

Physics of Kagome Metals

Subhro Bhattacharjee

ICTS-TIFR, Bangalore



Santu Baidya
SNBNCBS \Rightarrow Rutgers



Aabhaas Mallik,
ICTS \Rightarrow Bar-Ilan



Adhip Agarwala
ICTS \Rightarrow IIT Gandhinagar



Tanusri Saha-Dasgupta
SNBNCBS

References :

1. Interplay of magnetism and topological superconductivity in bilayer kagome metals, PRL, 2020
2. Upcoming preprint

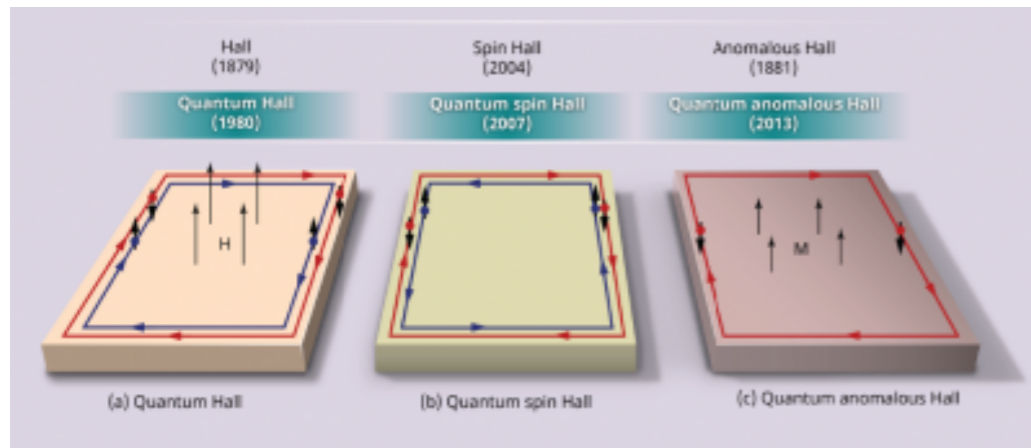
Funding :

1. SERB-DST
2. Max Planck Partner Group Grant

Two Central areas of excitement in present quantum condensed matter

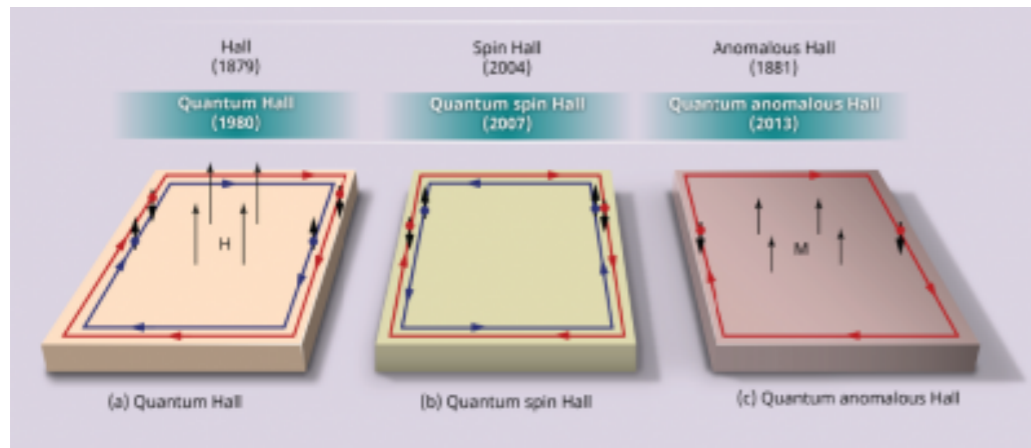
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Band Topology

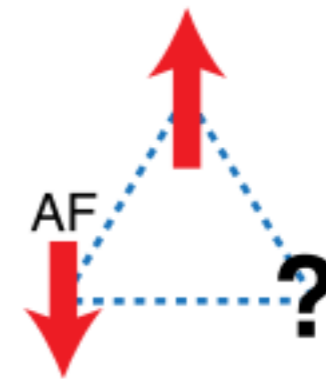


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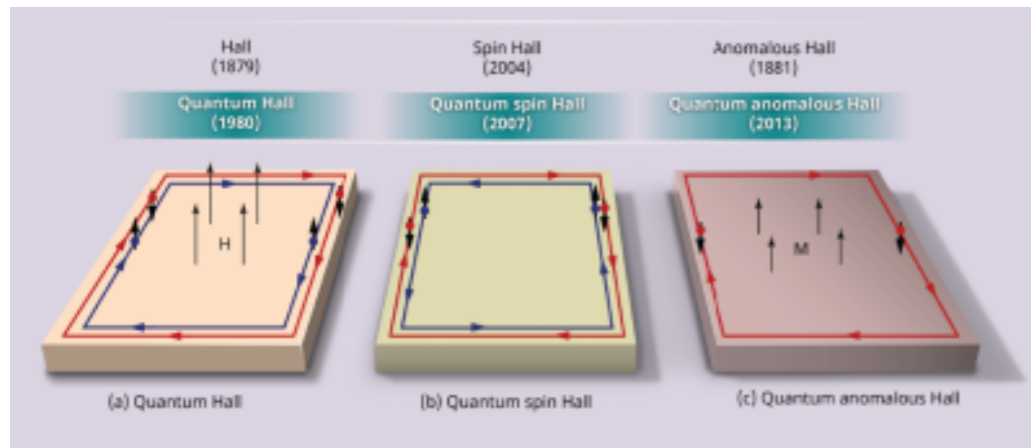


Competing Interactions

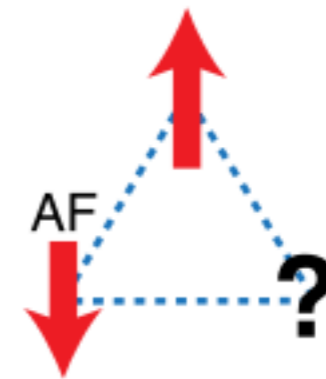


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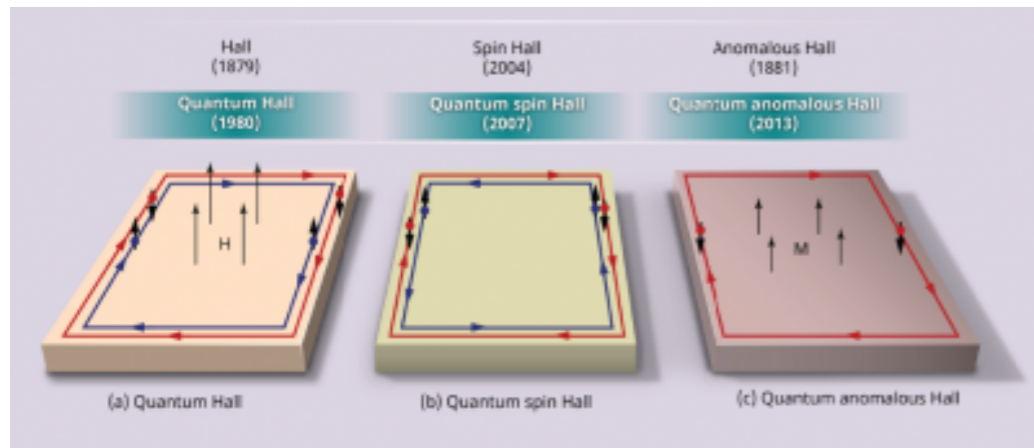
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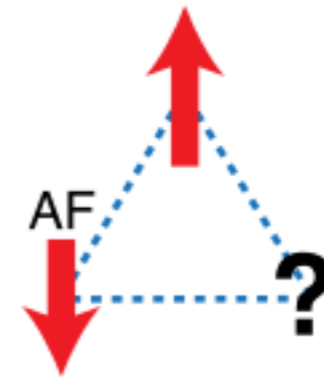
A lot of insights into the novel physics of these systems over the last four decades

Two Central areas of excitement in present quantum condensed matter

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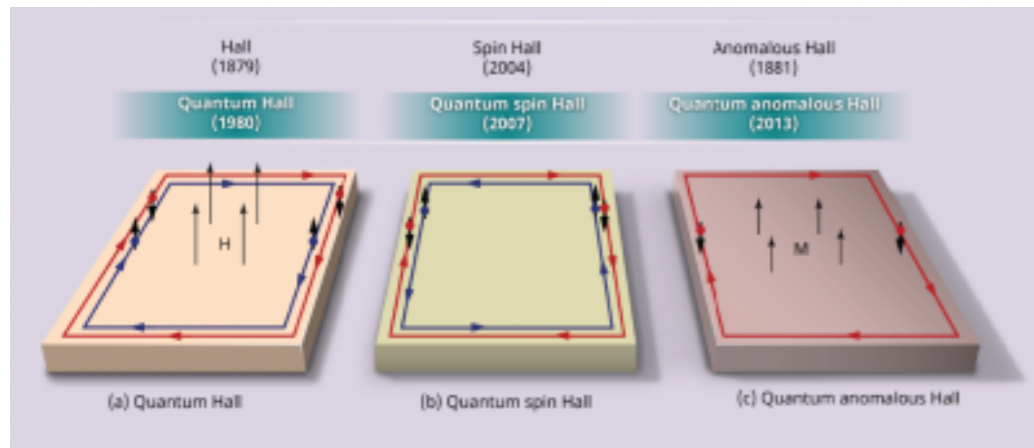
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Concretely sets up the question of the present times :

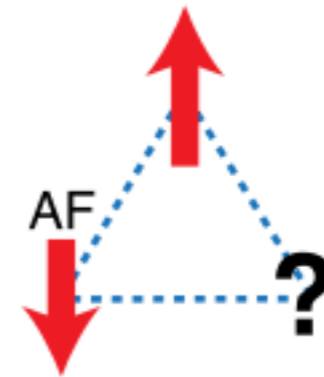
What is the fate of interactions in partially filled topological band ?

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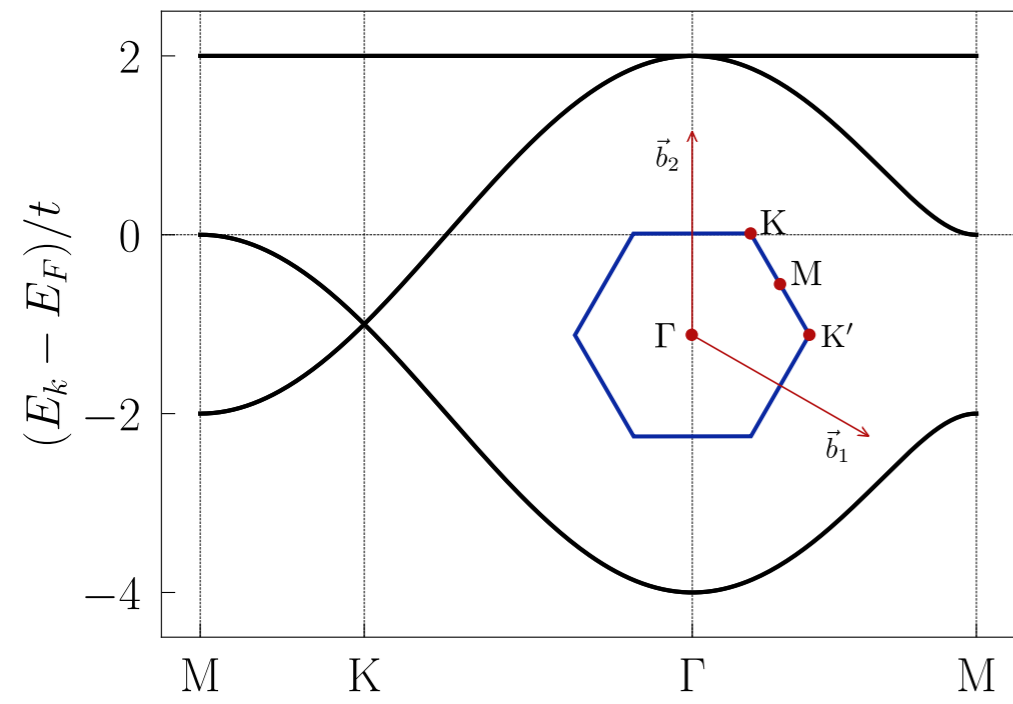
This generalizes the question of Fractional quantum hall effect to a much larger settings

With more **MANY** more material contexts

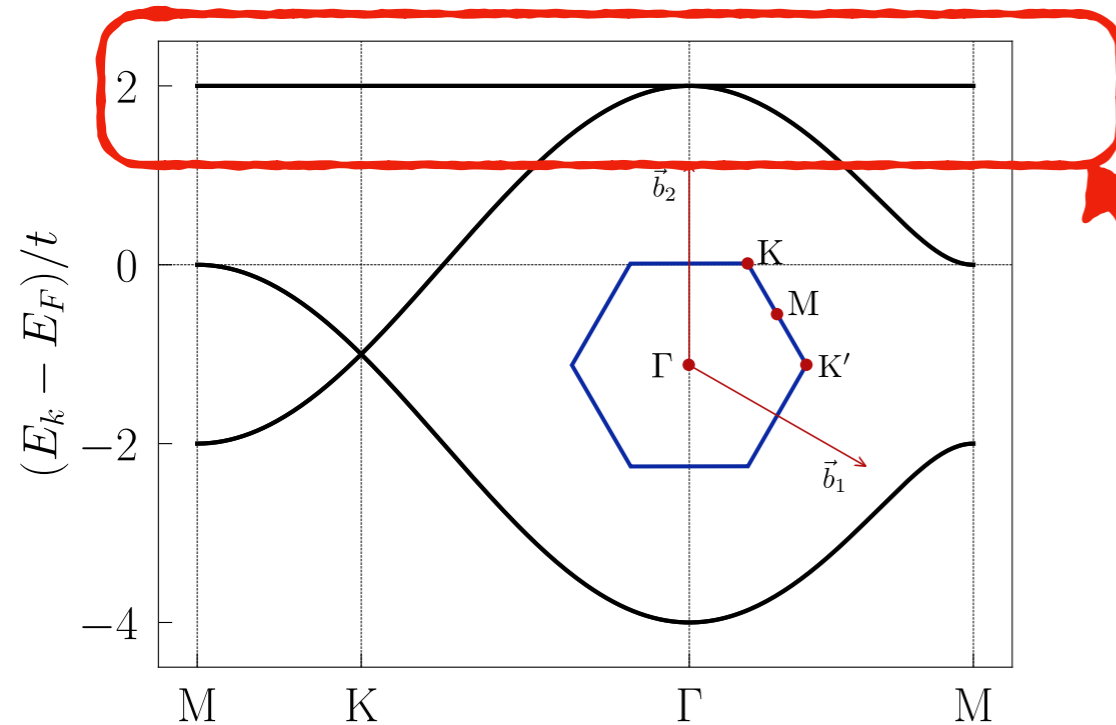
Fractional Chern Insulators, Moire systems, topological flat bands.....

A natural platform : Topological flat / almost flat bands

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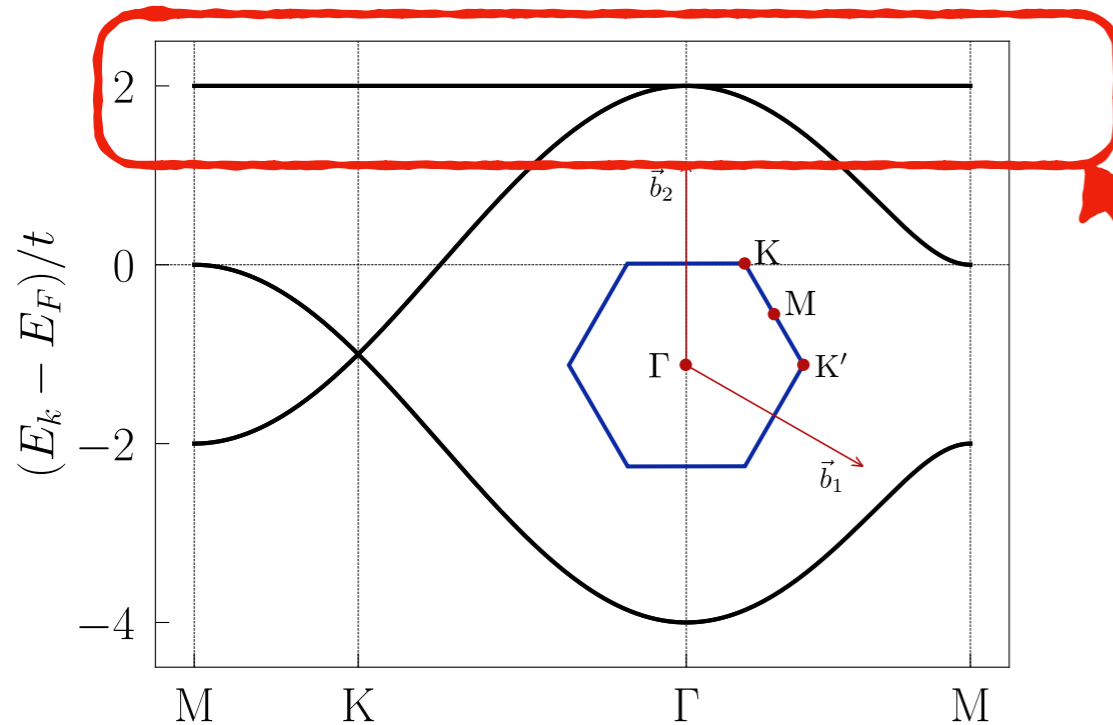
A natural platform : Topological flat / almost flat bands



- Trivial Flat bands (isolated orbitals) can be isolated but are singular but interesting (SYK, Topological order....)

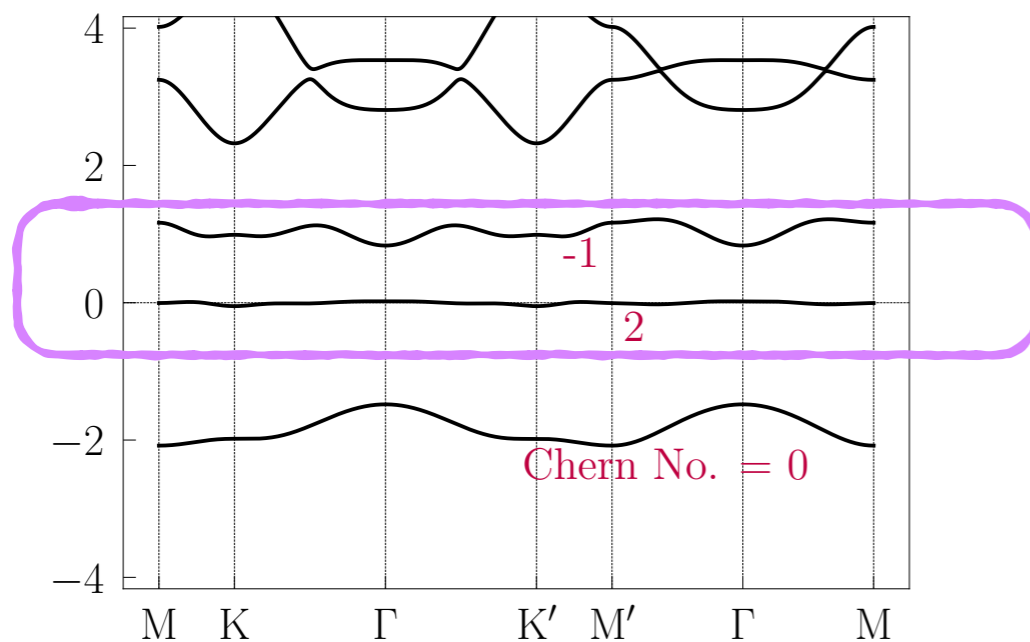
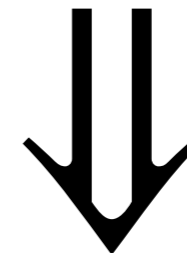
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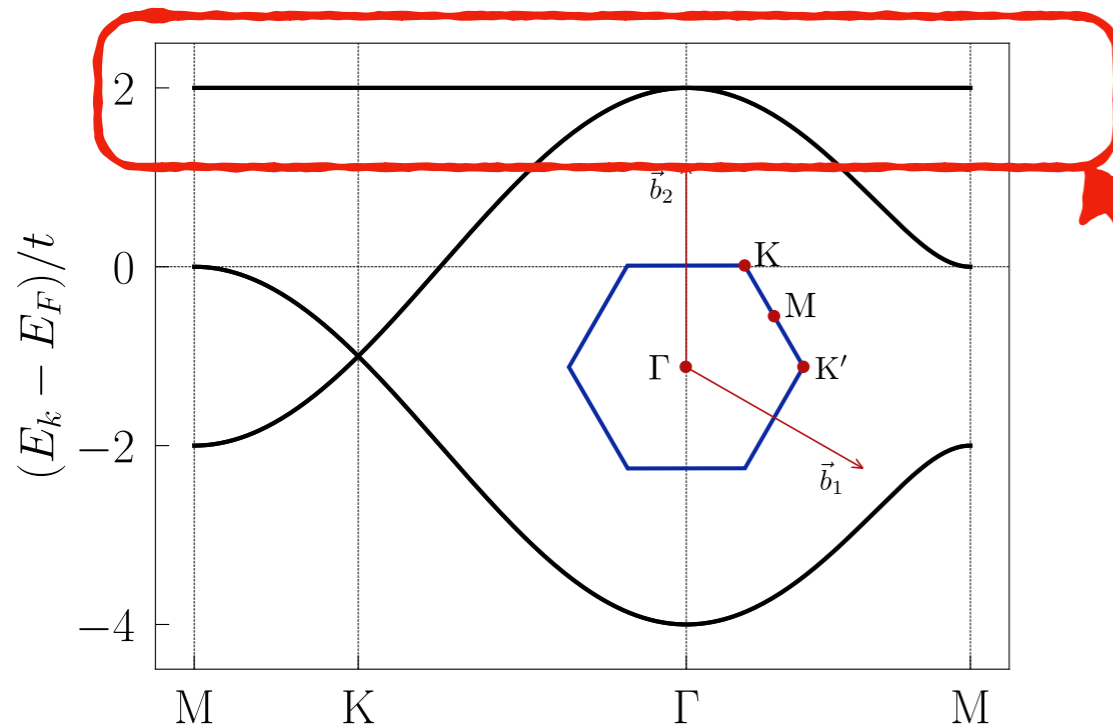
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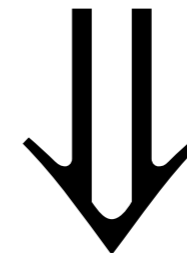
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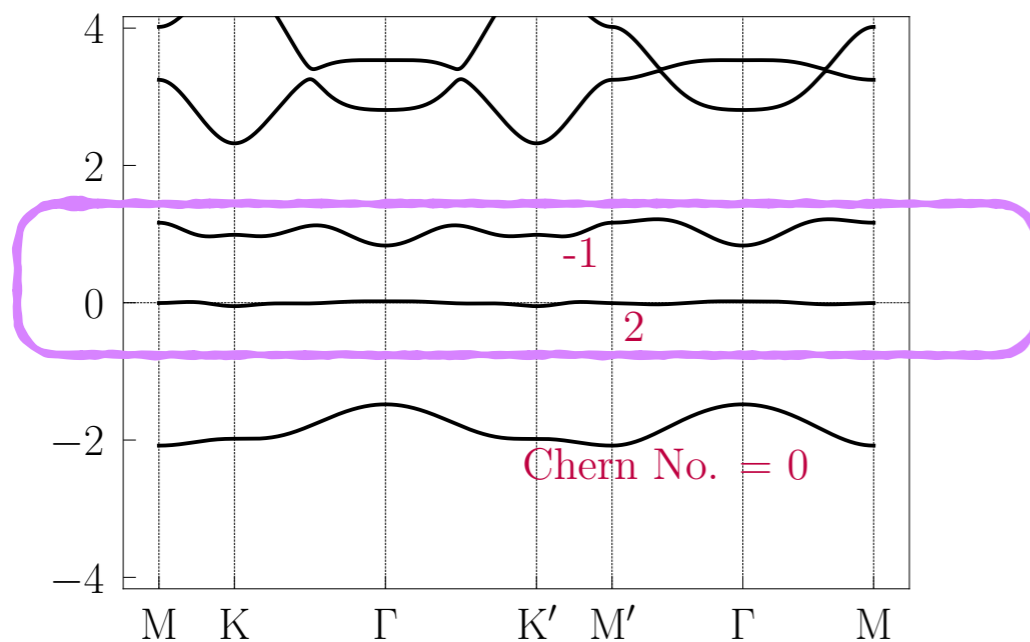


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Question for the talk :

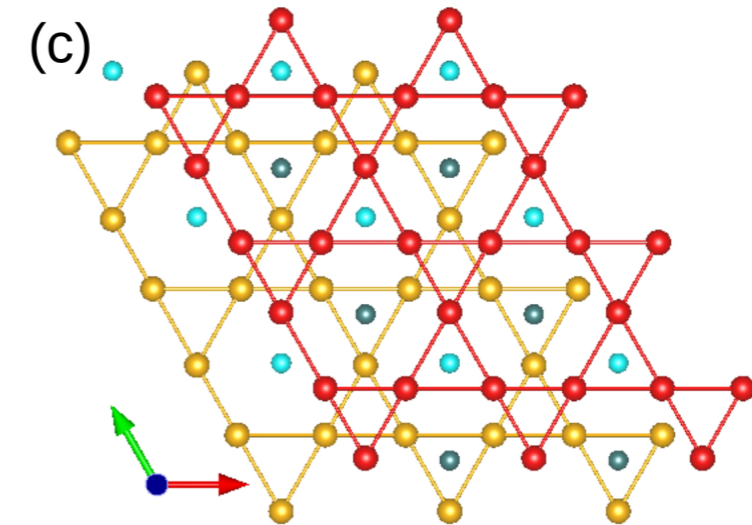
What is the effect of electron-electron interactions in a partially filled Chern band ?

A quick answer : Natural instabilities are different from that of a trivial band

The material Motivation : Many Kagome Metals

This Talk : Bilayer kagome intermetallics M_3Sn_2 M = 3d Transition metal

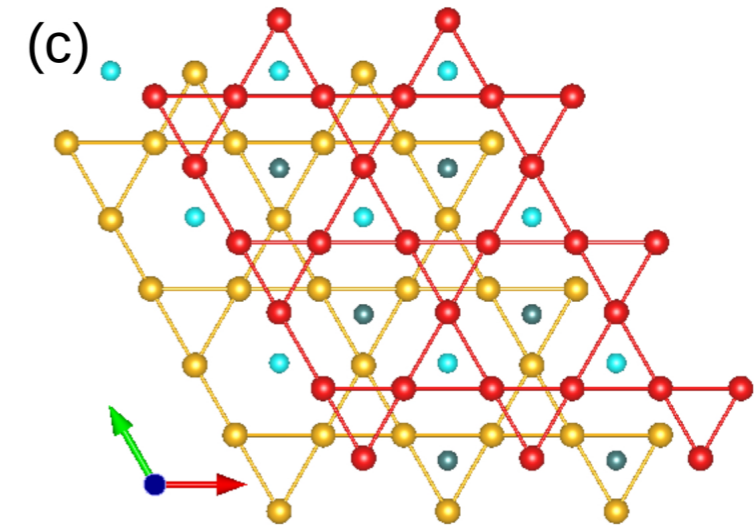
Our Interest : Fe_3Sn_2



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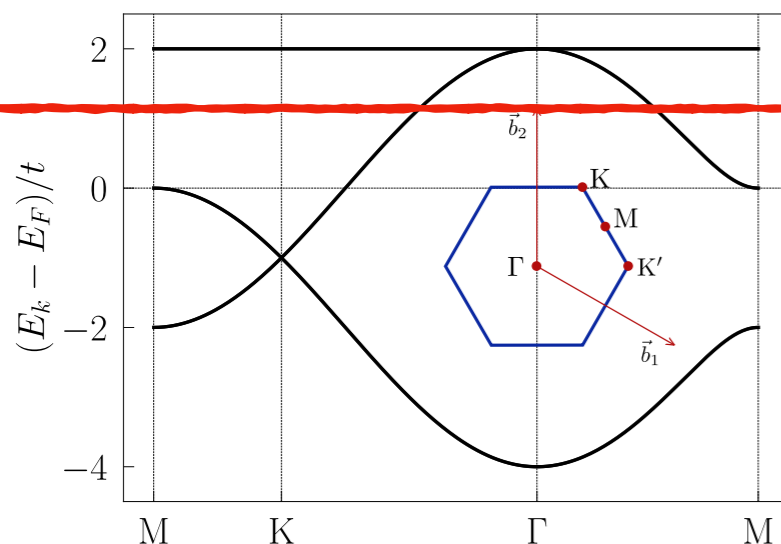
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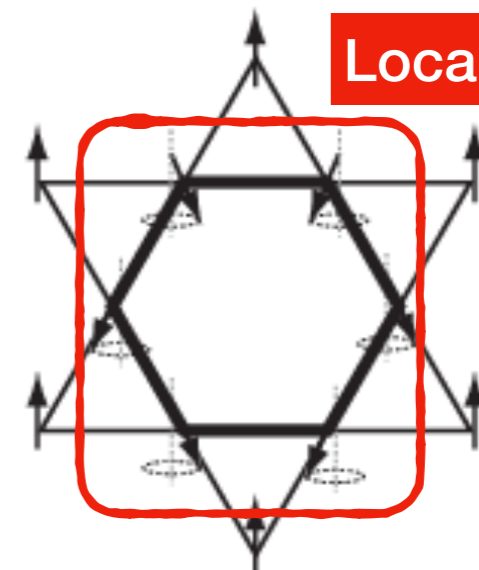


Both (antiferro)magnetic interactions as well as electron hopping can be frustrated in the Kagome geometry.

Flat band

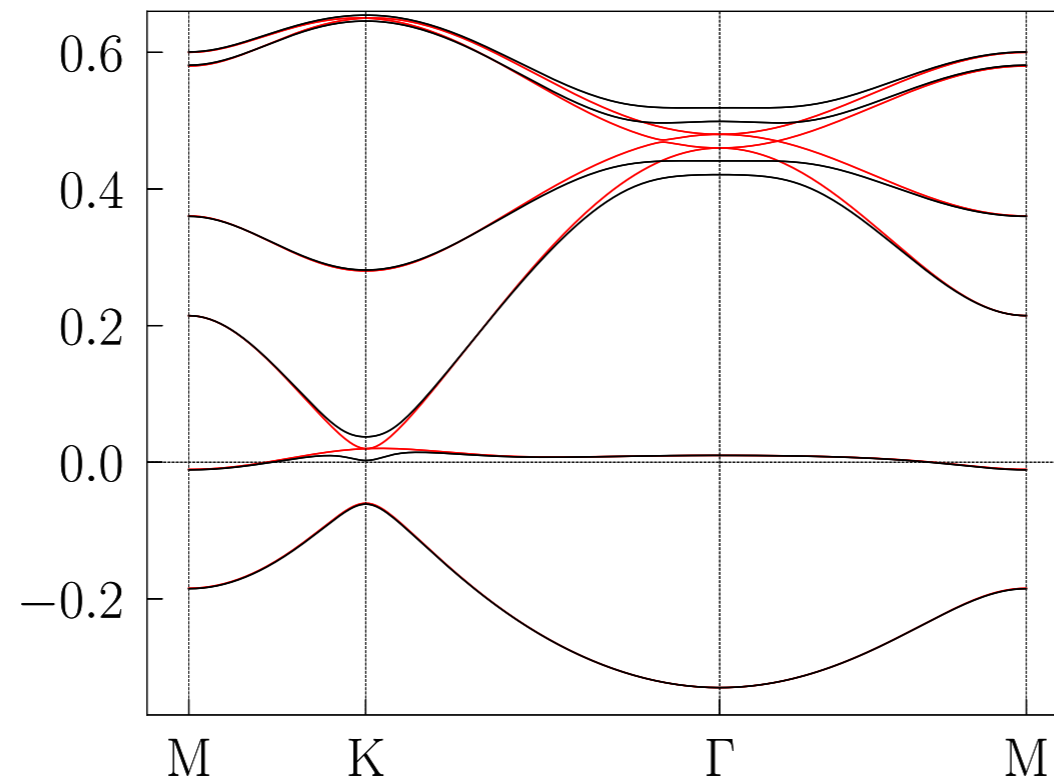


Local zero modes



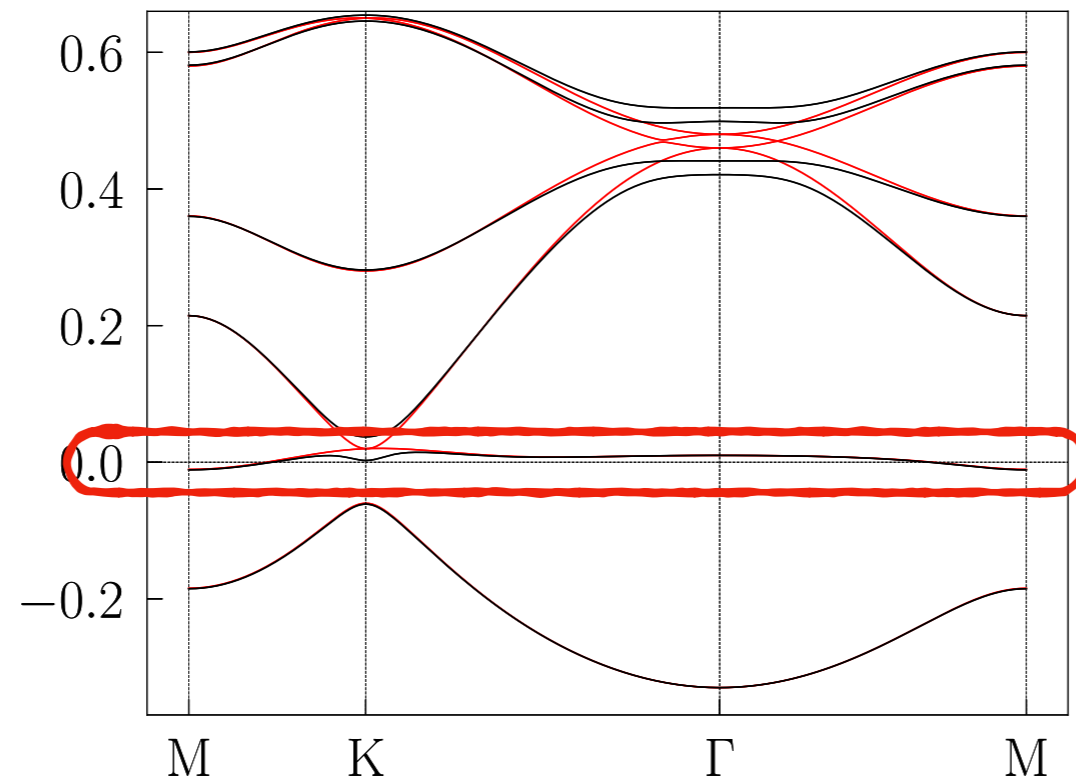
Minimal model for Bilayer Kagome Band-structure

Minimal one orbital hopping model with short range hopping and interlayer hybridization



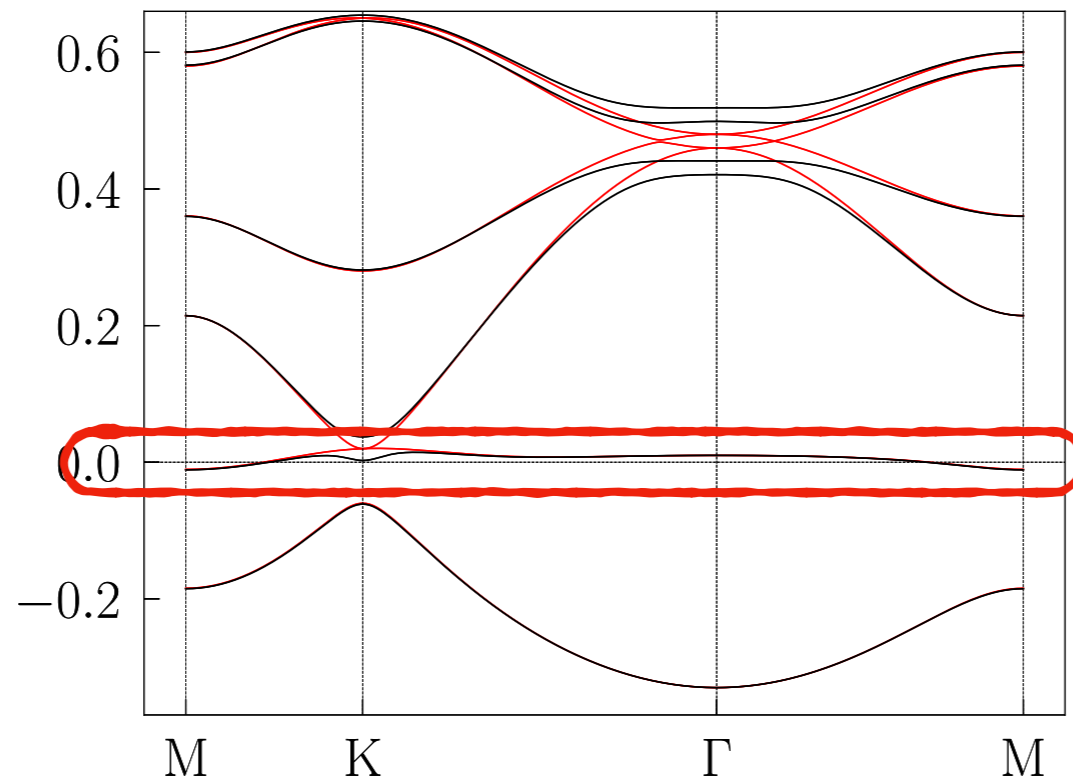
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Effect of short range interactions :

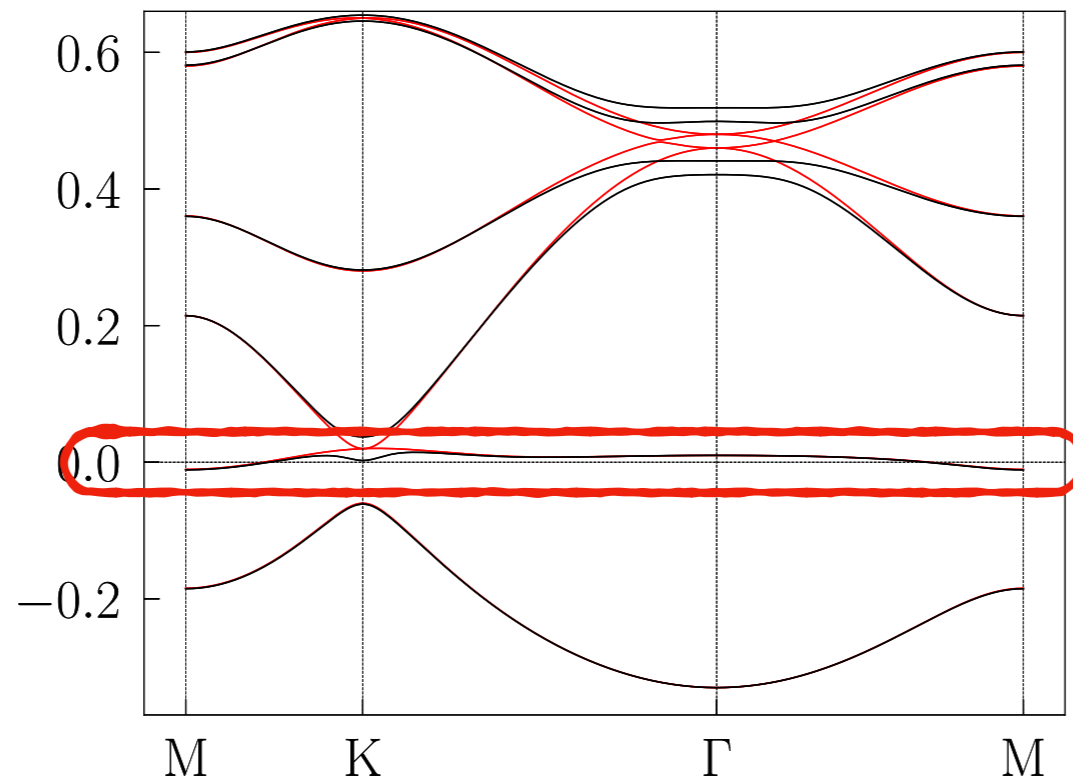
$$H_{Int} = U \sum_i n_i(n_i - 1) + \sum_{ij} V_{ij} n_i n_j$$

↑

Drives (almost) Flat-band ferromagnetism
(Seen in experiments for bulk materials)

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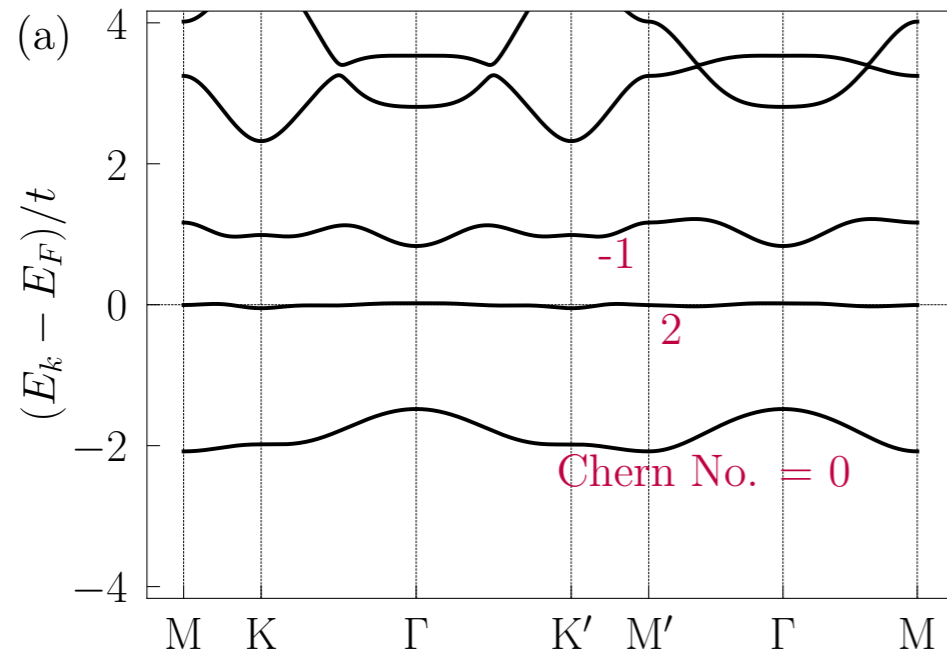
HF spin-polarised Band structure



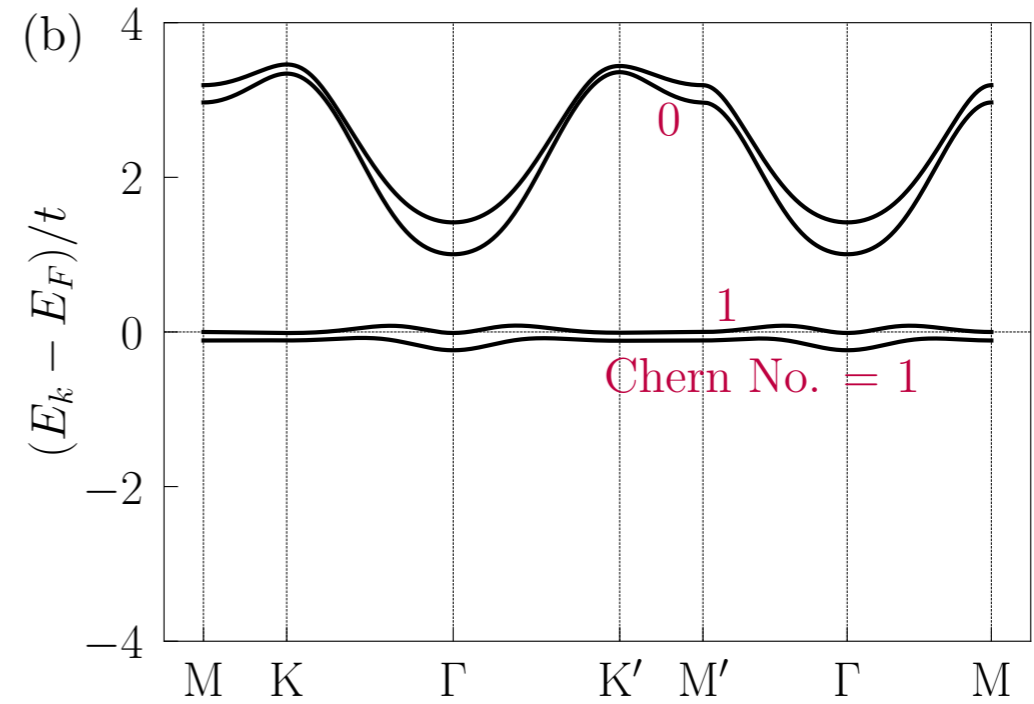
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HF spin-polarised Band structure : The Chern Metal

Strong inter-layer Hybridization

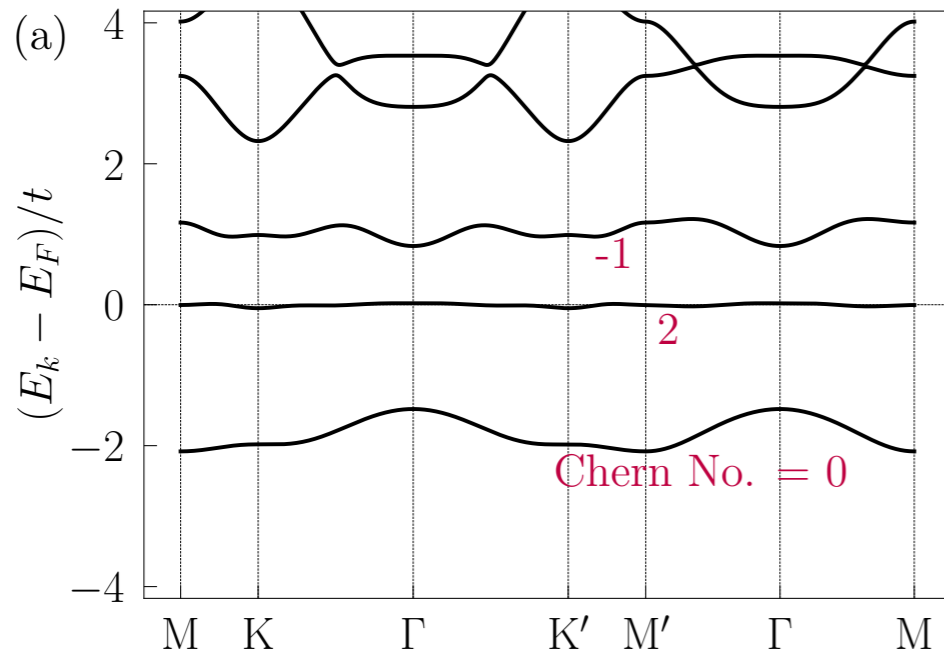


Weak inter-layer Hybridization

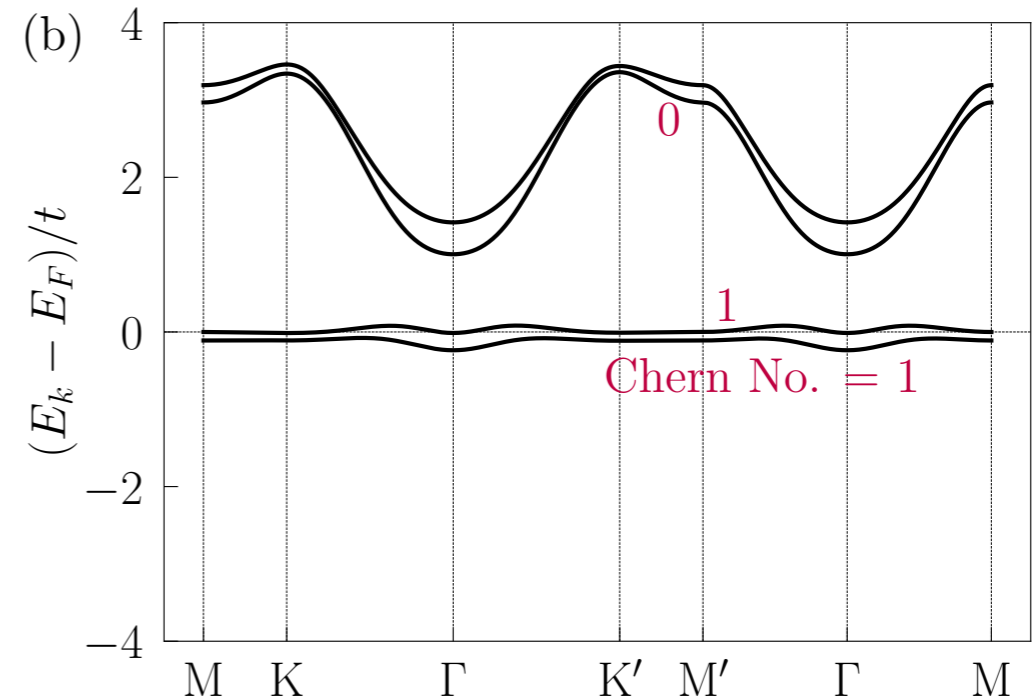


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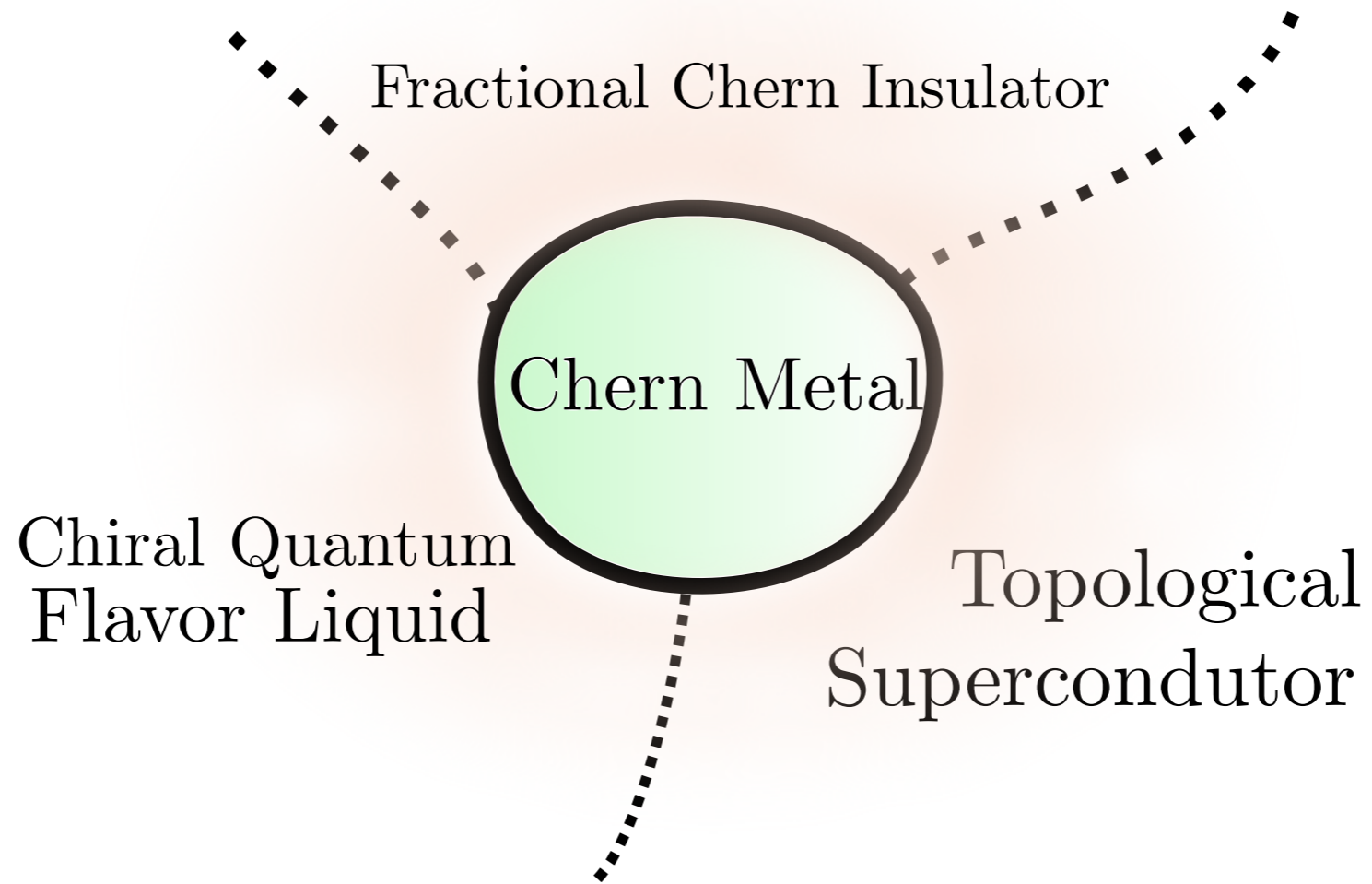


Partially filled Chern Band (Almost flat) : **Chern metal**

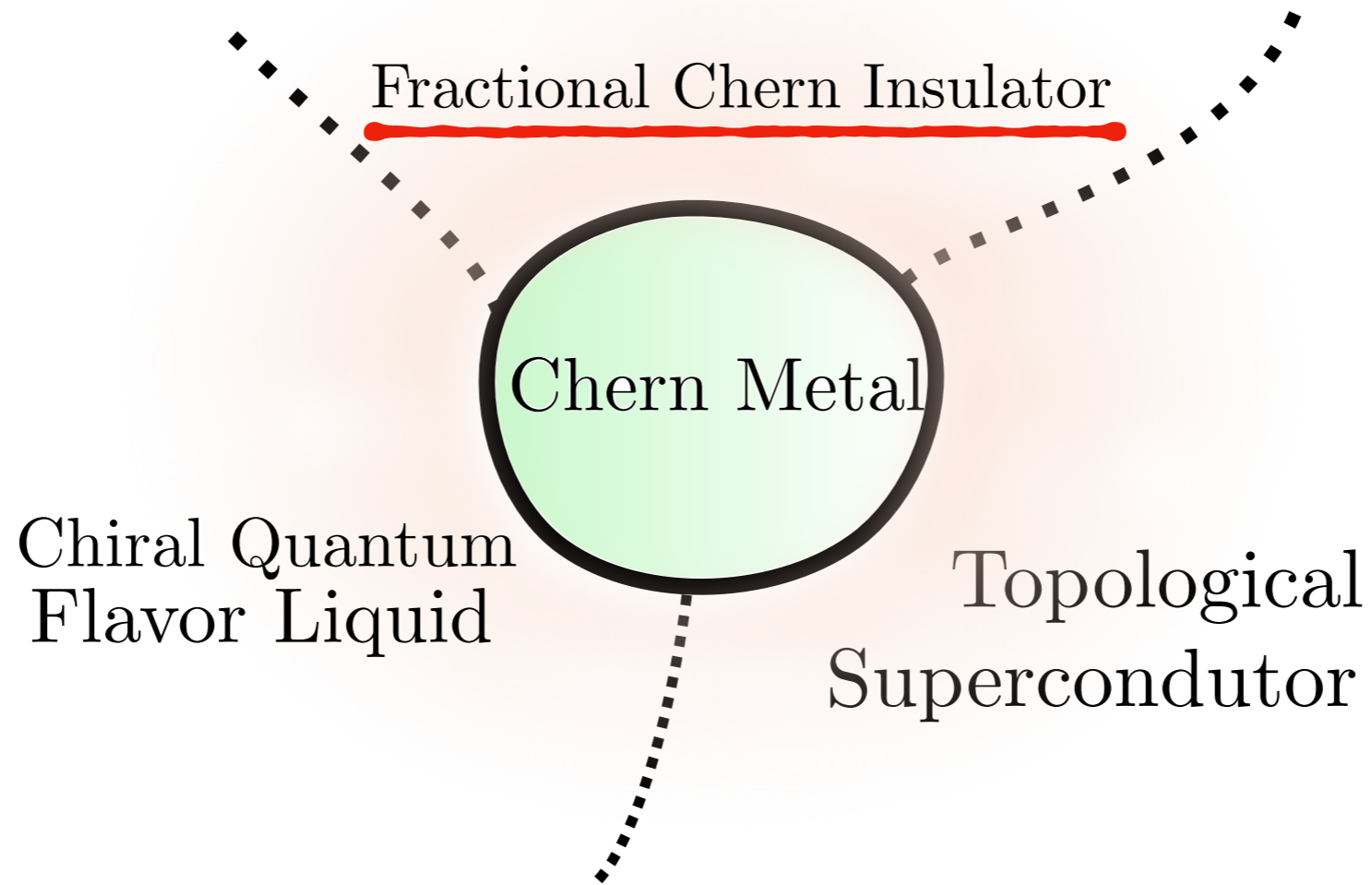
Question : What is the fate of the left over e-e interactions in the Chern band ?

$$H_{Int}^{eff} = \mathcal{P} \left[\sum_{ij} V_{ij} n_i n_j \right] \mathcal{P}$$

Chern Metal as the parent of many different Novel phases



Chern Metal as the parent of many different Novel phases

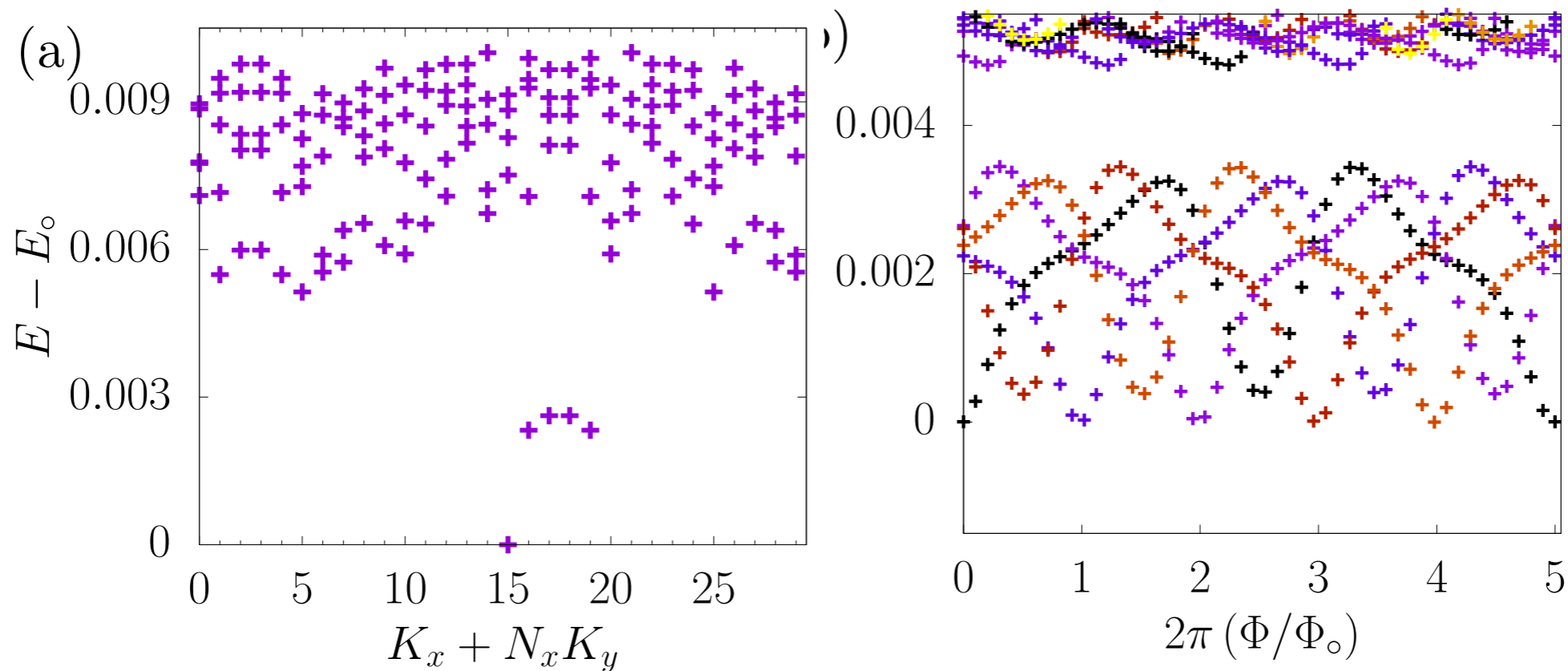


Fractional Chern Insulator

K-space ED of the projected Hamiltonian

$$H_{\text{int}} = \mathcal{P} \sum_{k_1, k_2, k_3, k_4} V_{k_1, k_2, k_3, k_4}^{\alpha_1, \alpha_2, \alpha_3, \alpha_4} c_{k_1, \alpha_1}^\dagger c_{k_2, \alpha_2}^\dagger c_{k_3, \alpha_3} c_{k_4, \alpha_4} \mathcal{P}.$$

1/5-Laughlin state in the **STRONG** interlayer hybridized limit



Energy Spectrum

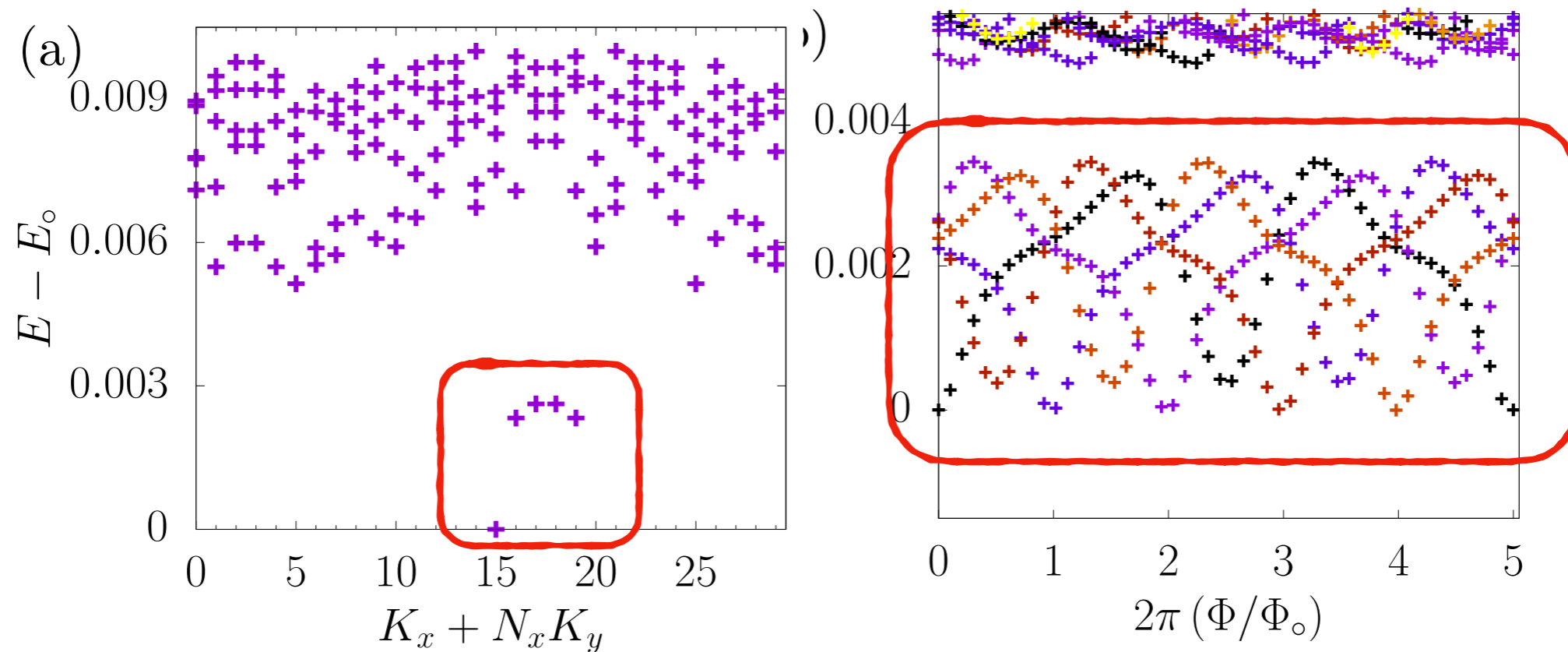
Flux threading

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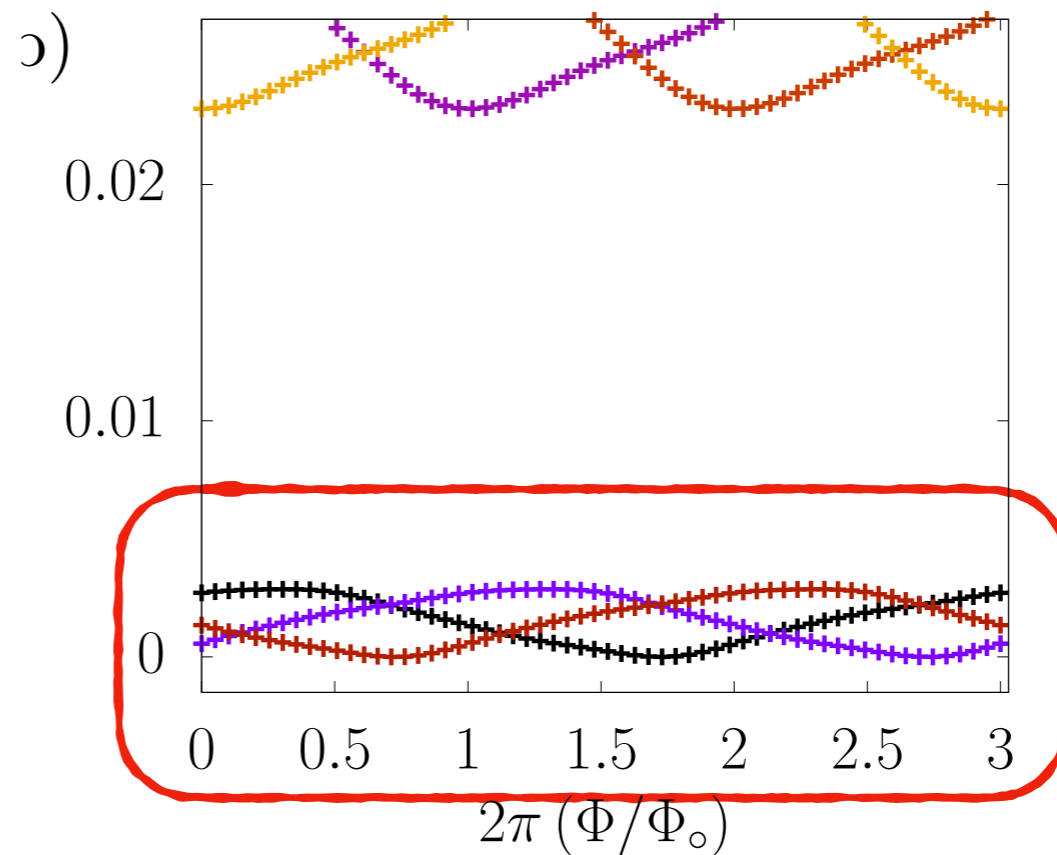
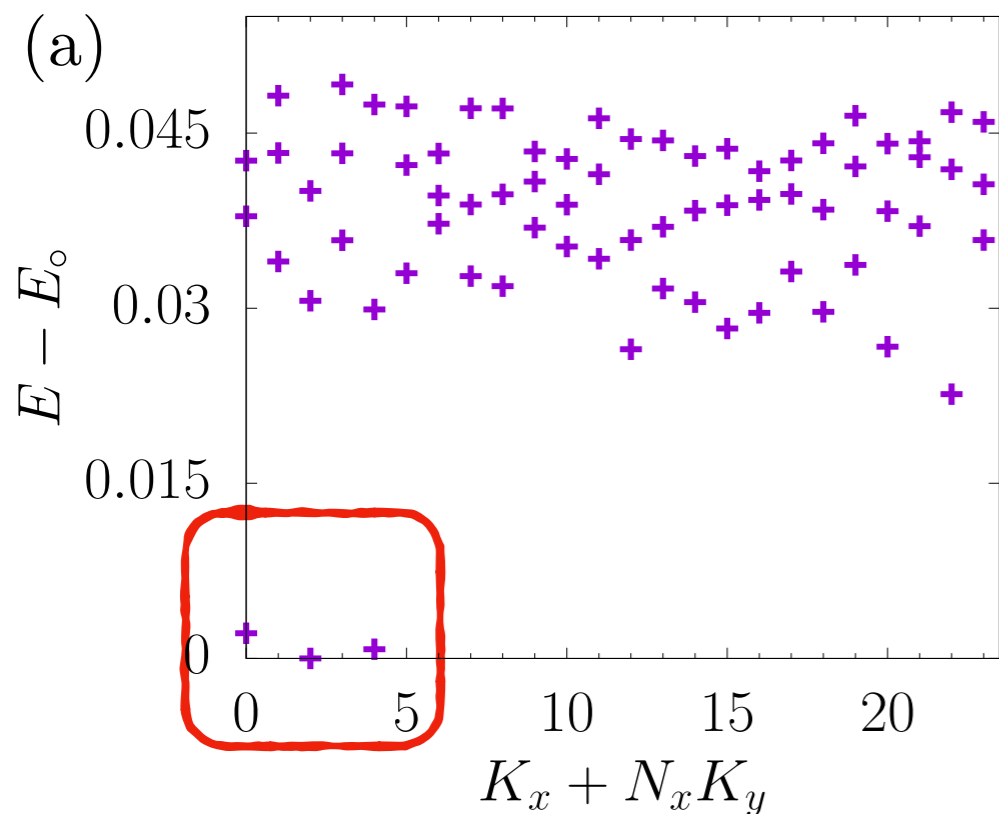
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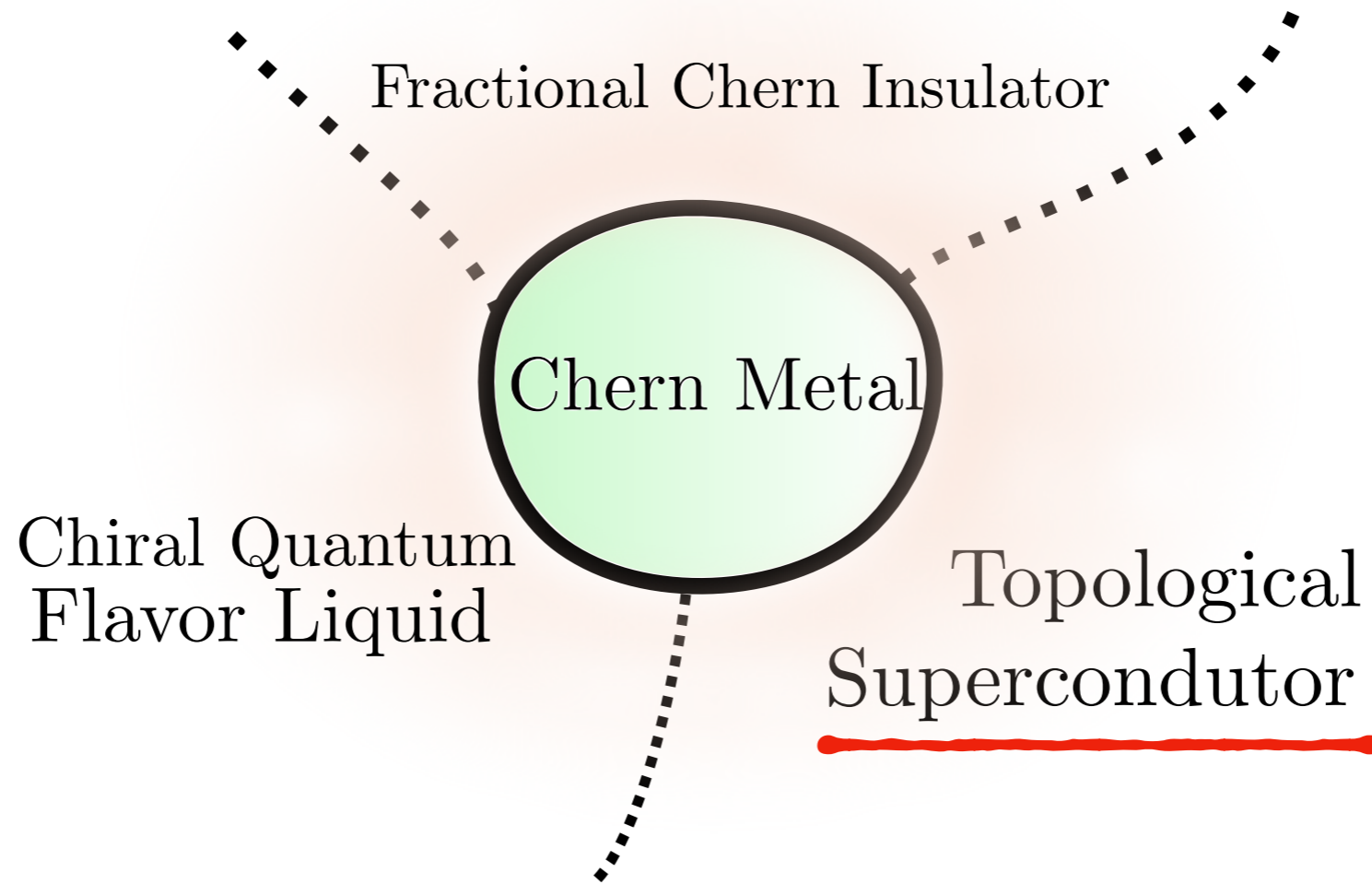
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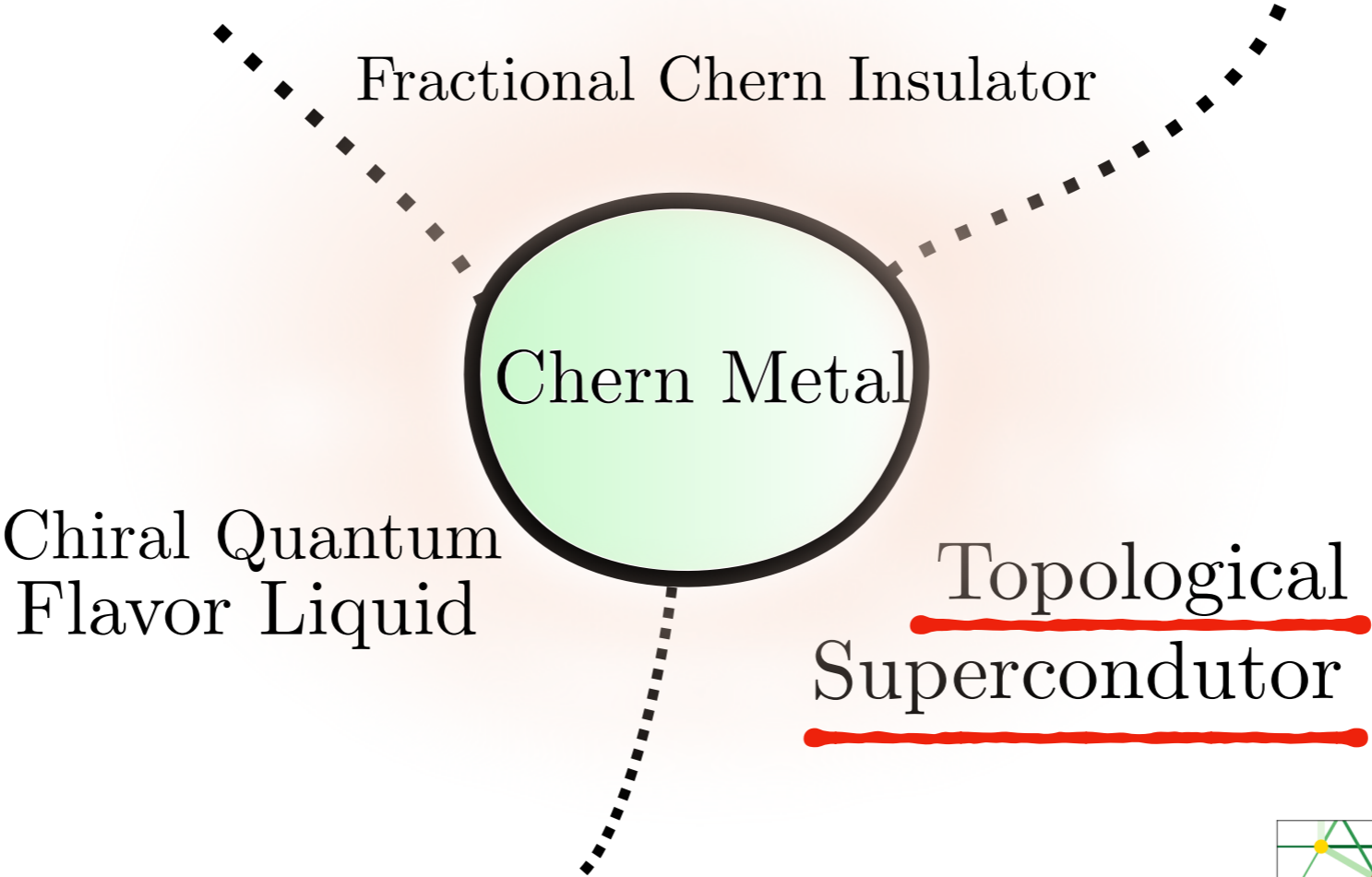
1/3-Laughlin state in the **WEAK** interlayer hybridized limit



Chern Metal as the parent of many different Novel phases

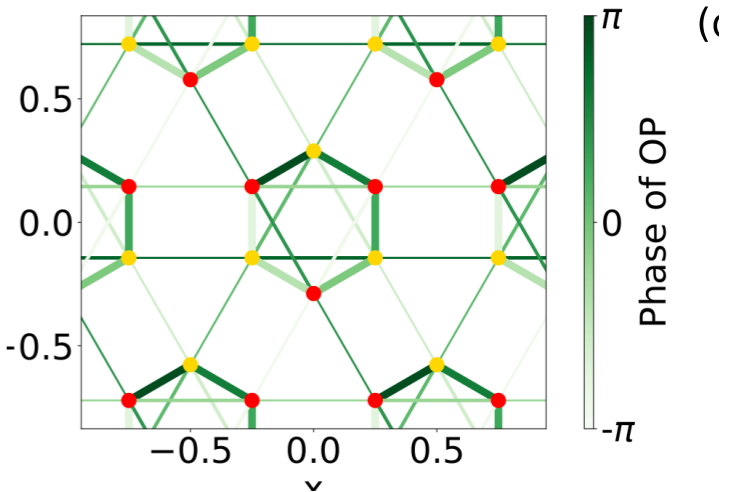


Chern Metal as the parent of many different Novel phases



BCS calculations

Chiral p-wave SC



Chern Metal as the parent of many different Novel phases

Electrons in terms of partons :

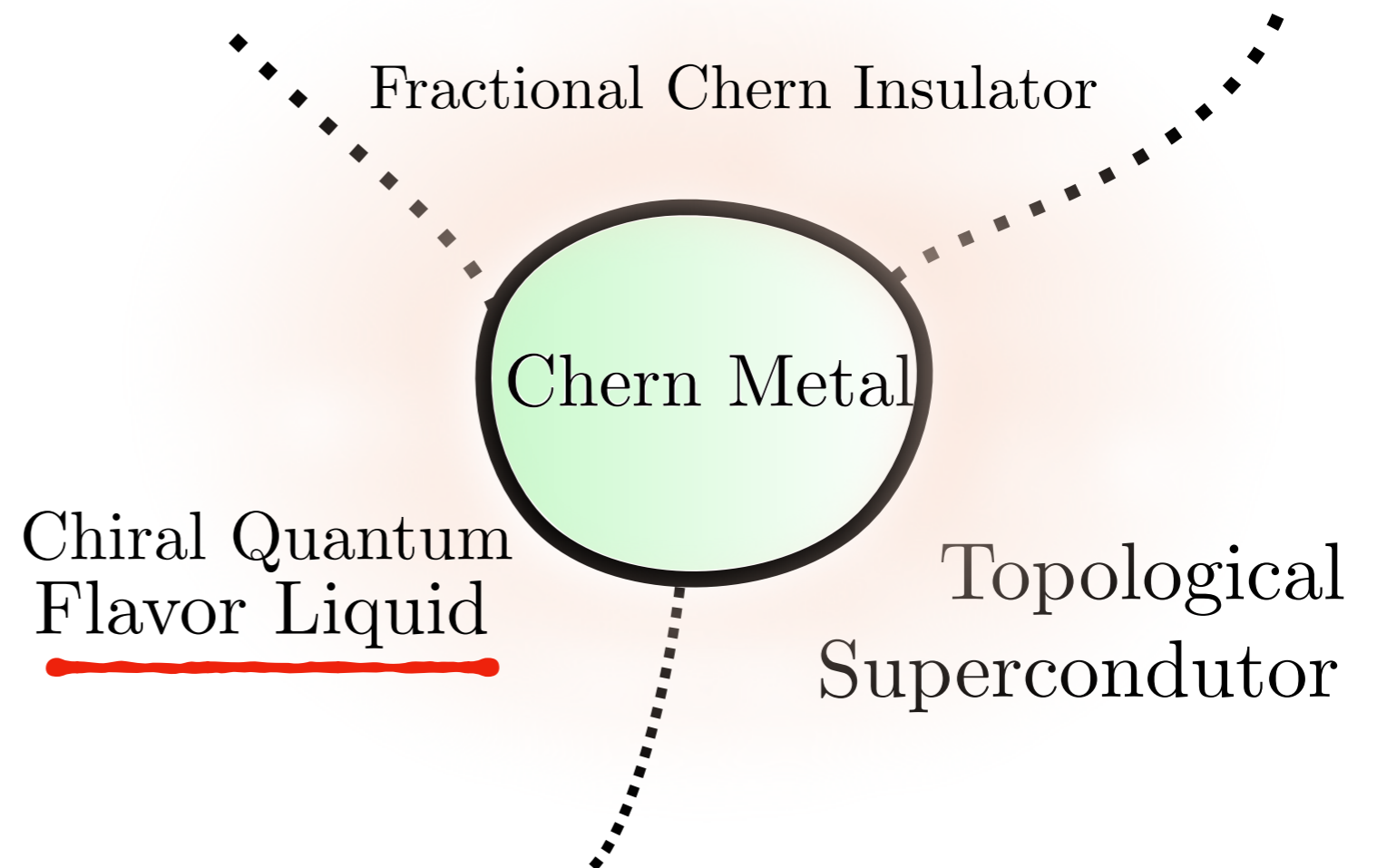
$$c_a = bf_a$$

(a is layer index \Rightarrow Flavour)

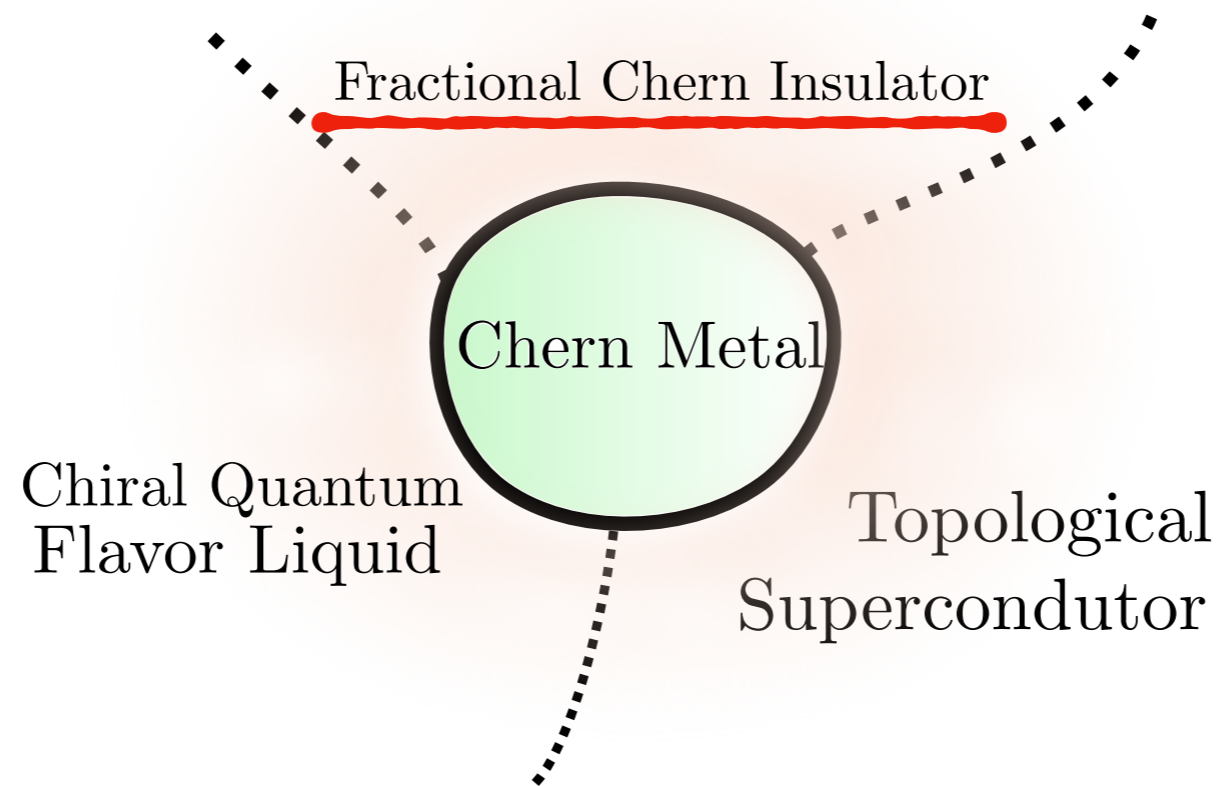
$b \rightarrow$ Bosonic chargon

$f \rightarrow$ Flavour Fermion

- Chern metal :
 - $f \rightarrow$ Chern band, $\langle b \rangle \neq 0$ (condensed, Superfluid)
- Chiral Flavour Liquid :
 - $f \rightarrow$ Chern band, $\langle b \rangle = 0$ (Trivial Mott Insulator)

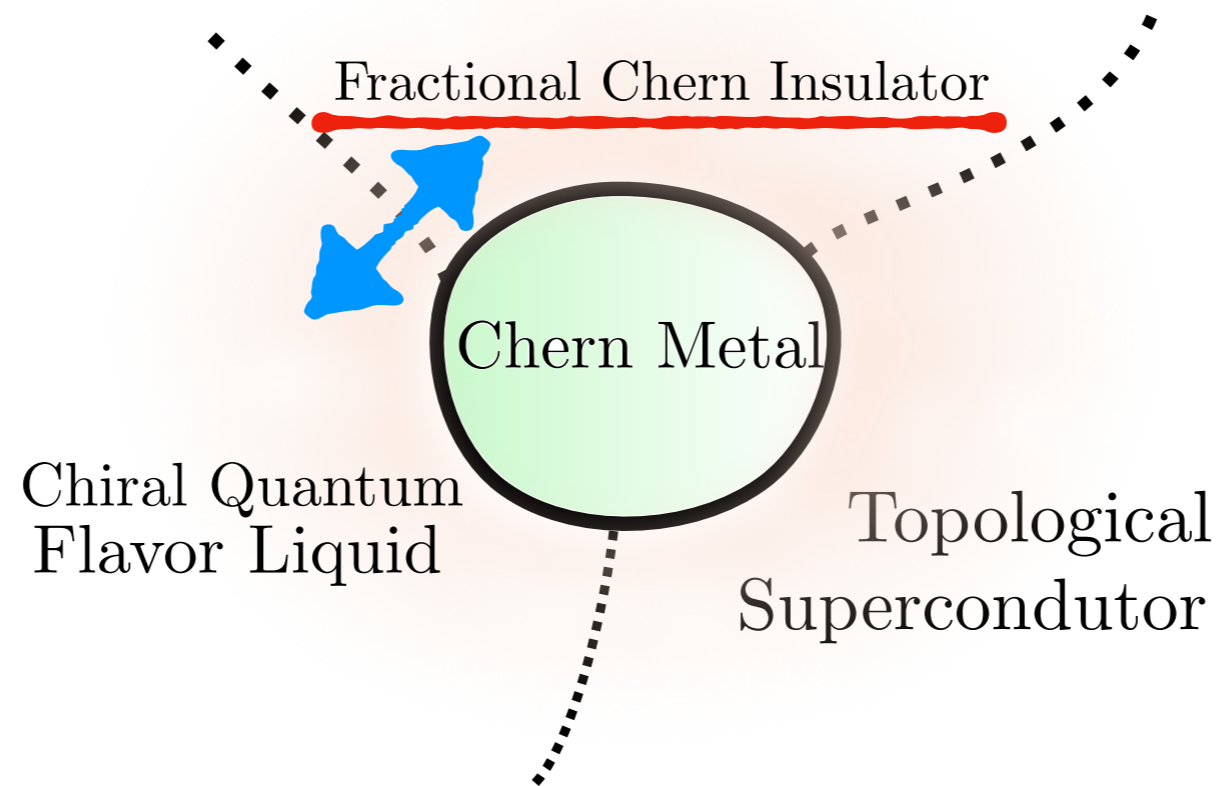


Recasting of the Fractional Chern Insulator in terms of the partons



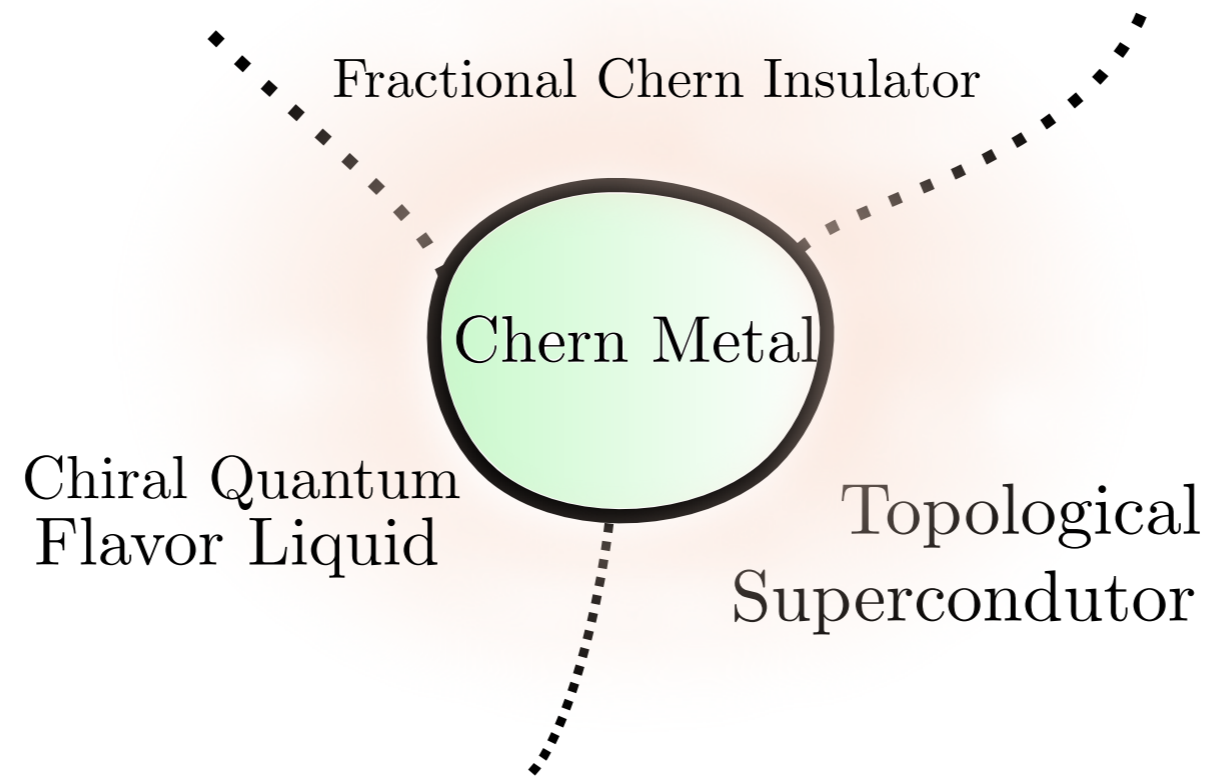
- The Fractional Chern Insulator :
 - $f \rightarrow$ Chern band, $b \rightarrow$ Bosonic Integer Hall Phase
 - The Effective filling of the Chern band is changed by the flux of the emergent U(1) gauge field.

Recasting of the Fractional Chern Insulator in terms of the partons



- The Fractional Chern Insulator :
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 - The Effective filling of the Chern band is changed by the flux of the emergent U(1) gauge field.
- The Transition between the FCI and the Chiral Flavour liquid is a BIQH plateau transition

Summary



- The chern metal is the parent of many novel phases
- A good place to look for such exotic phase and transitions is Kagome metals

Thank You