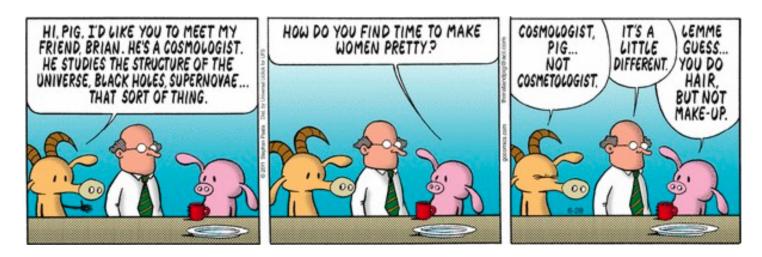
## Neutrinos in cosmology



Yvonne Y. Y. Wong, UNSW Sydney

Understanding the Universe through Neutrinos, ICTS-TIFR Bengaluru, April 22 – May 3, 2024

# Part 2: Neutrinos in inhomogeneous universe

- 1. Theory of inhomogeneities
- 2. Neutrinos and structure formation
- 3. Relativistic neutrino free-streaming and non-standard interactions

## 2. Neutrinos and structure formation...

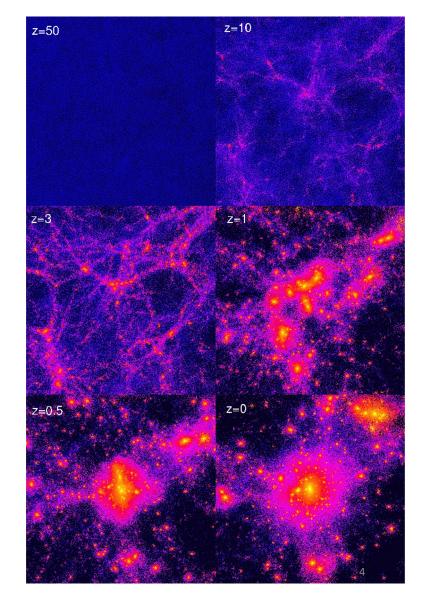


#### How structures form...

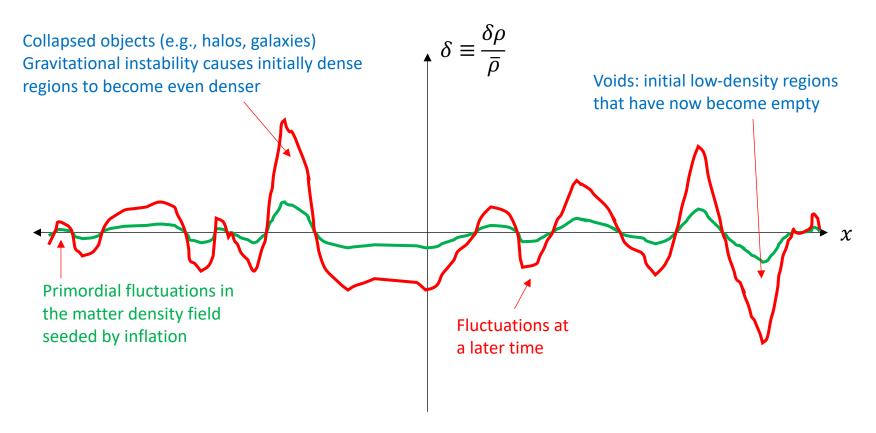
In the standard inflationary paradigm, the early universe is filled with an almost homogeneous matter density field with tiny random fluctuations:

Density contrast 
$$\longrightarrow$$
  $\delta \equiv \frac{\delta \rho}{\bar{\rho}}$  Mean density

 These fluctuations "grow" via gravitational instability and eventually collapse to form galaxies and clusters, etc.



#### How structures form...



#### Neutrino dark matter...

Standard hot big bang predicts a relic neutrino background with present-day properties:

• Temperature: 
$$T_{\nu,0} = \left(\frac{4}{11}\right)^{1/3} T_{\text{CMB},0} = 1.95 \text{ K} = 1.7 \times 10^{-4} \text{ eV}$$

• Number density per family: 
$$n_{\nu,0} = \frac{6}{4} \frac{\zeta(3)}{\pi^2} T_{\nu,0}^3 = 112 \text{ cm}^{-3}$$

• Total non-relativistic energy density: 
$$\Omega_{\nu,0} = \sum \frac{m_{\nu}}{94 \, h^2 \, \mathrm{eV}}$$

• Observations indicate are DM abundance of  $\Omega_{DM}\approx 0.25.$ 

Can standardmodel neutrinos be the dark matter?

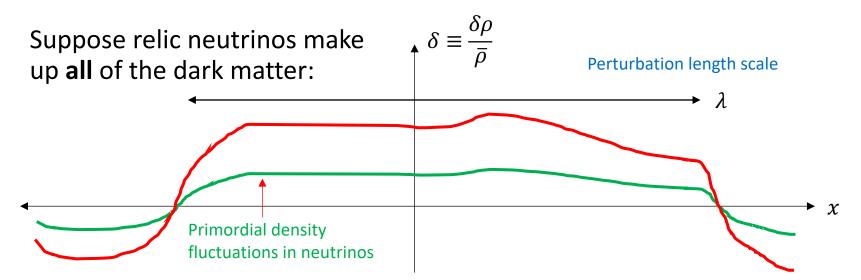
#### Neutrino dark matter...

Neutrinos cannot make up all of the dark matter.

- The **obvious reason**: a neutrino mass of  $\sim \! 10 \; {\rm eV}$  is required to give  $\Omega_{\nu,0} = \Omega_{\rm DM}$ , which is not allowed by the KATRIN limit  $m_e \lesssim 0.9 \; {\rm eV}$ .
- The **deeper reason**: the  $C\nu B$  has a lot of kinetic energy. The average speed of a NR relic neutrino is

$$v_{\nu} = \frac{p_{\nu}}{m_{\nu}} = \frac{3T_{\nu}}{m_{\nu}} \approx 150 (1 + z) \left(\frac{eV}{m_{\nu}}\right) \text{km s}^{-1}$$

- Typical velocity dispersions: galaxy cluster  $O(1000)~\rm km~s^{-1}$ , galaxy  $O(100)~\rm km~s^{-1}$ , dwarf galaxy  $< 100~\rm km~s^{-1}$ .
- An eV-mass relic neutrino has too much kinetic energy to have formed some of these objects.



- collapse time scale:  $\Delta t_{\rm collapse} \equiv (4\pi G \bar{\rho} a^2)^{-1/2}$  Instantaneous
- How long does it take an overdense region to collapse to a point

 Instantaneous escape time scale:

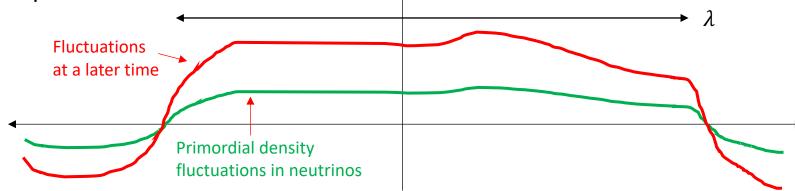
$$\Delta t_{
m escape} \equiv rac{\lambda}{v_{
u}}$$

How long does it take a neutrino to fly out of the region

Suppose relic neutrinos make up all of the dark matter:



Perturbation length scale



- collapse time scale:  $\Delta t_{\rm collapse} \equiv (4\pi G \bar{\rho} a^2)^{-1/2}$  Instantaneous
- Instantaneous escape time scale:

$$\Delta t_{
m escape} \equiv rac{\lambda}{v_{
u}}$$

#### **Limit 1: Growth**

Collapse happens **faster** than escape

$$\Delta t_{\rm collapse} \ll \Delta t_{\rm escape}$$

→ Perturbation grows.

Suppose relic neutrinos make Perturbation length scale up all of the dark matter: **Fluctuations** at a later time **Primordial density** fluctuations in neutrinos

collapse time scale:  $\Delta t_{\rm collapse} \equiv (4\pi G \bar{\rho} a^2)^{-1/2}$ Instantaneous

$$\Delta t_{\text{collapse}} \equiv (4\pi G \bar{\rho} a^2)^{-1/2}$$

 Instantaneous escape time scale:

$$\Delta t_{
m escape} \equiv rac{\lambda}{v_{
m v}}$$

#### Limit 2: Erasure

Collapse happens **slower** than escape

$$\Delta t_{\rm collapse} \gg \Delta t_{\rm escape}$$

→ Perturbation is erased.

**Growth or erasure**? Define the instantaneous free-streaming length  $\lambda_{FS}$  to be the scale at which  $\Delta t_{\rm collapse} = \Delta t_{\rm escape}$ , i.e.,

Using the NR speed from earlier and assuming matter domination 
$$\lambda_{\rm FS}(z) \equiv v_\nu \Delta t_{\rm collapse} \\ \approx 1.2~\Omega_{m,0}^{-1/2} (1+z)^{1/2} \left(\frac{\rm eV}{m_\nu}\right) \, h^{-1} {\rm Mpc}$$

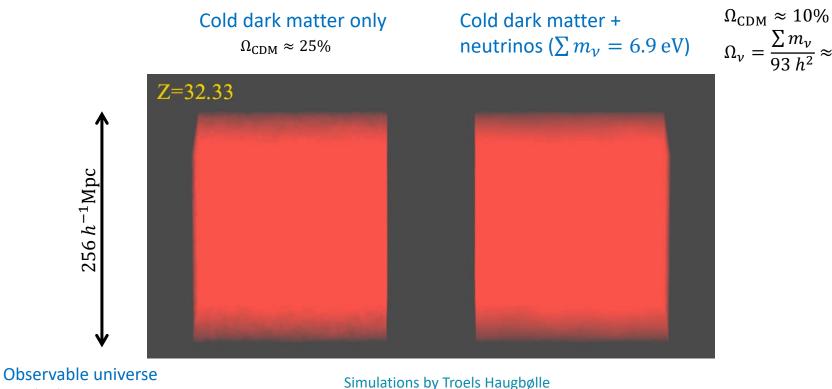
 $\rightarrow$  Unless density fluctuations are regenerated by other means, at any redshift z relic neutrinos **cannot form structures** of length scale  $\lambda < \lambda_{FS}(z)$ .

The **maximum instantaneous free-streaming length** is that at the time neutrinos just become non-relativistic:

$$\lambda_{\rm FS,max} \equiv \lambda_{\rm FS}(z_{
m nr}) \approx 55 \; \Omega_{m,0}^{-1/2} \left(\frac{{
m eV}}{m_{\nu}}\right)^{1/2} \; h^{-1} {
m Mpc} \qquad {{
m Using} \over 1 + z_{nr} pprox {m_{\nu} \over 3 \; T_{\nu,0}}}$$

- $\rightarrow \lambda_{FS,max}$  corresponds to the maximum size of objects that could not have been formed in a neutrino dark matter-only universe.
- $\rightarrow$  If a 10 eV-mass neutrino was the dark matter,  $\lambda_{FS,max} \sim 45$  Mpc, we would not have galaxies ( $\lambda \sim 10$  kpc) and galaxy clusters ( $\lambda \sim 1$  Mpc)

#### Neutrino masses & perturbation growth...



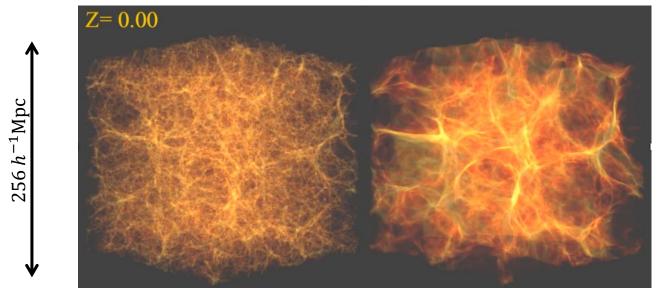
 $\sim 0(10) \rm{Gpc}$ 

#### Neutrino masses & perturbation growth...

Cold dark matter only  $\Omega_{\text{CDM}} \approx 25\%$ 

Cold dark matter + neutrinos ( $\sum m_{\nu} = 6.9 \text{ eV}$ )

 $\Omega_{\rm CDM} \approx 10\%$   $\Omega_{\nu} = \frac{\sum m_{\nu}}{93 h^2} \approx 15\%$ 



Observable universe  $\sim O(10) \text{Gpc}$ 

Simulations by Troels Haugbølle

#### Why study neutrino dark matter then?

Because the  $C\nu B$  is a prediction of standard cosmology.

- Neutrino oscillations provide a lower limit that at least one neutrino mass eigenstate has a mass > 0.05 eV.
- KATRIN (**tritium**  $\beta$ -decay) provides an upper limit on the effective  $\nu_e$  mass of < 0.9 eV.

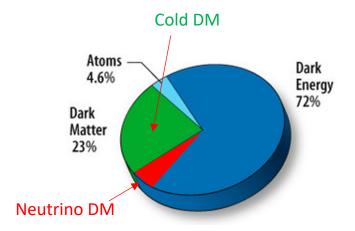
$$0.1\% < \Omega_{\nu,0} = \sum \frac{m_{\nu}}{94 \ h^2} < 6\%$$

- Although only a <u>subdominant DM</u> component, the free-streaming behaviour of neutrino DM still leaves an <u>imprint on large-scale structures</u>.
- $\rightarrow$  Can be used to establish  $\Omega_{\nu,0}$  and hence the neutrino mass.

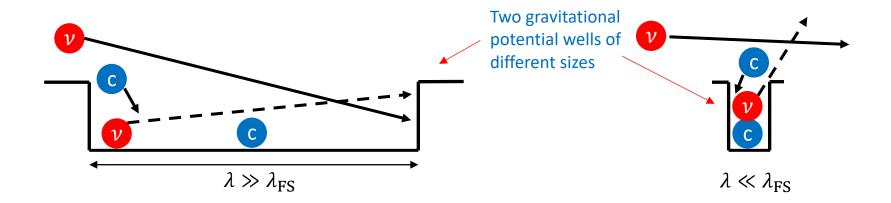
#### Subdominant neutrino DM...

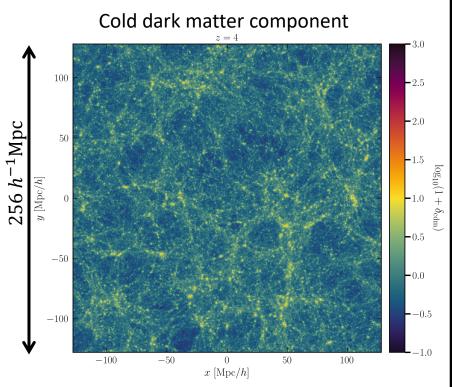
If neutrino DM is subdominant to CDM, the presence of CDM acts as a source of density perturbations.

- $\rightarrow$  Density fluctuations on length scales below the instantaneous freestreaming scale  $\lambda_{FS}$  are **not completely erased**.
- However, the neutrinos' kinetic energy still makes gravitational clustering very difficult.
- $\rightarrow$  Expect a suppression in the abundance of structures on scales below  $\lambda_{FS}$  through free-streaming-induced **potential decay**.



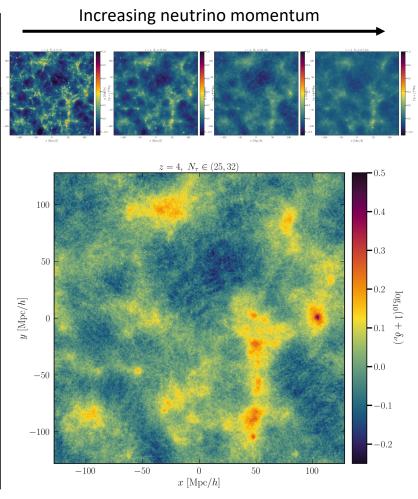
## Free-streaming-induced potential decay...





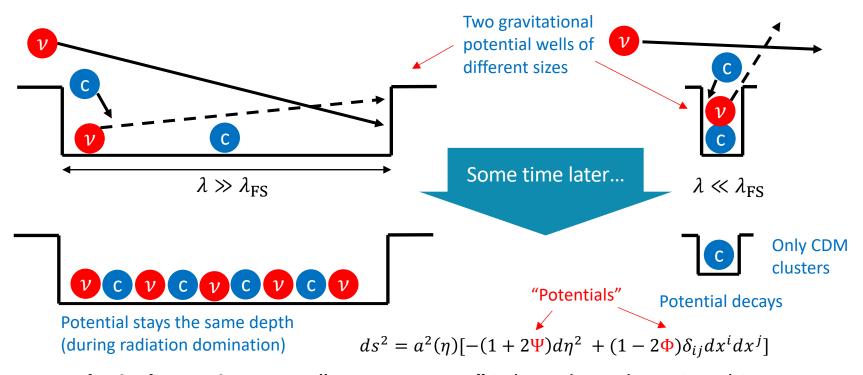
N-body code: Gadget-Hybrid:

Chen, Mosbech, Upadhye & Y<sup>3</sup>W 2023 Post-processing/graphics: G. Pierobon

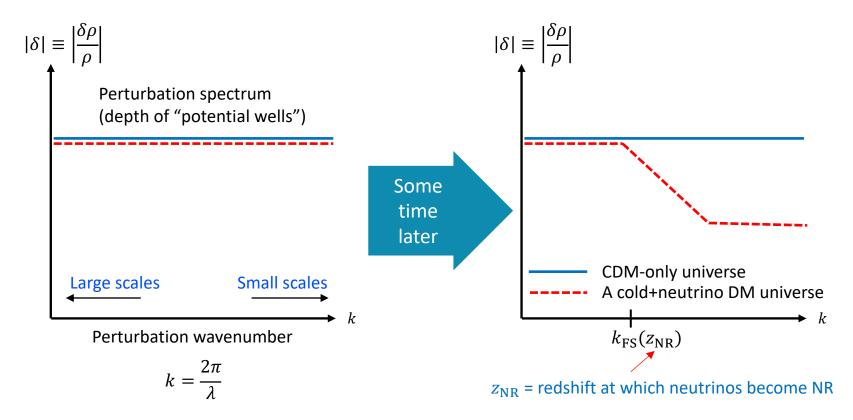


Neutrino component ( $\sum m_{\nu} = 0.5 \mathrm{eV}$ )

#### Free-streaming-induced potential decay...



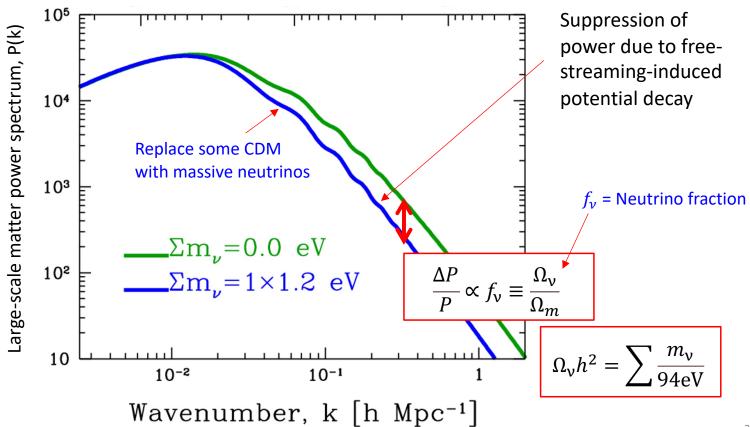
**Cosmological neutrino mass "measurement"** is based on observing this potential decay at  $\lambda \ll \lambda_{FS}$ .



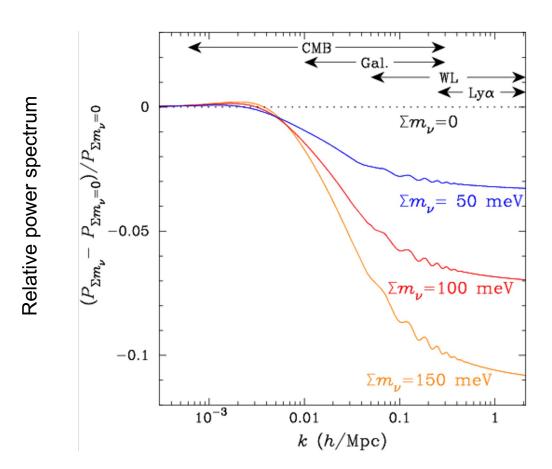
The presence of neutrino dark matter induces a step-like feature in the spectrum of gravitational potential wells.

### Large-scale matter power spectrum...

From linear perturbation theory



#### Large-scale matter power spectrum...



The larger the mass sum, the larger the suppression.

#### Who can measure it?

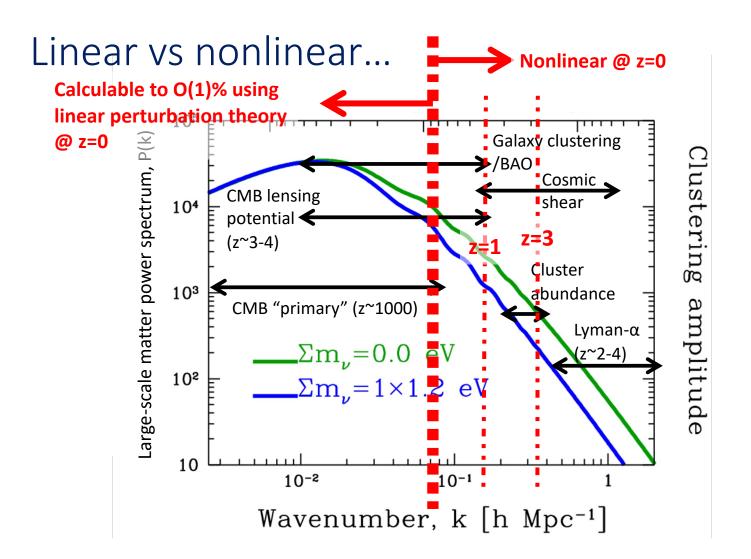
 $10^{5}$ 

density power spectrum, P(k) Galaxy clustering Clustering ►/BAO Cosmic . CMB lensing shear 104 potential <  $(z^{2}-4)$ "Anchor" Cluster ACDM model  $10^{3}$ abundance  $\sigma_8$ ,  $\Omega_m$ parameters CMB "primary" (z~1000) amplitude Large-scale matter  $\omega_m, \omega_b, n_s,$ Lyman-α  $A_s$ ,  $\tau$ , h $\Sigma m_{\nu} = 0.0 \text{ eV}$ z~2-4) 10<sup>2</sup> Small-scale  $\Sigma m_{\nu} = 1 \times 1.2 \text{ eV}$ fluctuation amplitude 10 10<sup>-2</sup>  $10^{-1}$ Wavenumber, k [h Mpc⁻¹]

 $\omega_m$  + geometry

Physical matter

23

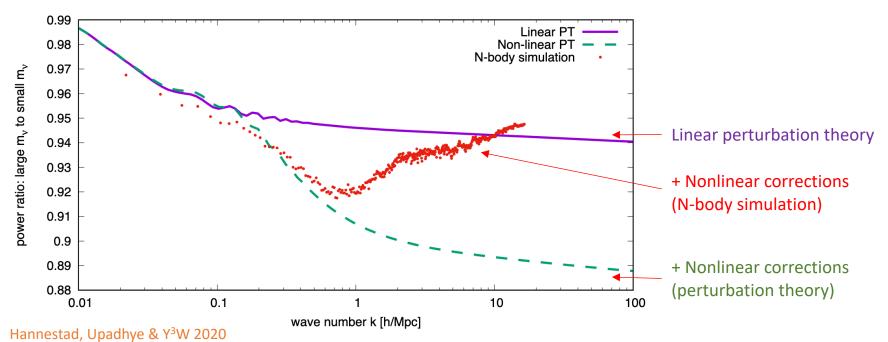


#### There are nonlinearities and nonlinearities...

	Nonlinear Dark matter (collisionless)	Baryonic astrophysics @ k ~ 1/Mpc	Empirical tracers or proxies
СМВ	No	No	No
ВАО	Mild	No	Mild
Cosmic shear	Yes	No	No
Galaxy power spectrum	Yes	No	Assume galaxy number density tracks DM density
Cluster abundance	Yes	No	X-ray temperature, cluster richness as proxies for mass
Lyman alpha	Yes	Hydrogen distribution	No
Calculable from first principles (i.e., described by a Lagrangian)?	Yes	No	No

#### "Fairly easily" calculable nonlinearities...

**Collisionless nonlinearities** concern only the gravitational interactions of the cold dark matter and neutrinos.



#### N-body simulations...

## Standard method for computing **nonlinear CDM dynamics**.

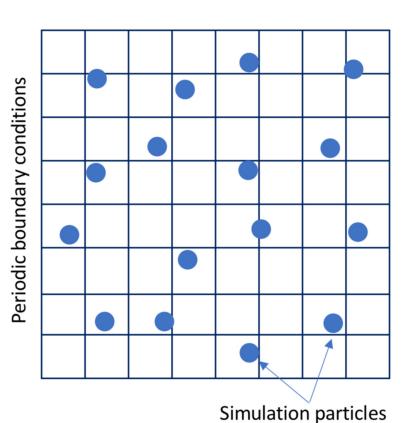
- Discretise CDM fluid into particles (10M to 10B, depending on what you want to do)
- Solve equations of motion for each particle under gravity.

**Equations of motion** 

$$\frac{d\vec{x}}{d\tau} = \frac{p}{am} \qquad \frac{d\vec{p}}{d\tau} = -am\nabla\Phi$$

Poisson equation

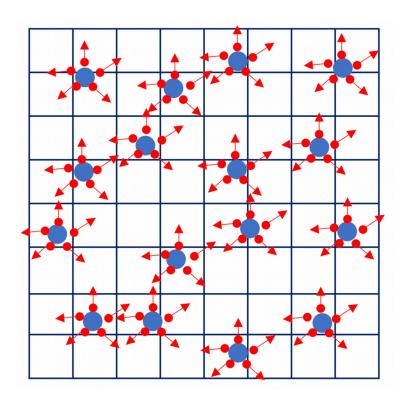
$$\nabla^2 \Phi = 4\pi G a^2 \delta \rho$$



#### N-body simulations with neutrinos...

We can in principle do the same thing with the  $C\nu B$ . But...

- Need several neutrino particles per CDM particles, sampled from the FD distribution, to model free-streaming.
- Neutrino particles have very large initial velocities.
- → In practice, this type of simulations very computationally demanding because of **shot-noise** and **long run time**.
- → Finding cleverer ways to do these simulations is an active area of research.



#### Currents bounds on the neutrino mass sum...

There is **no** cosmological measurement of the neutrino mass sum yet.

• Current constraints on  $\sum m_{\nu}$  are typically O(0.1-0.3) eV, depending on exactly how you do the analysis  $\rightarrow$  Model dependence.

6+1 fit parameters	Model	Degenerate	Normal	Inverted
Primordial	Baseline $\Lambda$ CDM+ $\Sigma m_{\nu}$	0.121	0.146	0.172
tensors	+ <i>r</i>	0.115	0.142	0.167
[ ]	+ <i>w</i>	0.186	0.215	0.230
Dynamical dark energy	+ $W_0W_a$	0.249	0.256	0.276
	$+ w_0 w_a$ , $w(z) > -1$	0.096	0.129	0.157
Spatial curvature	+ Ω <sub>k</sub>	0.150	0.173	0.198

Factor of 3 variation between min and max.

#### It is possible to relax the bound further...

You can also alter the physics and properties of the CvB itself to physically relax cosmological constraints.

- Neutrino decay
- Neutrino spectral distortion
- Late-time neutrino mass generation

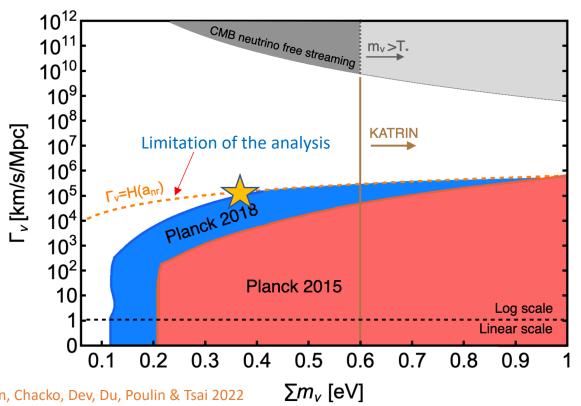
• ...

These "physics" games can usually buy you more room for play, provided you are happy to accept the non-standard neutrino physics.

## Non-relativistic neutrino decay...

#### Official Planck benchmark: $\sum m_{\nu} < 0.12 \text{ eV}$

#### ... into dark radiation



If neutrinos decay with a **lifetime** 

 $\tau_{\nu} \sim 0.1 \, \text{Myr}$ 

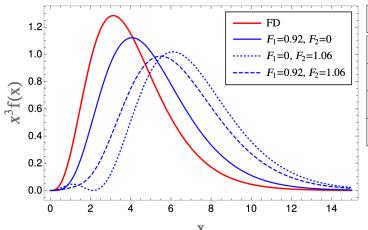
then it is possible to accommodate

$$\sum m_{\nu} \lesssim 0.42 \text{ eV}$$

Planck+BAO+SN

#### Neutrino spectral distortion...

Enhancing the average momentum (via decay, interaction, etc.) while maintaining the early-time neutrino energy density (i.e.,  $N_{\rm eff}$ ) relaxes the neutrino mass bound.



	TT+lowP (95 % CL)	TT+lowP+BAO (95 % CL)
FD	$\sum m_{\nu} < 0.73 \text{ eV}$	$\sum m_{\nu} < 0.18 \text{ eV}$
$F_1 = 0.92, F_2 = 0$	$\sum m_{\nu} < 0.95 \text{ eV}$	$\sum m_{\nu} < 0.26 \; \mathrm{eV}$
$F_1 = 0, F_2 = 1.06$	$\sum m_{\nu} < 1.45 \text{ eV}$	$\sum m_{\nu} < 0.37 \; \mathrm{eV}$
$F_1 = 0.92, F_2 = 1.06$	$\sum m_{\nu} < 1.34 \text{ eV}$	$\sum m_{\nu} < 0.32 \text{ eV}$

Oldengott, Barenboim, Kahlen, Salvado & Schwarz 2019

• If you're adventurous and take a Gaussian momentum distribution, you could even relax the bound to  $\sum m_{\nu} \lesssim 3$  eV. Alvey, Escudero & Sabti 2022

#### Late-time $\nu$ mass generation...

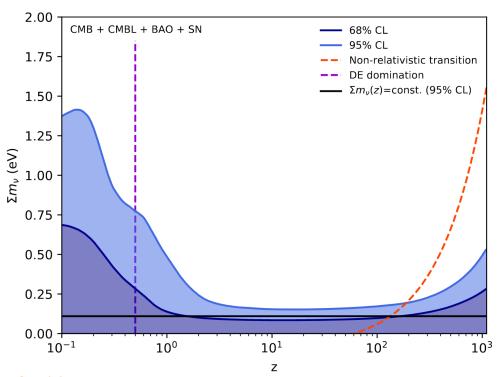
Official Planck benchmark:  $\sum m_{\nu} < 0.12 \text{ eV}$ 

Late-time mass through a phase transition at  $T \sim \text{meV}$ .

Dvali & Funcke 2016

 But phenomenologically, if neutrinos pick up masses only after z~1, then this is allowed:

$$\sum m_{\nu} \lesssim 1.46 \text{ eV}$$



Lorenz, Funcke, Löffler & Calabrese 2021

#### Take-home message so far...

Massive neutrinos leave an imprint on the cosmic large-scale structure.

- We can use this to measure/constrain neutrino masses with cosmological observations.
- Current constraint the **neutrino mass sum is** conservatively  $\sum m_{\nu} \lesssim O(0.1-0.3)~{\rm eV}.$ 
  - The range comes from how exactly you do the analysis, e.g., what background cosmology you use, etc.
  - You can evade the tightest constraints to a good extent with very non-standard neutrino physics.

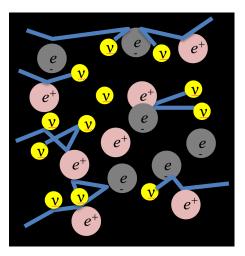
# 3. Relativistic neutrino free-streaming and non-standard interactions...

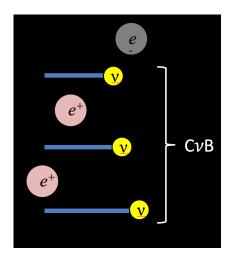


#### Cosmic neutrino background ... Interaction rate: $\Gamma_{\text{weak}} \sim G_F^2 T^5$

Expansion rate:  $H \sim M_{\rm nl}^{-2} T^2$ 

The CvB is formed when neutrinos decouple from the cosmic plasma.





**Neutrinos** "free-stream" to infinity.

 $(T_{\odot \text{core}} \sim 1 \text{ keV})$ 

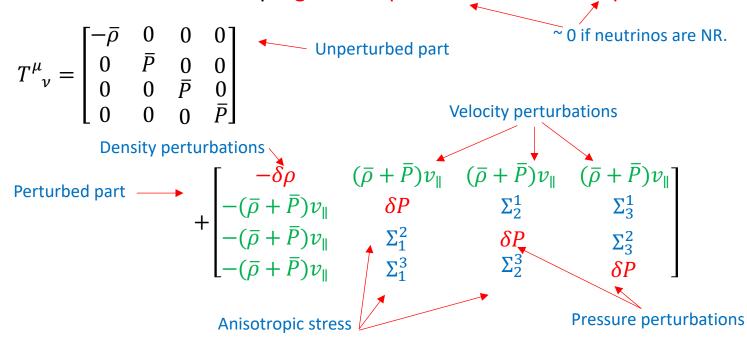
Above  $T \sim 1$  MeV, even weakly-interacting neutrinos can be produced, scatter off  $e^+e^-$  and other neutrinos, and attain thermodynamic equilibrium

Below  $T \sim 1$  MeV, expansion dilutes plasma, and reduces interaction rate: the universe becomes transparent to neutrinos.

### Relativistic neutrino free-streaming..

Fundamentally the same as non-relativistic neutrino free-streaming.

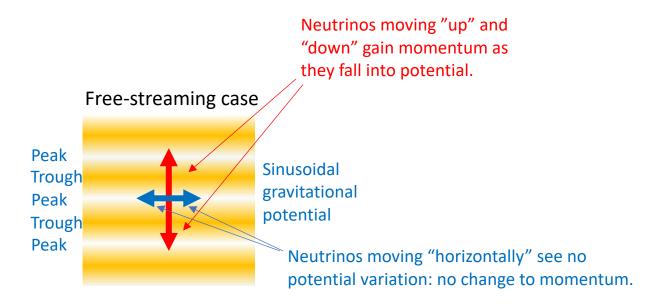
• But relativistic = can develop significant pressure and anisotropic stress.



### Free-streaming and anisotropic stress...

#### Standard-model neutrinos free-stream.

• Free-streaming in an inhomogeneous background induces anisotropic stress (aka momentum anisotropy).



### Neutrino anisotropic stress and the metric...

**Neutrino anisotropic stress** (or lack thereof) leaves distinct imprints on the spacetime metric perturbations.

Scale factor 
$$\mathrm{d}s^2 = a^2(\tau)[-(1+2\psi)\mathrm{d}\tau^2 + (1-2\phi)\mathrm{d}x^i\mathrm{d}x_i]$$

where

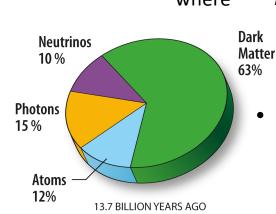
$$k^{2}(\phi - \psi) = 12\pi Ga^{2}(\bar{\rho} + \bar{P})\sigma$$

Mean energy density & pressure

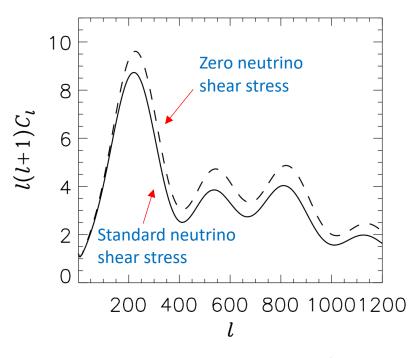
Anisotropic stress

In  $\Lambda$ CDM, mainly from ultra-relativistic neutrinos and photons.

• Changes to  $(\phi - \psi)$  around CMB times  $(t \sim 400 \ \text{kyr})$  affect the evolution of CMB perturbations and are observable in the CMB TT power spectrum.



### Neutrino anisotropic stress & the CMB...

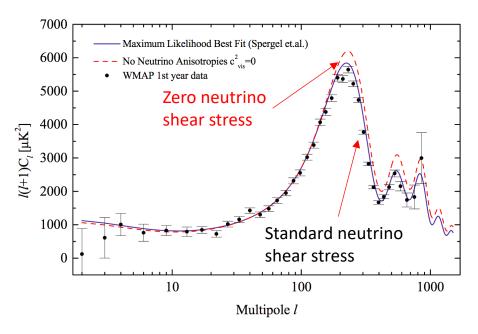


Hannestad 2005

Removing neutrino anisotropic stress enhances power at multipoles  $\ell \gtrsim 200$  in the CMB TT spectrum.

- Effect is mildly degenerate with the primordial fluctuation amplitude and spectral tilt.
- But even with WMAP-1<sup>st</sup> year data, it was already possible to exclude zero neutrino anisotropic stress at  $\gtrsim 2\sigma$ .

### Neutrino anisotropic stress & the CMB...



Melchiorri & Trotta 2005

So what can we do with this??

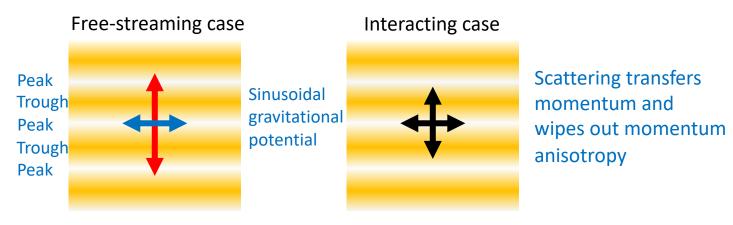
Removing neutrino anisotropic stress enhances power at multipoles  $\ell \gtrsim 200$  in the CMB TT spectrum.

- Effect is mildly degenerate with the primordial fluctuation amplitude and spectral tilt.
- But even with WMAP-1<sup>st</sup> year data, it was already possible to exclude zero neutrino anisotropic stress at  $\geq 2\sigma$ .

### Free-streaming vs interacting...

#### Standard-model neutrinos free-stream.

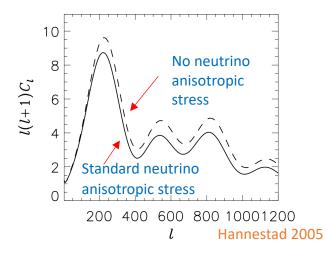
- Free-streaming in an inhomogeneous background induces anisotropic stress (aka momentum anisotropy).
- Conversely, interactions transfer momentum and, if sufficiently efficient, can wipe to out anisotropy.



### Using anisotropic stress to test $\nu$ interactions.

Demanding that neutrinos free-streaming at CMB times ( $t \sim 400 \text{ kyr}$ ), we can constrain non-standard neutrino interactions in that epoch.

- Neutrino self-interaction
- Relativistic neutrino decay
- (Neutrino-DM interactions wipe anisotropic stress too. But because it involves DM, the phenomenology is slightly different.)



To do so, we need to figure out the **isotropisation timescale**  $T_{\rm isotropise}$  given an interaction.

### Tracking neutrino perturbations...

The standard approach is to use the **relativistic Boltzmann equation** to describe the neutrino phase space distribution  $f_i(x^{\mu}, P^i)$ .

Liouville operator 
$$P^{\mu}\frac{\partial f_i}{\partial x^{\mu}} - \Gamma^{\nu}_{\rho\sigma}P^{\rho}P^{\sigma}\frac{\partial f_i}{\partial P^{\nu}} = 0$$

**Gravitational effects** 

- Split into  $f_i(x^\mu, P^i) = \bar{f}_i(x^0, |P^i|) + F_i(x^\mu, P^i)$
- Linearise and go to Fourier space  $x^i \leftrightarrow k^i$
- **Decompose**  $F_i(x^o, k^i, P^i)$  into a Legendre series in  $k \cdot P$ .

Integrate in momentum:

 $\ell = 0 \rightarrow$  density and pressure perturbations

 $\ell = 1 \rightarrow \text{velocity perturbations}$ 

 $\ell \geq 2 \rightarrow$  anisotropies



### Adding a short-range particle interaction...

To describe a **short-range interaction**, add a **collision integral** to the RHS of the relativistic Boltzmann equation for  $f_i(x^{\mu}, P^i)$ .

$$\text{Liouville operator} \quad P^{\mu} \frac{\partial f_i}{\partial x^{\mu}} - \Gamma^{\nu}_{\rho\sigma} P^{\rho} P^{\sigma} \frac{\partial f_i}{\partial P^{\nu}} = m_i \left(\frac{\mathrm{d}f_i}{\mathrm{d}\sigma}\right)_C \quad \text{Collision integral}$$

**Gravitational effects** 

- Split into  $f_i(x^\mu, P^i) = \bar{f}_i(x^0, |P^i|) + F_i(x^\mu, P^i)$
- Linearise and go to Fourier space  $x^i \leftrightarrow k^i$
- **Decompose**  $F_i(x^o, k^i, P^i)$  into a Legendre series in  $k \cdot P$ .

Integrate in momentum:

 $\ell = 0 \rightarrow$  density and pressure perturbations

 $\ell = 1 \rightarrow \text{velocity perturbations}$ 

 $\ell \ge 2 \rightarrow$  anisotropies



## Collision integral and the isotropisation rate...

Given an interaction Lagrangian, the collision integral for  $f_i(x^{\mu}, P^i)$  is

$$m_{i} \left(\frac{\mathrm{d}f_{i}}{\mathrm{d}\sigma}\right)_{C} = \frac{1}{2} \left(\prod_{j=1}^{N} \int g_{j} \frac{\mathrm{d}^{3}\mathbf{n}_{j}}{(2\pi)^{3} 2E_{j}(\mathbf{n}_{j})}\right) \left(\prod_{k=1}^{M} \int g_{k} \frac{\mathrm{d}^{3}\mathbf{n}_{k}}{(2\pi)^{3} 2E_{k}(\mathbf{n}_{k})}\right)$$

$$\times (2\pi)^{4} \delta_{D}^{(4)} \left(p + \sum_{j=1}^{N} n_{j} - \sum_{k=1}^{M} n_{k}'\right) |\mathcal{M}_{i+j_{1}+\dots+j_{N}\leftrightarrow k_{1}+\dots+k_{M}}|^{2}$$

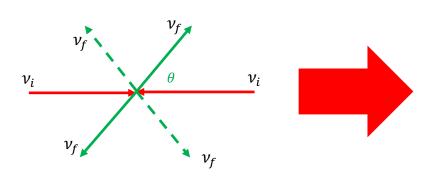
$$\times [f_{k_{1}} \cdots f_{k_{N}}(1 \pm f_{i})(1 \pm f_{j_{1}}) \cdots (1 \pm f_{j_{N}}) - f_{i}f_{j_{1}} \cdots f_{j_{N}}(1 \pm f_{k_{1}}) \cdots (1 \pm f_{k_{M}})]$$

- To compute the isotropisation rate, follow the previous procedure of linearisation and decomposition into a Legendre series.
- $\rightarrow$  The damping rate of the quadrupole ( $\ell=2$ ) moment represents the lowest-order isotropisation rate of the neutrino ensemble.

Tedious stuff, but this is really the only correct way to calculate these things, else you can get it very wrong... However, the result can usually be understood in simple terms.  $\rightarrow$  **Next slide** 

### Isotropisation from $\nu$ self-interaction...

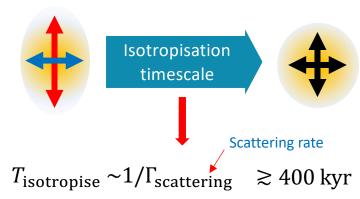
Consider a 2  $\rightarrow$  2 scattering event  $\nu_i + \nu_i \rightarrow \nu_f + \nu_f$ .



• The probability of  $v_f$  emitted at any angle  $\theta$  is the same for all  $\theta \in [0, \pi]$ .

Cyr-Racine & Sigurdson 2014; Oldengott, Rampf & Y<sup>3</sup>W 2015; Lancaster, Cyr-Racine, Knox & Pan 2017; Oldengott, Tram, Rampf & Y<sup>3</sup>W 2017; Kreisch, Cyr-Racine & Dore 2019; Forastieri et al. 2019; etc.

 $\rightarrow$  Particles in two head-on  $v_i$  beams need only scatter once to transfer their momenta equally in all directions.



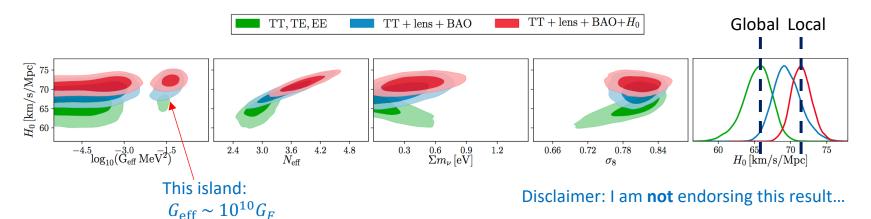
 $\rightarrow$  Upper limit on  $\Gamma_{\text{scattering}}$  (hence coupling).

## $\nu$ self-interaction and the $H_0$ tension...

Kreisch, Cyr-Racine & Dore 2019

#### Recent claim that self-interaction alleviates the Hubble tension.

- Local/late time: Cepheid-calibrated SNIa (SH0ES) and strong-lensing time delays (H0liCOW);  $H_0 = (73.5 \pm 1.4) \text{ km/s/Mpc}$
- Global/early time: Statistical inference from CMB anisotropies (Planck), weak lensing, BAO;  $H_0 = (67.4 \pm 0.5) \text{ km/s/Mpc}$



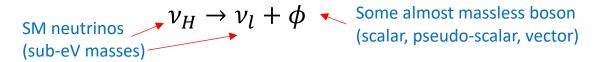
### Isotropisation from invisible neutrino decay...

Invisible here means the decay products do **not** include a photon.

- SM 1  $\rightarrow$  3 decay:  $\nu_j \rightarrow \nu_i \nu_k \bar{\nu}_k$ , but the rate is proportional to  $m_{\nu}^6$ .
  - $\rightarrow$  For sub-eV neutrino masses, the neutrino lifetime would be  $> 10^{10}$  longer than the present age of the universe, i.e., not very interesting.

Bahcall, Cabibbo & Yahil 1972

Beyond SM: generically one could consider

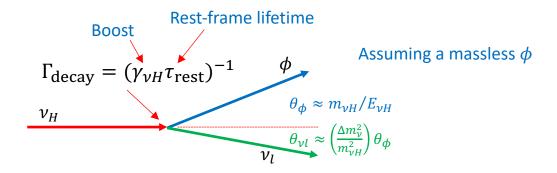


- More freedom with the coupling strength and hence lifetime.
- Predicted by a many extensions to the SM (mostly linked to neutrino mass generation or dark matter).
   Gelmini & Roncadelli 1981; Chikashige, Mohapatra & Peccei 1981; Schechter & Valle 1982; Dror 2020; Ekhterachian, Hook, Kumar & Tsai 2021; etc.

### Isotropisation from relativistic $1 \rightarrow 2$ decay...

How long does it take  $\nu_H \rightarrow \nu_l + \phi$  and its inverse process to wipe out momentum anisotropies? (Hint: it's not the lifetime of  $\nu_H$ .)

In relativistic decay, the decay products are beamed.



## Isotropisation from relativistic $1 \rightarrow 2$ decay...

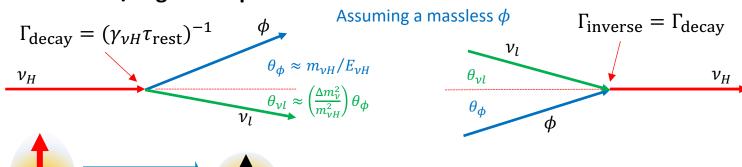
How long does it take  $\nu_H \rightarrow \nu_l + \phi$  and its inverse process to wipe out momentum anisotropies? (Hint: it's not the lifetime of  $\nu_H$ .)

In relativistic decay, the decay products are beamed.

Isotropisation

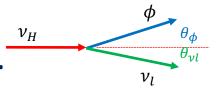
timescale

 Inverse decay also only happens when the daughter particles meet strict momentum/angular requirements.

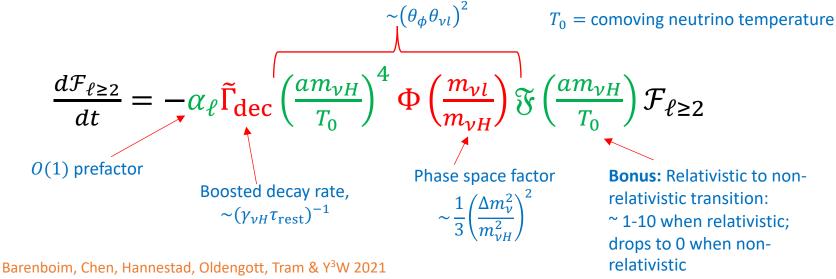


 $\rightarrow$  Isotropisation is going to take a loooong time compared with the  $\nu_H$  lifetime.

## The isotropisation rate is calculable...

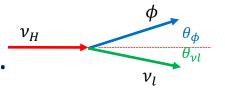


With some reasonable approximations (e.g., separation of scales), we have calculated the damping rate of the  $\ell$ th neutrino kinetic moment from relativistic  $\nu_H \rightarrow \nu_l + \phi$  and its inverse process:



Chen, Oldengott, Pierobon & Y<sup>3</sup>W 2022

# The isotropisation rate is calculable...



With some reasonable approximations (e.g., separation of scales), we have calculated the damping rate of the  $\ell$ th neutrino kinetic moment from relativistic  $\nu_H \rightarrow \nu_l + \phi$  and its inverse process:

$$\frac{d\mathcal{F}_{\ell\geq 2}}{dt} \sim -T_{\text{isotropisation}}^{-1} \mathcal{F}_{\ell\geq 2}$$

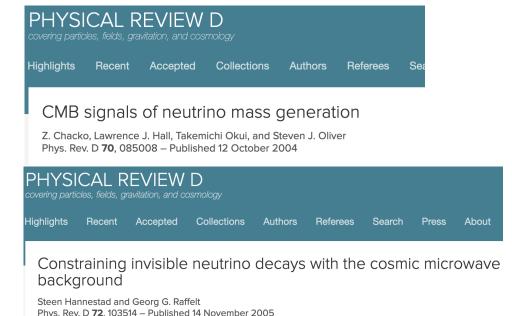
Isotropisation timescale from relativistic decay/inverse decay

$$T_{\text{isotropisation}} \sim \left(\theta_{\phi} \theta_{\nu_l}\right)^{-2} \gamma_{\nu H} \tau_{\text{rest}}$$

It's model-independent; any dependence on the interaction structure is contained in  $\tau_{\rm rest}$ ; the rest is just kinematics.

### Comparison with older works...

Two works in the 2000s that considered how long it would take relativistic  $1 \rightarrow 2$  decay and inverse to isotropise a neutrino ensemble.



 Neither work actually calculated it... But this is the isotropisation timescale they guessed:

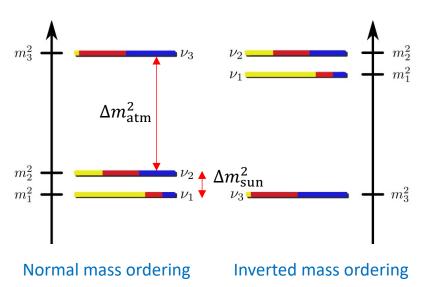
$$T \sim (\theta_{\nu l} \theta_{\phi})^{-1} \gamma_{\nu H} \tau_{\text{rest}}$$

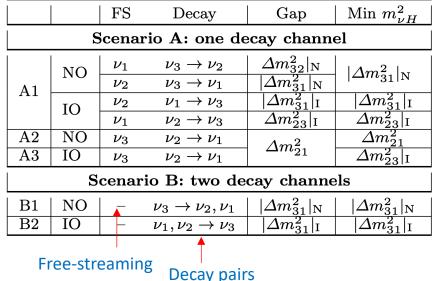
cf our first-principles rate:

$$T \sim (\theta_{\phi} \theta_{\nu_l})^{-2} \gamma_{\nu H} \tau_{\text{rest}}$$

### Bounds on the neutrino lifetime: scenarios...

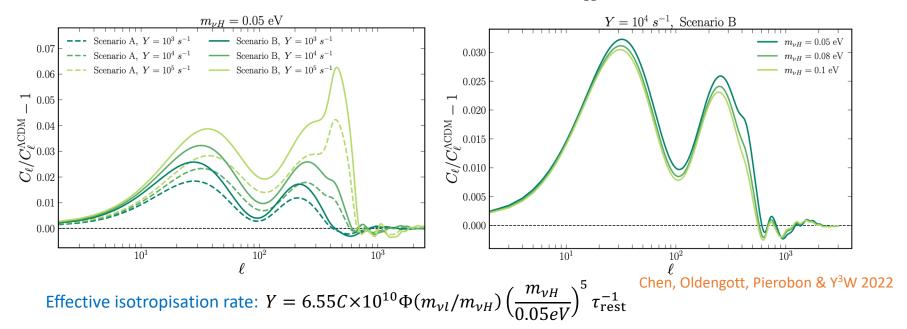
Global neutrino oscillation data currently point to two possible orderings of neutrino masses → several possible decay/free-streaming patterns.





## Signatures in the CMB TT power spectrum...

Fractional deviations in the CMB TT power spectrum from  $\Lambda$ CDM for various the effective isotropisation rate Y and  $\nu_H$  masses.



Scenario A = 2 neutrinos participate in decay/inverse decay; Scenario B = all 3 participate

### CMB lower bounds on the neutrino lifetime...

Implementing the isotropisation rate in CLASS and using the Planck 2018 CMB TTTEEE+low+lensing data, our lifetime constraint is:

Rel to non-rel factor

$$\tau_{\rm rest} \gtrsim 1.2 \times 10^6 \ \Im \left[0.12 \left(\frac{m_{\nu H}}{0.05 \ {\rm eV}}\right)\right] \Phi \left(\frac{m_{\nu l}}{m_{\nu H}}\right) \left(\frac{m_{\nu H}}{0.05 \ {\rm eV}}\right)^5 \ {\rm s}$$
 Phase space factor  $\sim \frac{1}{3} \left(\frac{\Delta m_{\nu}^2}{m_{\nu H}^2}\right)^2$  Chen, Oldengott, Pierobon & Y³W 2022

• Or equivalently:

$$\nu_3 \to \nu_{1,2} + \phi \text{ (NO)} 
\nu_{1,2} \to \nu_3 + \phi \text{ (IO)}$$
 $\tau_{\text{rest}} \gtrsim (6 - 10) \times 10^5 \text{s}$ 

$$v_2 \to v_1 + \phi$$
  $\tau_{\text{rest}} \gtrsim (400 - 500) \text{s}$ 

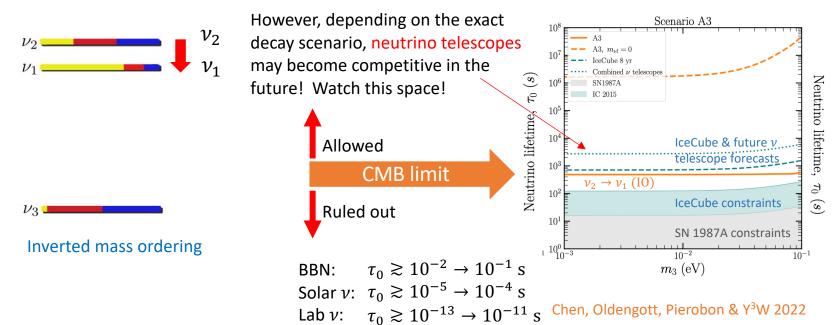
Cf old constraints (using a guesstimated *T*<sub>isotropise</sub>):

$$\tau_{\rm rest} \gtrsim 10^9 \left(\frac{m_{\nu H}}{0.05 \text{ eV}}\right)^3 \text{ s}$$

Hannestad & Raffelt 2005

### CMB lower bounds on the neutrino lifetime...

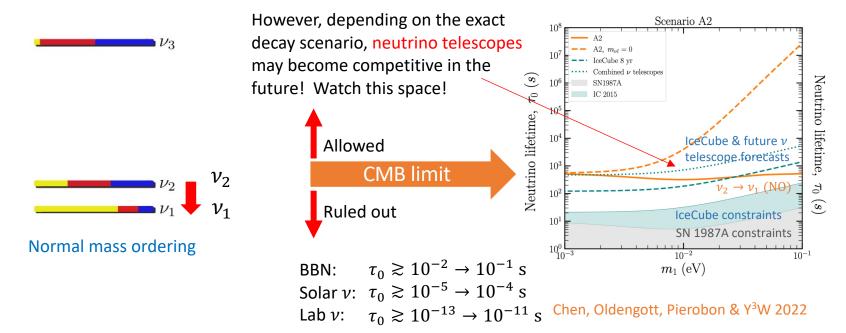
... currently the best limits on invisible neutrino decay  $\nu_H \rightarrow \nu_l + \phi$ .



<sup>\*</sup> IceCube constraints & forecasts from Song et al. 2021

### CMB lower bounds on the neutrino lifetime...

... currently the best limits on invisible neutrino decay  $\nu_H \rightarrow \nu_l + \phi$ .



<sup>\*</sup> IceCube constraints & forecasts from Song et al. 2021

### Summary: Part 2...

- The cosmic neutrino background is a fundamental prediction of standard hot big bang cosmology.
- Given this, we can contemplate using precision cosmological observables to measure/constrain
  - Neutrino masses
  - Non-standard neutrino properties like self-interaction and invisible decay.
- Current cosmological data constrain the **neutrino mass sum** conservatively to  $\sum m_{\nu} \lesssim O(0.1-0.3)$  eV.
  - You can get around these to an extent with non-standard neutrino physics.
- We have calculated the isotropisation rate from first-principles and revised the CMB constraint on the neutrino lifetime by many orders of magnitude.