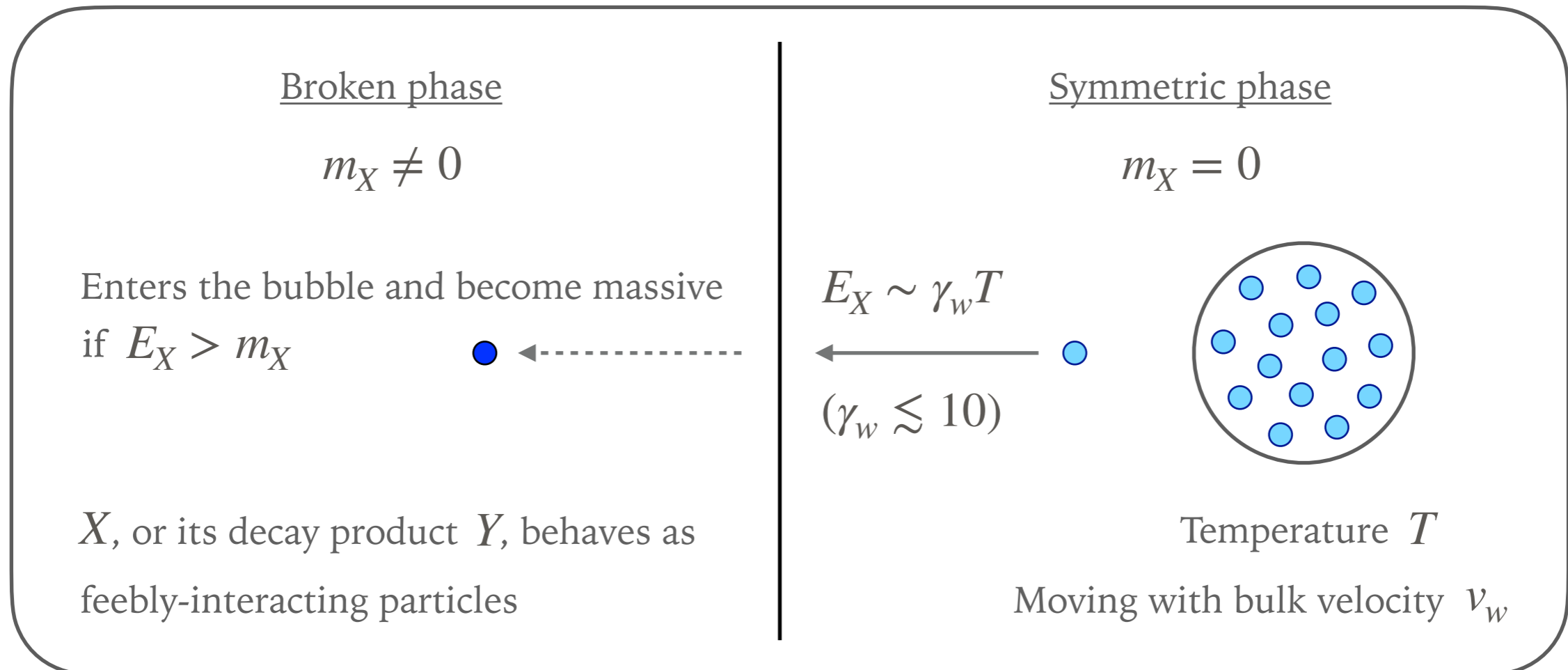
Feebly-interacting particles

Particles in the broken phase are only feebly interacting and free-stream.

GW PRODUCTION: THE STANDARD LORE & BEYOND

- ▶ Particle dynamics seen in the wall rest frame

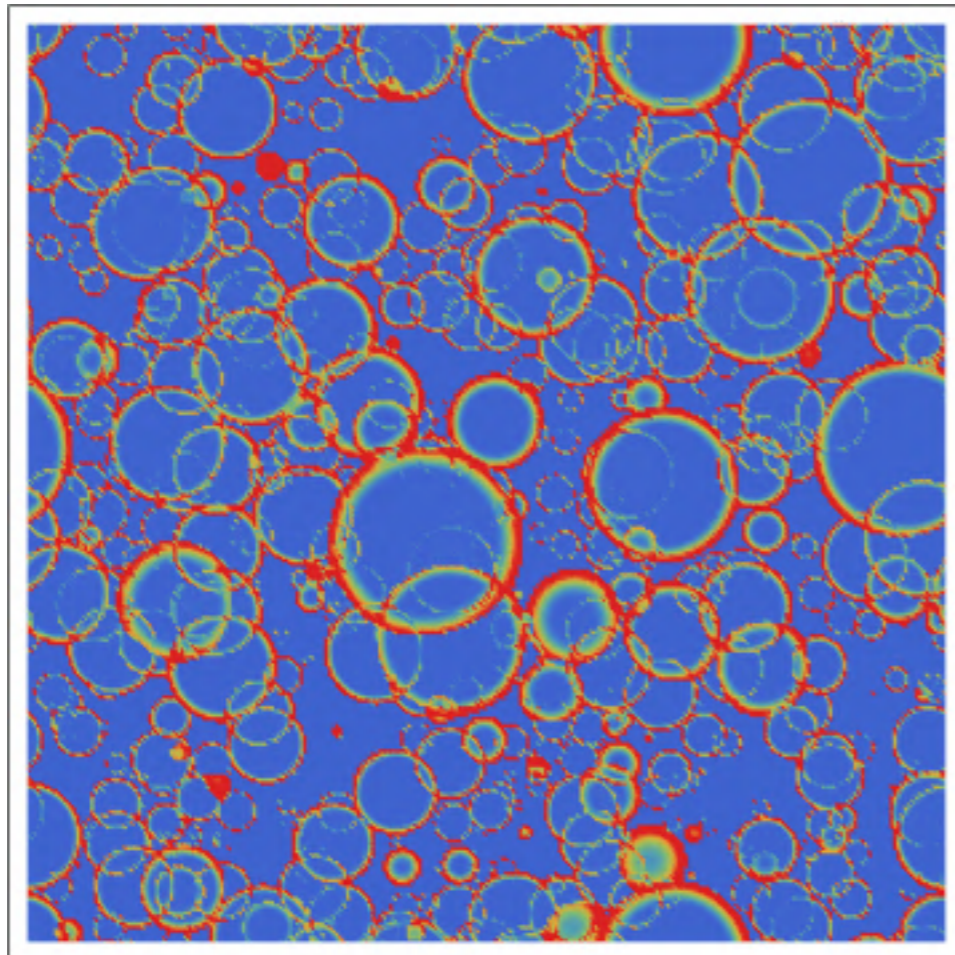
Bubble wall



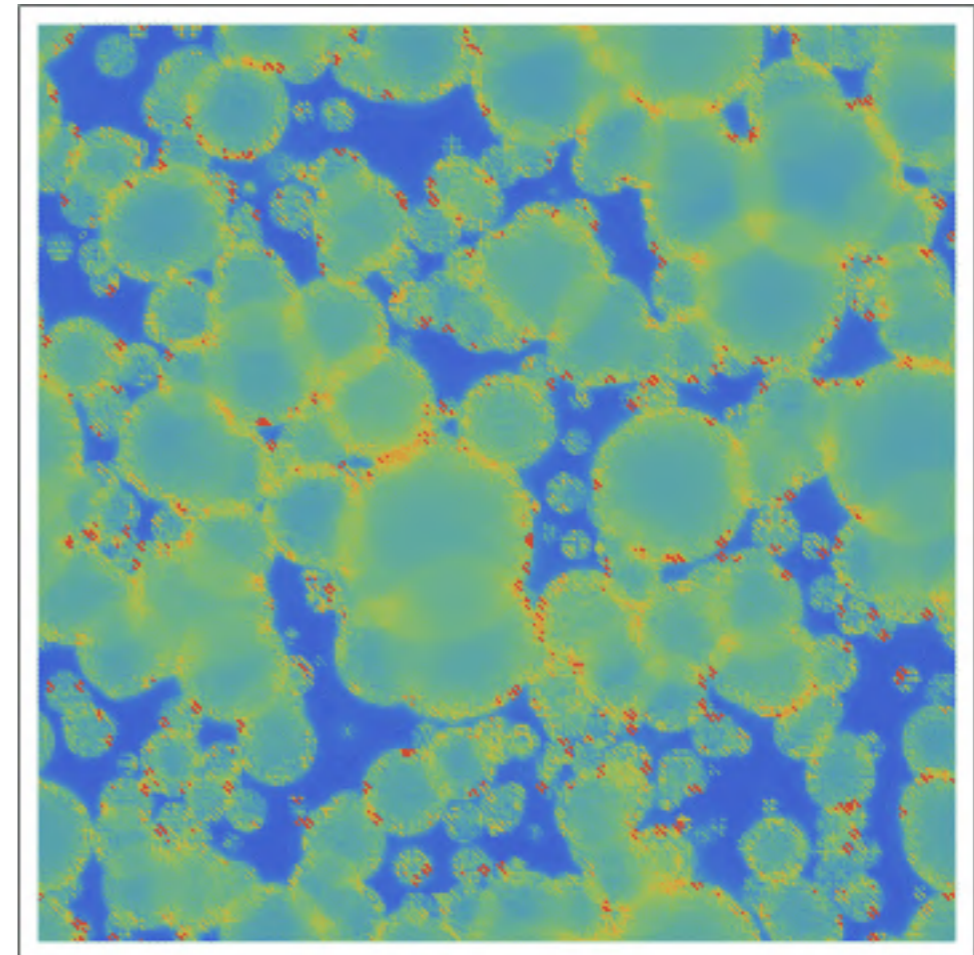
FLUID VS. FREE-STREAMING PARTICLES

- Evolution of the system for fluid and free-streaming sources

Fluid

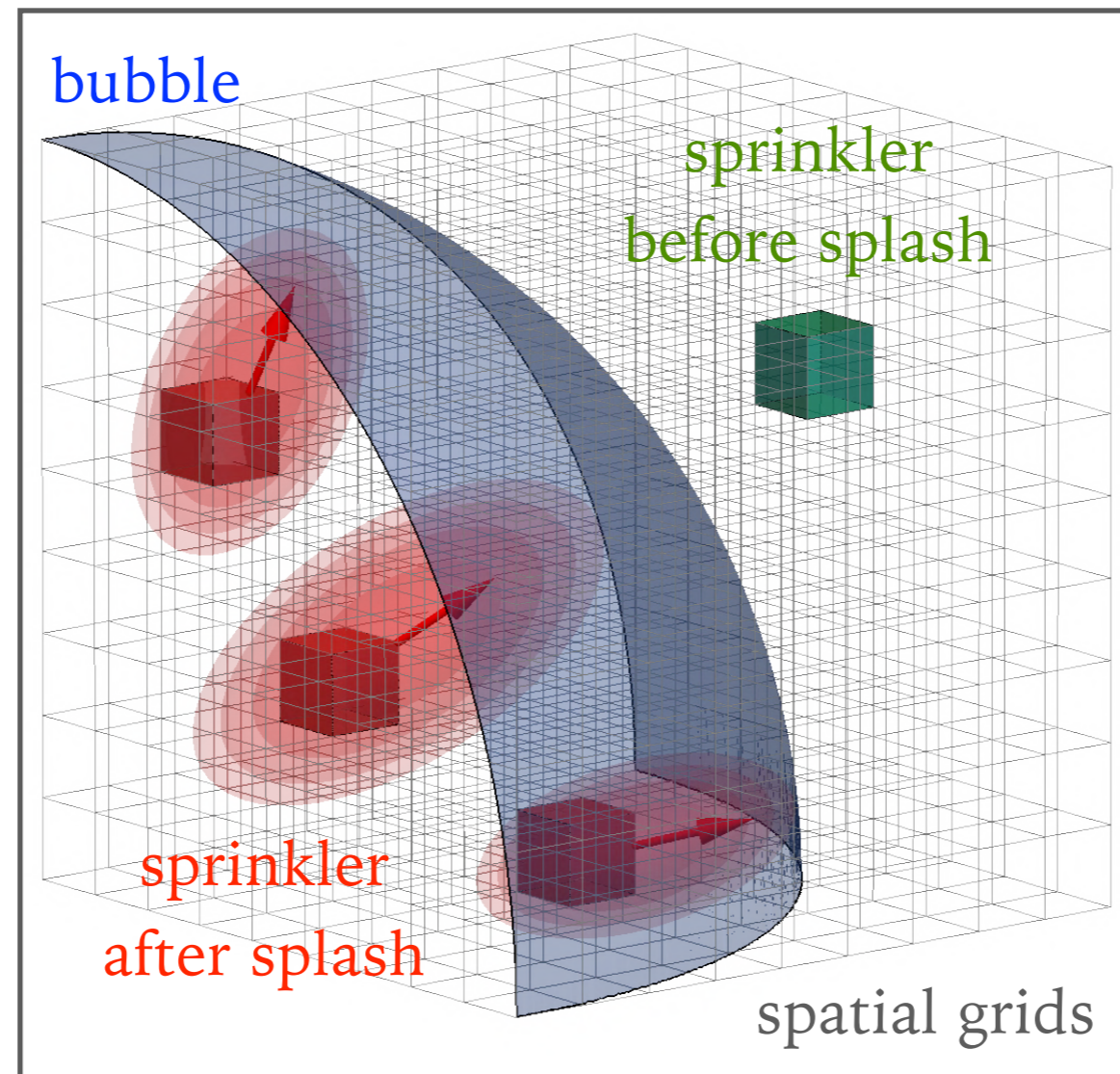


Free-streaming



HOW TO CALCULATE GW PRODUCTION

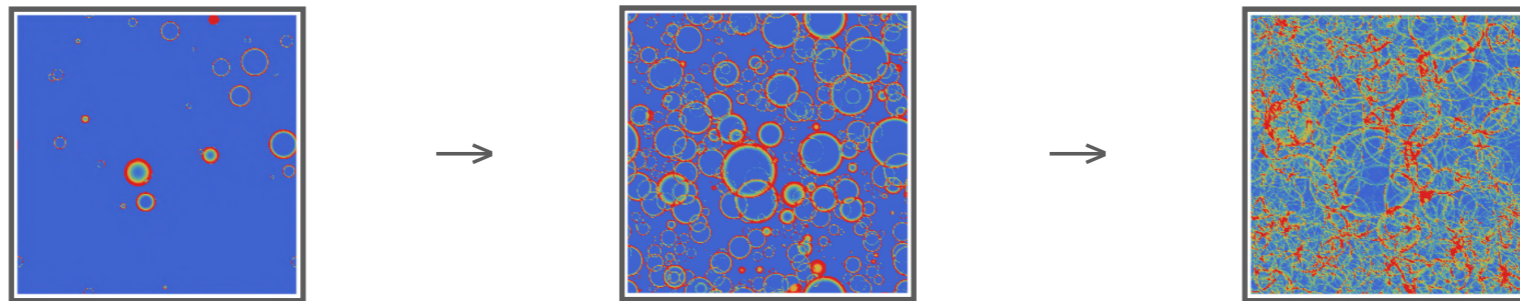
- To calculate the GW spectrum,
we propose a new calculation scheme – "sprinkler picture"



GW SPECTRUM FOR SOUND-WAVE SOURCE

➤ How to calculate the GW spectrum for sound waves

① Calculate the time evolution of the system without GWs



② Calculate GWs from $\square h_{ij} \sim G\Lambda_{ij,kl}T_{kl}$ using FFT

➤ Basically there is no shortcut, essentially because of nonlinearity:

Sound waves are linear phenomena $(\partial_t^2 - c_s^2 \nabla^2)\vec{v}_{\text{fluid}} \simeq 0,$

but GW production is nonlinear in \vec{v}_{fluid} because $\square h_{ij} \sim T_{ij} \sim (v_{\text{fluid}})_i (v_{\text{fluid}})_j$

GW SPECTRUM FOR FREE-STREAMING SOURCE

- However, for free-streaming particles, GW production is linear

in each free-streaming particle

$$\square h_{ij} \sim T_{ij} \sim \sum_{\text{particle } p} T_{ij}^{(p)}$$

- Thus we propose "sprinkler picture"

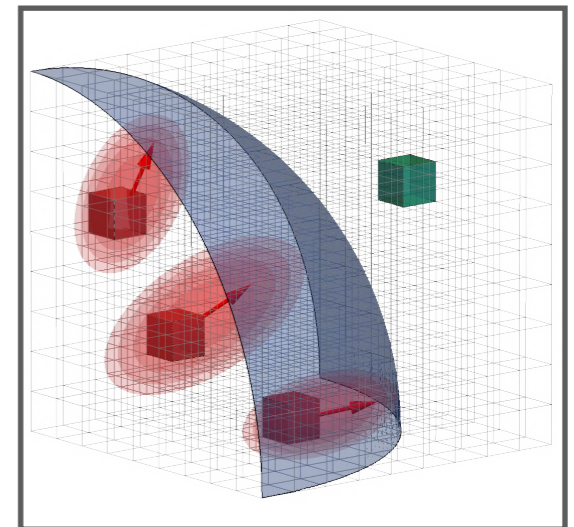
① Imagine **each grid point has a sprinkler** that splashes free-streaming particles when hit by the wall

② **Sprinklers are universal:**

their only difference is when and in which direction they are hit

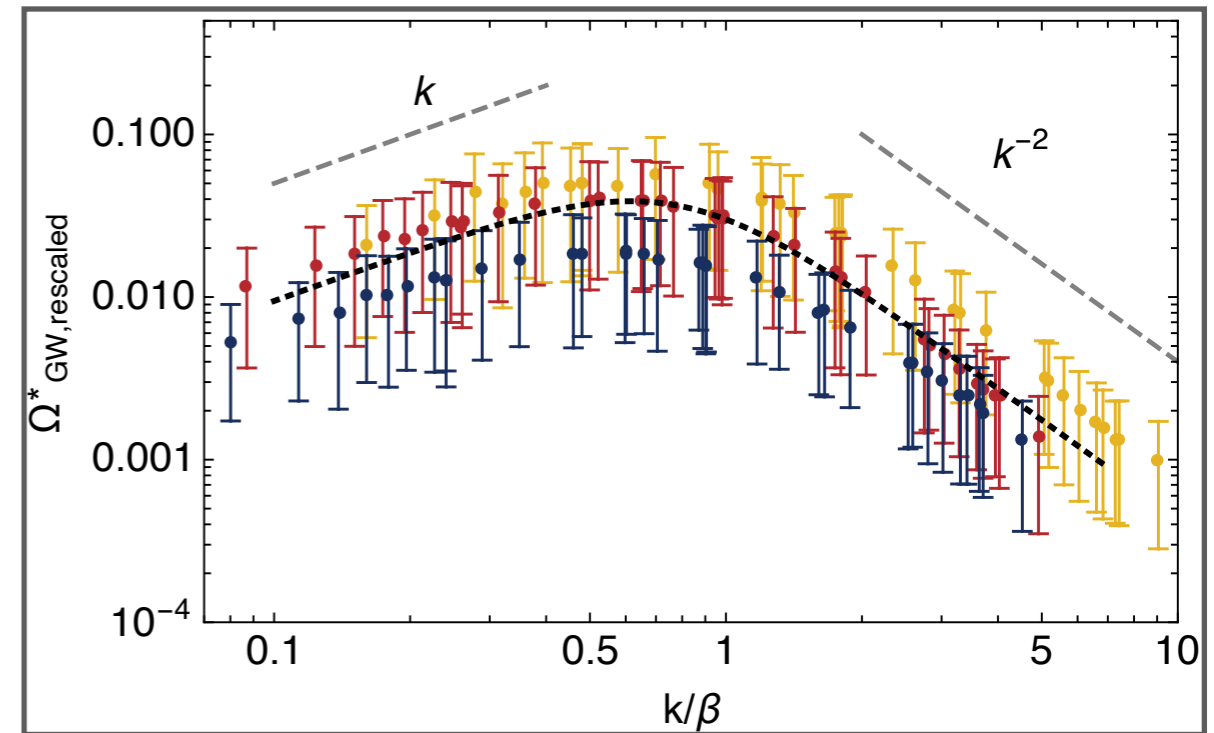
③ GW production from one sprinkler is easily calculable,

and **the contributions from different sprinklers (= grids) are linearly superposed**

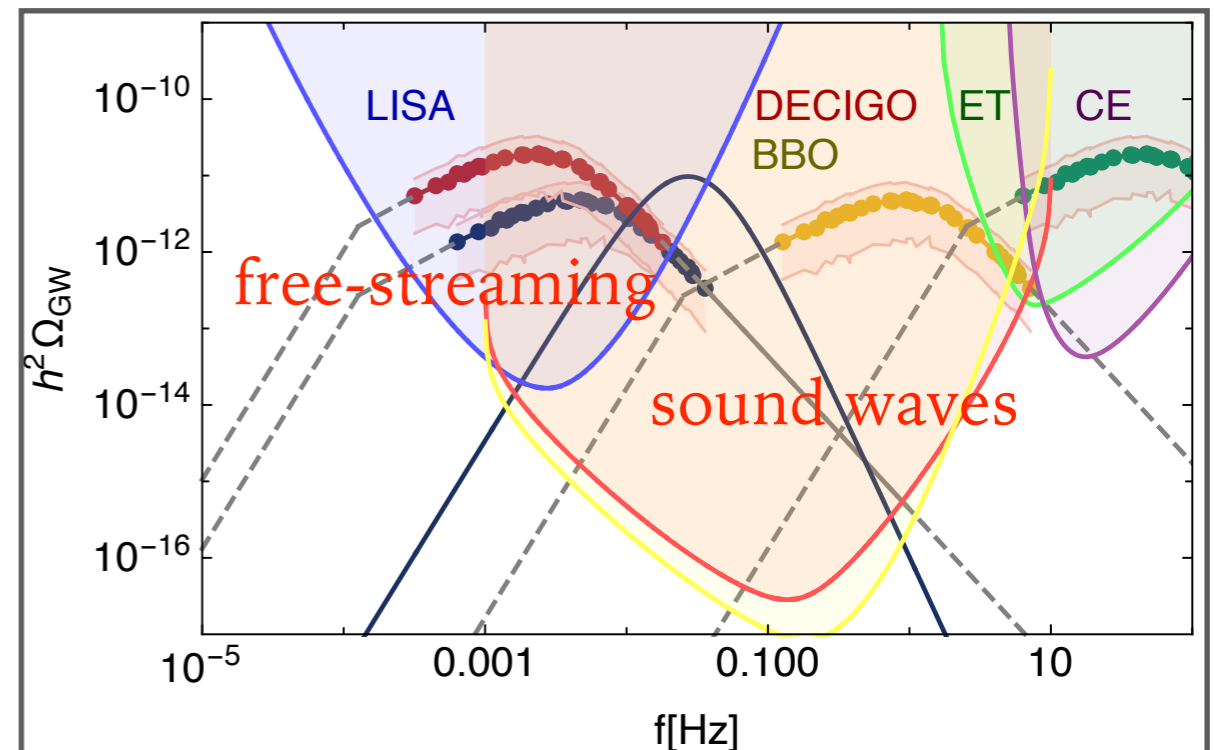


RESULT

- GW spectral shape is universal
(after normalizing by some factor)



- GW spectral shape is clearly different from sound-wave sources: it stretches over wider frequencies

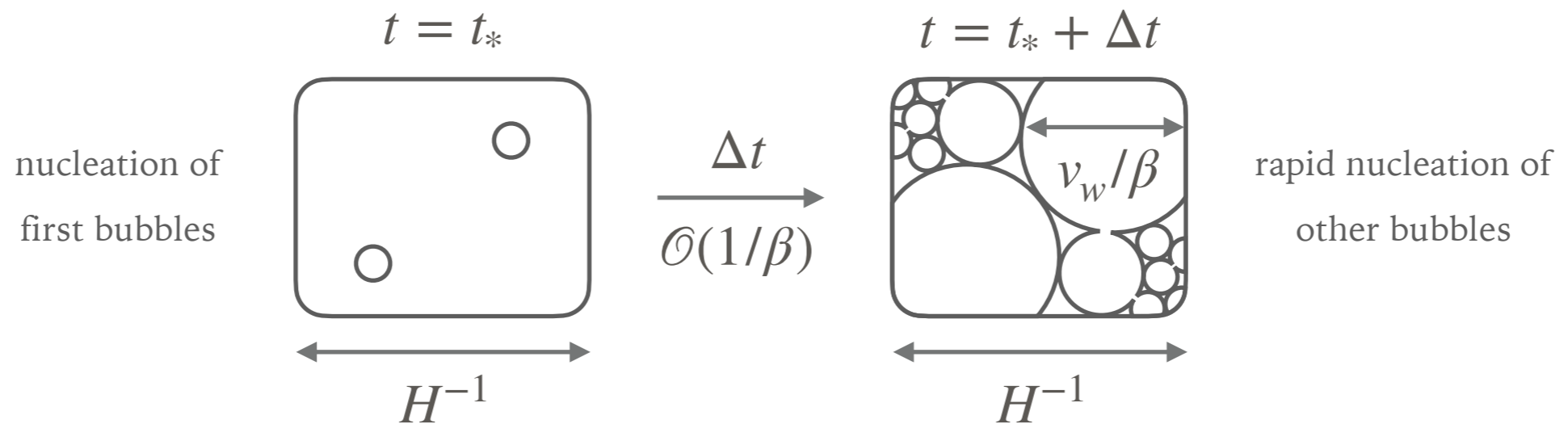


PARTICLE PHYSICS FRAMEWORK

- Consider a dark-sector thermal bath, with temperature T
- Assume a first-order phase transition in this sector
 - scalar field s acquires a vev $\langle s \rangle$
 - nucleation of bubbles (with wall thickness $\sim 1/\langle s \rangle$)
 - walls reach a terminal velocity v_w (or equivalently $\gamma_w = 1/\sqrt{1 - v_w^2}$)
- Feebly-interacting particles can be generated during this transition
 - particle X becomes massive at the phase transition, due to coupling to s

CONDITIONS ON FEEBLE INTERACTION

- Free-streaming particle should free-stream over a cosmological scale, which we take the transition timescale $\Delta t \sim \mathcal{O}(1/\beta)$

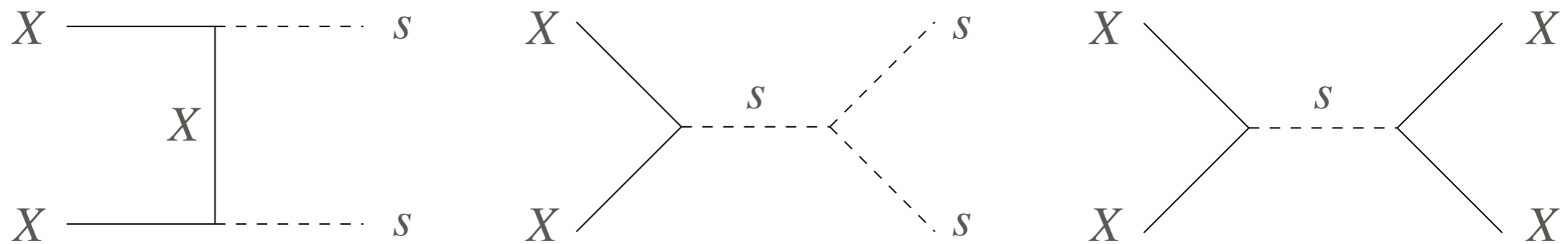


- So, we need the condition $n\sigma\Delta t \sim \frac{T^3\sigma}{\beta} \lesssim 1$

CONDITIONS ON FEEBLE INTERACTION

- How do X particles interact? $m_X = g'\langle s \rangle$

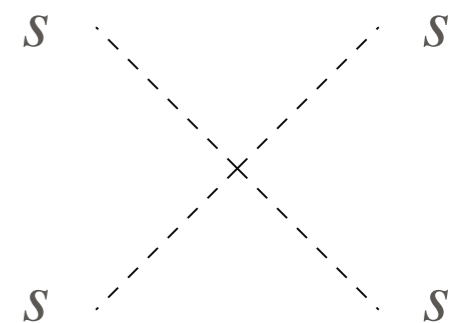
The couplings that gives rise to mass also give rise to interactions



- Can X be the scalar particle s itself?

s needs to gain large mass (for the s particles to be dominant),

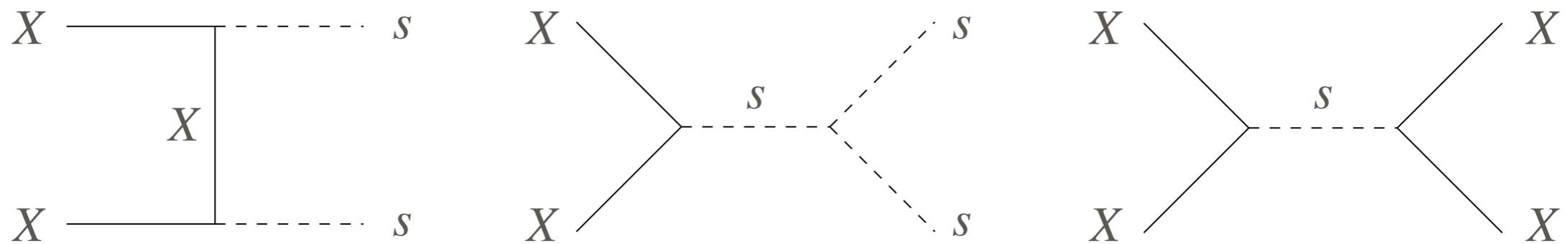
but this means a large quartic coupling among s particles



CONDITIONS ON FEEBLE INTERACTION

- How do X particles interact? $m_X = g'\langle s \rangle$

The couplings that gives rise to mass also give rise to interactions



- Can X be a gauge boson $X = Z'$?

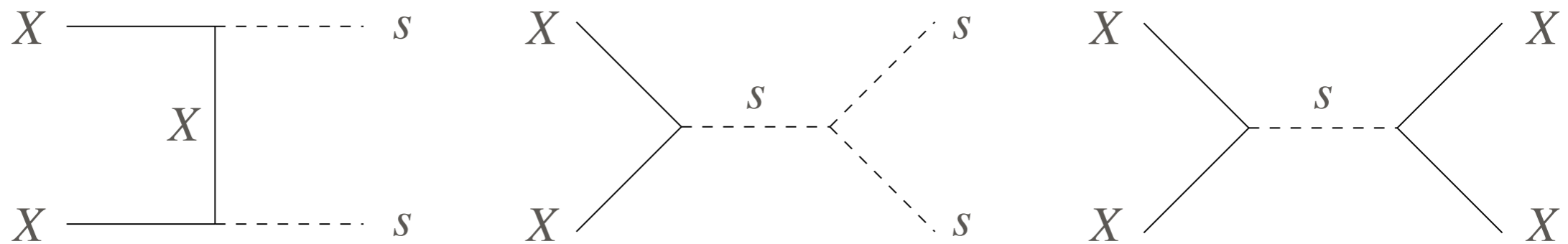
Assuming $m_s \sim \langle s \rangle$, feeble-interaction condition reduces to

$$n\sigma\Delta t \sim \frac{T^3\sigma}{\beta} \sim \frac{T^3}{\beta} \frac{g'^4}{(4\pi)^2} \frac{m_{Z'}^2}{m_s^4} \lesssim 1 \quad \longrightarrow \quad \frac{\langle s \rangle}{g'^3 T} > 10^6 \quad \text{for TeV transitions}$$

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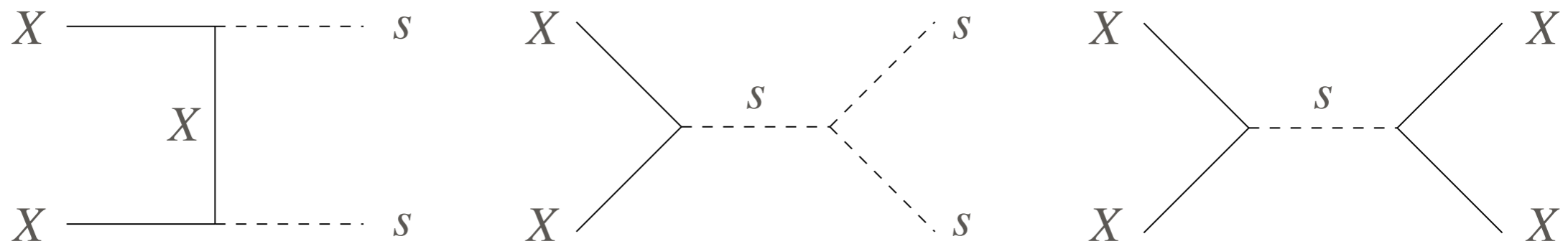
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Doable,
but not generic

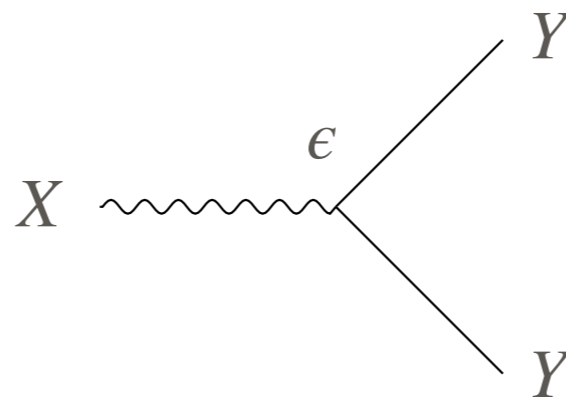
CONDITIONS ON FEEBLE INTERACTION

- How do X particles interact? $m_X = g'\langle s \rangle$

The couplings that gives rise to mass also give rise to interactions



- More viable possibility: particle decay $X = Z' \rightarrow YY$ with $\epsilon \ll 1$





Introduction

*GWs from
sound-wave
sources*

*GWs from
free-streaming
sources*

Summary

SUMMARY (PART 2)

- GW spectrum from free-streaming particles differ from that from sound waves, because of the (non-)linearity of the source
- GW spectrum, if observed, will provide us with the information on the nature of the source