Non-linearity * Variability - Diversity

Interplay between non-linearity and variability

Spatial \checkmark

Temporal

Interplay between non-linearity (local dynamics) and temporal variation

Local dynamics

Competition

Consumer-resource interactions (predation, parasitism)

Temporal variation

Abiotic environment Temperature variation Climate warming

The storage effect

Peter Chesson (1985, 1994, ..., 2019)



What does storage mean?

The gain in reproduction during favorable periods is stored in some way (e.g., through adult longevity in species with overlapping generations, or dormant seeds in annual plants) so that the population can survive the losses it suffers during unfavorable periods.

Storage effect

Species experience little or no interspecific interactions (e.g., competition, predation) when rare, and experience mostly self-limitation (e.g., intra-specific competition) when abundant.

Components of the storage effect

1. Species-specific responses to environmental variation

2. Negative or no correlation between favorability of the environment and strength of inter-specific competition

3. Buffered population growth

1. Species specific responses to environmental variation

Environmental variation mostly abiotic (e.g., temperature, rainfall)

1. Species-specific responses to environmental variation

The environment that maximizes fitness is not the same for all species (e.g., colder vs. warmer periods of the year, serpentine vs. non-serpentine soil)

Species differ in the way they respond to abiotic environmental variation (e.g., temperature, rainfall)

e.g., some do better at warmer temperatures, others do better at cooler temperatures

Species-specific responses ==> an environment favorable to one species is unfavorable to its competitors

==>mostly encounter conspecifics ==> strong intra-specific competition and little or no inter-specific competition

Components of the storage effect

1. Species-specific responses to environmental variation \checkmark

2. Correlation between environmental favorability and strength of competition

3. Buffered population growth

An environment favorable to one species is unfavorable to its competitors

==> little or no inter-specific competition during unfavorable periods for competitor

==> strong intra-specific competition during favorable periods for focal species

2. Correlation between environmental favorability and strength of competition

Negative or zero correlation between favorability of the environment and strength of inter-specific competition

Components of the storage effect

1. Species-specific responses to environmental variation \checkmark

Correlation between environmental favorability and strength of competition √

3. Buffered population growth

3. Buffered population growth

Species have a mechanism to survive unfavorable environments in space or time (e.g., dormancy, dispersal, high adult longevity)

Components of the storage effect

1. Species-specific responses to environmental variation

2. Zero or Negative correlation between favorability of the environment and strength of inter-specific competition

3. Buffered population growth

Spatial/temporal niche partitioning via the storage effect

Storage effect

A mechanism for temporal niche partitioning framed in terms of species' responses to abiotic environmental variation

A hierarchy of mechanisms

Mechanism for temporal niche partitioning: Storage effect

Mechanism of the **Storage effect**:

Interplay between environment variation and competition increases intra-specific interactions relative to inter-specific interactions

Mechanistic basis of the storage effect

Temperature as the axis of abiotic variation

Temperature as the axis of abiotic variation

- 1. Ubiquitous (diurnal, seasonal)
- 2. Direct (ectotherms) and indirect (endotherms) effects
- 3. Perturbations (climate warming)

Challenge

Non-linearities due to density dependence

Non-linearity in species' responses to abiotic (temperature) variation

Interplay between non-linearities

Community level: temporal niche partitioning

Species level: storage effect

Individual level: phenotypic traits

Goal

Predict outcomes of temporal niche partitioning via the storage effect based on how temperature variation affects the underlying life history and consumption traits

Characterizing temperature responses of phenotypic traits

Life history:

Birth, maturation and mortality rates **Consumption**:

Attack rate, handling time

Mechanistic basis of trait responses to temperature



Temperature (K)



Monotonic temperature responses: mortality



Left-skewed temperature responses: maturation



Unimodal temperature responses: reproduction

Unimodal temperature responses: attack and maximum uptake rates



Temperature effects on life history and consumption traits

Data: trait responses conserved across ectotherm taxa

 \Rightarrow

Trait-based framework that applies broadly



Trait-based models of species interactions

Exploitative competition


Exploitative competition in constant environment

$$\begin{split} \frac{dR}{dt} &= R \bigg(r \big(1 - \frac{R}{K} \big) - a_1 C_1 - a_2 C_2 \bigg) & \text{Resource} \\ \frac{dC_1}{dt} &= C_1 \bigg(e_1 a_1 R - d_1 \bigg) & \text{Consumer 1} \\ \frac{dC_2}{dt} &= C_2 \bigg(e_2 a_2 R - d_2 \bigg) & \text{Consumer 2} \end{split}$$

R* rule: competitive exclusion

Exploitative competition in seasonally varying environments

Trait-based consumer-resource model



Mechanistic trait responses

Seasonal temperature variation

Mutual invasibility criteria in seasonally varying environments

Mutual invasibility criteria

$$\frac{1}{\tau} \int_0^\tau \frac{1}{C_i(t)} \frac{dC_i(t)}{dt} \, \mathrm{d}t > 0$$
$$i=1, 2$$

Time-averaged per capita growth rate when rare

Mutual invasibility criteria

$$\frac{1}{\tau} \int_{0}^{\tau} \frac{dC_{i}}{dt} \frac{1}{C_{i}} = \frac{1}{\tau} \int_{0}^{\tau} e_{i} a_{i}(T(t)) R_{C_{j}}(T(t)) - d_{i}(T(t)) dt > 0$$

$$i, j = 1, 2, i \neq j$$
(1)

 $R_{C_j}(T(t))$: instantaneous resource availability set by the resident consumer in a seasonally varying environment (time-varying R^*) When the consumers exhibit linear functional responses and temperature variation is predictable (i.e., mean temperature and the amplitude of seasonal fluctuations remain approximately constant over time), the instantaneous resource availability set by the resident consumer is given by:

 $R_{C_j}(T(t)) = \frac{d_j(T(t))}{e_j a_j(T(t))}.$

Mutual invisibility criteria in seasonal environments

$$\frac{1}{\tau} \int_0^\tau \frac{dC_i}{dt} \frac{1}{C_i} = \frac{1}{\tau} \int_0^\tau e_i a_i(T(t)) \frac{d_j(T(t))}{e_j a_j(T(t))} - d_i(T(t)) \, \mathrm{d}t > 0$$
$$i, j = 1, 2, i \neq j$$

Mutual invasibility criteria in seasonal environments

$$\frac{\int_0^\tau \frac{e_i a_i(T(t))}{e_j a_j(T(t))} d_j(T(t)) dt}{\int_0^\tau d_i(T(t)) dt} > 1.$$

Consumer *i*'s lifetime reproductive success in a seasonal environment

After separating the temperature-independent components and doing some algebra, we can derive the **sufficient** condition for mutual invasibility.

Sufficient condition for mutual invasibility

$$\frac{\int_0^\tau d'_2(T(t)) dt}{\int_0^\tau a'_2(T(t)) \frac{d'_1(T(t))}{a'_1(T(t))} dt} < \frac{R_{1T_{\text{opt}}}}{R_{2T_{\text{opt}}}} < \frac{\int_0^\tau a'_1(T(t)) \frac{d'_2(T(t))}{a'_2(T(t))} dt}{\int_0^\tau d'_1(T(t)) dt}$$
(1)

where

$$R_{iT_{\text{opt}}} = \frac{d_{i_{T_R}}}{e_i a_{i_{T_{\text{opt}}}}} \quad i, j = 1, 2, i \neq j, \text{ and},$$

 $d'_i(T(t))$ and $a'_i(T(t))$ are the temperature-dependent mortality and consumption rates.

Necessary condition for mutual invasibility

$$\frac{\int_0^\tau d_2(T(t)) dt}{\int_0^\tau a_2(T(t)) \frac{d_1(T(t))}{a_1(T(t))} dt} < \frac{\int_0^\tau a_1(T(t)) \frac{d_2(T(t))}{a_2(T(t))} dt}{\int_0^\tau d_1(T(t)) dt}$$
(1)

1 (55(.))

Note: hats have been dropped for convenience.

Necessary condition for mutual invasibility

$$\left(\frac{\int_0^\tau d_1(T(t))dt}{\int_0^\tau a_2(T(t))\frac{d_1(T(t))}{a_1(T(t))}dt}\right) \left(\frac{\int_0^\tau d_2(T(t))dt}{\int_0^\tau a_1(T(t))\frac{d_2(T(t))}{a_2(T(t))}dt}\right) < 1$$

Criteria for coexistence in seasonal environments

Necessary and sufficient ==> species limit themselves more than they do others ==> stable coexistence

Necessary only ==> one species excludes the other ==> competitive dominance

Neither necessary nor sufficient ==> outcome depends on initial conditions ==> **priority effects**

The necessary condition from the consumer-resource model:

$$\left(\frac{\int_0^\tau d_1(T(t))dt}{\int_0^\tau a_2(T(t))\frac{d_1(T(t))}{a_1(T(t))}dt}\right) \left(\frac{\int_0^\tau d_2(T(t))dt}{\int_0^\tau a_1(T(t))\frac{d_2(T(t))}{a_2(T(t))}dt}\right) < 1$$
(1)

is equivalent to the necessary condition for for mutual invasibility in the Lotka-Volterra framework:

$$\left(\frac{\alpha_{21}}{\alpha_{11}}\right) \left(\frac{\alpha_{12}}{\alpha_{22}}\right) < 1 \tag{2}$$

with

$$\alpha_{ii} = \frac{1}{\int_0^\tau d_i(T(t)) \mathrm{d}t}$$

Intra-specific competition coefficient

$$\begin{split} \alpha_{ji} &= \frac{1}{\int_0^\tau a_j(T(t)) \frac{a_i(T(t))}{d_i(T(t))} \mathrm{d}t} \quad \begin{array}{l} \text{Inter-specific} \\ \text{competition coefficient} \\ i, j &= 1, 2, i \neq j \end{split}$$

$$\begin{split} \alpha_{ii} &= \frac{1}{\int_0^\tau d_i(T(t)) \mathrm{d}t} & \underset{\text{comparison}}{\text{Mechan}} \\ \alpha_{ji} &= \frac{1}{\int_0^\tau a_j(T(t)) \frac{a_i(T(t))}{d_i(T(t))} \mathrm{d}t} \\ i, j &= 1, 2, i \neq j \end{split}$$

Mechanistic derivation of competition coefficients based on species' consumption and mortality rates

Intra-specific competition

$$\alpha_{ii} = \frac{1}{\frac{1}{\tau} \int_0^{\tau} d_i(T(t)) dt}$$

Intra-specific competition coefficient proportional to the consumer's timeaveraged mortality rate

$$i=1, 2$$

Smith and Amarasekare, (2018)

Inter-specific competition

 $\alpha_{ji} = \frac{1}{\int_0^\tau a_j(T(t)) \frac{a_i(T(t))}{d_i(T(t))} dt}$

Invader's consumption rate Resource availability set by resident consumer

Smith and Amarasekare, (2018)

Mutual invasibility

- 1. Intra-specific competition (Invader's mortality rate)
- 2. Inter-specific competition

2.1 Resource availability set by resident (Resident's consumption and mortality rates)

2.2 Invader's resource acquisition ability (Invader's consumption rate)

Temperature effects on determinants of invasion success

- Resource availability
- Resource consumption
- Mortality

Temperature response of mortality rate



$$d(T) = d_{T_R} e^{A_d \left(\frac{1}{T_R} - \frac{1}{T}\right)}$$

Boltzmann-Arrhenius function

A_d determines temperature sensitivity of mortality

Temperature response of consumption rate



$$a(T) = a_{T_{\text{opt}}} e^{-\frac{(T - T_{\text{opt}_a})^2}{2s_a^2}}$$

Gaussian function

Relative strengths of intra- and interspecific competition depends on the nature of thermal adaptation

Thermal adaptation driven by latitudinal variation in seasonal temperature regimes

Latitudinal variation in seasonal thermal regimes

Tropical climates: high mean temperature, low-amplitude seasonal fluctuations

Temperate climates: low mean temperature, high-amplitude seasonal fluctuations

Nature of thermal adaptation

Higher-latitude species cold adapted: lower thermal optima, active at lower temperatures

Lower-latitude species warm-adapted: species: higher thermal optima, active at higher temperature

Nature of thermal adaptation

Lower-latitude species thermal specialists: narrower response breadths, active during narrow temperature range

Higher-latitude species, thermal generalists: wider response breadths, active during wider temperature range Intra-specific competition (self-limitation) depends on thermal adaptation



Self-limitation strength inversely proportional to average mortality rate





Cold-adapted Lower average mortality Stronger self-limitation Warm-adapted Higher average mortality Weaker self-limitation

Cold-adapted species experience stronger selflimitation than warm-adapted species

Inter-specific competition

Resource availability set by resident [R*(T(t))] (Resident's consumption and mortality rates)

Invader's resource acquisition ability (Invader's consumption rate)

Resource availability set by resident

Resident species' consumption and mortality rates







Cold-adapted Lower resource availability (Lower R^{*}) Warm-adapted Higher resource availability (Higher R^{*})

Cold-adapted species depress resources to lower levels than warm-adapted species

Differential adaptation to seasonal environments (thermal optima)

Cold-adapted species experience stronger self-limitation than their warm-adapted competitors

Cold-adapted species deplete resource to lower levels (have lower R^{*}) than do their warm-adapted competitors
Differential adaptation to seasonal environments (response breadth)



Thermal specialist Lower average mortality Stronger self-limitation Thermal generalist Higher average mortality Weaker self-limitation

Thermal specialists experience stronger selflimitation than thermal generalists



Thermal specialist Lower resource availability (Lower R^{*})

Thermal generalist Higher resource availability (Higher R^{*})

Thermal specialists depress resources to lower levels than thermal generalists

Differential adaptation to seasonal environments (response breadth)

Thermal specialists limit themselves more than their generalist competitors

Thermal specialists deplete resource to lower levels (have lower R^{*}) than do their generalist competitors

Mechanistic basis of storage effect in thermally variable environments

Species that exert **strong inter-specific competition** (e.g., cold-adapted species, thermal specialists) are **more self-limited** than those that exert only weak inter-specific competition (e.g., warm-adapted species and thermal generalists)

Developing testable predictions

Scaling temperature response parameters in terms of seasonal temperature regime

Empirical observations

1. Difference between thermal optimum and mean habitat temperature increases with increasing latitude



Empirical observations

2. Response breadth increases with increasing latitude (adaptation to larger seasonal fluctuations)



Empirical observations

3. Species differ in their temperature sensitivity of mortality



Scaling of thermal optima

Let M_T denote the mean habitat temperature and A_T , the amplitude of seasonal fluctuations.

Consider Consumer 1 to be the resident species and Consumer 2 to be the invader.

Resident consumer's consumption rate: $T_{\text{opt}_{a_1}} = M_T + m$ where m is the deviation of the consumption optimum from mean habitat temperature.

Invader's consumption rate: $T_{\text{opt}_{a_2}} = T_{\text{opt}_{a_1}} + x$ where x is the deviation of invader's consumption optimum from that of resident.

Scaling of response breadth

Let s_{a_1} be the resident consumer's consumption response breadth.

Then
$$v = \frac{s_{a_2}}{s_{a_1}}$$

where v is the ratio of invader's and resident's consumption response breadths

Scaling of temperature sensitivity of mortality

Let A_{d_1} be the resident consumer's Arrhenius constant for increase in mortality with temperature.

Then
$$p = \frac{A_{d_2}}{A_{d_1}}$$

where p is the ratio of invader's and resident's temperature sensitivities of mortality.

By incorporating these scaling relationships into the mutual invisibility criteria

$$\left(\frac{\int_{0}^{\tau} d_{1}(T(t)) dt}{\int_{0}^{\tau} a_{2}(T(t)) \frac{d_{1}(T(t))}{a_{1}(T(t))} dt}\right) \left(\frac{\int_{0}^{\tau} d_{2}(T(t)) dt}{\int_{0}^{\tau} a_{1}(T(t)) \frac{d_{2}(T(t))}{a_{2}(T(t))} dt}\right) < 1$$
(1)

and simplifying,

The necessary condition for mutual invasibility is given by:

$$\left(\frac{\int_{0}^{\tau} e^{-\frac{A_{d_{1}}}{M_{T}-A_{T}S(t)}} dt}{\int_{0}^{\tau} e^{-AS(t)(S(t)+2n)-DS(t)-\frac{A_{d_{1}}}{M_{T}-A_{T}S(t)}} dt}\right) \left(\frac{\int_{0}^{\tau} e^{-\frac{pA_{d_{1}}}{M_{T}-A_{T}S(t)}} dt}{\int_{0}^{\tau} e^{AS(t)(S(t)+2n)+DS(t)-\frac{pA_{d_{1}}}{M_{T}-A_{T}S(t)}} dt}\right) < 1$$

where
$$A = \frac{1-v^2}{2m^2v^2}, B_1 = \frac{A_{d_1}A_T}{M_T + nA_T}, B_2 = \frac{A_{d_1}A_T}{M_T + (n+x)A_T}, C = \frac{x}{m^2}, D = \frac{C}{v^2}$$

Mechanistic description of mutual invasibility criteria consisting entirely of measurable parameters

Testable predictions with just five parameters

Abiotic

Seasonal temperature regime: M_T and A_T

Biotic

Differences between consumer species in:

Thermal optima (x)

Response breadth (v)

Temperature sensitivity of mortality (p)

Insights

Density-independent mortality, which drives intra-specific competition (self-limitation), is crucial to coexistence in thermally variable environments.

Trait-based model provides mechanism for species-specific responses to temperature variation (temperature sensitivity of mortality *p*).

Predictions

1. Mutual invasibility possible if cold-adapted species (lower thermal optimum) experiences greater temperature sensitivity of mortality (steeper mortality curve).

Steeper mortality curve, Lower attack rate at higher temperatures

Warm-adapted species

Shallower mortality curve Higher attack rate at higher temperatures

1. Steeper mortality curve means lower mortality at lower temperatures and stronger self-limitation during favorable (colder) periods of the year.

2. Steeper mortality curve also means higher mortality at high temperatures.

This, combined with its lower attack rate at higher temperatures increases the cold-adapted species' R^{*}, leading to **weaker competition** on the warm-adapted species when the **thermal environment is favorable to the warm-adapted species**.

Lower attack rate optimum and greater temperature sensitivity of mortality ==> coldadapted species limits itself more than it does its warm-adapted competitor.

Warm-adapted species

1. Shallower mortality curve means lower mortality at higher temperatures and stronger self-limitation during favorable (warmer) periods of the year.

Warm-adapted species

Shallower mortality curve also means higher mortality at lower temperatures. This, combined with its lower attack rate at lower temperatures increases the warm-adapted species' R^{*}, leading to **weak competition on the cold-adapted species** when the thermal environment is favorable to the cold-adapted species.

Warm-adapted species

Higher attack rate optimum and lower temperature sensitivity of mortality ==> warmadapted species limits itself more than it does its cold-adapted competitor. Thermal adaptation leads to negative covariance between the abiotic environment and the strength of interspecific competition Criteria for coexistence in seasonal environments

Necessary and sufficient ==> species limit themselves more than they do others ==> stable coexistence

Necessary only ==> one species excludes the other ==> competitive dominance

Neither necessary nor sufficient ==> outcome depends on initial conditions ==> **priority effects**

Conditions for mutual invasibility

When **cold-adapted** species are **more** sensitive to temperature effects on densityindependent mortality than warm-adapted species, *necessary condition for mutual invasibility criterion is always met*

Priority effects are not possible

Conditions for priority effects

When **cold-adapted** species are **less** sensitive to temperature effects on density-independent mortality than **warm-adapted** species, necessary condition for mutual invasibility is violated and **priority effects** arise.

Trait-based invasibility criteria

Predict conditions for coexistence, competitive dominance, and priority effects in thermally varying environments

Testing predictions

Data from host-parasitoid community



Coexistence of parasitoids on common host

Parasitoid coexistence patterns



Lab: Ooencyrtus excludes Trissolcus
Parasitoid coexistence patterns



Field: Coexistence, temporal partitioning

Parasitoids have similar response breadths (v=0.98) but differ in attack rate optima (**x=1.04**⁰) and temperature-sensitivity of mortality (**p=0.82**).

Species with the lower attack rate optimum (*Trissolcus*) exhibits greater temperature sensitivity of mortality.

Predictions

Necessary condition for mutual invasibility should be satisfied

Priority effects should not be possible

Necessary condition for mutual invasibility

$$\left(\frac{\int_0^\tau d_1(T(t))dt}{\int_0^\tau a_2(T(t))\frac{d_1(T(t))}{a_1(T(t))}dt}\right) \left(\frac{\int_0^\tau d_2(T(t))dt}{\int_0^\tau a_1(T(t))\frac{d_2(T(t))}{a_2(T(t))}dt}\right) < 1$$

Necessary condition for mutual invasibility



Difference in attack rate optima (x)



Sufficient condition for mutual invasibility



Difference in attack rate optima (x)



Difference in response breadth (v)





Exploitative competition in seasonally varying environments

Approach: derive mutual invasibility criteria in terms of mechanistic descriptions of trait responses to temperature

Key insights

1. Exponential nature of the mortality response causes self-limitation strength to decrease with increasing temperature

==> cold-adapted species and thermal specialists experience stronger intra-specific competition than warm-adapted species and thermal generalists. 2. Exponential nature of the mortality response translates into lower R* and stronger interspecific competition at temperatures below the attack rate optimum than above it.

Thermal adaptation is such that cold-adapted species and thermal specialists exert weaker competition warm-adapted species and thermal generalists when environment is favorable to warm-adapted species and thermal generalists and *vice versa*

Mechanistic basis on the storage effect in terms of temperature effects on life history and consumption traits

Species-specific responses arise from temperature effects on biochemical processes underlying species' traits

These trait effects translate into relative strengths of intra- vs. inter-specific competition at the population level.

Make testable predictions about population-level patterns of coexistence based solely on trait response data and completely independently on populationlevel information