Neutrino Phenomenology

Atmospheric, Long-baseline, Three-flavor effects, Earth matter effects....



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Panorama of Neutrinos: Across 18 orders in E and 25 orders in L



Remarkable progress over the last two decades

Neutrinos detected from various sources having different energy and distance scales

Detection of cosmic neutrinos opened a new window onto the Universe



Era of Neutrino Astronomy began



2002 Nobel Prize to Raymod Davis Jr. (Sun) and Masatoshi Koshiba (Supernova)

Neutrino Oscillation – A Signature for BSM Physics



Neutrinos change their flavor as they move in space and time \rightarrow Neutrinos Oscillate

Solar, Atmospheric, Reactor, and Accelerator (LBL) experiments firmly established Neutrino Flavor Oscillation \rightarrow implies Neutrinos are <u>Massive</u> and <u>Mix</u> with each other

Neutrinos are Massless in the basic Standard Model (SM) of particle physics

Physics beyond the Standard Model (BSM) necessary to explain non-zero v mass & mixing



2015 Nobel Prize to Takaaki Kajita (Super-K) & Arthur B. McDonald (SNO)



Probing BSM Scenarios Across I8 orders in E and 25 orders in L

Non-zero neutrino mass: first experimental proof (gateway) for BSM physics

Several BSM possibilities can be introduced in the framework of Effective Field Theory (EFT)

$$\mathcal{L}_{ ext{eff}} = \mathcal{L}_{ ext{SM}} + rac{c^{d=5}}{\Lambda} \mathcal{O}^{d=5} + rac{c^{d=6}}{\Lambda^2} \mathcal{O}^{d=6} + \cdots
ight)$$

d=5 Weinberg Operator: LLHH, Λ: New Physics Scale S. Weinberg, PRL 43 (1979) 1566

BSM Scenarios naturally arise due to different mechanisms for generating v masses (e.g. seesaw)

Many models of BSM physics suggest new fundamental particles and interactions, new sources of CP violation, lepton number and lepton flavor violations, possibilities of Lorentz and CPT violation

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ight) igg(e^{d=1} + e^{d=1} +$$

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Probe BSM Physics at High Energies (TeV-PeV)

High-Energy (TeV-PeV) Astrophysical Neutrinos coming from cosmic distances (Mpc-Gpc)

Giant Neutrino Telescopes: IceCube@South Pole, KM3NeT@Mediterranean Sea, future IceCube-Gen2

Novel Approach --New Physics beyond the reach of modern Colliders

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ight) iggl(\mathbf{C}_{ ext{off}} + \mathbf{C}_{ ext{SM}} + \mathbf{C}_{ ext{off}} + \mathbf{C}_{ ext{$$

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Novel Approach --New Physics beyond the reach of modern Colliders

Probe BSM Physics at Low Energies (MeV-GeV)

Low-Energy (MeV-GeV) Accelerator & Atmospheric **v**s travelling terrestrial distances (few m - 1000s of km)

Accelerator: DUNE@USA, T2HK@Japan Atmospheric: DeepCore, DUNE, Hyper-K, INO

Expected to measure oscillation parameters with a precision around a few % -- sensitive to sub-leading BSM physics at low energies

Complement BSM search @ High-Energy Colliders

Golden Age of Neutrino Physics (1998 – 2024 & Beyond)



Over the last two decades or so, marvelous data from world-class experiments

- Solar neutrinos (ν_e)
- **I** Atmospheric neutrinos $(\nu_{\mu}, \bar{\nu}_{\mu}, \nu_{e}, \bar{\nu}_{e})$
- Reactor anti-neutrinos ($\bar{\nu}_e$)
- Accelerator neutrinos $(\nu_{\mu}, \bar{\nu}_{\mu})$

Data from various neutrino sources and vastly different energy and distance scales

Neutrinos change their flavor as they move in space and time

We have just started our journey in the mysterious world of neutrinos

Three-Flavor Neutrino Oscillation Framework: Simple & Robust

It happens because flavor (weak) eigenstates do not coincide with mass eigenstates $c_{ij} = \cos \theta_{ij}$ and $s_{ij} = \sin \theta_{ij}$ $\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$ θ_{23} : P($v_{\mu} \rightarrow v_{\mu}$) by θ_{12} : P($v_e \rightarrow v_e$) by θ₁₃: P(ν_e→ν_e) by Reactor ν $\theta_{13} \& \delta$: P($\nu_{\mu} \rightarrow \nu_{e}$) by ν beam Atoms. v and v beam Reactor and solar v $\begin{bmatrix} L/E = 500 \text{ km/GeV} \\ \Delta m_{31}^2 \sim 2.5 \times 10^{-3} \text{ eV}^2 & P(v_{\alpha} \rightarrow v_{\beta}) = \sin^2 2\theta_{ij} * \sin^2 \left(1.27 \Delta m_{ij}^2 \frac{L}{E}\right) & \Delta m_{21}^2 \sim 7.6 \times 10^{-5} \text{ eV}^2 \end{bmatrix}$ L/E = 15,000 km/GeVThree mixing angles: $|\theta_{23}, \theta_{13}, \theta_{12}|$ and one CP-violating (Dirac) phase $|\delta_{CP}|$ $\tan^2 \theta_{12} \equiv \frac{|U_{e2}|^2}{|U_{e1}|^2}; \quad \tan^2 \theta_{23} \equiv \frac{|U_{\mu3}|^2}{|U_{\pi3}|^2}; \quad U_{e3} \equiv \sin \theta_{13} e^{-i\delta}$ 3 mixing angles simply related to flavor components of 3 mass eigenstates

Over a distance L, changes in the relative phases of the mass states may induce flavor change

$$\begin{pmatrix}
P(\nu_{\alpha} \rightarrow \nu_{\beta}) = \delta_{\alpha\beta} - 4 \sum_{i>j} \operatorname{Re}[U_{\alpha i}^{*}U_{\alpha j}U_{\beta i}U_{\beta j}^{*}] \sin^{2}\Delta_{ij} - 2 \sum_{i>j} \operatorname{Im}[U_{\alpha i}^{*}U_{\alpha j}U_{\beta i}U_{\beta j}^{*}] \sin 2\Delta_{ij}, \\
\int \Delta_{ij} = \Delta m_{ij}^{2}L/4E_{\nu} \\
\Delta m_{ij}^{2} = m_{i}^{2} - m_{j}^{2}
\end{cases}$$

eplace o_{CP} by -o_{CP}

S. K. Agarwalla, Understanding the Universe through Neutrinos, ICTS-TIFR, Bengaluru, Karnataka, India, 29th April to 1st May 2024

Three-Flavor Neutrino Oscillations



 $= R(\theta_{23}) \cdot R(\theta_{13}, \delta_{CP}) \cdot R(\theta_{12})$



- Oscillations among the three neutrino flavors depend on:
 - The mixing matrix
 - $\theta_{23}, \theta_{13}, \delta_{CP}, \theta_{12}$
 - The mass differences
 - $\Delta m_{32}^2, \Delta m_{21}^2$

 $\Delta m_{21}^2 \to O(10^{-5} \mathrm{eV}^2)$

The Pontecorvo-Maki-Nakagawa-Sakata Matrix

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{CP}} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta_{CP}} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta_{CP}} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta_{CP}} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta_{CP}} & c_{23}c_{13} \end{pmatrix}$$

$$egin{aligned} heta_{12} = 33.41^{\circ\,+0.75^{\circ}}_{-0.72^{\circ}} & heta_{23} = 49.1^{\circ\,+1.0^{\circ}}_{-1.3^{\circ}} & heta_{13} = 8.54^{\circ\,+0.11^{\circ}}_{-0.12^{\circ}} & heta_{ ext{CP}} = 197^{\circ\,+42^{\circ}}_{-25^{\circ}} & heta_{ ext{CP}} = 197^{\circ\,+42^{\circ}}_{-25^{\circ}} & heta_{ ext{CP}} = 107^{\circ\,+42^{\circ}}_{-25^{\circ}} & heta_{ ext{CP}} = 107^{\circ\,+42^{\circ}}_{-25^$$

w/o Super-K atmospheric neutrino data assuming normal mass ordering

	$ U_{\mathrm{e1}} $	$ U_{ m e2} $	$ U_{ m e3} $		$0.803\sim 0.845$	$0.514\sim 0.578$	$0.142\sim 0.155$
U =	$ U_{\mu 1} $	$ U_{\mu 2} $	$ U_{\mu 3} $	=	$0.233 \sim 0.505$	$0.460\sim 0.693$	$0.630 \sim 0.779$
	$ U_{ au 1} $	$ U_{ au2} $	$ U_{ au3} $		$0.262\sim 0.525$	$0.473 \sim 0.702$	$0.610\sim 0.762$

3σ ranges (99.73% C.L.) for the magnitudes of the elements of the PMNS matrix (NuFIT.org)

+ Neutrino mixings in the PMNS matrix are large as compared to the quark mixings in the CKM matrix

- + In the CKM matrix, the quark mixing angles are $\theta_{12} = 13.04^{\circ} \pm 0.05^{\circ}$, $\theta_{23} = 2.38^{\circ} \pm 0.06^{\circ}$, $\theta_{13} = 0.201^{\circ} \pm 0.011^{\circ}$
- + Neutrino mixings are inconsistent with TBM neutrino mixing ($\theta_{12} \approx 35.3^{\circ} \theta_{23} \approx 45^{\circ} \theta_{13} = 0^{\circ}$) at > 5 σ

Neutrino Mass Ordering: Important Open Question

I The sign of Δm_{31}^2 $(m_3^2 - m_1^2)$ is not known



Matter effect inside the Sun played an important role to fix the ordering between m₂ & m₁

Matter effect inside the Earth will play a crucial role to fix the ordering between m₃ & m₁

Mass Ordering Discrimination : A Binary yes-or-no type question

Octant of 2-3 Mixing Angle: Important Open Question

- \rightarrow In v_µ survival probability, the dominant term is mainly sensitive to sin²2 θ_{23}
 - → If $\sin^2 2\theta_{23}$ differs from 1 (recent hints), we get two solutions for θ_{23}
 - → One in lower octant (LO: $\theta_{23} < 45$ degree)
 - → Other in higher octant (HO: $\theta_{23} > 45$ degree)



Octant ambiguity of θ_{23} Fogli and Lisi, hep-ph/9604415

 $v_{\mu} \rightarrow v_{e}$ oscillation channel can break this degeneracy Preferred value would depend on the choice of neutrino mass ordering Leptonic CP Violation: Important Open Question

Is CP violated in the neutrino sector, as in the quark sector?

Mixing can cause CPV in neutrino sector, provided $\delta_{CP} \neq 0^{\circ}$ and 180° Need to measure the CP-odd asymmetries:

$$\Delta P_{\alpha\beta} \equiv P(\nu_{\alpha} \to \nu_{\beta}; L) - P(\bar{\nu}_{\alpha} \to \bar{\nu}_{\beta}; L) \ (\alpha \neq \beta)$$

$$\Delta P_{e\mu} = \Delta P_{\mu\tau} = \Delta P_{\tau e} = 4J_{CP} \times \left[\sin\left(\frac{\Delta m_{21}^2}{2E}L\right) + \sin\left(\frac{\Delta m_{32}^2}{2E}L\right) + \sin\left(\frac{\Delta m_{13}^2}{2E}L\right) \right]$$

Jarlskog CP-odd Invariant $\rightarrow J_{CP} = \frac{1}{8} \cos \theta_{13} \sin 2\theta_{13} \sin 2\theta_{23} \sin 2\theta_{12} \sin \delta_{CP}$

Three-flavor effects are key for CPV, need to observe interference

Conditions for observing CPV: 1) Non-degenerate masses \checkmark 2) Mixing angles $\neq 0^{\circ} \& 90^{\circ} \checkmark$ 3) $\delta_{CP} \neq 0^{\circ}$ and 180° (Hints)

Quark Mixing vs. Neutrino Mixing

$ V_{\rm CKM} =$	$egin{pmatrix} 0.97435 \pm 0.0\ 0.22486 \pm 0.0\ 0.00857^{+0.00}_{-0.00} \end{bmatrix}$	$\begin{array}{cccc} 00016 & 0.22500 \\ 00067 & 0.97349 \\ 0020 & 0.0411 \\ 0018 \end{array}$	± 0.00067 ± 0.00016 $10^{+0.00083}_{-0.00072}$	0.00369 ± 0.000 $0.04182^{+0.00085}_{-0.00074}$ $0.999118^{+0.00003}_{-0.00003}$ PDG 2	$ \begin{array}{c} 11 \\ 5 \\ 4 \\ 31 \\ 36 \end{array} $ 2022
	(0.801 -	→ 0.845 0.5	$513 \rightarrow 0.579$	$0.144 \rightarrow 0.1$.56
$ U _{3\sigma \text{ PMNS}}^{\text{with SK-at}}$	m = 0.244 -	→ 0.499 0.5	$505 \rightarrow 0.693$	$0.631 \rightarrow 0.7$	68
	(0.272 -	→ 0.518 0.4	$471 \rightarrow 0.669$	$0.623 \rightarrow 0.7$	′61

NuFIT 5.1 (2021)

The goal is to achieve the CKM level precision for the PMNS A Long Journey Ahead! But the precision is improving rapidly for PMNS

Good News: There may be large CPV in neutrino sector than quark sector

$$J_{CP} = \frac{1}{8}\cos\theta_{13}\,\sin 2\theta_{13}\,\sin 2\theta_{23}\,\sin 2\theta_{12}\,\sin \delta_{CP}$$

 $J_{\rm CKM} \sim 3~\times~10^{\text{-5}},$ whereas $J_{\rm PMNS}$ can be as large as 3 $\times~10^{\text{-2}}$

CP Violation: Necessary Requirement for Matter-Antimatter Asymmetry

Five irreducible CP-Violating Phases in the v Standard Model

In the Quark Sector:

+ The CP-odd phase in the CKM matrix – measured to be $\gamma \simeq 70^{\circ}$ - Governs all the CP-violating phenomena observed so far

+ The strong CP-phase θ of the QCD Vacuum
 - Known to be vanishingly small < 10⁻¹⁰

In the Lepton Sector:

+ The Dirac CP-odd phase δ_{CP} in the 3 × 3 unitary ν mixing matrix - Can be measured in ν oscillation experiments (hints)

+ The Majorana neutrinos can have two more CP-violating phases
- No effect in v oscillations, only affect LNV processes (unknown)

The CKM CP phase <u>is not responsible</u> for the baryon asymmetry of the Universe

The PMNS CP phase <u>is the only hope</u>

The discovery of <u>non-zero CP-violating phase</u> δ_{CP} in neutrino oscillation experiments would be a strong indication (even if not a proof) of <u>leptogenesis</u> as the origin of the <u>baryon asymmetry of the Universe</u>

The determination of CP violation requires the full interplay of <u>3-flavor effects in neutrino oscillations</u>

Three-Flavor Effects in $v_{\mu} \rightarrow v_{e}$ *Oscillation Channel*

The appearance probability $(\nu_{\mu} \rightarrow \nu_{e})$ in matter, upto second order in the small parameters $\alpha \equiv \Delta m_{21}^2 / \Delta m_{31}^2$ and $\sin 2\theta_{13}$, $\frac{\sin^2 2\theta_{13} \sin^2 \theta_{23}}{(1-\hat{A})^2} \longrightarrow \theta_{13} \operatorname{driven}$ $\frac{\alpha \sin 2\theta_{13}}{\hat{\xi}} \sin \delta_{CP} \sin(\Delta) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin[(1-\hat{A})\Delta]}{(1-\hat{A})} \Longrightarrow CP\text{-odd}$ Resolves 0.009octant $+ \alpha \sin 2\theta_{13} \xi \cos \delta_{CP} \cos(\Delta) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin[(1-\hat{A})\Delta]}{(1-\hat{A})} \Longrightarrow \text{CP-even}$ + $(\alpha^2)\cos^2\theta_{23}\sin^22\theta_{12}\frac{\sin^2(\hat{A}\Delta)}{\hat{A}^2};$ \implies Solar Term where $\Delta \equiv \Delta m_{31}^2 L/(4E)$, $\xi \equiv \cos \theta_{13} \sin 2\theta_{21} \sin 2\theta_{23}$, and $\hat{A} \equiv \pm (2\sqrt{2}G_F n_e E)/\Delta m_{31}^2$ Cervera et al., hep-ph/0002108 changes sign with $sgn(\Delta m_{31}^2)$ changes sign with polarity Freund et al., hep-ph/0105071 key to resolve hierarchy! causes fake CP asymmetry! Agarwalla et al., e-Print: 1302.6773 [hep-ph]

This channel suffers from: (Hierarchy $-\delta_{CP}$) & (Octant $-\delta_{CP}$) degeneracies. How can we break them?

Hierarchy – δ_{CP} *degeneracy in* $\nu_{\mu} \rightarrow \nu_{e}$ *oscillation channel*



Octant – δ_{CP} *degeneracy in* $\nu_{\mu} \rightarrow \nu_{e}$ *oscillation channel*



Unfavorable CP values for neutrino are favorable for antineutrino & vice-versa

Agarwalla, Prakash, Sankar, arXiv: 1301.2574

Oscillation Probabilities with One Mass Scale Dominance

$$\begin{aligned} \tan ke \ \Delta m_{21}^2 &= 0 \\ A &= 2\sqrt{2}G_F N_e E_\nu \end{aligned} \qquad \begin{array}{l} P_{\mu\mu}^{approx} &= 1 - \sin^2 \theta_{13}^M \sin^2 2\theta_{23} \sin^2 \frac{\left[(\Delta m_{31}^2 + A) - (\Delta m_{31}^2)^M\right]L}{8E_\nu} \\ &- \cos^2 \theta_{13}^M \sin^2 2\theta_{23} \sin^2 \frac{\left[(\Delta m_{31}^2 + A) + (\Delta m_{31}^2)^M\right]L}{8E_\nu} \\ &- \sin^2 2\theta_{13}^M \sin^4 \theta_{23} \sin^2 \frac{(\Delta m_{31}^2)^M L}{4E_\nu} , \end{aligned}$$

$$P_{e\mu}^{approx} = \sin^2 2\theta_{13}^M \sin^2 \theta_{23} \sin^2 \frac{(\Delta m_{31}^2)^M L}{4E_\nu}$$

where,

$$(\Delta m_{31}^2)^M = \left((\Delta m_{31}^2 \cos 2\theta_{13} - A)^2 + \Delta m_{31}^2 \sin^2 2\theta_{13} \right)^{1/2}$$
$$\sin^2 2\theta_{13}^M = \frac{\Delta m_{31}^2 \sin^2 2\theta_{13}}{\left((\Delta m_{31}^2 \cos 2\theta_{13} - A)^2 + \Delta m_{31}^2 \sin^2 2\theta_{13} \right)}.$$

Choubey, Roy, hep-ph/0509197v2

- If θ_{13} would have been zero, there is no Earth matter effect
- No discrimination between Normal Ordering and Inverted Ordering
- Large $\theta_{13} \rightarrow$ good news for Neutrino Mass Ordering

Correlations & Degeneracies between 1-3 & 2-3 Mixing Angles



Capozzi, Valentino, Lisi, Marrone, Melchiorri, Palazzo, arXiv:2107.00532v2 [hep-ph]

Correlations & Degeneracies between 2-3 Oscillation Parameters



Capozzi, Valentino, Lisi, Marrone, Melchiorri, Palazzo, arXiv:2107.00532v2 [hep-ph]

S. K. Agarwalla, Understanding the Universe through Neutrinos, ICTS-TIFR, Bengaluru, Karnataka, India, 29th April to 1st May 2024

Correlations & Degeneracies between CP Phase & 2-3 Mixing Angle



Capozzi, Valentino, Lisi, Marrone, Melchiorri, Palazzo, arXiv:2107.00532v2 [hep-ph]

Tension between Solar and KamLAND data removed



< 2 σ tension between Solar and KamLAND data

Capozzi, Lisi, Marrone, Palazzo, arXiv:1804.09678v1 [hep-ph]

The tension is removed now! Due to a slightly smaller day-night asymmetry in SK-IV 2970-day Solar data

Capozzi, Valentino, Lisi, Marrone, Melchiorri, Palazzo, arXiv:2107.00532v1 [hep-ph]

Global Fit of Neutrino Oscillation Parameters Circa 2022

Preference for Normal Mass Ordering (~ 2.5 σ), θ_{23} < 45 degree and sin δ < 0 (both at 90% C.L.)



Capozzi, Valentino, Lisi, Marrone, Melchiorri, Palazzo, arXiv:2107.00532v2 [hep-ph]

Parameter	Ordering	Best fit	3σ range	"1σ" (%)
$\delta m^2/10^{-5}~{\rm eV^2}$	NO, IO	7.36	6.93 - 7.93	2.3
$\sin^2 \theta_{12}/10^{-1}$	NO, IO	3.03	2.63 - 3.45	4.5
$ \Delta m^2 /10^{-3} \text{ eV}^2$	NO	2.485	2.401 - 2.565	1.1
	IO	2.455	2.376 - 2.541	1.1
$\sin^2 \theta_{13} / 10^{-2}$	NO	2.23	2.04 - 2.44	3.0
	IO	2.23	2.03 - 2.45	3.1
$\sin^2 \theta_{23}/10^{-1}$	NO	4.55	4.16 - 5.99	6.7
	IO	5.69	4.17 - 6.06	5.5
δ/π	NO	1.24	0.77 - 1.97	16
	IO	1.52	1.07 - 1.90	9
$\Delta \chi^2_{\rm IO-NO}$	IO-NO	+6.5		

Capozzi, Valentino, Lisi, Marrone, Melchiorri, Palazzo, arXiv:2107.00532v1 [hep-ph]

See also, Esteban, Gonzalez-Garcia, Maltoni, Schwetz, Zhou, arXiv:2007.14792v1 [hep-ph]

See also, de Salas, Forero, Gariazzo, Martinez-Mirave, Mena, Ternes, Tortolla, Valle, arXiv:2006.11237v2 [hep-ph]

Remarkable Precision on Neutrino Oscillation Parameters



Robust three-flavor neutrino oscillation paradigm

Agarwalla, Kundu, Prakash, Singh, JHEP 03 (2022) 206

Atmospheric Neutrinos

Atmospheric Neutrinos



Atmospheric Flux Ratio



Upward and Downward Directions for Atmospheric Neutrinos



$$L_{\nu} = \sqrt{(R+h)^2 - (R-d)^2 \sin^2 \theta_{\nu}} - (R-d) \cos \theta_{\nu}$$

 $\begin{array}{l} {\rm R} = {\rm radius \ of \ Earth \ (6371 \ km)} \\ {\rm h} = {\rm average \ } \nu \ {\rm production \ height \ from \ surface \ (\sim \ 10 \ to \ 25 \ km)} \\ {\rm d} = {\rm depth \ of \ the \ detector \ underground \ (\sim \ 100 \ m \ to \ 2 \ km)} \end{array}$

Upward-going neutrinos feel Earth's matter effect during oscillations inside Earth – key for neutrino oscillation tomography of Earth

Atmospheric Flux: Up/Down Symmetry



Atmospheric Neutrino Flux



Athar, Honda, Kajita, Kasahara, Midorikawa, PLB 718 (2013) 1375 - 1380

S. K. Agarwalla, Understanding the Universe through Neutrinos, ICTS-TIFR, Bengaluru, Karnataka, India, 29th April to 1st May 2024

Atmospheric Neutrino Flux: Effect of Geomagnetic Field



Athar, Honda, Kajita, Kasahara, Midorikawa, PLB 718 (2013) 1375 - 1380

Atmospheric Neutrinos





- Almost isotropic flux up-down symmetric
- Known flavor composition $(\nu_{\rm e}, \nu_{\mu}, \text{ and their antiparticles})$
- Wide range of energies (MeV to PeV)
- Steeply falling power-law spectrum

Detection of Atmospheric Neutrinos



Detector in Kolar Gold Fields

DETECTION OF MUONS PRODUCED BY COSMIC RAY NEUTRINO DEEP UNDERGROUND

C. V. ACHAR, M. G. K. MENON, V. S. NARASIMHAM, P. V. RAMANA MURTHY and B. V. SREEKANTAN, Tata Institute of Fundamental Research, Colaba, Bombay

> K. HINOTANI and S. MIYAKE, Osaka City University, Osaka, Japan

D.R. CREED, J.L. OSBORNE, J.B.M. PATTISON and A.W. WOLFENDALE University of Durham, Durham, U.K.

Received 12 July 1965

Physics Letters 18, (1965) 196 (15th Aug 1965)

EVIDENCE FOR HIGH-ENERGY COSMIC-RAY NEUTRINO INTERACTIONS*

F. Reines, M. F. Crouch, T. L. Jenkins, W. R. Kropp, H. S. Gurr, and G. R. Smith

Case Institute of Technology, Cleveland, Ohio

and

J. P. F. Sellschop and B. Meyer

University of the Witwatersrand, Johannesburg, Republic of South Africa (Received 26 July 1965)

PRL 15, (1965) 429 (30th Aug 1965)
PREM and Neutrino Trajectories Deep Inside the Earth



S. K. Agarwalla, Understanding the Universe through Neutrinos, ICTS-TIFR, Bengaluru, Karnataka, India, 29th April to 1st May 2024

Event Signatures in Super-Kamiokande

muon from ν_{μ}



electron from v_{e}



 detector responsible for discovery of atmospheric ν oscillations (1998), being used for T2K to measure ν_µ → ν_e oscillations with accelerator ν's

Each dot is one phototube, and its color represents the relative amount of light it collected, in terms of the amount of electric charge produce by the phototube, during the 1.3 μ s time window in which the displayed data were logged. The location and shape of the ring tell us the direction of the outgoing charged particle.

DeepCore Detector



- Uses IceCube as VETO
- Fiducial volume ~ 10 Mton

The design and performance of IceCube DeepCore (2012): Astroparticle Physics, 35(10), 615-624 (2012)

Event Signatures in IceCube



Track-like events:

- Elongated
- Source: ν_{μ} CC





Cascade-like events:

- Spherical
- Source: v_e CC, v_τ CC, all NC



Size of the colored sphere: amount of photon/energy observed in a DOM

Neutrino Oscillations in Matter: MSW Effect

- The MSW Effect (Wolfenstein 1978, Mikheyev and Smirnov 1985)
- Matter can change the pattern of neutrino oscillations significantly
- Resonant enhancement of oscillations and resonant flavor conversion possible
- Causes flavor conversion of solar neutrinos (LMA MSW solution established)



Lincoln Wolfenstein



Stanislav Mikheyev



Alexei Smirnov

Neutrino Oscillations in Matter: MSW Effect

Neutrino propagation through matter modify the oscillations significantly <u>Coherent forward</u> scattering of neutrinos with matter particles Charged current interaction of v_e with electrons creates an <u>extra potential</u> for v_e MSW matter term: $A = \pm 2\sqrt{2}G_F N_e E$ or $A(eV^2) = 0.76 \times 10^{-4}\rho$ (g/cc)E(GeV)N_e = electron number density , + (-) for neutrinos (antineutrinos) , ρ = matter density in Earth

Matter term changes sign when we switch from neutrino to antineutrino

 $P(\nu_{\alpha} \rightarrow \nu_{\beta}) - P(\bar{\nu}_{\alpha} \rightarrow \bar{\nu}_{\beta}) \neq 0$ even if δ_{CP} = 0, causes fake CP asymmetry

Matter term modifies oscillation probability differently depending on the sign of Δm^2

$$\Delta m^{2} \simeq A \quad \Leftrightarrow \quad E_{\text{res}}^{\text{Earth}} = 6 - 8 \text{ GeV} \quad \Longrightarrow \quad \text{Resonant conversion} - \text{Matter effect}$$

$$\boxed{\frac{\nu \quad \bar{\nu}}{\Delta m^{2} > 0}}_{\Delta m^{2} < 0} \quad \underbrace{\text{MSW}}_{-} \quad \blacksquare \quad \text{Resonance occurs for neutrinos (antineutrinos)}}_{\text{if } \Delta m^{2} \text{ is positive (negative)}}$$

Effective Mixing Angles in the presence of Matter Effect



S. K. Agarwalla, Understanding the Universe through Neutrinos, ICTS-TIFR, Bengaluru, Karnataka, India, 29th April to 1st May 2024

Neutrino Oscillation Length Resonance / Parametric Resonance

- Oscillations of atmospheric neutrinos inside Earth can feel this resonance when neutrino trajectories cross the core of Earth
- The probabilities of neutrino flavor transitions can be strongly enhanced if the oscillation phase undergoes certain modification in matter
- This can happen if the variation in the matter density along the neutrino path is correlated in a certain way with the change in the oscillation phase
- This amplification of the neutrino oscillation probability in matter due to specific phase relationships can get accumulated if the matter density profile along the neutrino path repeats itself (periodic)

Petcov 1998, Liu and Smirnov 1998, Akhmedov 1998

Parametric Resonance inside Earth



- Resonance occurs when frequency of density modulation matches with the frequency of oscillation
- Oscillation probability in PREM profile starts to differ from uniform density profile, once it sees the density jump in PREM at the coremantle boundary (3480 km)
- Significant enhancement in probability in PREM is visible for corepassing trajectories due to parametric resonance



Matter Resonances inside Earth



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Matter Resonances inside Earth



Similar oscillation patterns for antineutrinos with inverted mass ordering

Neutrino Oscillation Probabilities for a Core-Passing Track-Like Events



Similar oscillation patterns for antineutrinos with inverted mass ordering

Neutrino Oscillation Probabilities for a Core-Passing Cascade-Like Events



Similar oscillation patterns for antineutrinos with inverted mass ordering

Atmospheric Neutrino Anomaly

Super-Kamiokande

Double ratio:





K.S. Hirata, et al., Experimental study of the atmospheric neutrino flux, Phys. Lett. B 205 (1988) 416.



Zenith angle dependence



- Electron neutrinos match predictions
- High energy ν_{μ} from above: match predictions
- High energy ν_{μ} through the earth: partially lost
- Low energy ν_{μ} : lost even when coming from above, loss while passing through the Earth even greater

Neutrino Flavor Oscillations

Flavor States: v_e and v_µ (produced in Weak Interactions)
 Mass Eigenstates: v₁ and v₂ (propagate from Source to Detector)

A Flavor State is a linear superposition of Mass Eigenstates



If the masses of these two states are different, then they will take different times to reach the same point and there will be a phase difference and hence interference

Two Neutrino Mixing



Oscillation Dip in Muon Neutrino Survival Probability

Atmospheric neutrinos have access to a wide range of baselines:

- Vertically downward-going neutrinos: 15 km
- Vertically upward-going neutrinos: 12757 km

For $E_{\nu} = 1$ GeV:

- At smaller baselines: neutrino oscillations are not developed
- At larger baselines: about 50% ν_{μ} have oscillated
- At certain baselines: about 100% ν_{μ} have oscillated

Oscillation dip feature corresponds to the case when all muon neutrinos are oscillated, i.e. $P(\nu_{\mu} \rightarrow \nu_{\mu}) = 0.$



Oscillation Dip in Muon Neutrino Survival Probability

The L/E dependence of survival probability $P(\nu_{\mu} \rightarrow \nu_{\mu})$ in two-flavor oscillation is given as:

$$P(
u_{\mu}
ightarrow
u_{\mu}) = 1 - \sin^2 2 heta_{23} \cdot \sin^2 \left(1.27 \cdot |\Delta m_{32}^2| \left(\mathrm{eV}^2
ight) \cdot rac{L_{
u} \, (\mathrm{km})}{E_{
u} \, (\mathrm{GeV})}
ight)$$



$$\frac{1.27\Delta m_{32}^2 L_{\nu}}{E_{\nu}} = \frac{\pi}{2}$$
$$\frac{L_{\nu}}{E_{\nu}} = 515.35 \text{ km/GeV \& } \log_{10}\left(\frac{L_{\nu}}{E_{\nu}}\right) = 2.71$$





Solution to the Atmospheric Neutrino Anomaly



- Indeed, more ν_μ travelling through the Earth are lost
- The zenith angle dependence fits the form of the probability expressions exactly
- Neutrino oscillation hypothesis proved!



Atmospheric Neutrino Oscillation



1998 to 2015: Impressive Journey of Atmospheric Neutrinos establishing Neutrino Oscillations

L/E Dependence of Super-K Atmospheric Neutrino Data



- A scan in $\Delta \varkappa^2$ for oscillation frequency proportional to L × E⁻ⁿ
- The oscillation frequency due to neutrino mass has an index of n
 = 1, which is the index that best fits the Super-Kamiokande atmospheric neutrino data
- Alternate models of muon neutrino deficit (such as neutrino decay, decoherence, Lorentz violation) may be found that have n ≠ 1, however the Super-Kamiokande data favors L/E dependence, i.e., n = 1

T. Kajita, E. Kearns, M. Shiozawa (Super-Kamiokande Collaboration), Nuclear Physics B 908 (2016) 14-29

L/E Dependence of Super-K Atmospheric Neutrino Data



- The ratio of data to MC events (in the absence of neutrino oscillation) as a function of the reconstructed L/E
- Solid red line: the best-fit threeflavor expectation for neutrino oscillation
- The dashed blue line: the best-fit expectation for neutrino decay
- The dotted green line: the bestfit expectation for neutrino decoherence

There is more than 4σ evidence for a dip in the rate of muon neutrinos near 500 GeV/km supporting the L/E dependence of mass-induced neutrino flavor transition. The observation of this dip is crucial to reject the other hypotheses of neutrino oscillation

T. Kajita, E. Kearns, M. Shiozawa (Super-Kamiokande Collaboration), Nuclear Physics B 908 (2016) 14-29

Oscillation Dip in Muon Neutrino Survival Probability

Three-flavor oscillation framework in the presence of Earth's matter (PREM profile)



Anil Kumar, Amina Khatun, Sanjib Kumar Agarwalla, Amol Dighe, EPJC 81 (2021) 2, 190, arXiv: 2006.14529

- Oscillation dip can be observed around $\log_{10} (L_{\nu}/E_{\nu}) = 2.7$
- Matter effect in $P(\nu_{\mu} \rightarrow \nu_{\mu})$ for the case of neutrino (due to normal mass ordering) can be observed around $\log_{10} (L_{\nu}/E_{\nu}) = 3.0$

Oscillation Valley in Muon Neutrino Survival Probability



Kumar, Khatun, Agarwalla, Dighe, EPJC 81 (2021) 2, 190

Oscillation Valley in Muon Neutrino Survival Probability

Neutrinos (antineutrinos) feel Earth's matter effect for normal (inverted) mass ordering



S. K. Agarwalla, Understanding the Universe through Neutrinos, ICTS-TIFR, Bengaluru, Karnataka, India, 29th April to 1st May 2024

Latest Oscillation Results from DeepCore



- These new result are compatible & complementary with the existing measurements
 - High-precision measurement on Δm²₃₂
- Very high-energy sample (5 100 GeV) & different systematic uncertainties
 - Strong validation of the standard 3-flavor oscillation



ICRC2023 arXiv:2307.15855

A New Extension of DeepCore: IceCube Upgrade

- 2 Mton of dense instrumentation for low-energy measurements
- 7 new strings in the center region of detector: energy threshold ~ 1 GeV
- Higher event rate: 4 x DeepCore
- To be deployed in the Antarctic summer of 2025/26





30 GeV Neutrino

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Sensitivity of IceCube Upgrade: Atmospheric Oscillation Parameters



ICRC2023 arXiv:2307.15295

- 90% confidence level after 3 years with the new strings assuming NuFit 5.2 best-fit values
- With the new strings, IceCube's sensitivity to Δm_{31}^2 and θ_{23} increases by about 20 to 30%
- 4 times enhancement in the sensitivity to neutrino mass ordering

Superbeams



Traditional approach: Neutrino beam from pion decay

The Pursuit of Leptonic CPV in LBL Experiments



The whole idea is based on comparing the rates of two CP-mirror-image processes

Above experimental approach is a perfectly valid probe of leptonic CPV regardless of whether neutrinos are Dirac or Majorana particles

Accelerator Long-Baseline Neutrino Experiments

 $v_{\mu} \rightarrow v_{e}$ and $\overline{v}_{\mu} \rightarrow \overline{v}_{e}$: Appearance Channel

 $v_{\mu} \rightarrow v_{\mu}$ and $\overline{v}_{\mu} \rightarrow \overline{v}_{\mu}$: Disappearance Channel

T2K (Japan) & NOvA (USA) [running, off-axis]

FD: 295 km FD: 810 km 1st Osc. Max. ~ 0.6 GeV 1st Osc. Max. ~ 1.6 GeV narrow-band beam

DUNE (USA) [upcoming, on-axis]

FD: 1285 km 1st Osc. Max. ~ 2.6 GeV

wide-band beam

T2HK (Japan) [upcoming, off-axis]

FD: 295 km 1st Osc. Max. ~ 0.6 GeV

narrow-band beam

Current Long-Baseline Experiments: T2K and NOvA



T2K and NOvA operate at different energies and baselines

Complement each other and help to remove degeneracies among various oscillation parameters





Latest CP Measurements from T2K and NOvA



Complementarity between T2K & NOvA

Both T2K & NOvA individually show a slight preference for NMO

NMO: T2K excludes large regions of the NOvA constraints at 90% C.L., & NOvA excludes parts of T2K's 90% C.L. region

IMO: Both the experiments consistently favour the $\pi < \delta_{CP} < 2\pi$ region, with a weak preference for the upper octant

Both the experiments need more data (at present statistically limited) to have better measurements

Joint oscillation analyses between T2K, Super-K, & NOvA would be very helpful

> T2K: arXiv:2303.03222 [hep-ex] NOvA: arXiv: 2108.08219 [hep-ex]

Future Long-Baseline Experiments: DUNE, T2HK, and T2HKK





Essential Features of DUNE, T2HK (JD), and T2HKK (JD+KD)

Characteristics	DUNE	JD/KD
Baseline (km)	1285	295 (1100)
$ ho_{ m avg}~(m g/cm^3)$	2.848	2.7(2.8)
Beam Type	wide-band, on-axis	narrow-band, 2.5° off-axis
Beam Power	1.2 MW	1.3 MW
Proton Energy	$120 {\rm GeV}$	$30 { m GeV}$
P.O.T./year	1.1×10^{21}	2.7×10^{22}
Flux peaks at (GeV)	2.5	0.6
1^{st} (2^{nd}) oscillation maxima	2.6(0.87)	$0.6\ (0.2)\ /\ 1.8\ (0.6)$
for appearance channel (GeV)		
Detector mass (kt)	40, LArTPC	187 each, water Cherenkov
Runtime $(\nu + \bar{\nu})$ yrs	5 + 5	2.5 + 7.5
Exposure (kt·MW·yrs)	480	2431
Signal Norm. Error (App.)	2%	5% (2.7%)
Signal Norm. Error (Disapp.)	5%	3.5%

DUNE Collaboration: arXiv:2103.04797 [hep-ex]

Hyper-Kamiokande Collaboration: arXiv:1611.06118 [hep-ex]

Due to upgraded ND280 & a new Intermediate Water Cherenkov Detector (IWCD) ~ at 1 km
CP Violation in DUNE for three different choices of θ_{23}



CP violation sensitivity deteriorates around maximal mixing choices of true θ_{23} while minimizing over test θ_{23} in the fit. Why?

CP Coverage for Leptonic CP Violation at $\geq 3\sigma$ as a function of θ_{23}

mixing



S. K. Agarwalla, S. Das, A. Giarnetti, D. Meloni, and M. Singh, arXiv:2211.10620 [hep-ph]

High-Precision Measurement of Dirac CP Phase



DUNE + T2HK (JD) can measure any value of δ_{CP} with a 1 σ precision $\leq 10^{\circ}$

S. K. Agarwalla, S. Das, A. Giarnetti, D. Meloni, and M. Singh, in preparation

S. K. Agarwalla, Understanding the Universe through Neutrinos, ICTS-TIFR, Bengaluru, Karnataka, India, 29th April to 1st May 2024

Deviation from Maximal θ_{23}



Agarwalla, Kundu, and Singh, in preparation

Discovery of θ_{23} Octant



Agarwalla, Kundu, and Singh, in preparation

Precision Measurement of Atmospheric Oscillation Parameters



	Relative 1σ precision (%)							
Parameter	T2HK	DUNE	T2HK+DUNE	$T2K+NO\nu A$	Capozzi <i>et al</i> .	JUNO		
$\sin^2 \theta_{23}$	1.18	1.40	0.88	7.10	6.72			
Δm^2_{31}	0.25	0.31	0.20	0.99	1.09	0.2		

Agarwalla, Kundu, and Singh, in preparation

S. K. Agarwalla, Understanding the Universe through Neutrinos, ICTS-TIFR, Bengaluru, Karnataka, India, 29th April to 1st May 2024

Precision Measurement of Atmospheric Oscillation Parameters



Agarwalla, Kundu, and Singh, in preparation

S. K. Agarwalla, Understanding the Universe through Neutrinos, ICTS-TIFR, Bengaluru, Karnataka, India, 29th April to 1st May 2024

Allowed Regions in Plane ($\sin^2\theta_{23} - \delta_{CP}$) Plane



Agarwalla, Kundu, and Singh, in preparation

S. K. Agarwalla, Understanding the Universe through Neutrinos, ICTS-TIFR, Bengaluru, Karnataka, India, 29th April to 1st May 2024

The Jiangmen Underground Neutrino Observatory (JUNO)



- 20 kt liquid scintillator detector with an unprecedented 3% energy resolution at 1 MeV
- Neutrino mass ordering measurement & improved precision on oscillation parameters

Interference effects in JUNO

The electron antineutrino survival probability in vacuum :

$$P_{ee}(L/E) = 1 - P_{21} - P_{31} - P_{32}$$

$$P_{21} = \cos^4(\theta_{13}) \sin^2(2\theta_{12}) \sin^2(\Delta_{21})$$

$$P_{31} = \cos^2(\theta_{12}) \sin^2(2\theta_{13}) \sin^2(\Delta_{31})$$

$$P_{32} = \sin^2(\theta_{12}) \sin^2(2\theta_{13}) \sin^2(\Delta_{32})$$

$$\Delta_{ij} = 1.27 \Delta m_{ij}^2 L/E$$

Depending on the NMH, the oscillation frequency differs :



×10⁶



JUNO antineutrino energy spectrum:

Neutrino Mass Ordering with JUNO



Sensitivity does not depend on Earth matter effect, θ_{23} , and δ_{CP}



High-Precision Measurement of Oscillation Parameters with JUNO

Pup time	Parameter precision (%)					
Run time	$ \Delta m_{31}^2 $	Δm_{21}^2	$\sin^2 heta_{12}$	$\sin^2 \theta_{13}$		
$100 \mathrm{~days}$	0.8	1.0	1.9	47.9		
6 years	0.2	0.3	0.5	12.1		
20 years	0.1	0.2	0.3	7.3		
PDG 2020	1.3	2.4	4.2	3.2		



World-leading precision in 100 days!

Sub-precent precision in 6 years on solar oscillation parameters & atmospheric mass-squared splitting

JUNO Collaboration: Chinese Phys. C 46 123001 (2022)

Very Bright Future Ahead: Triumph of JUNO



Maxim Gonchar (JUNO Collaboration) EPS-HEP 2021, July 26

JUNO will improve significantly our knowledge on neutrino oscillation parameters. These developments are crucial to probe sub-leading three-flavor effects in next-generation long-baseline experiments for the discovery of NMO, leptonic CPV, and Octant of 2-3 mixing angle

The Two Fundamental Questions



	θ_{23}	θ_{13}	θ_{12}	δ
Leptons	$\sim 45^{\circ}$	8.5°	34°	?
Quarks	2.4°	0.20°	13°	69°

Why are lepton mixings so different from quark mixings?

The Flavor Puzzle!

Neutrino Oscillograms for a Core-Passing Track-Like Events



We get similar oscillograms for antineutrinos with inverted mass ordering

Neutrino Oscillograms for a Core-Passing Cascade-Like Events



We get similar oscillograms for antineutrinos with inverted mass ordering

Muon Neutrino Survival Probabilities with Varying CMB



Muon Neutrino Survival Oscillograms with Standard CMB



The Role of the CP-Violating CKM Phase

If the SM extensions do not violate CP (this would be rather unnatural), could the CKM phase generate the observed baryogenesis ?

KM CP-violating asymmetries, d_{CP} , must be proportional to the Jarlskog invariant J:

$$\boldsymbol{d}_{CP} = \boldsymbol{J} \cdot \tilde{\boldsymbol{F}}_{U} \cdot \tilde{\boldsymbol{F}}_{D}$$

where:
$$J = Im(V_{ud}V_{cs}V_{us}^*V_{cd}^*) \simeq A^2\lambda^6\eta$$
, and: $\tilde{F}_U = (m_t^2 - m_c^2) \cdot (m_t^2 - m_u^2) \cdot (m_c^2 - m_u^2)$
= $(3.1 \pm 0.2) \times 10^{-5}$ $\tilde{F}_D = (m_b^2 - m_s^2) \cdot (m_b^2 - m_d^2) \cdot (m_s^2 - m_d^2)$

- Since (some) non-zero quark masses are required, *CP* symmetry can only be broken where the Higgs field has already condensed to $v_T \neq 0$ (i.e., electroweak symmetry is broken)
- To make d_{CP} dimensionless, we divide by dimensioned parameter $D = T_c$ at the EW scale ($T_c = T_{EW} \sim 100 \text{ GeV}$), with [D] = GeV¹²

$$\hat{d}_{CP} = \frac{d_{CP}}{D^{12}} \approx 10^{-19} \ll \eta \approx O(10^{-10})$$

KM *CP* violation seems to be *irrelevant* for baryogenesis !