

Learning the High Redshift Universe using nano-hertz and hecto-hertz GW Background

Suvodip Mukherjee

Tata Institute of Fundamental Research

HEARING BEYOND THE STANDARD MODEL WITH COSMIC SOURCES OF GRAVITATIONAL WAVES

ICTS-TIFR,
January 7th, 2025

Image Credit: LIGO



PROBING THE COSMIC HISTORY

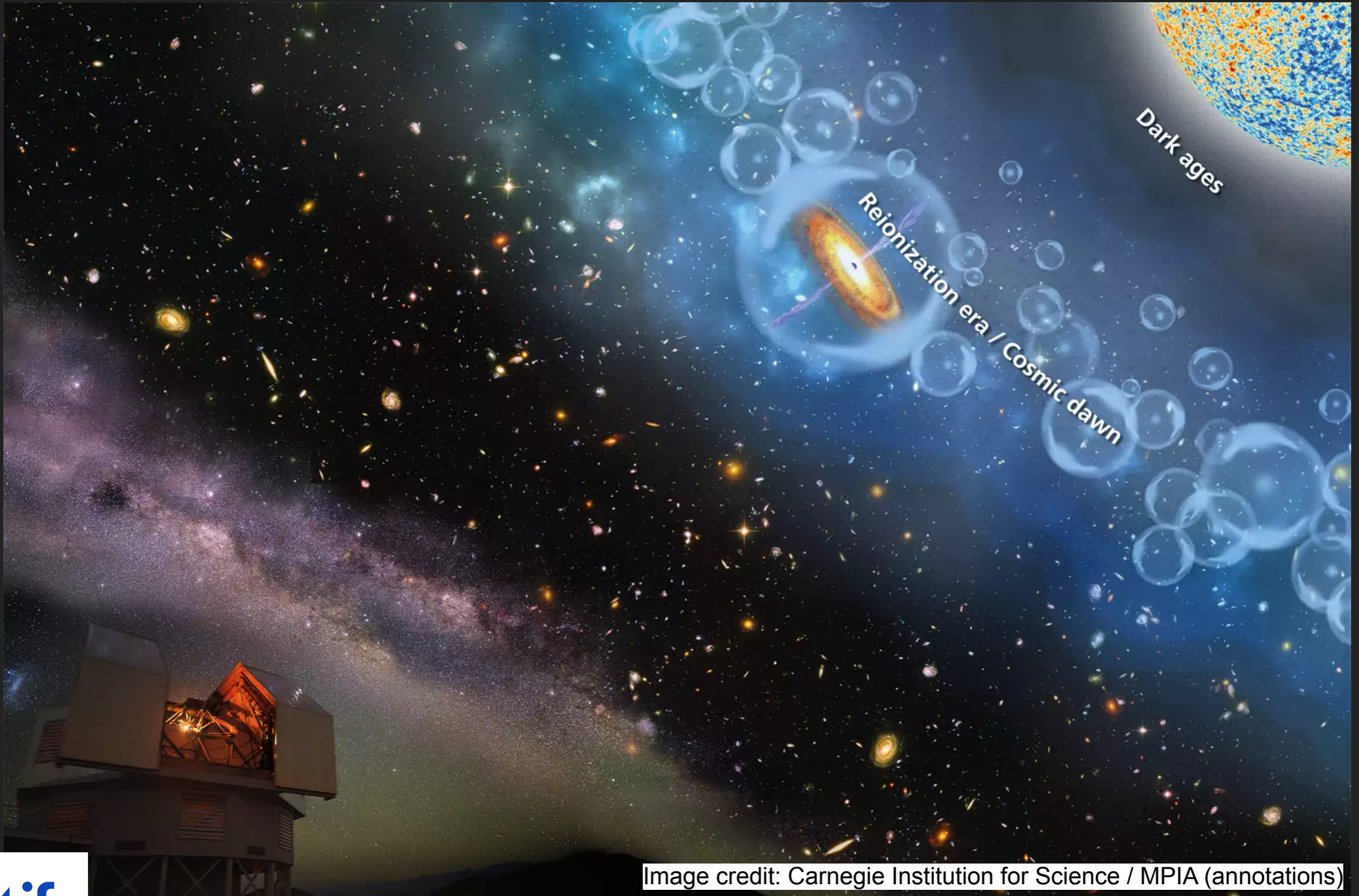


Image credit: Carnegie Institution for Science / MPIA (annotations)

Suvodip Mukherjee, 2025

PROBING THE COSMIC HISTORY

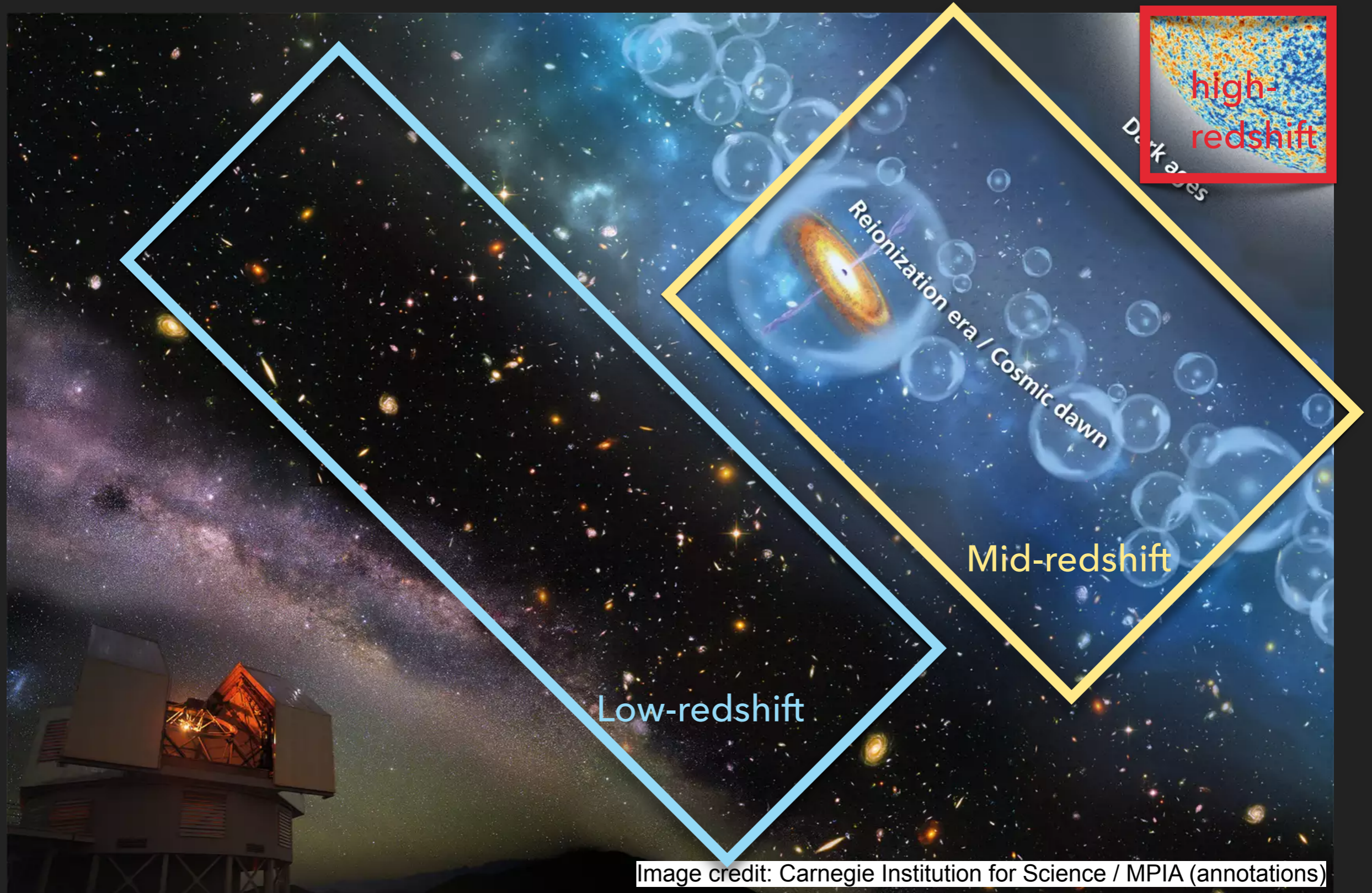


Image credit: Carnegie Institution for Science / MPIA (annotations)

PROBING THE COSMIC HISTORY USING STELLAR GRAVEYARDS

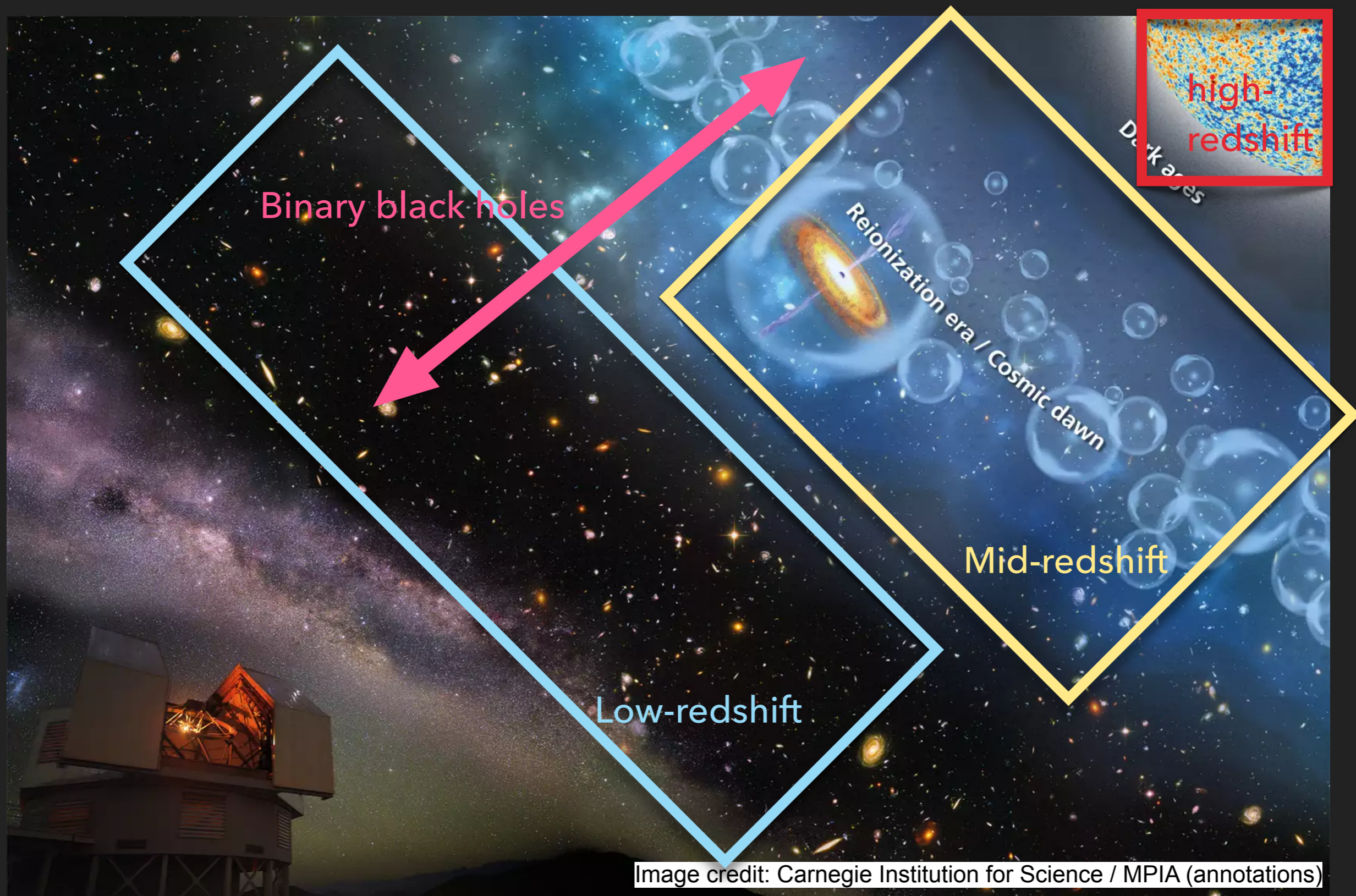


Image credit: Carnegie Institution for Science / MPIA (annotations)

PROBING THE COSMIC HISTORY USING STELLAR GRAVEYARDS FROM HECTO-HERTZ TO NANO-HERTZ

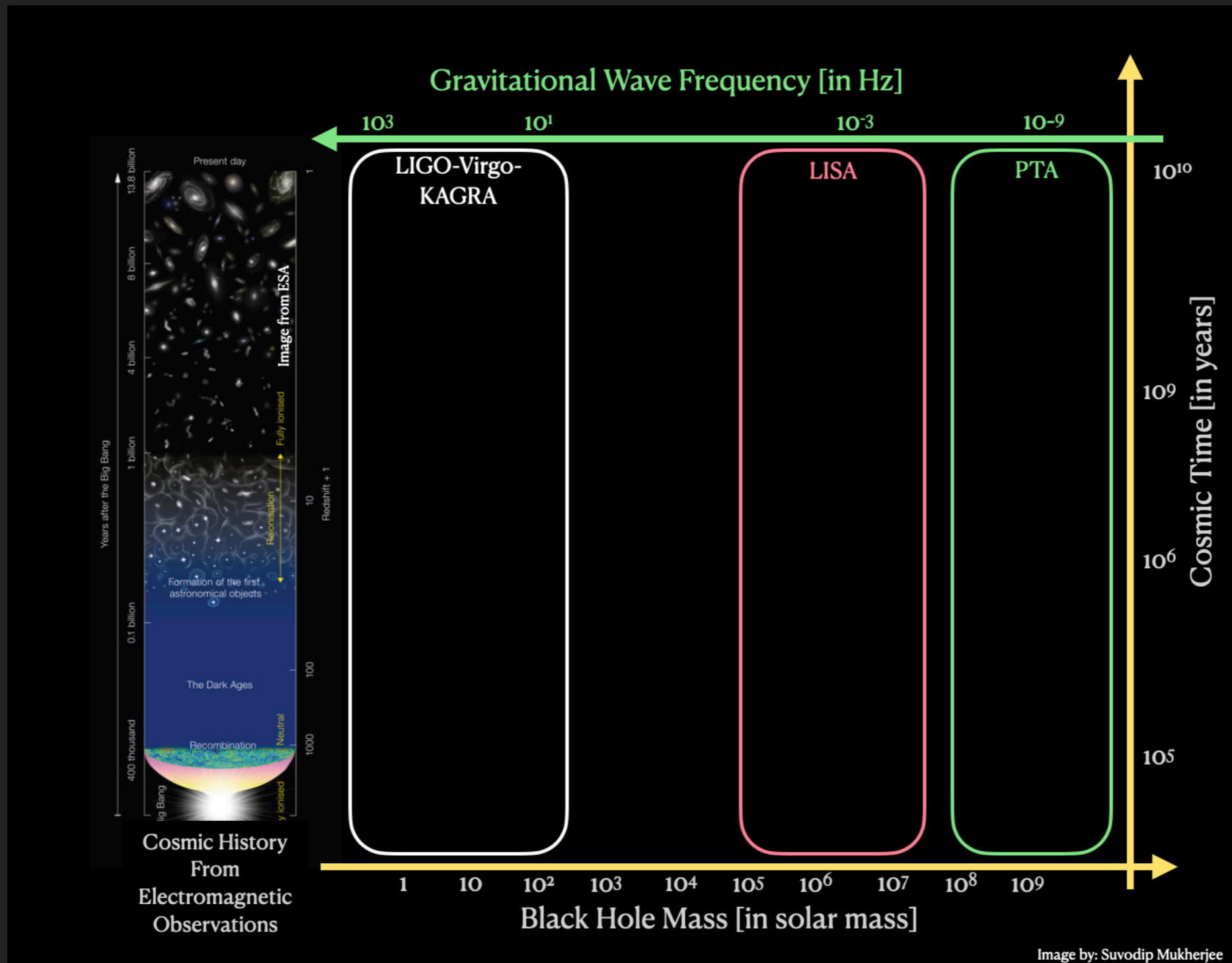
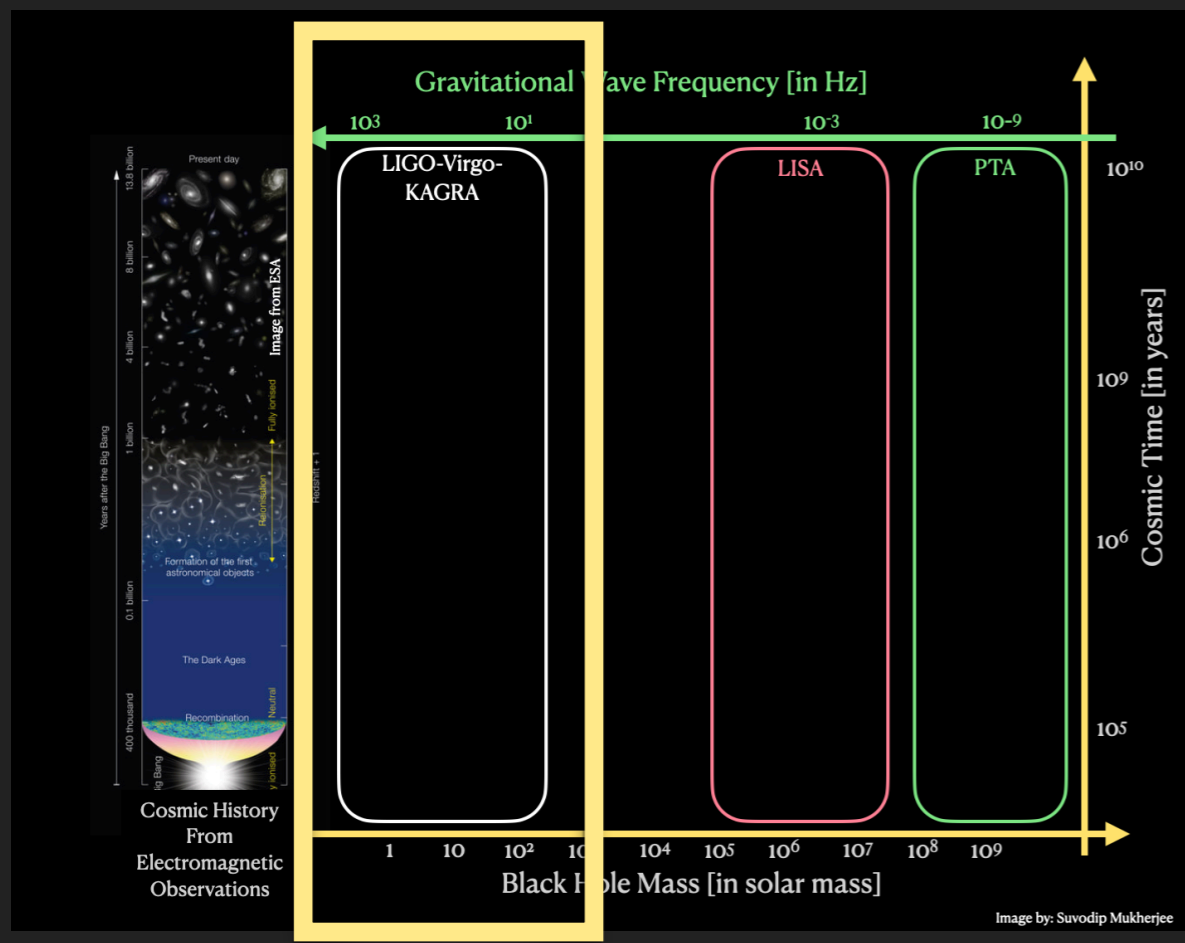


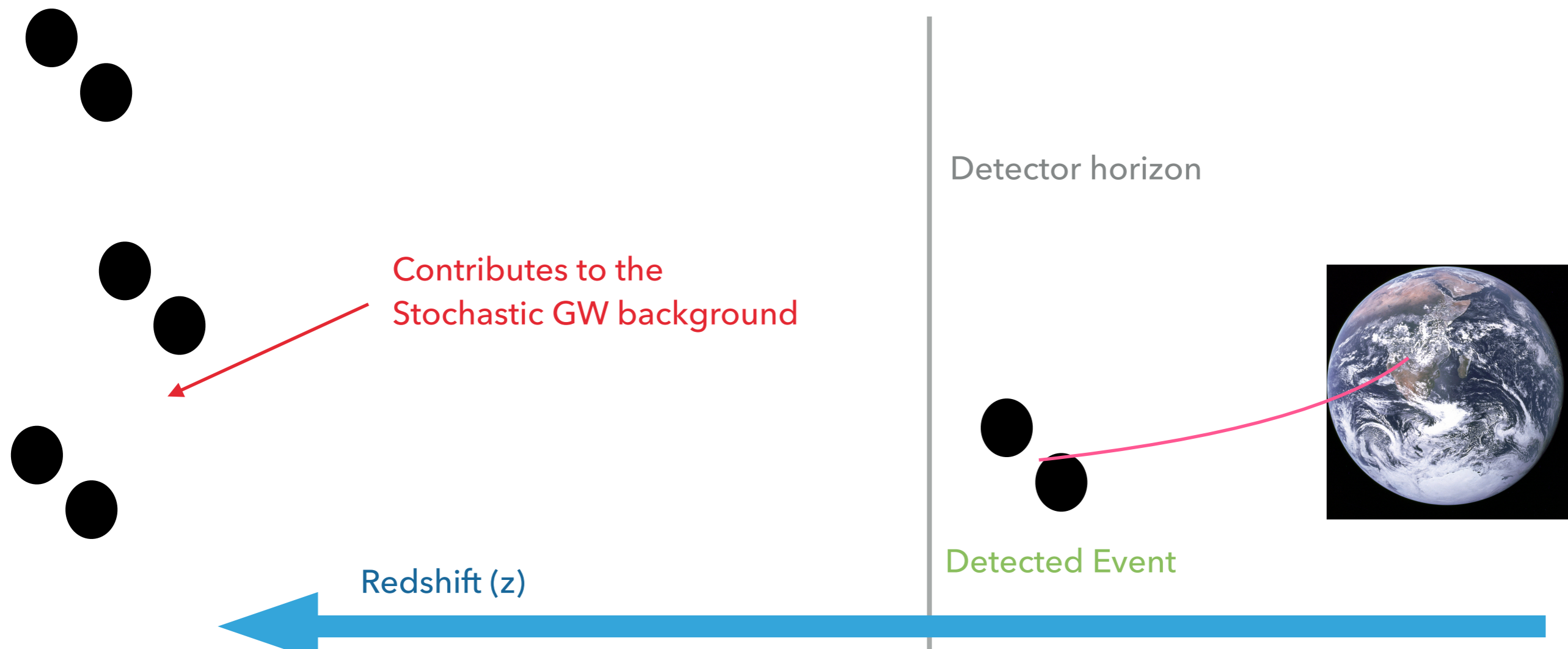
Image by: Suvodip Mukherjee



WHERE AND HOW THE BLACK HOLE FORM?

- + Events (Low redshift)
- + Backgrounds (High redshift)

LESS OBJECTS COALESCING AT HIGH REDSHIFT LEAD TO WEAK STOCHASTIC BACKGROUND



Contributes to the Stochastic GW background

Detector horizon

Detected Event

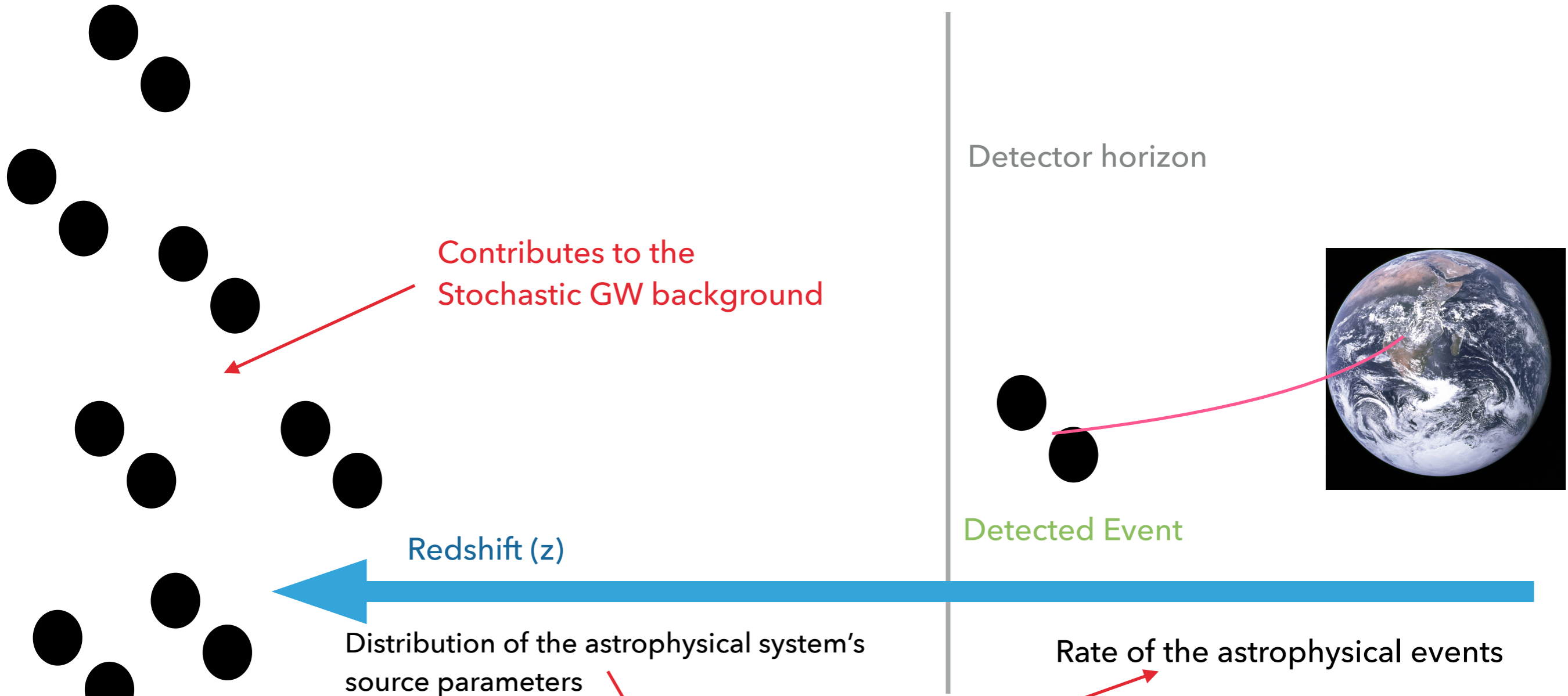
Redshift (z)

Distribution of the astrophysical system's source parameters

Rate of the astrophysical events

$$\Omega_{GW}(f) = \frac{f}{\rho_c c^2} \int d\theta p(\theta) \int_{z_{min}}^{z_{max}} dz \frac{R(z, \theta) dE_{GW}(\theta) / df_r}{(1+z)H(z)}$$

MORE OBJECTS COALESCING AT HIGH REDSHIFT LEAD TO LOUD STOCHASTIC BACKGROUND



Redshift (z)

Distribution of the astrophysical system's source parameters

Detector horizon

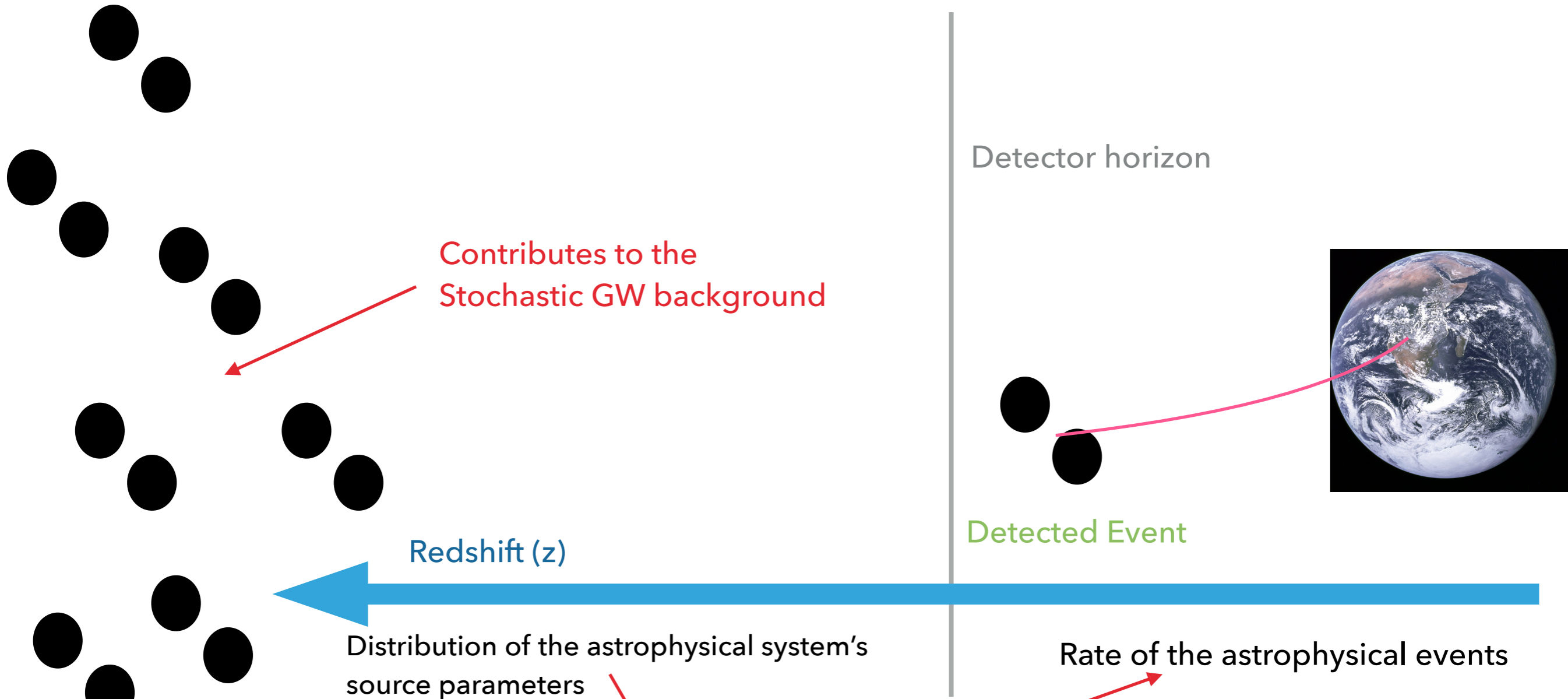
Detected Event

Rate of the astrophysical events

$$\Omega_{GW}(f) = \frac{f}{\rho_c c^2} \int d\theta p(\theta) \int_{z_{min}}^{z_{max}} dz \frac{R(z, \theta) dE_{GW}(\theta) / df_r}{(1+z)H(z)}$$



MORE OBJECTS COALESCING AT HIGH REDSHIFT LEAD TO LOUD STOCHASTIC BACKGROUND
HOW CAN WE INFER THE SOURCES AT HIGH REDSHIFT FROM BACKGROUND?

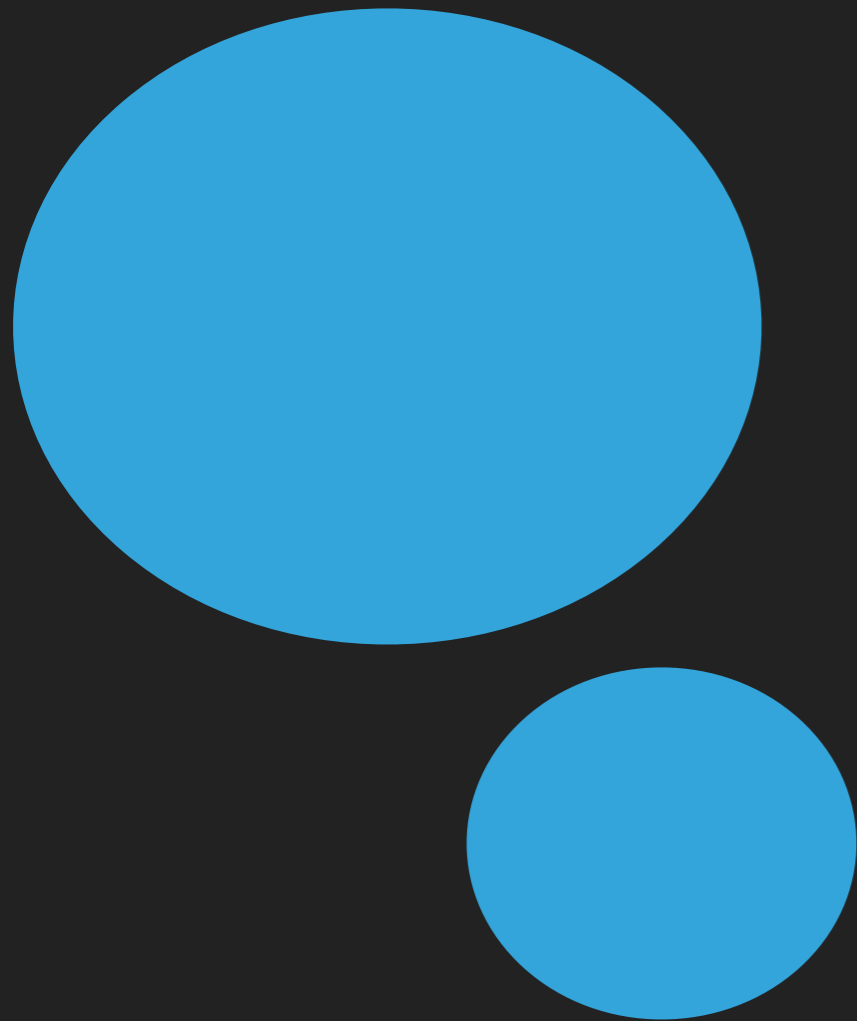


$$\Omega_{GW}(f) = \frac{f}{\rho_c c^2} \int d\theta p(\theta) \int_{z_{min}}^{z_{max}} dz \frac{R(z, \theta) dE_{GW}(\theta) / df_r}{(1+z)H(z)}$$

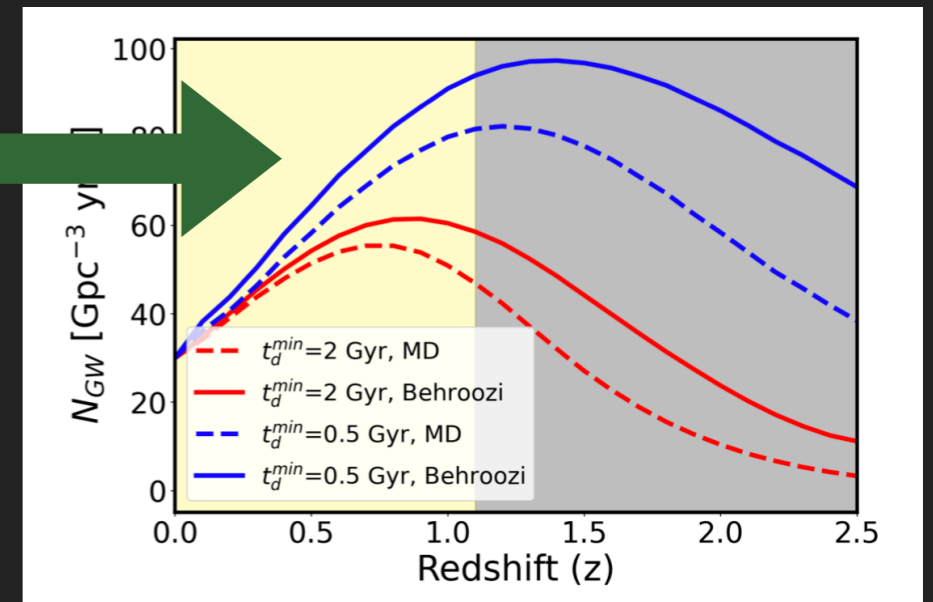
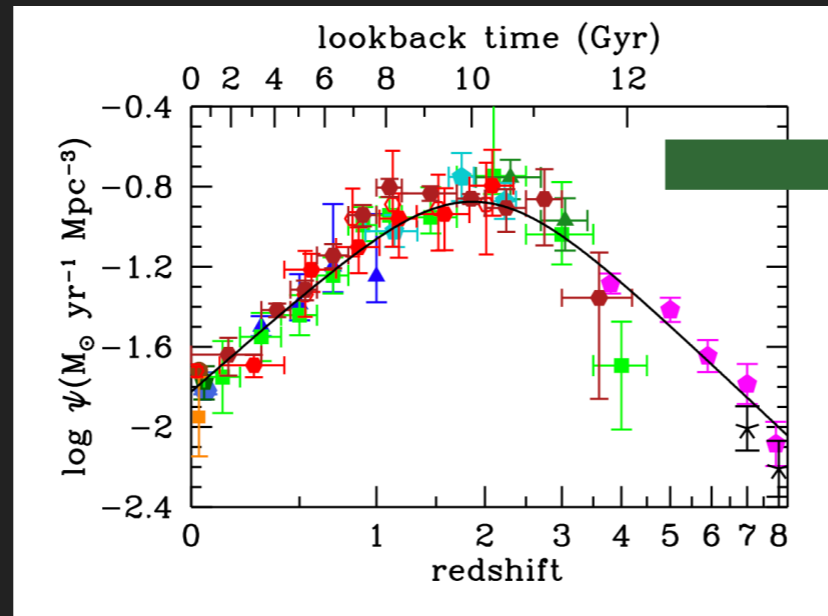
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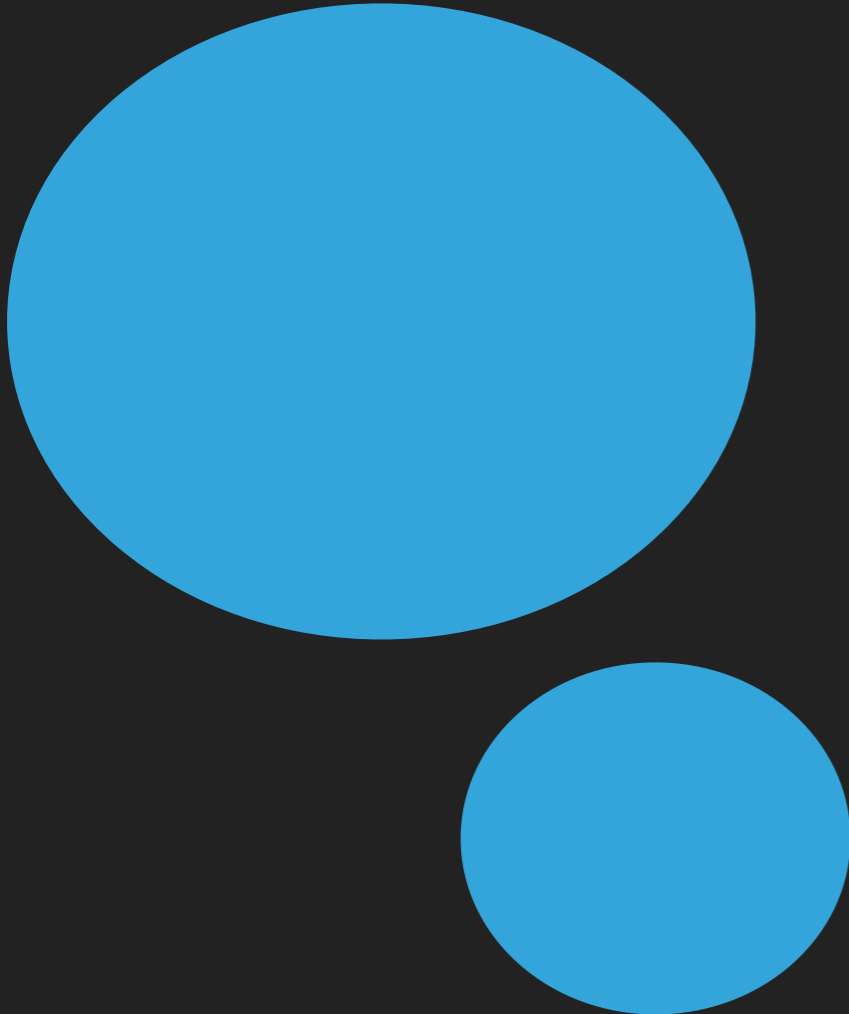
ASTROPHYSICAL BLACK HOLE OR PRIMORDIAL BLACK HOLE?



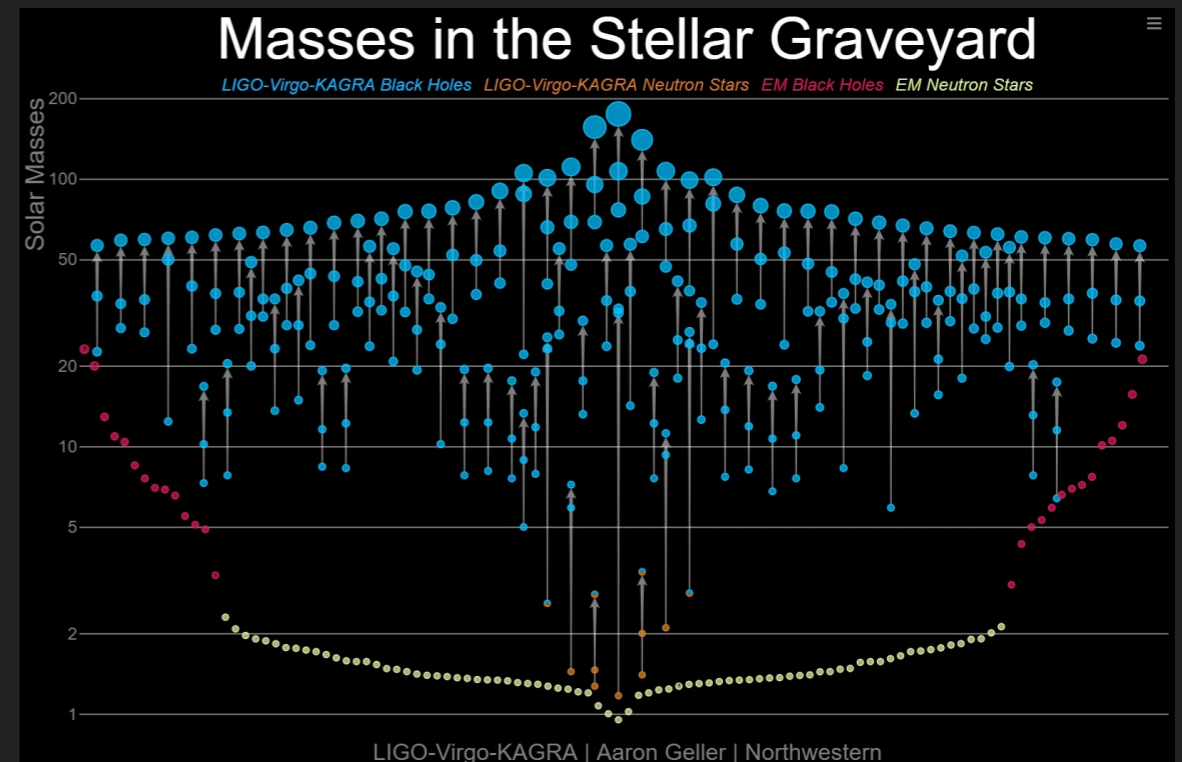
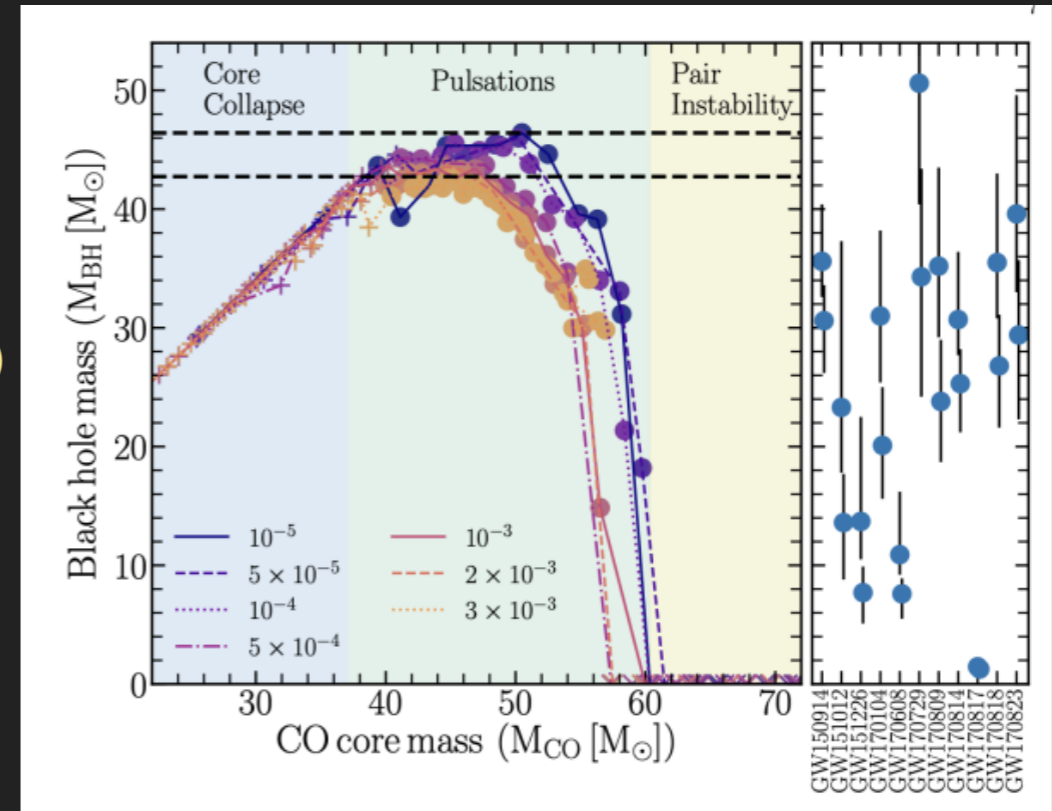
ASTROPHYSICAL BLACK HOLES: WILL TRACE STAR FORMATION RATE



ASTROPHYSICAL BLACK HOLES: MASS DISTRIBUTION WILL HAVE GAPS



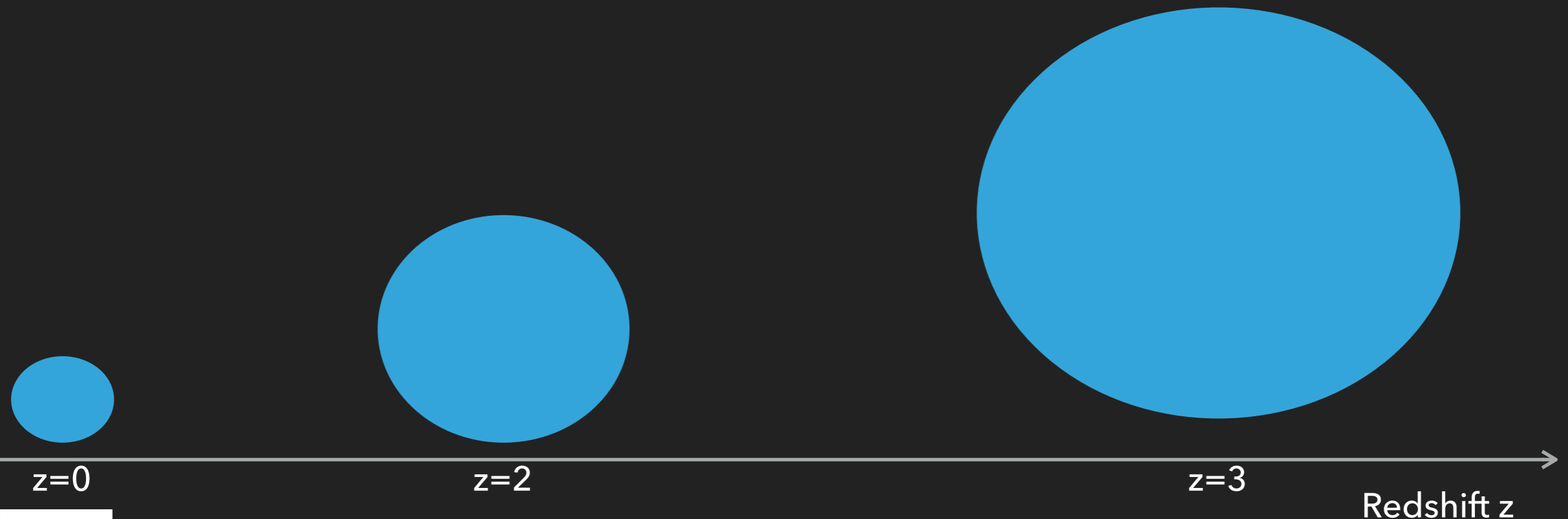
Farmer et al (2020)



WHAT CHARACTERISES THE BLACK HOLE POPULATION (SO FAR)

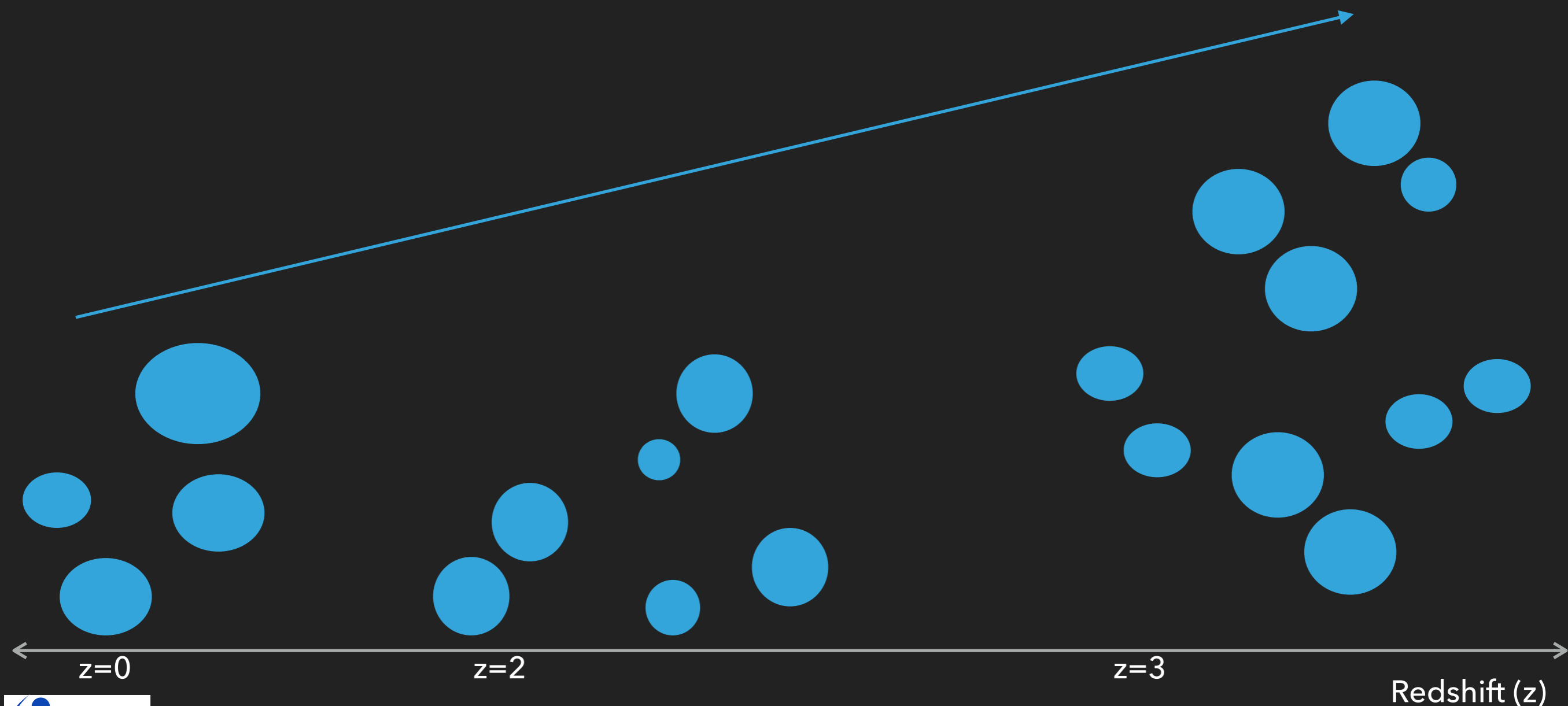
- ▶ We observe 'redshifted masses'

$$M_z = (1 + z)M_{true}$$

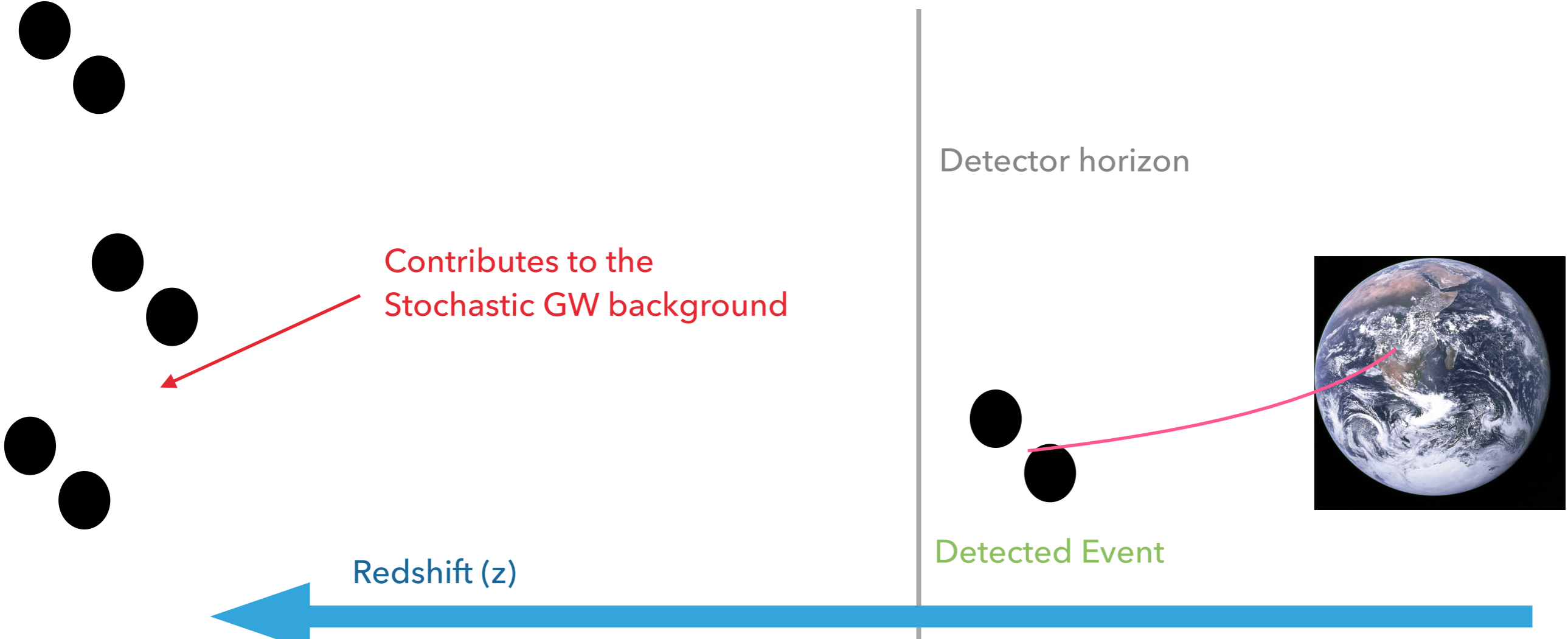


WHAT CHARACTERISES THE BLACK HOLE POPULATION (SO FAR)

- ▶ Merger rate of compact objects



LESS OBJECTS COALESCING AT HIGH REDSHIFT LEAD TO WEAK STOCHASTIC BACKGROUND



Contributes to the Stochastic GW background

Detector horizon

Detected Event

Redshift (z)

Distribution of the astrophysical system's source parameters

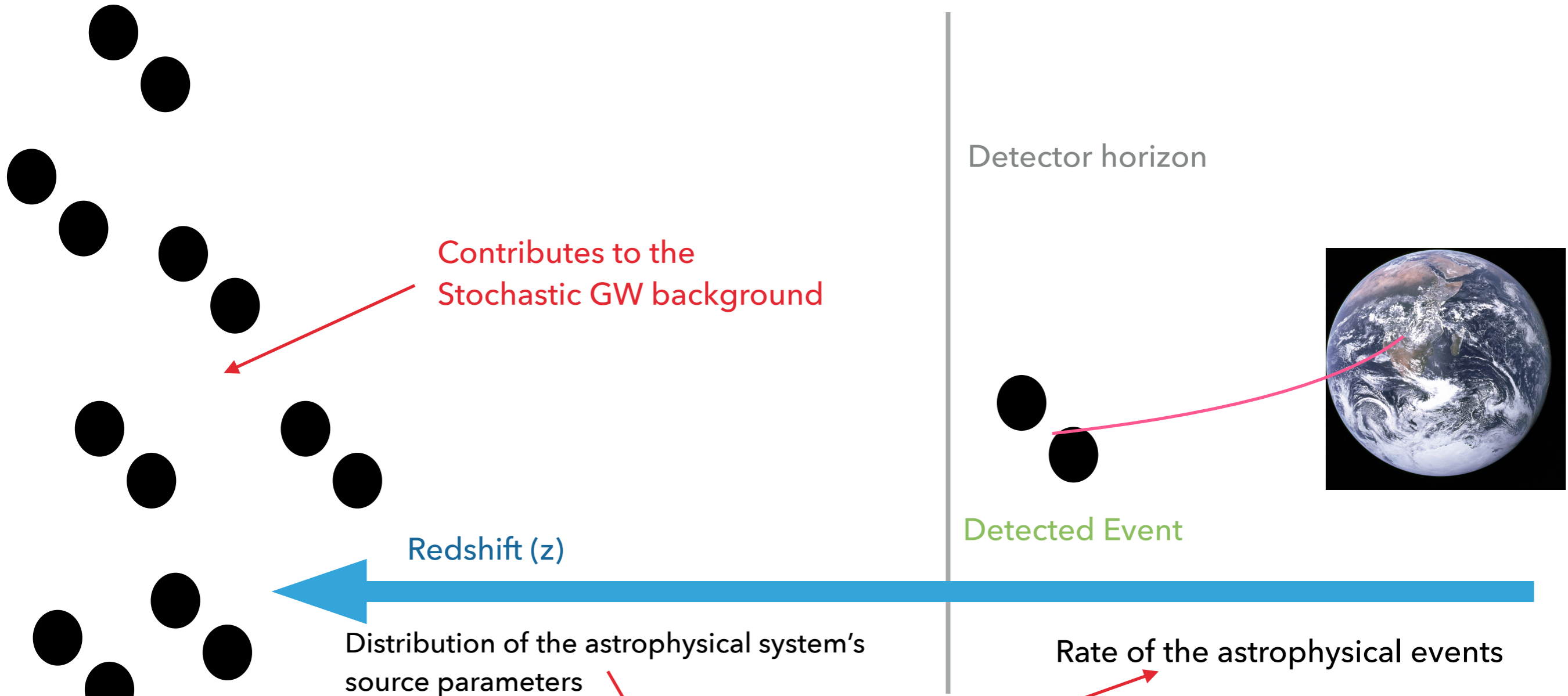
Rate of the astrophysical events

$$\Omega_{GW}(f) = \frac{f}{\rho_c c^2} \int d\theta p(\theta) \int_{z_{min}}^{z_{max}} dz \frac{R(z, \theta) dE_{GW}(\theta) / df_r}{(1+z)H(z)}$$

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MORE OBJECTS COALESCING AT HIGH REDSHIFT LEAD TO LOUD STOCHASTIC BACKGROUND



Contributes to the Stochastic GW background

Redshift (z)

Distribution of the astrophysical system's source parameters

Detector horizon

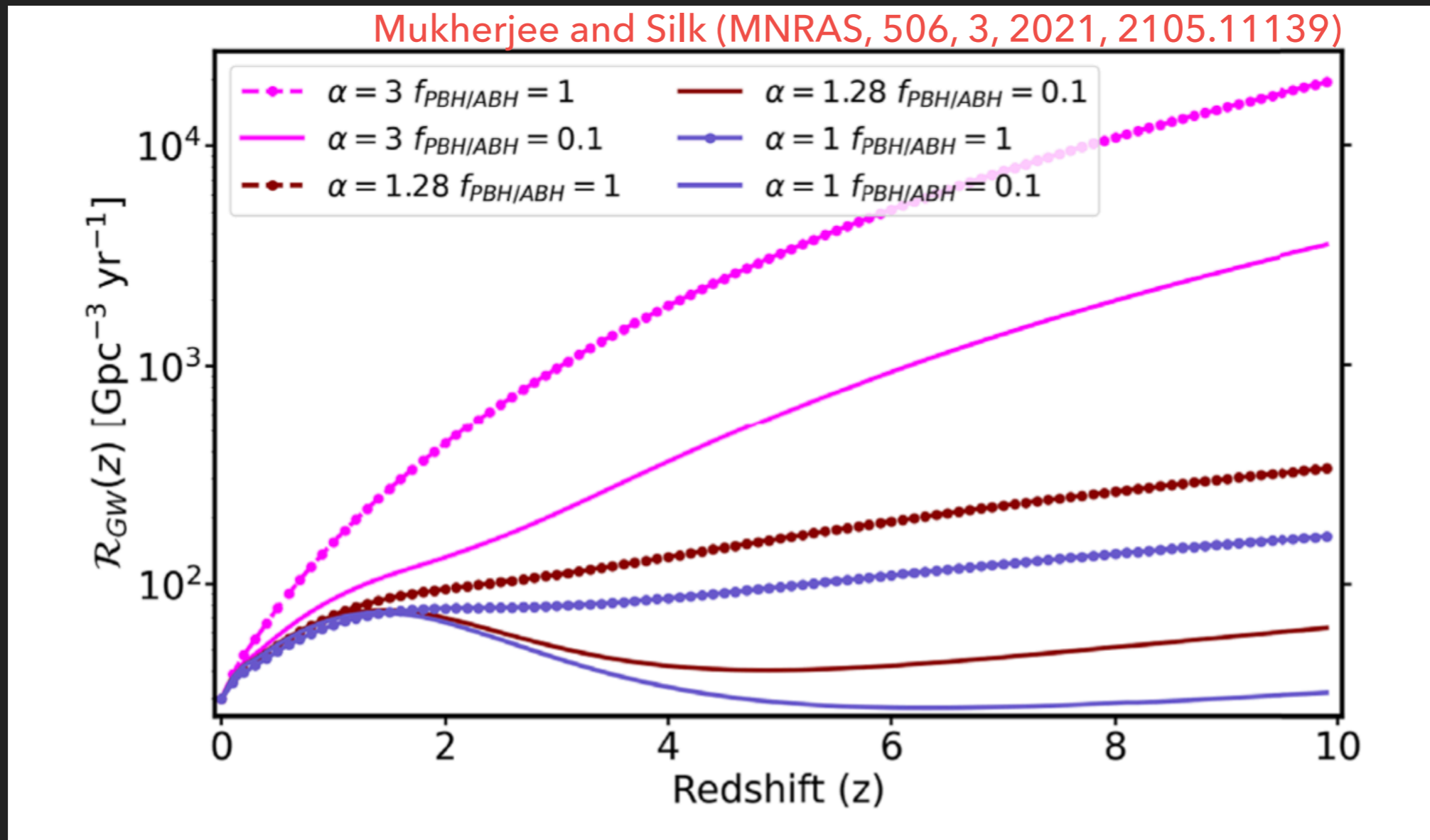
Detected Event

Rate of the astrophysical events



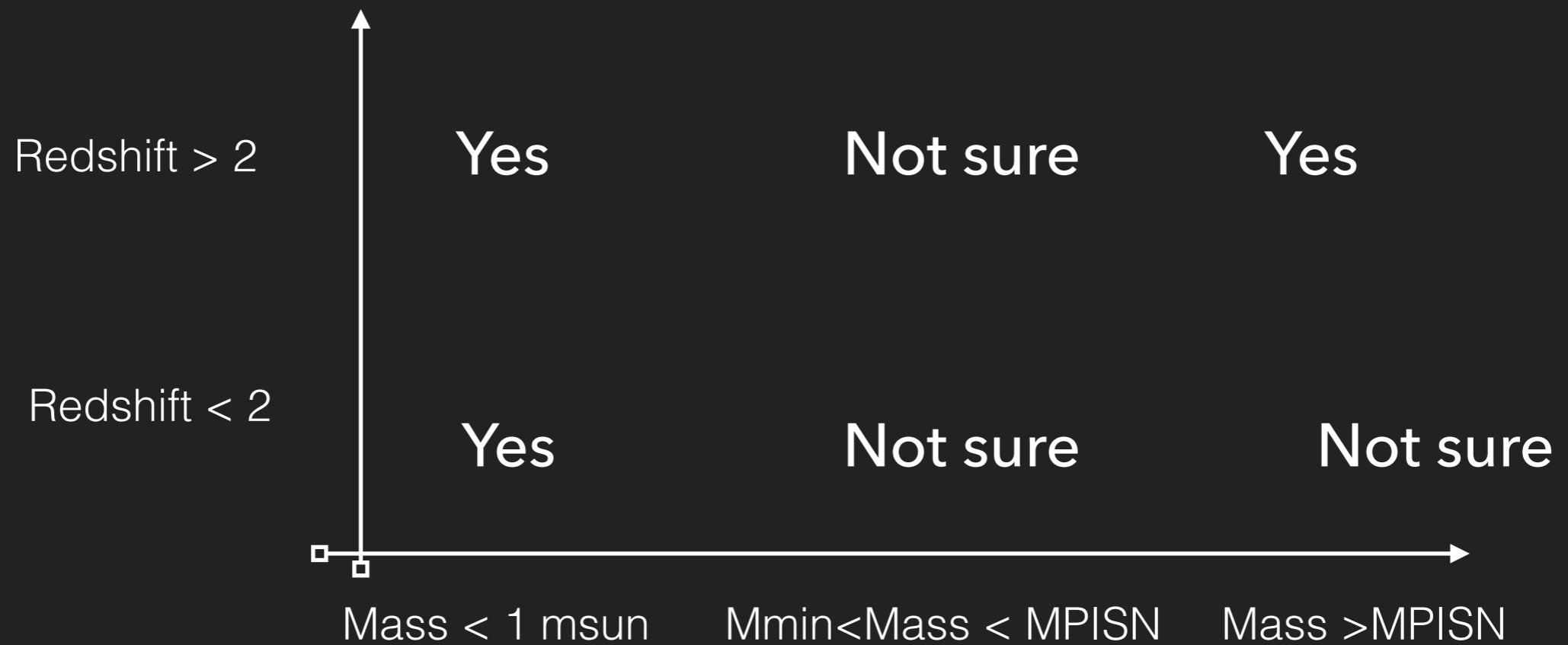
$$\Omega_{GW}(f) = \frac{f}{\rho_c c^2} \int d\theta p(\theta) \int_{z_{min}}^{z_{max}} dz \frac{R(z, \theta) dE_{GW}(\theta) / df_r}{(1+z)H(z)}$$

MERGER RATE

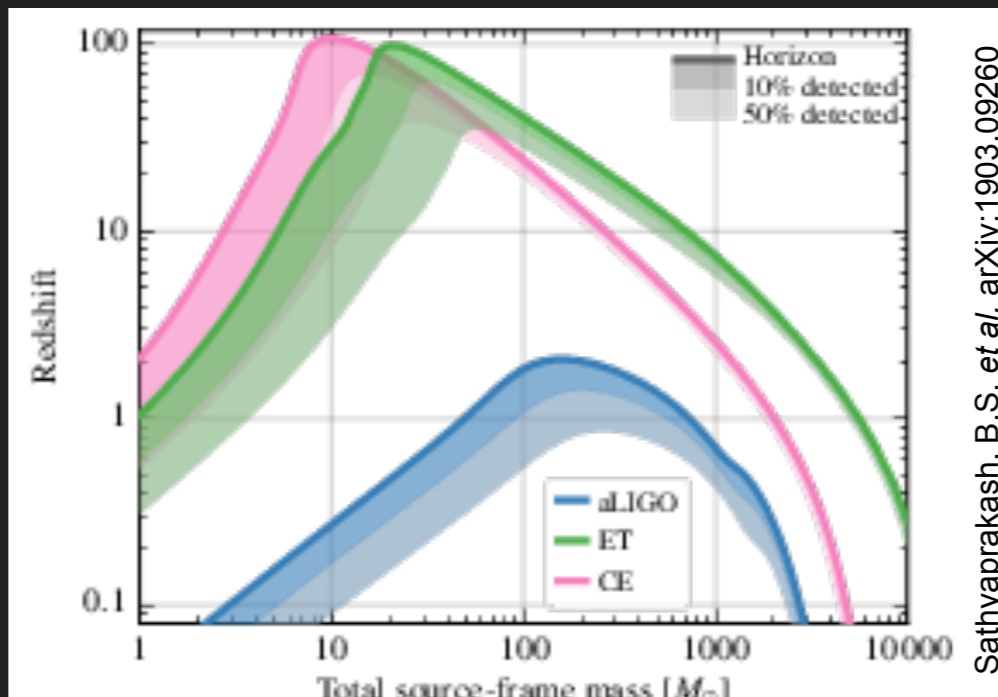


Redshift evolution of the merger rate is more reliable than the amplitude of the merger rate.

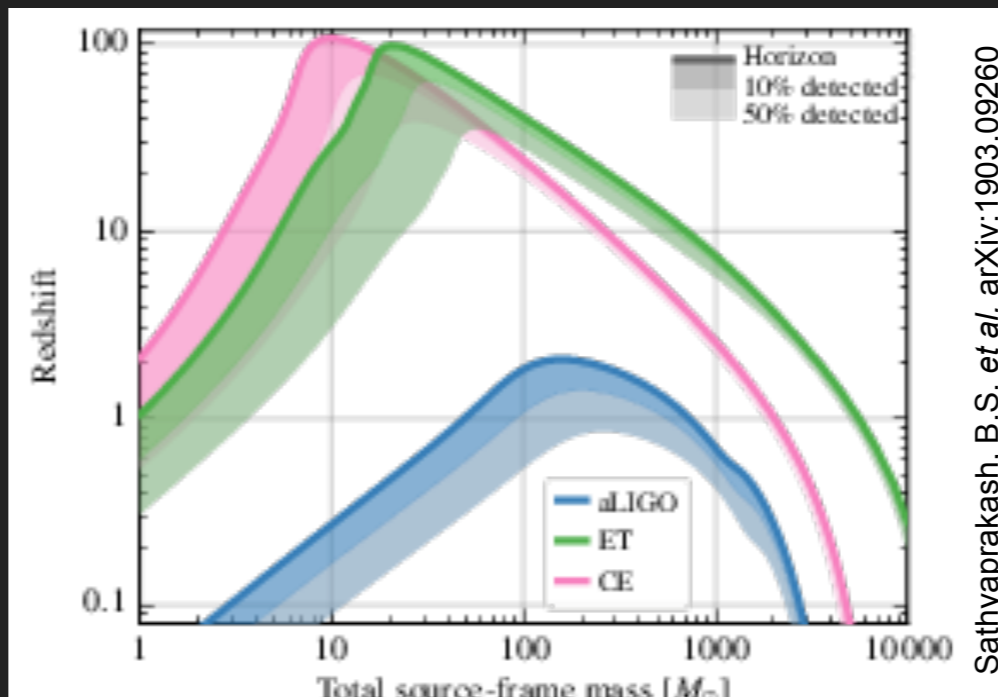
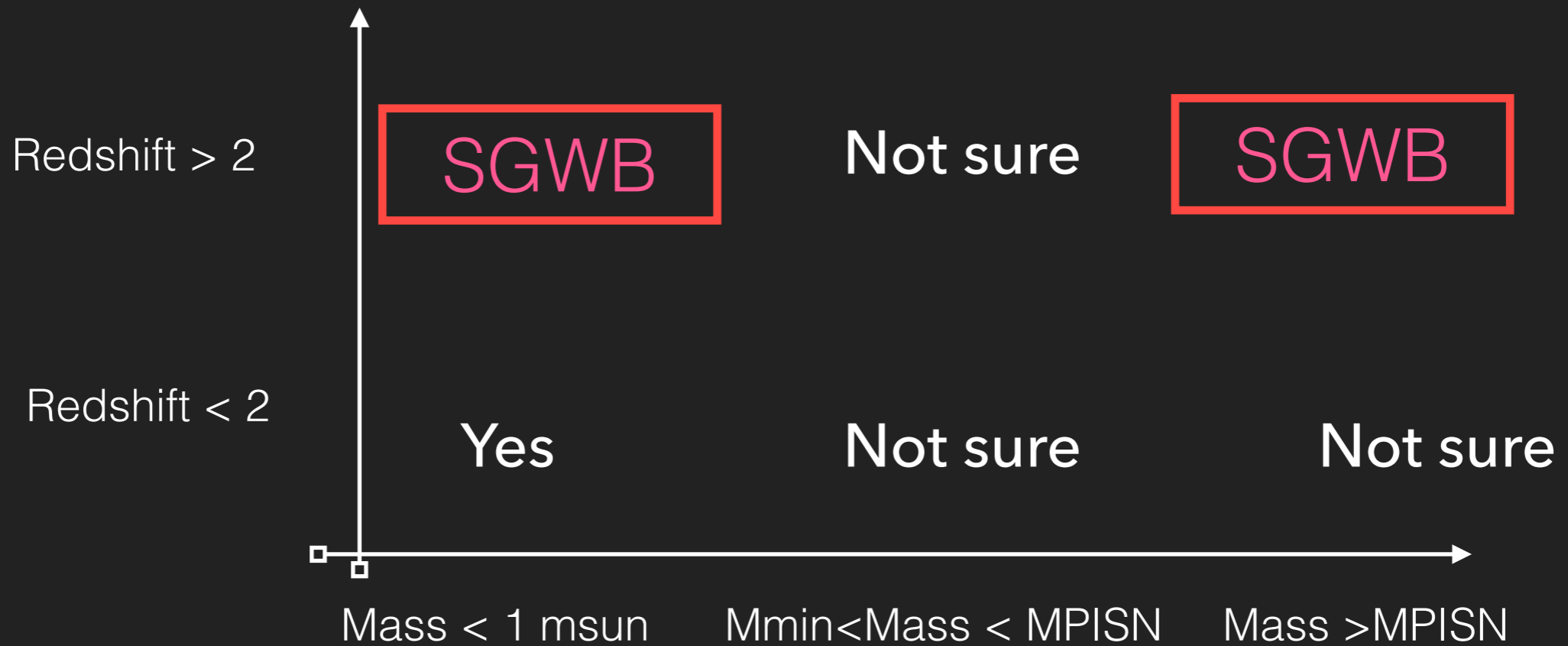
MASS-REDSHIFT RANGE WHERE BLACK HOLES CAN BE DISTINGUISHED



MASS-REDSHIFT RANGE WHERE BLACK HOLES CAN BE DISTINGUISHED

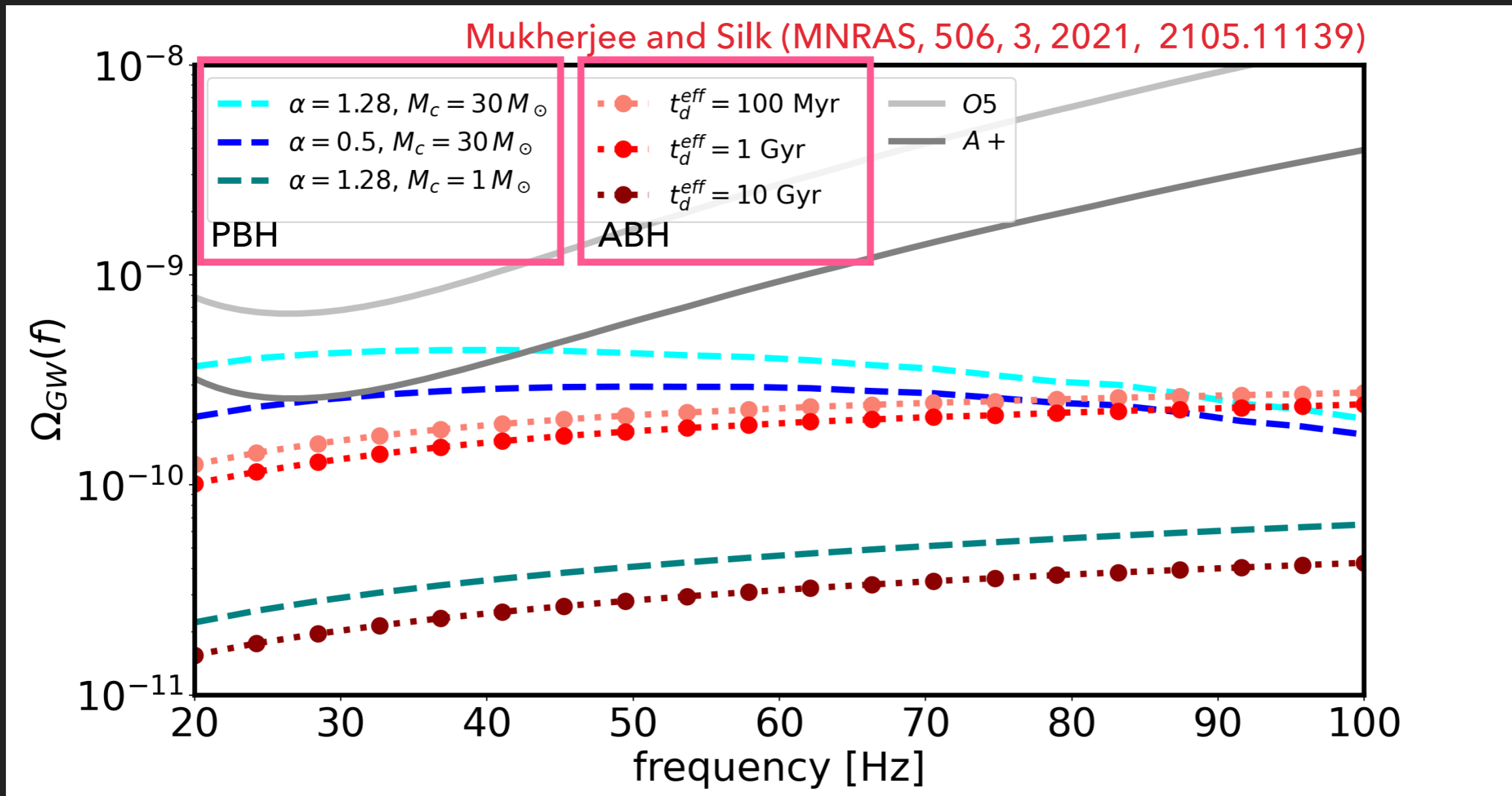


STOCHASTIC GW BACKGROUND CAN PROVIDE SMOKING GUN SIGNATURE FOR PBHS



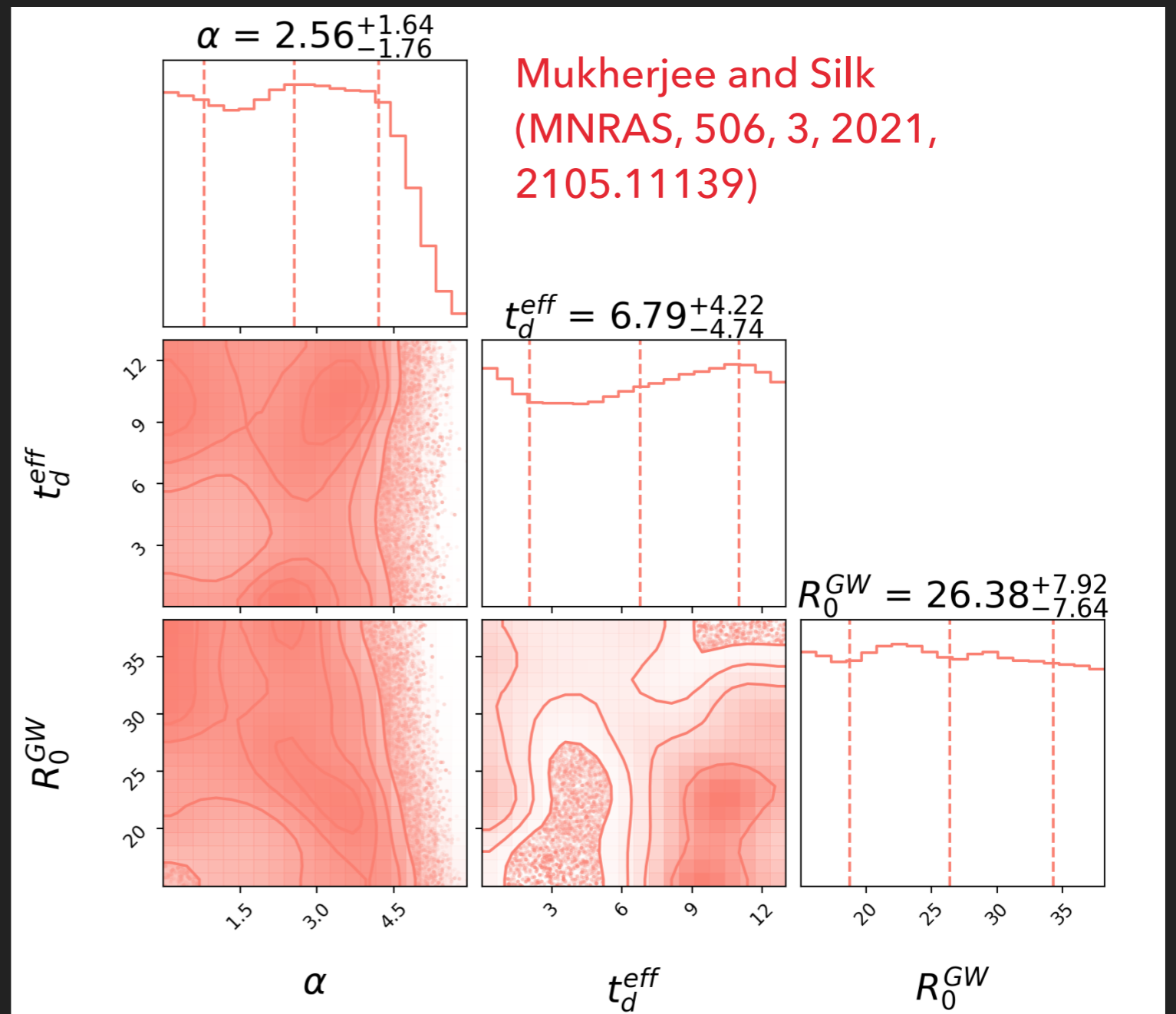
Sathyaprakash, B.S. et al. arXiv:1903.09260

STOCHASTIC GW BACKGROUND FOR DIFFERENT SCENARIOS



BOUND FROM THE O3 DATA OF LIGO-VIRGO

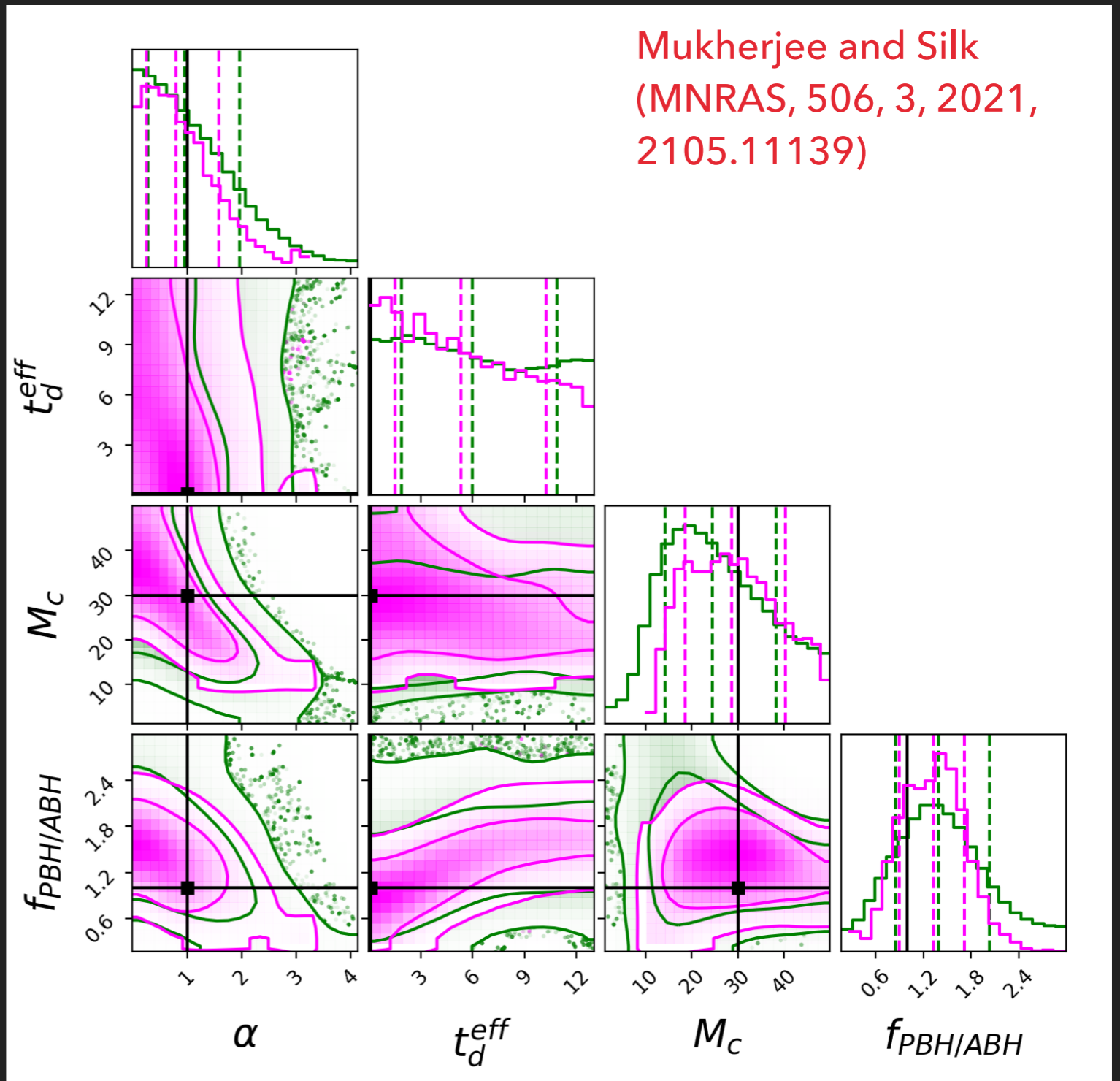
Weak constraints from the current observations.



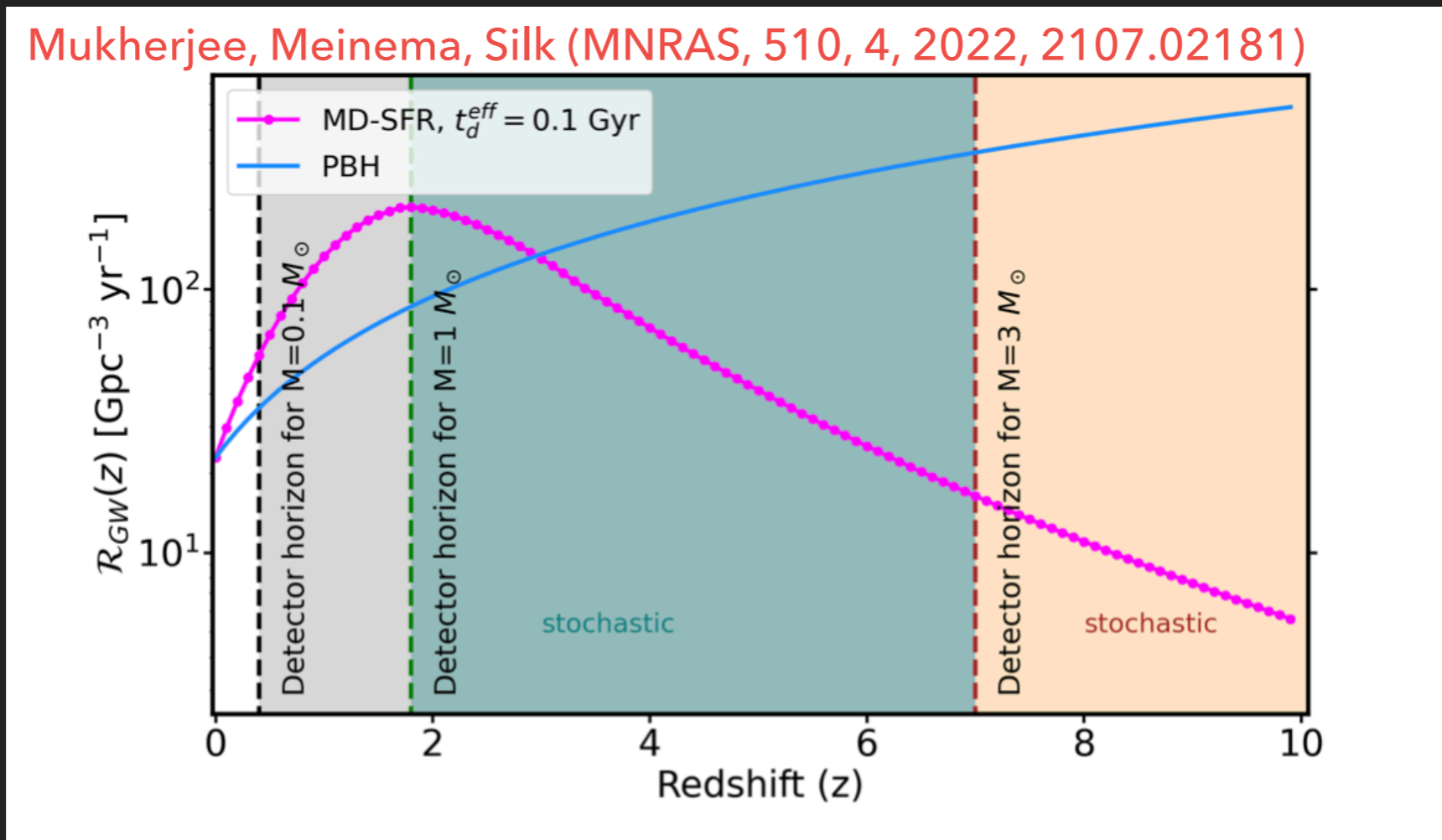
FORECAST FOR O5 AND A+ SENSITIVITY TO DISTINGUISH ABHS AND PBHS

Take home message: We can distinguish between the population of ABHs and PBHs using the stochastic GW background.

Mukherjee and Silk
(MNRAS, 506, 3, 2021,
2105.11139)



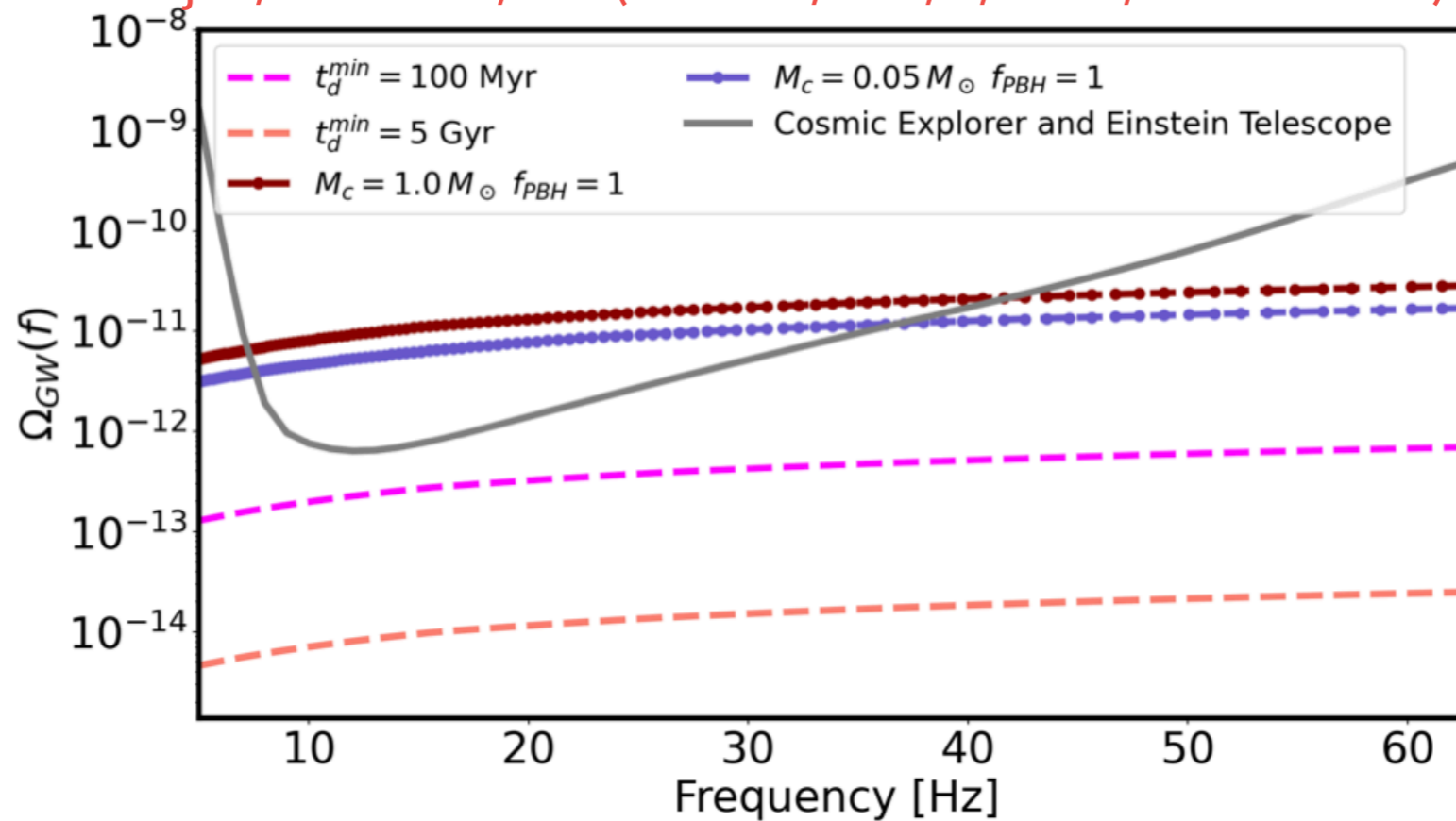
MERGER RATE



Redshift evolution of the merger rate is more reliable than the amplitude of the merger rate.

STOCHASTIC GW BACKGROUND FOR DIFFERENT SCENARIOS

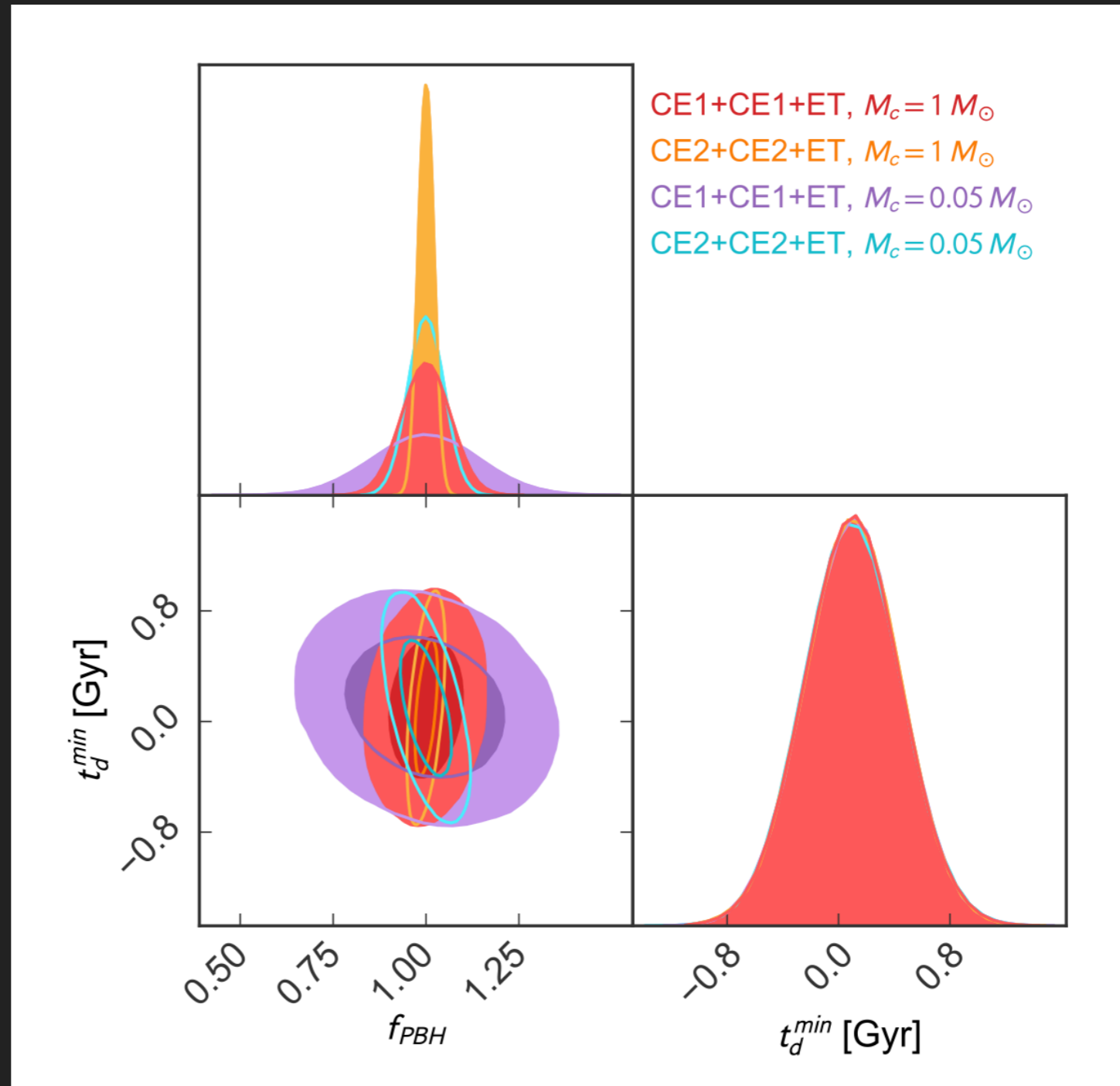
Mukherjee, Meinema, Silk (MNRAS, 510, 4, 2022, 2107.02181)



FORECAST FOR CE AND ET SENSITIVITY TO DISTINGUISH ABHS AND PBHS

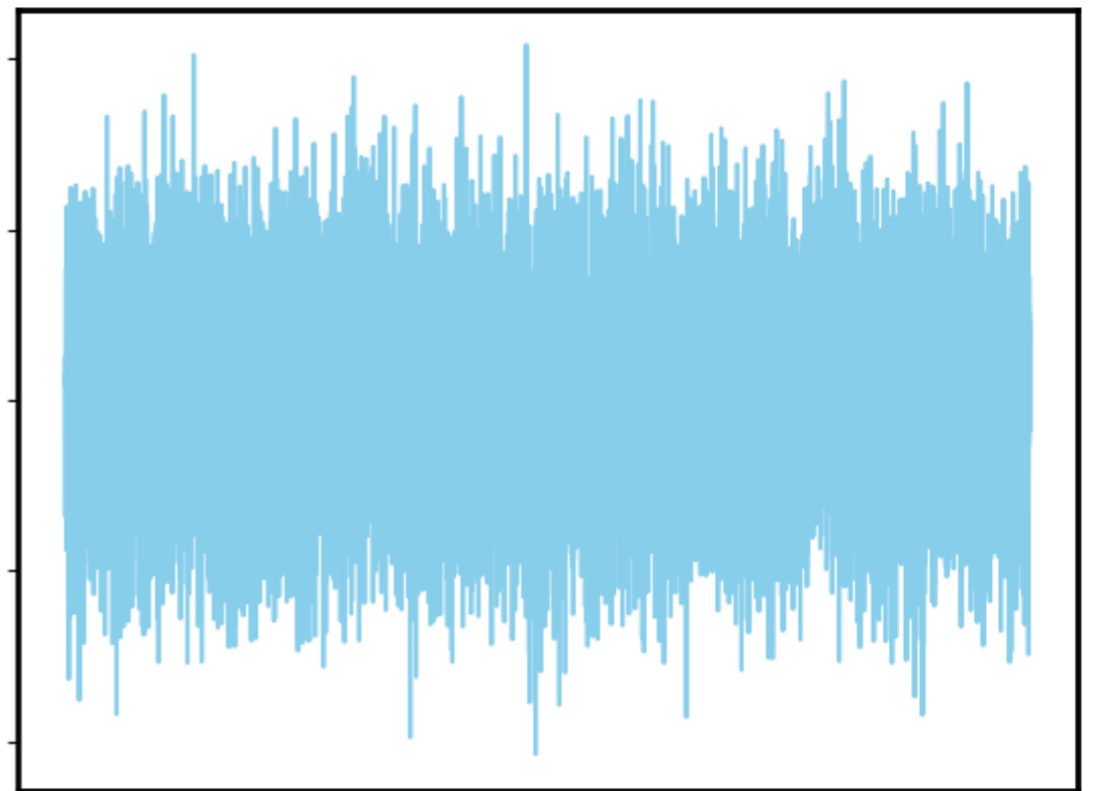
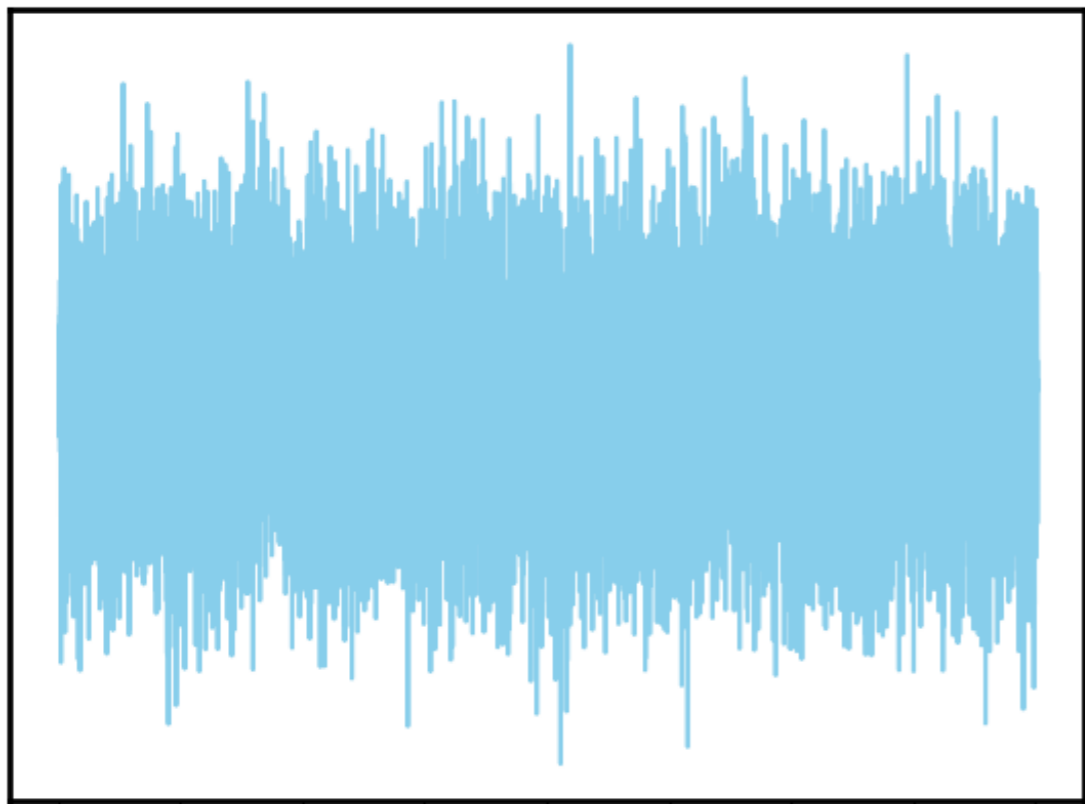
Mukherjee, Meinema, Silk (MNRAS, 510, 4, 2022, 2107.02181)

Take home message: We can distinguish between the population of ABHs and PBHs at the lower mass end.



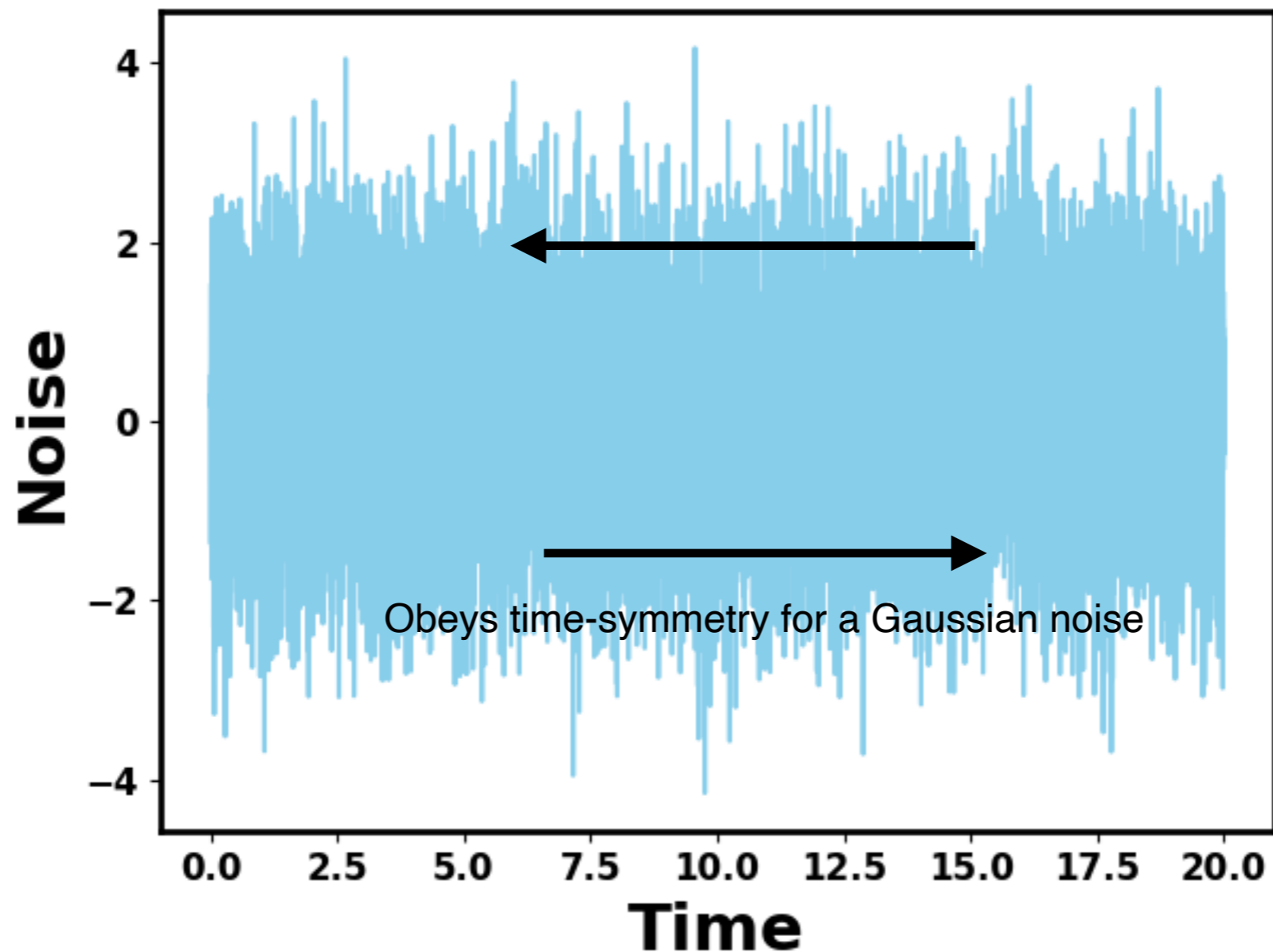
IS POWER SPECTRUM THE SUFFICIENT STATISTICS?

IS SGWB SIGNAL TIME-REVERSAL?



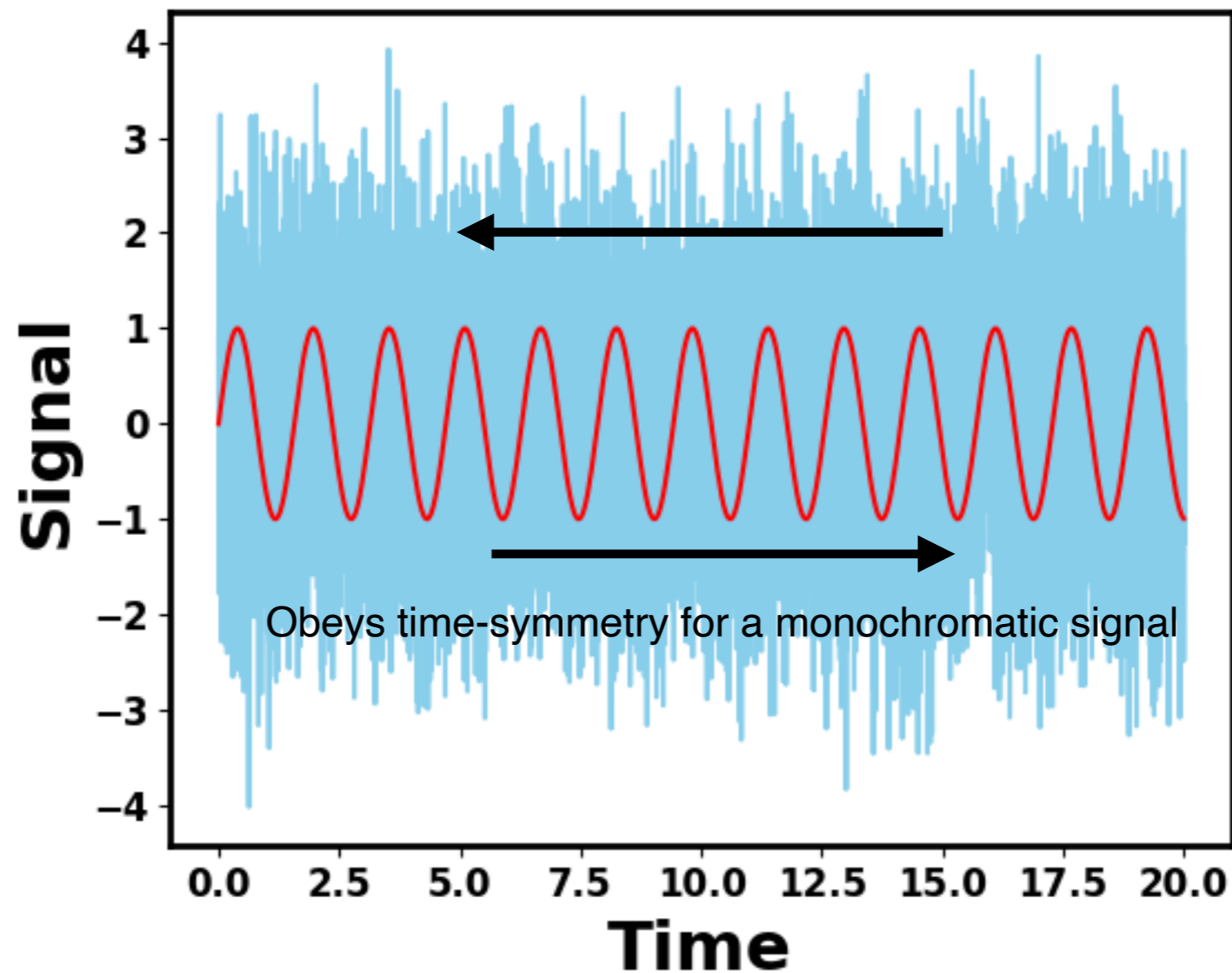
IS SGWB SIGNAL TIME-REVERSAL?

Sah and Mukherjee (2023)



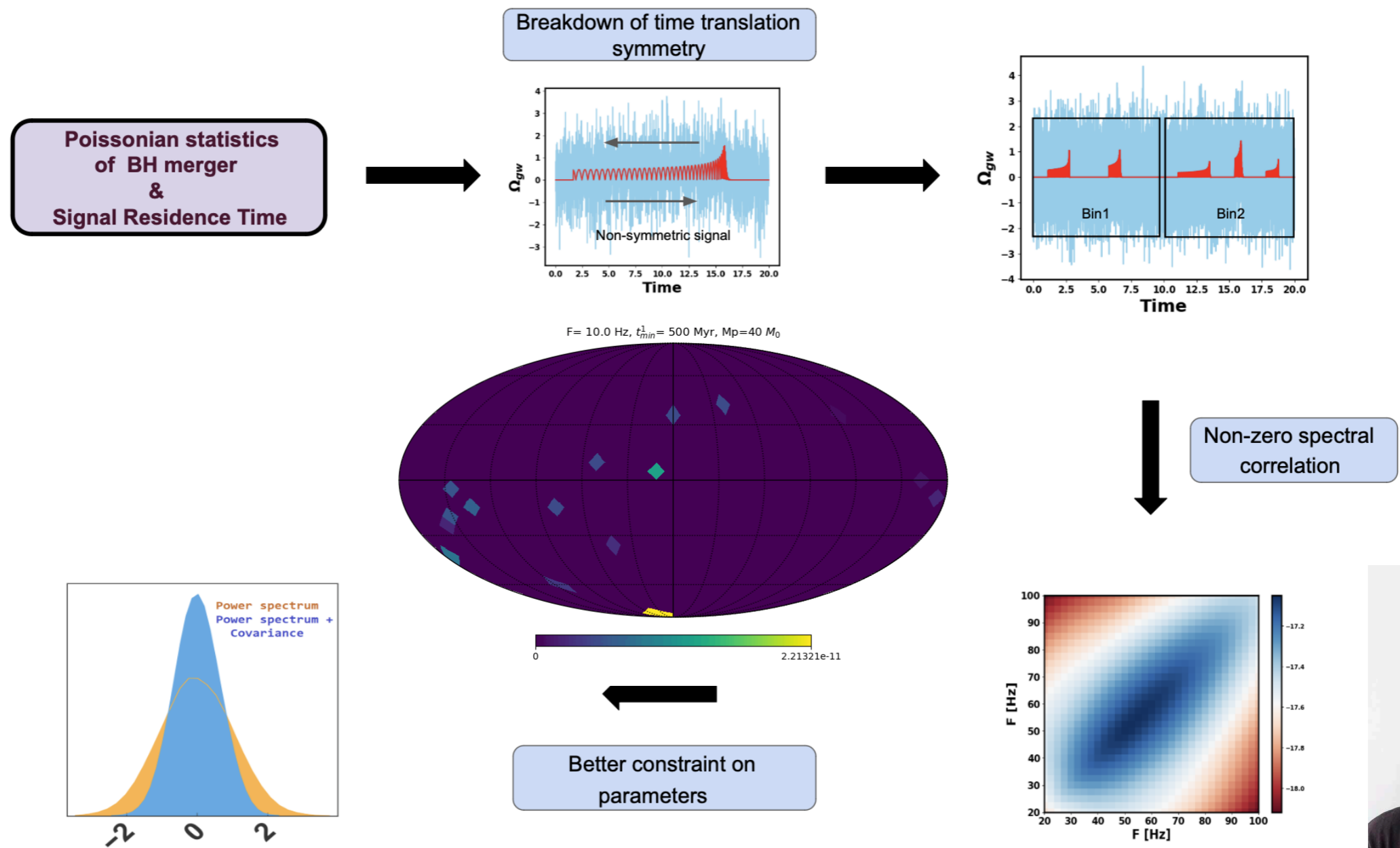
IS SGWB SIGNAL TIME-REVERSAL?

Sah and Mukherjee (2023)



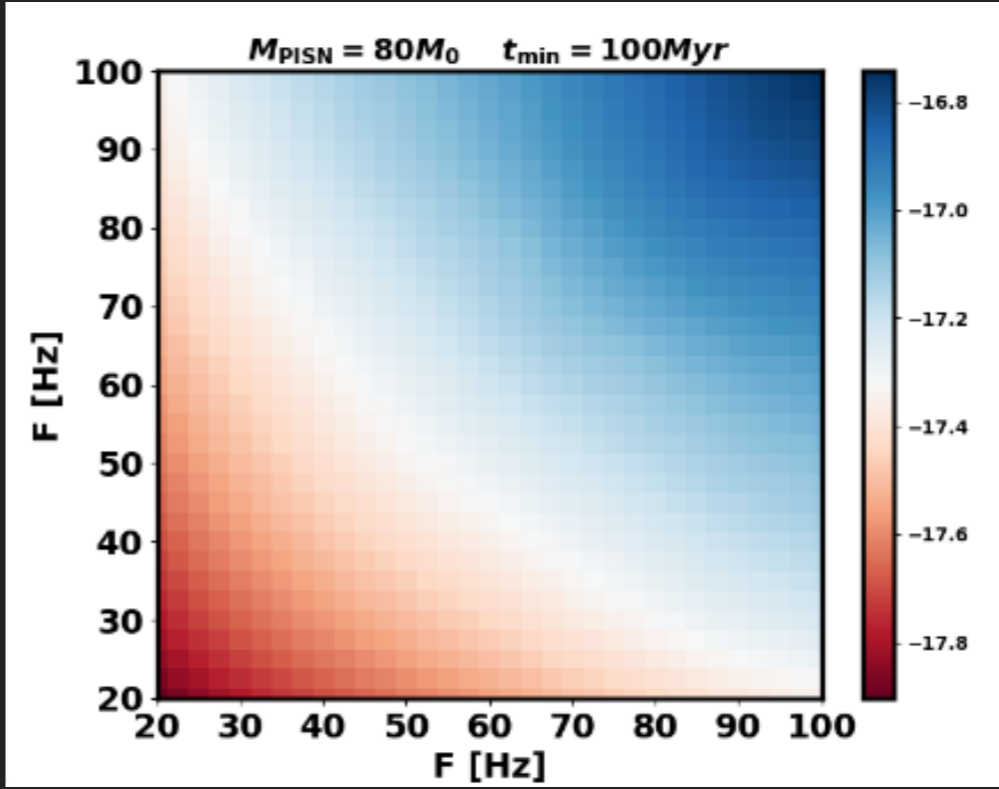
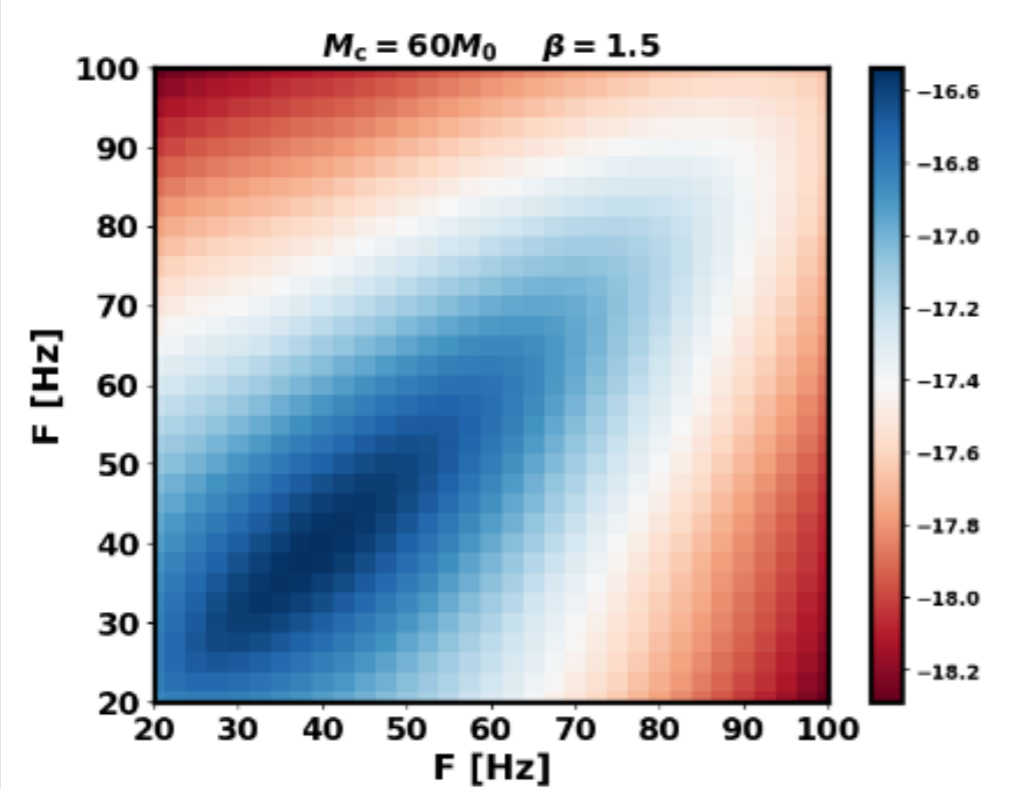
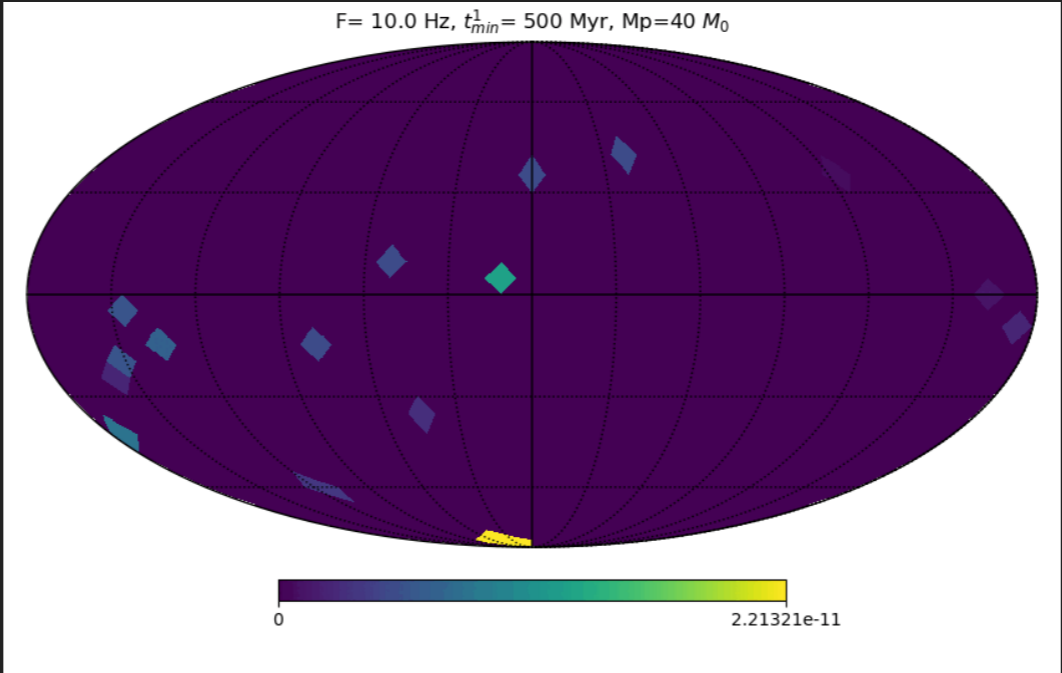
BREAK DOWN OF TIME-TRANSLATION SYMMETRY LEADS TO CORRELATION IN THE SIGNAL COVARIANCE MATRIX

Sah and Mukherjee (2023)



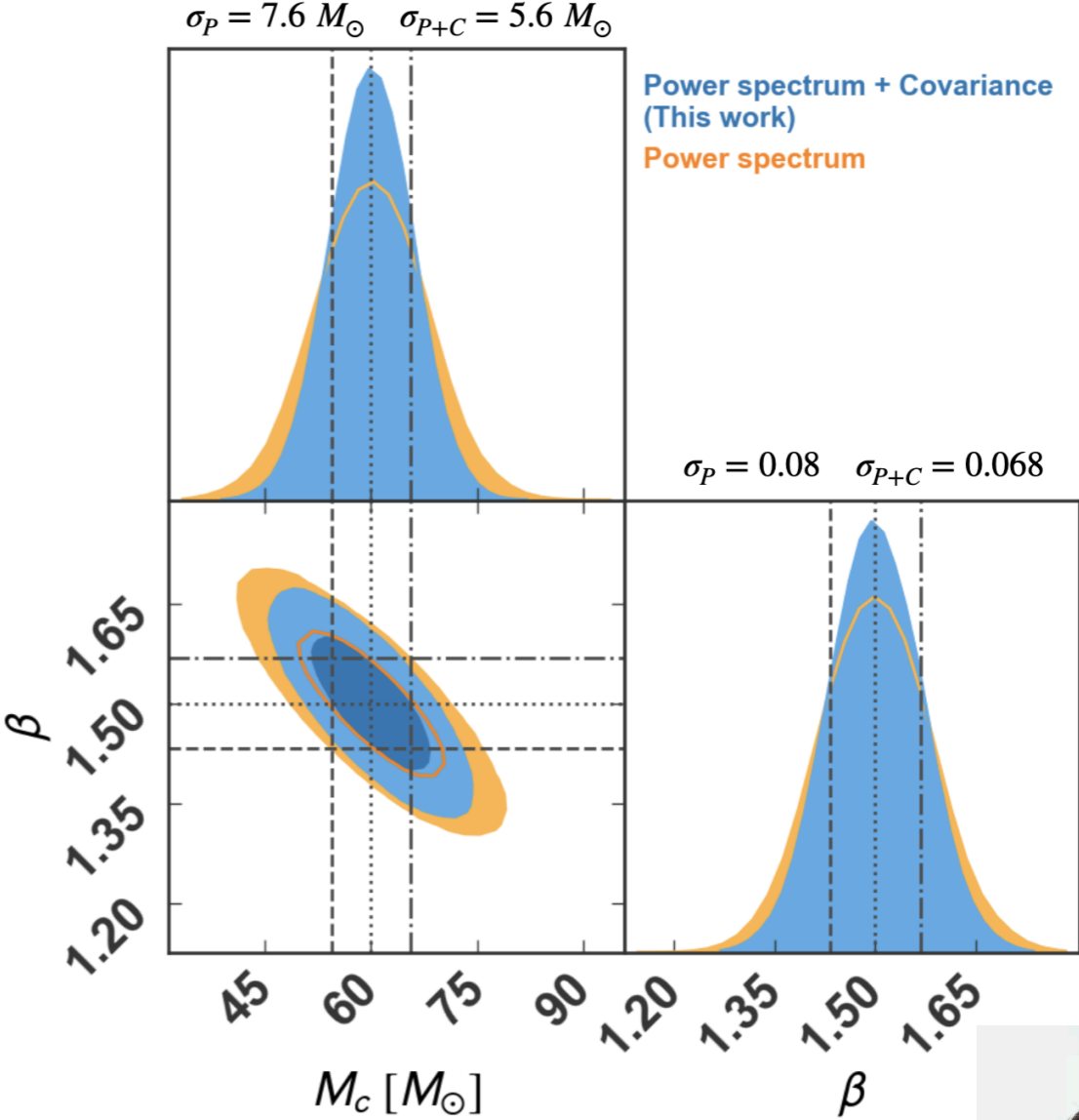
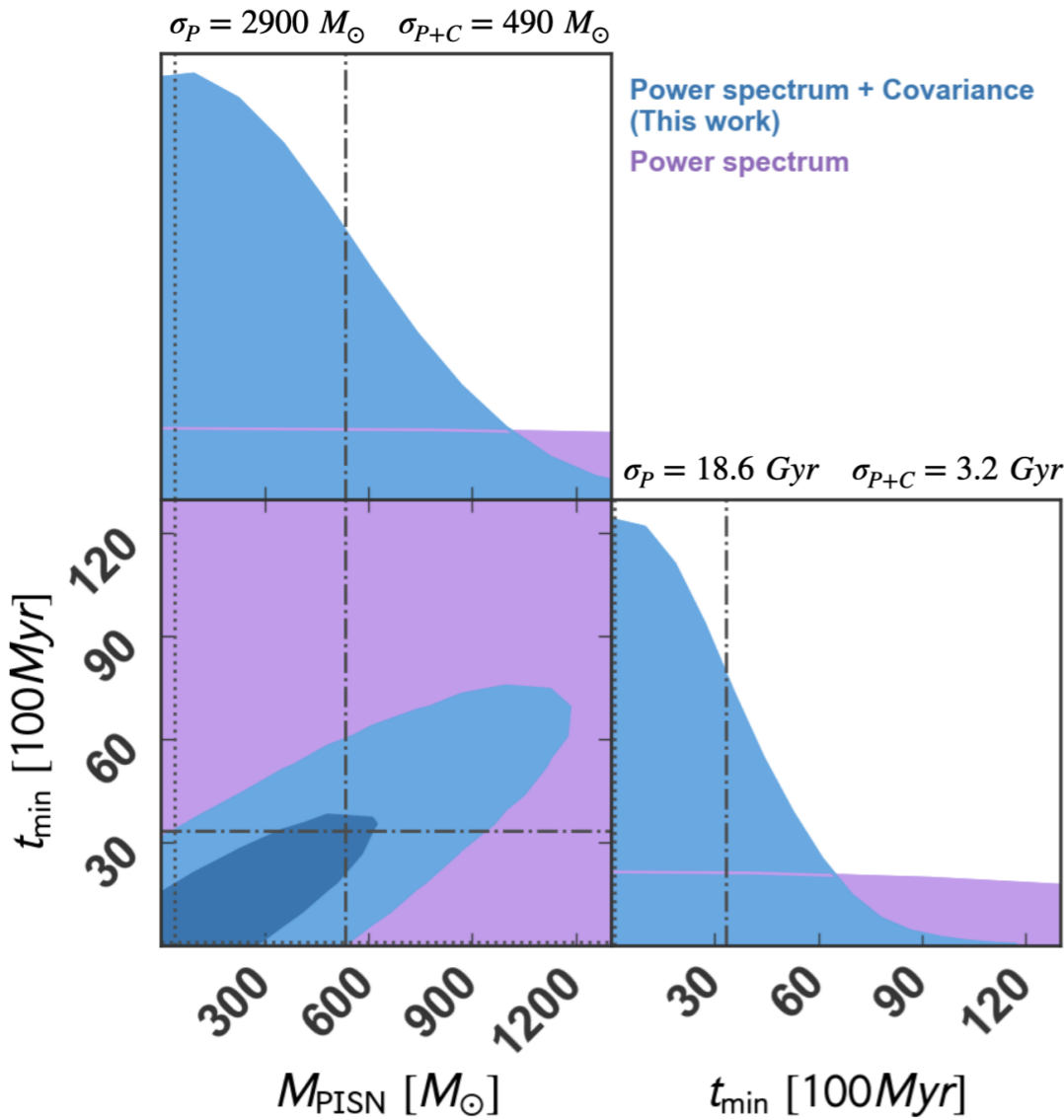
BLACK HOLE PROPERTIES AT HIGH REDSHIFT CAN BE PROBED USING BREAKDOWN OF TIME-SYMMETRY

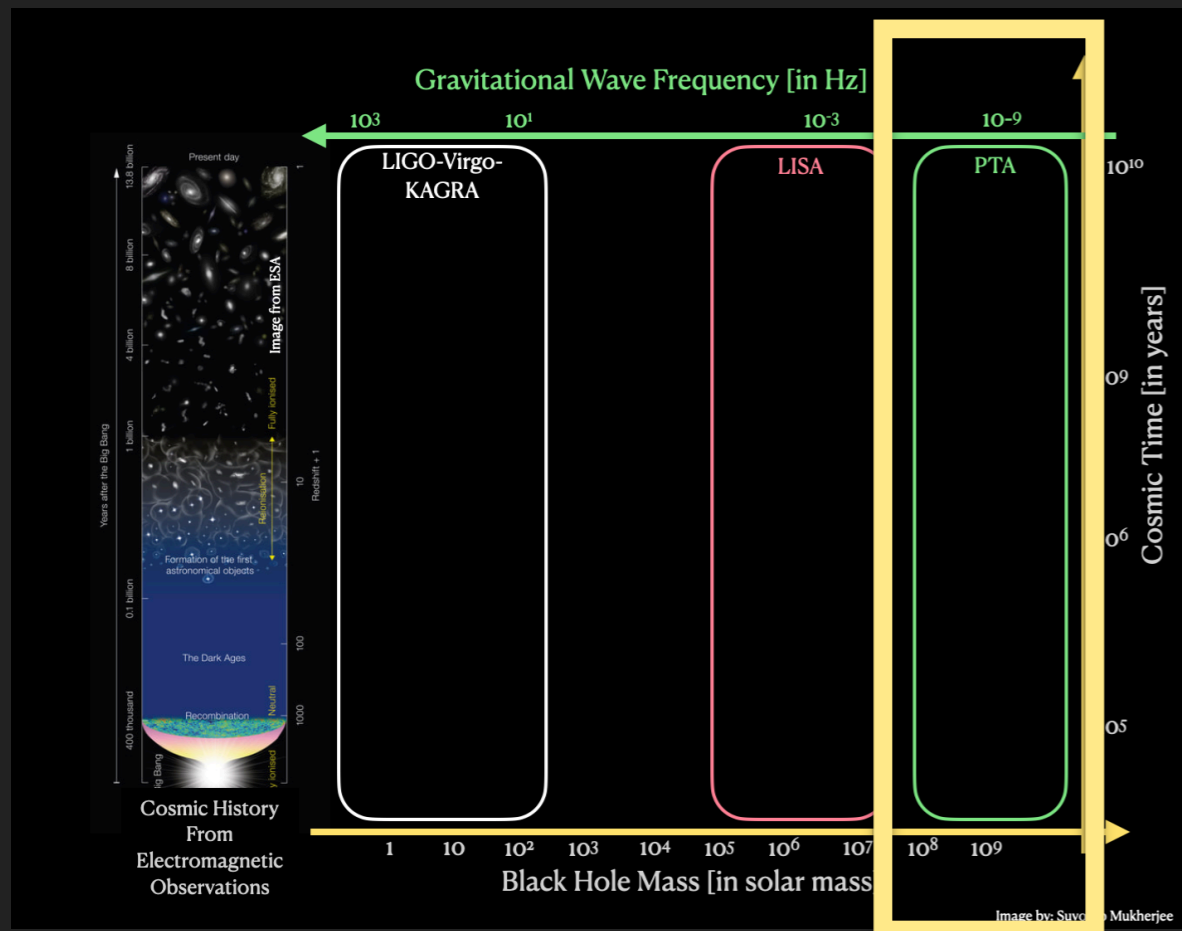
Sah and Mukherjee (2023)



BLACK HOLE PROPERTIES AT HIGH REDSHIFT CAN BE PROBED USING BREAKDOWN OF TIME-SYMMETRY

Sah and Mukherjee (2023)

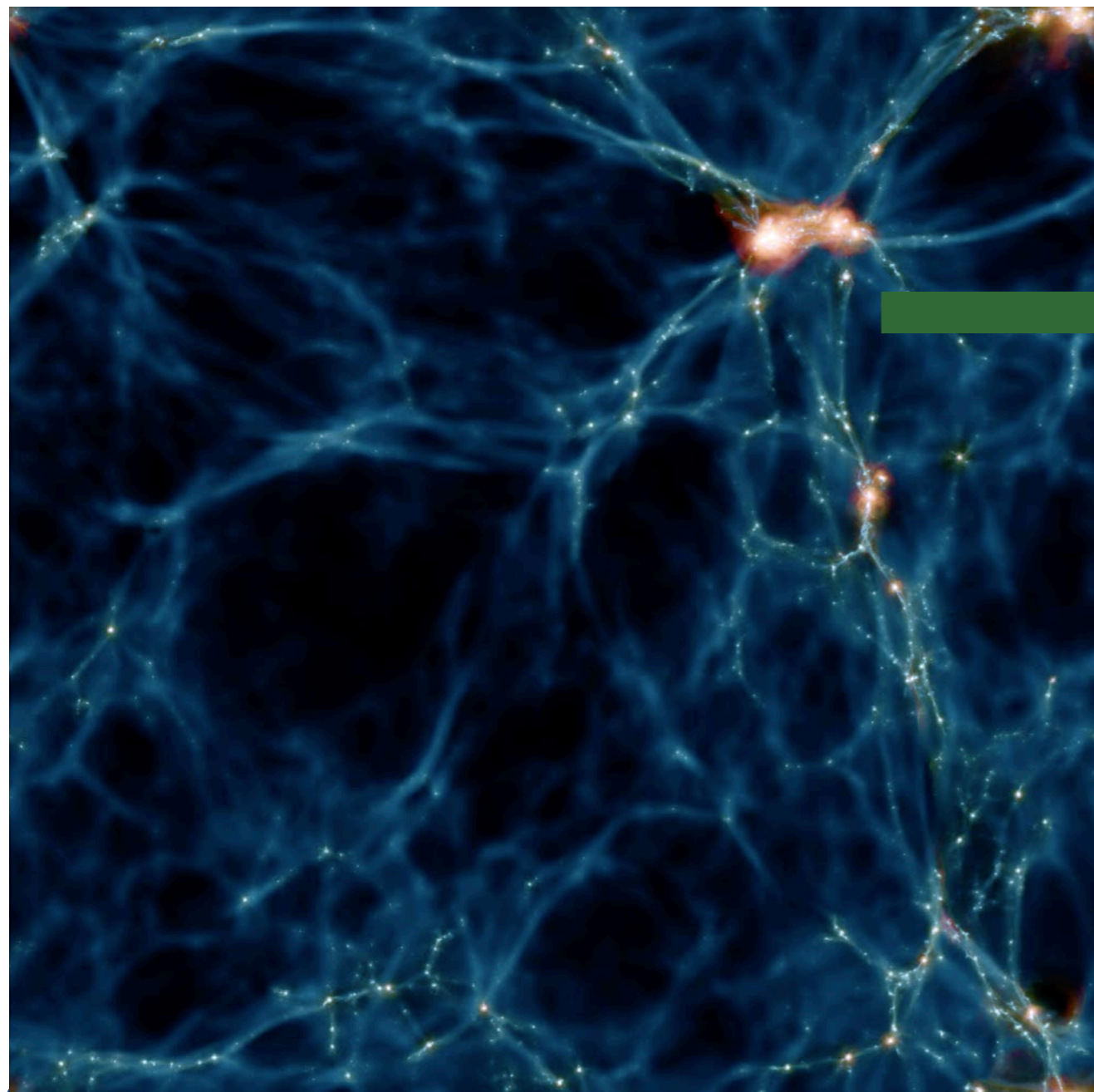




HIGH REDSHIFT UNIVERSE @NANO-HERTZ

Using PTA GW sources

WHERE ARE THE BIG BLACK HOLES FORMING?

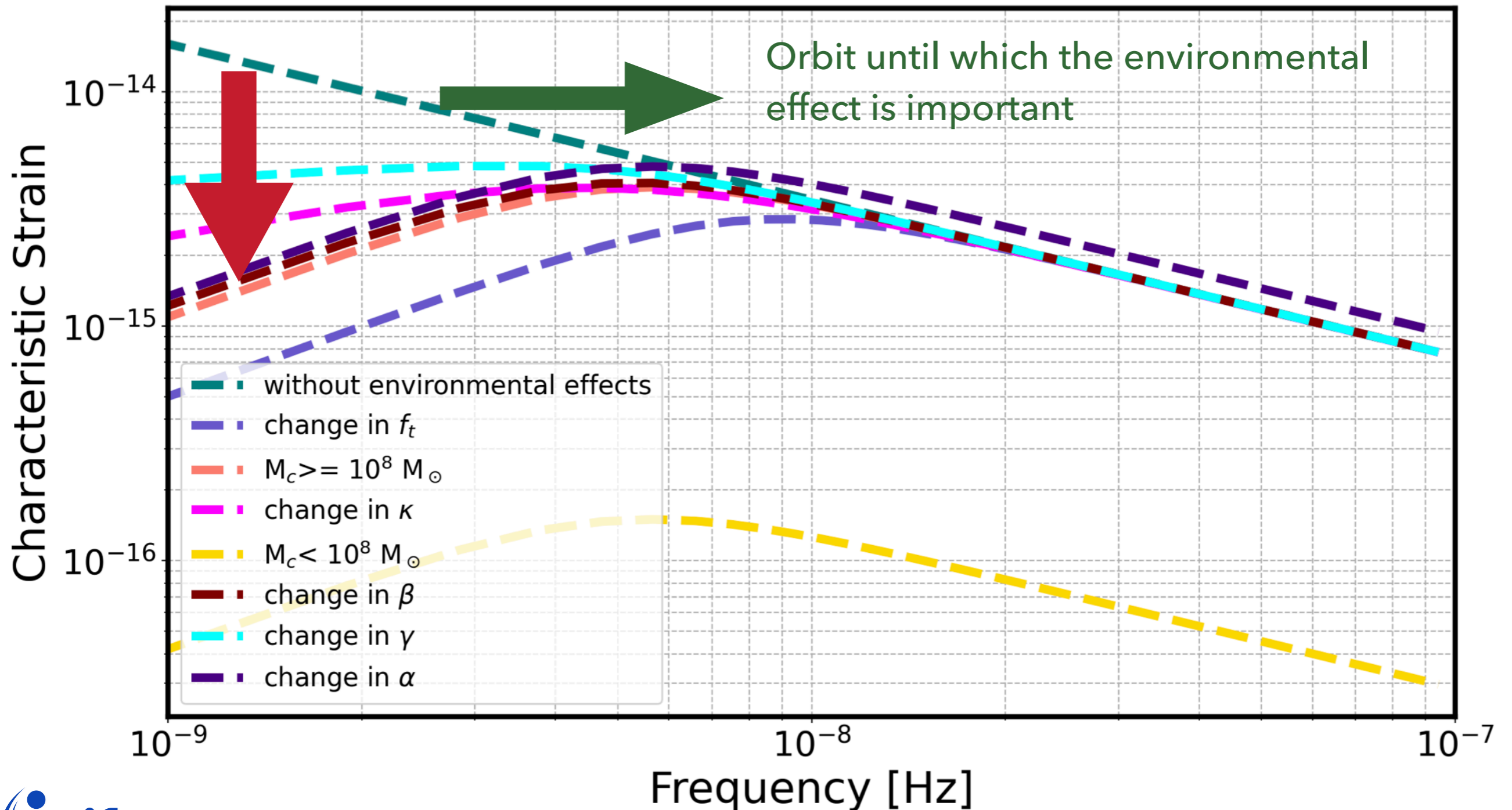


Gravitational Waves from VERY
Big Black Holes

ASTROPHYSICAL SGWB SIGNAL IN THE NANO-HZ RANGE FROM SMBBHs

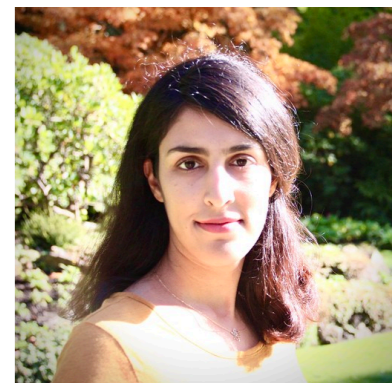
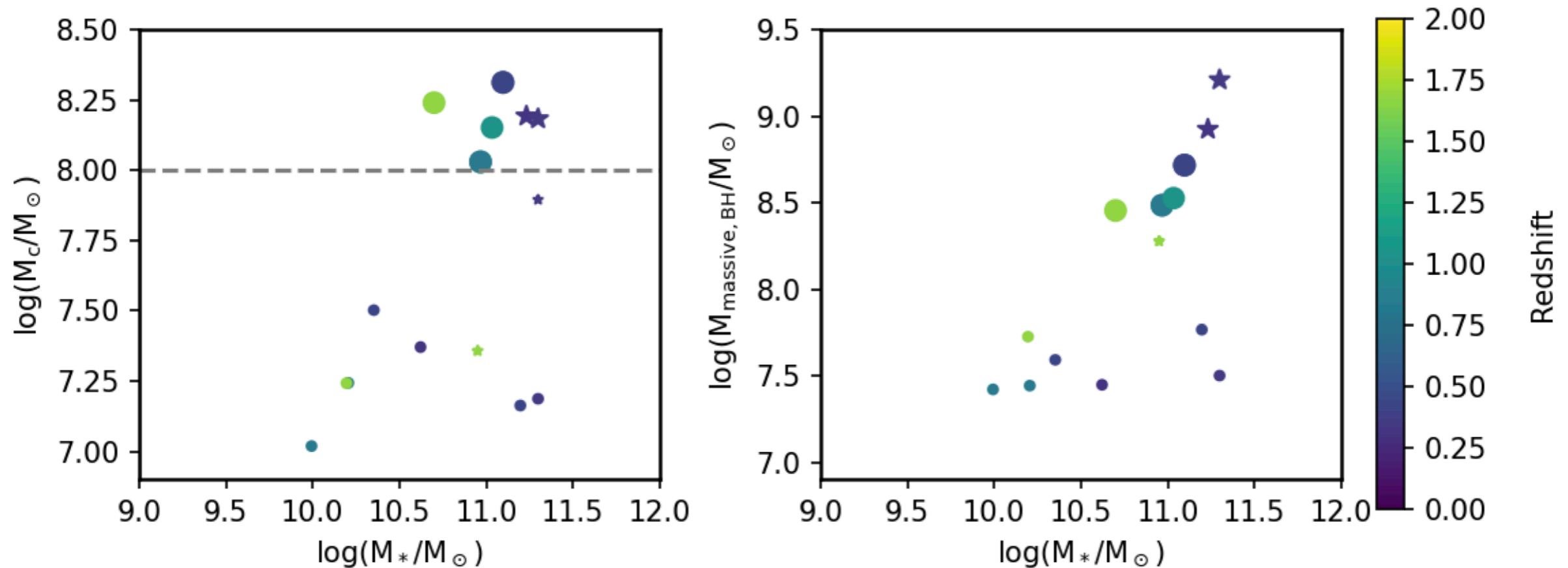
How much energy is lost in the interaction with the environment

Saeedzadeh, Mukherjee, Babul, Tremmel, Quinn (2024)



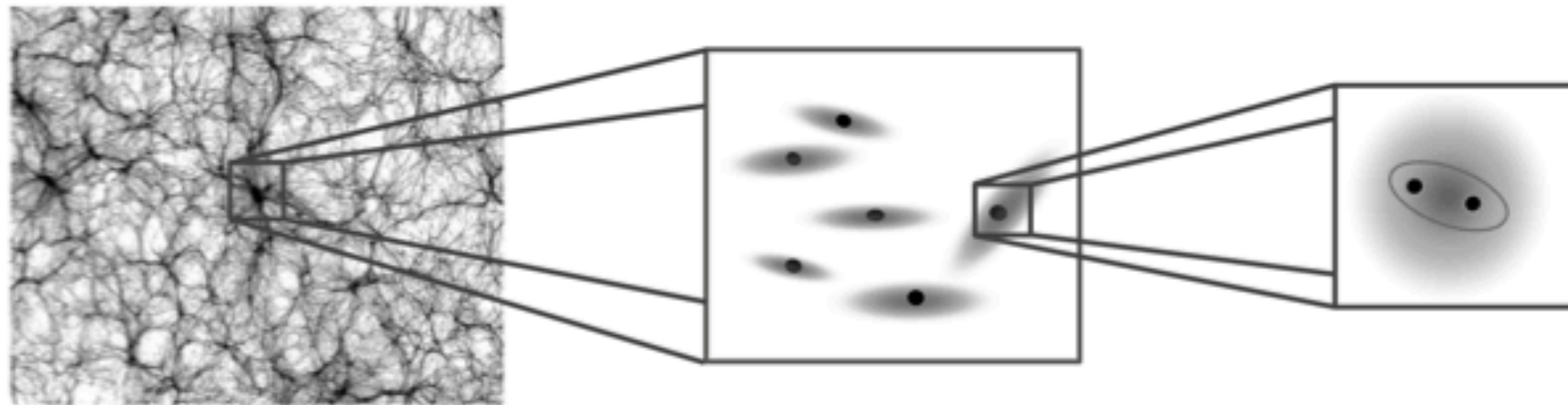
PROPERTIES OF THE SOURCES OF THE HOST OF THE BLACK HOLES

Saeedzadeh , Mukherjee, Babul, Tremmel, Quinn (2024)



BRIDGING THE SCALES: ADAPTIVE TECHNIQUE

Sah, Mukherjee, Saeedzadeh, Babul, Tremmel, Quinn (2024)



MICECAT Simulation
(Gpc scale)

$$H_0 \quad \Omega_m \quad \Omega_\Lambda \quad \sigma_8$$

ROMULUS Simulation
(Mpc scale)

$$\dot{M}_* \quad \epsilon_{SN} \quad \epsilon_r \quad \epsilon_f$$

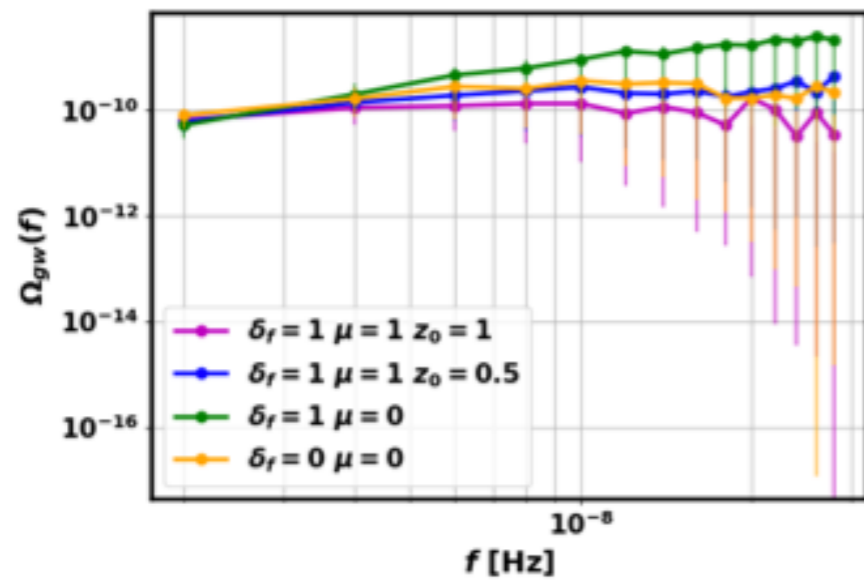
BH binary modeling in gas dynamic
(< pc scale)

$$\beta \quad \kappa \quad \gamma$$

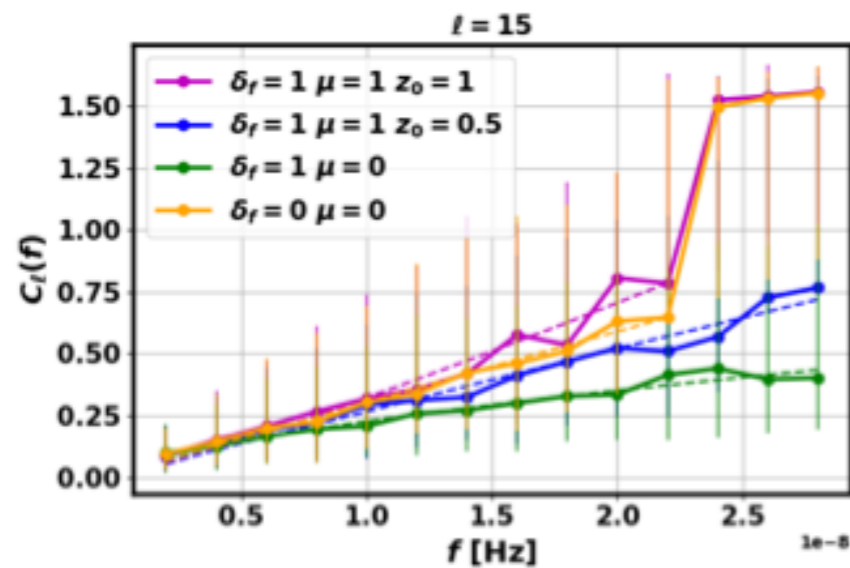


SPECTRAL AND SPATIAL ANISOTROPY IN NANO-HERTZ GW

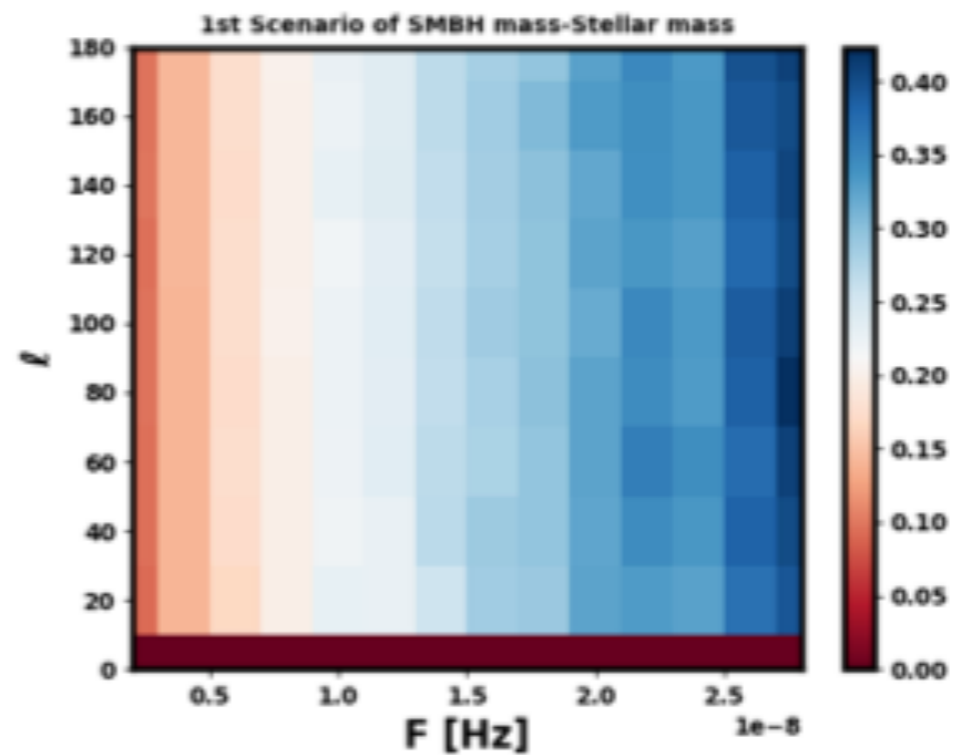
Sah, Mukherjee, Saeezadeh, Babul, Tremmel, Quinn (2024)



(a)



(b)



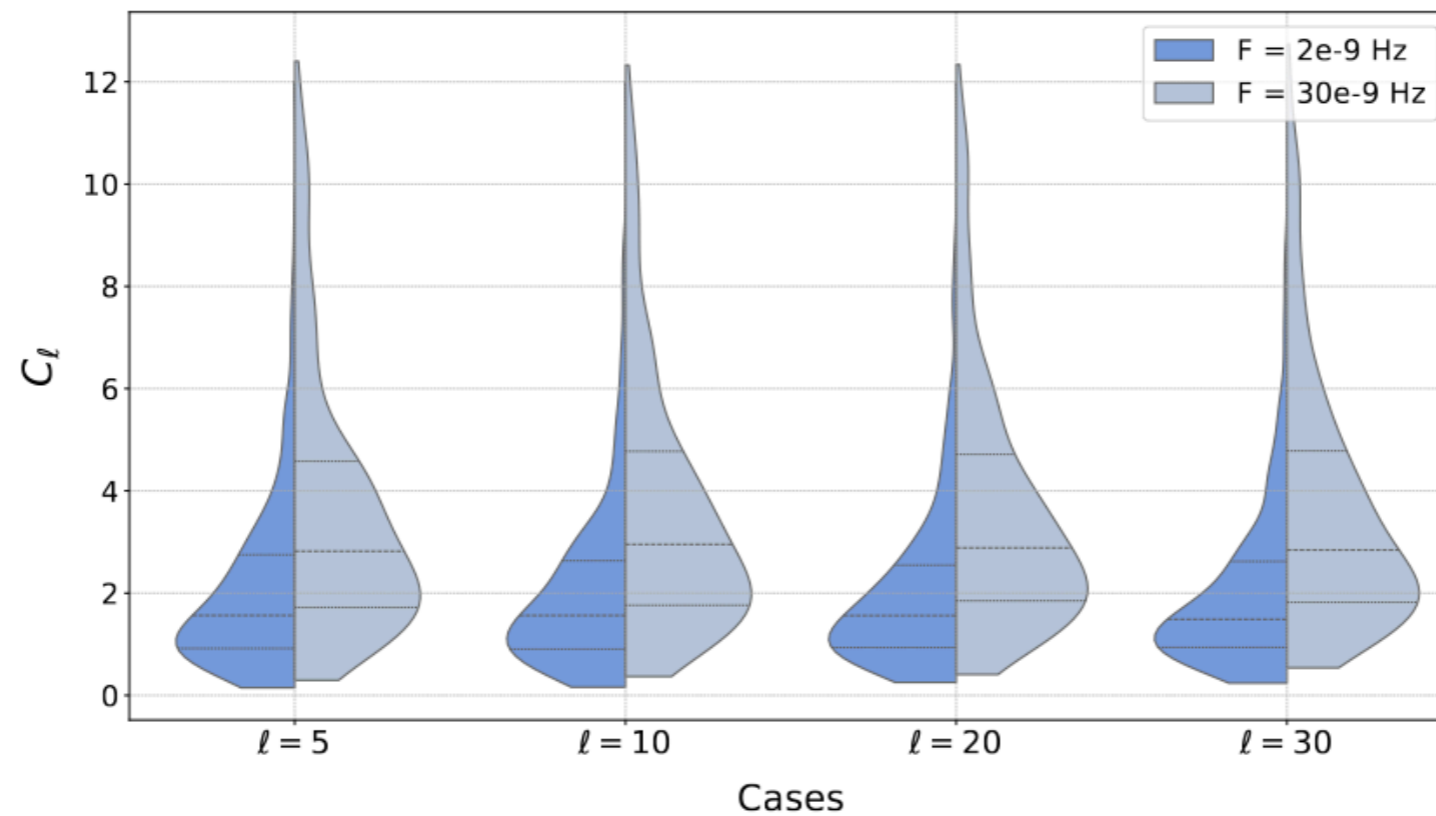
(a)



SPECTRAL AND SPATIAL ANISOTROPY IN NANO-HERTZ GW: HOW TO FIND THEM?

Sah and Mukherjee (2025)

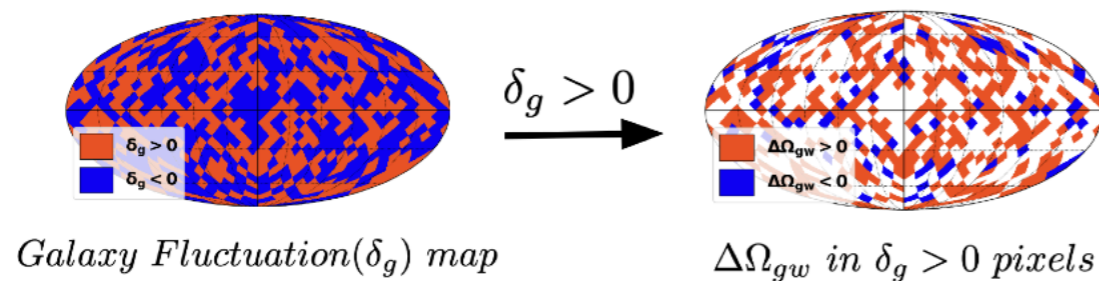
Can we use the angular power spectra?



MULTI-TRACER CORRELATED STACKING: A NEW TECHNIQUE

Sah and Mukherjee (2025)

Can discover anisotropy in nano-hertz GW



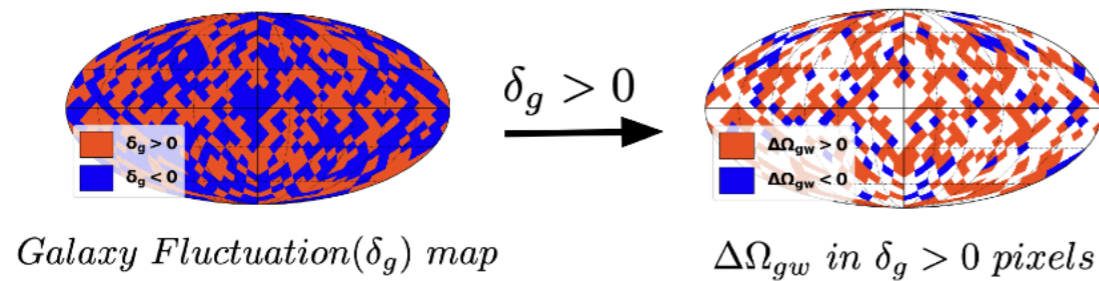
$$\hat{\Omega}_{\text{stacked}} = \sum_{i \in \delta_g(i) > 0} \Delta\Omega_{\text{GW}}^i$$



MULTI-TRACER CORRELATED STACKING: A NEW TECHNIQUE

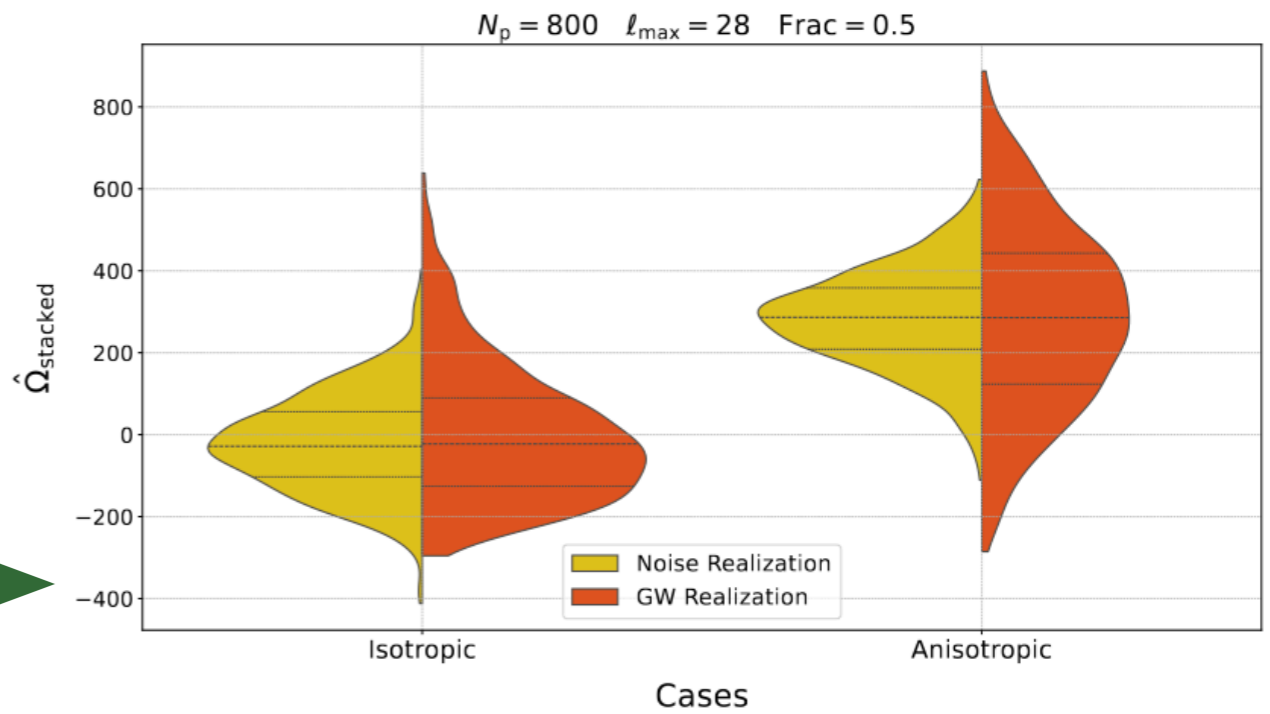
Sah and Mukherjee (2025)

Can discover anisotropy in nano-hertz GW



+

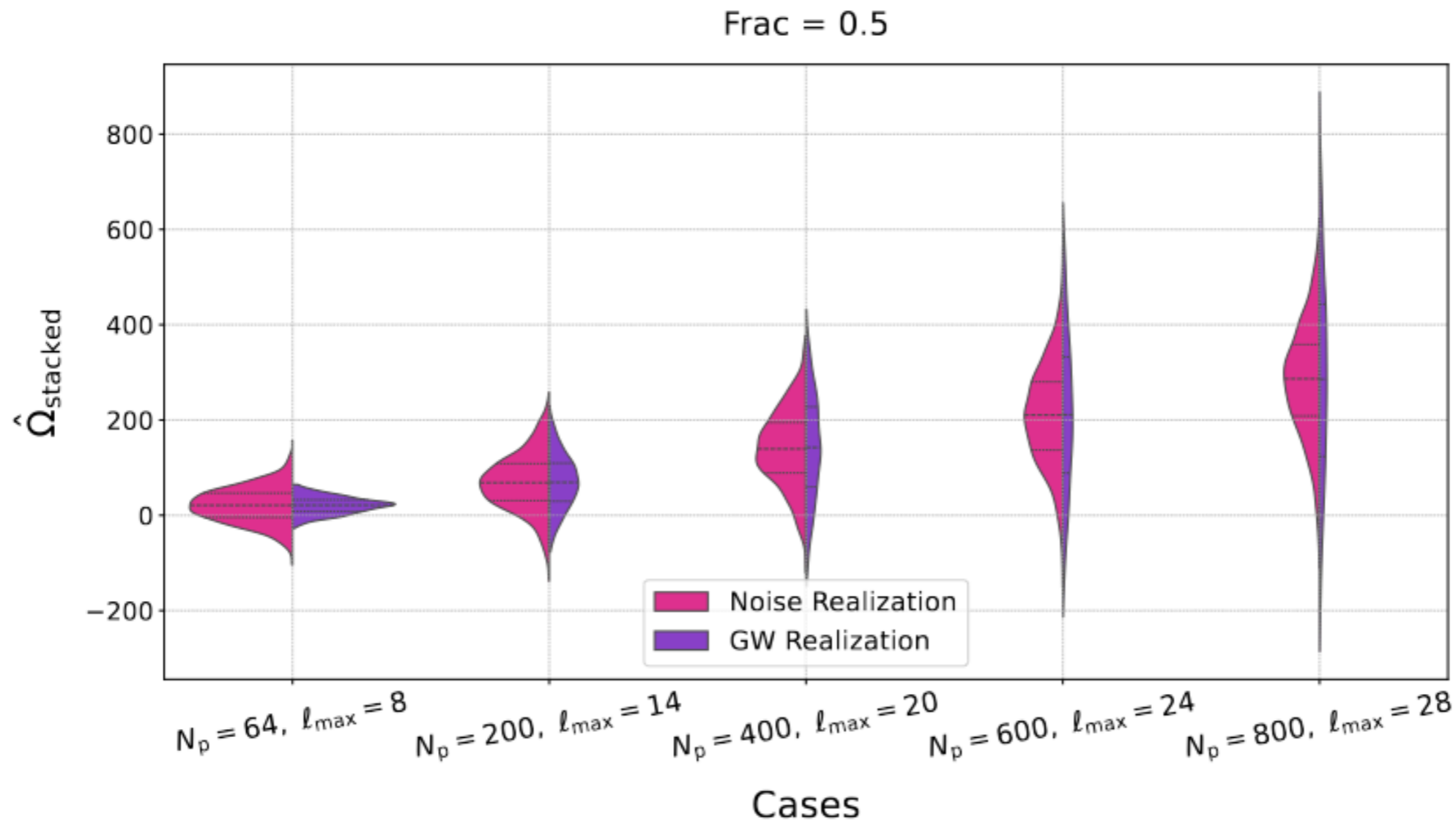
$$\hat{\Omega}_{\text{stacked}} = \sum_{i \in \delta_g(i) > 0} \Delta\Omega_{\text{GW}}^i$$



MULTI-TRACER CORRELATED STACKING: VARIATION WITH NUMBER OF PULSARS

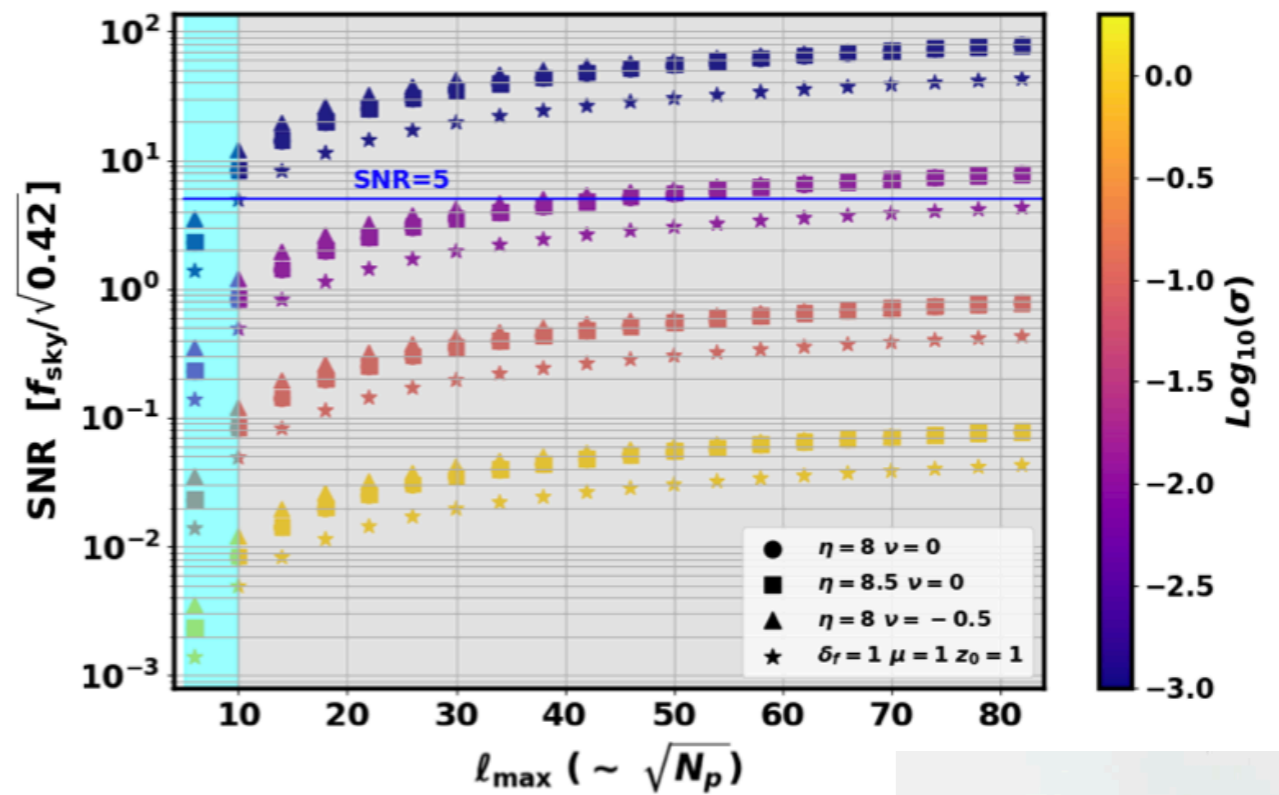
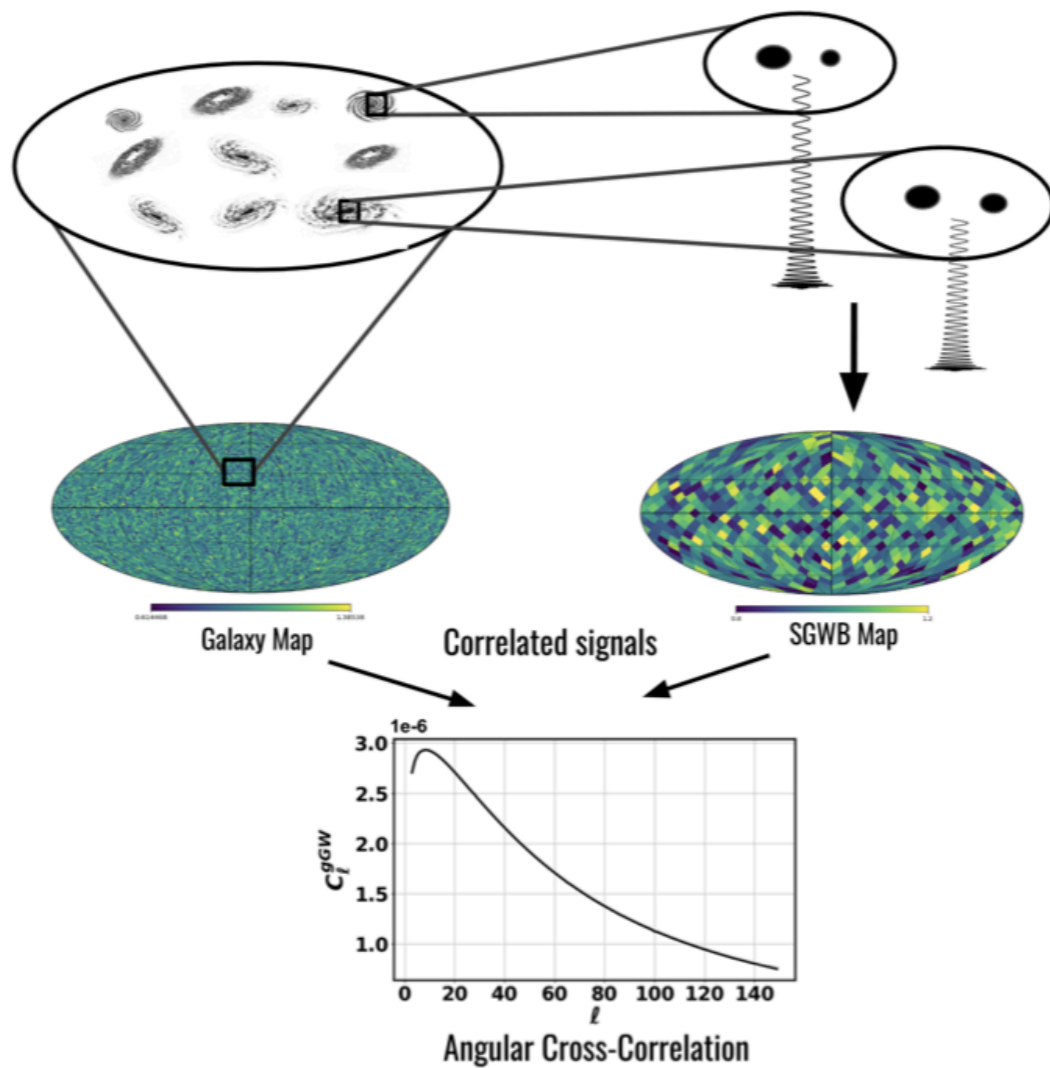
Sah and Mukherjee (2025)

Can discover anisotropy in nano-hertz GW



COSMIC EVOLUTION OF SUPERMASSIVE BLACK HOLES

Sah and Mukherjee (2024)



PROBING THE COSMOS USING STELLAR GRAVEYARDS

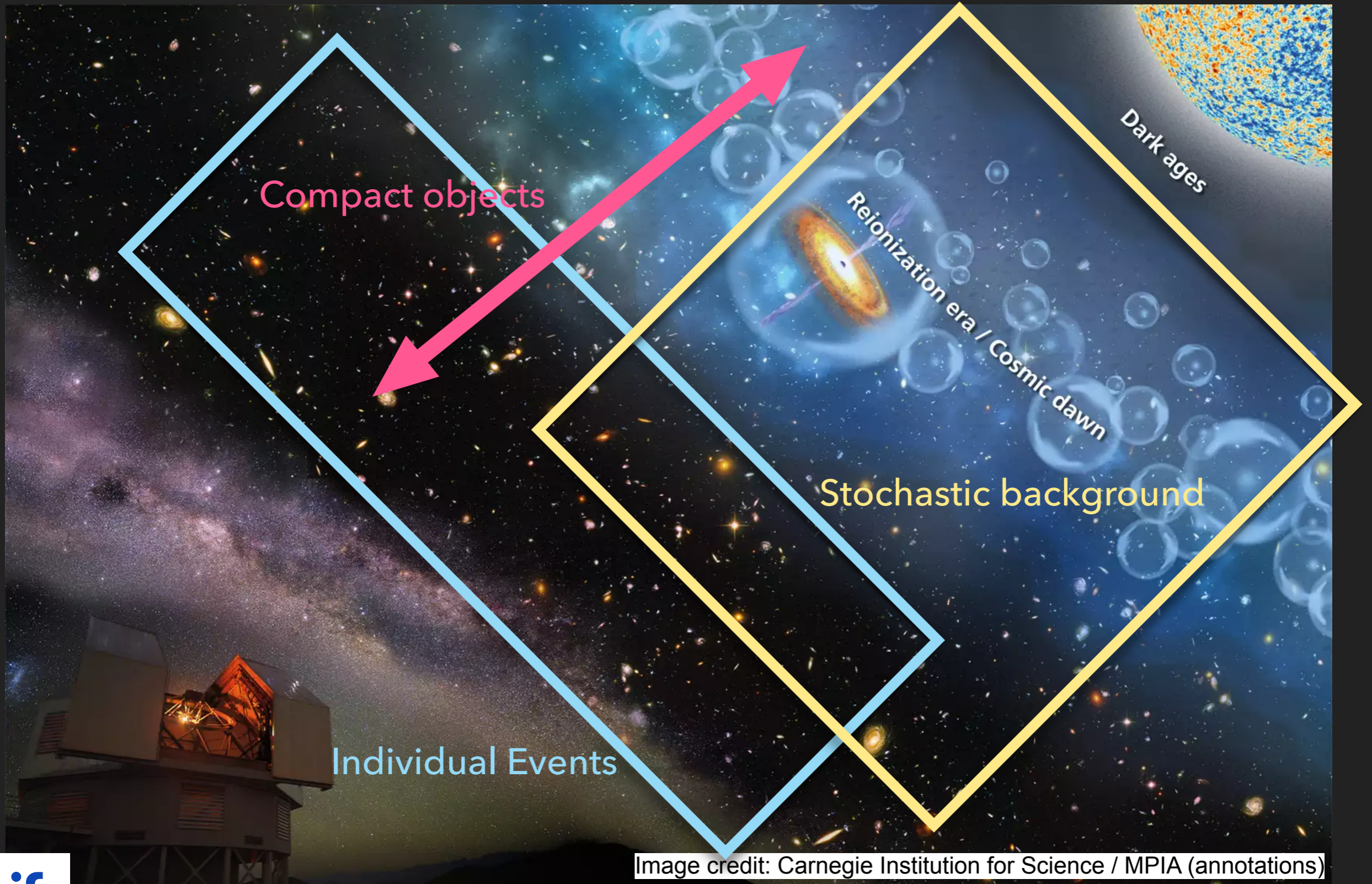
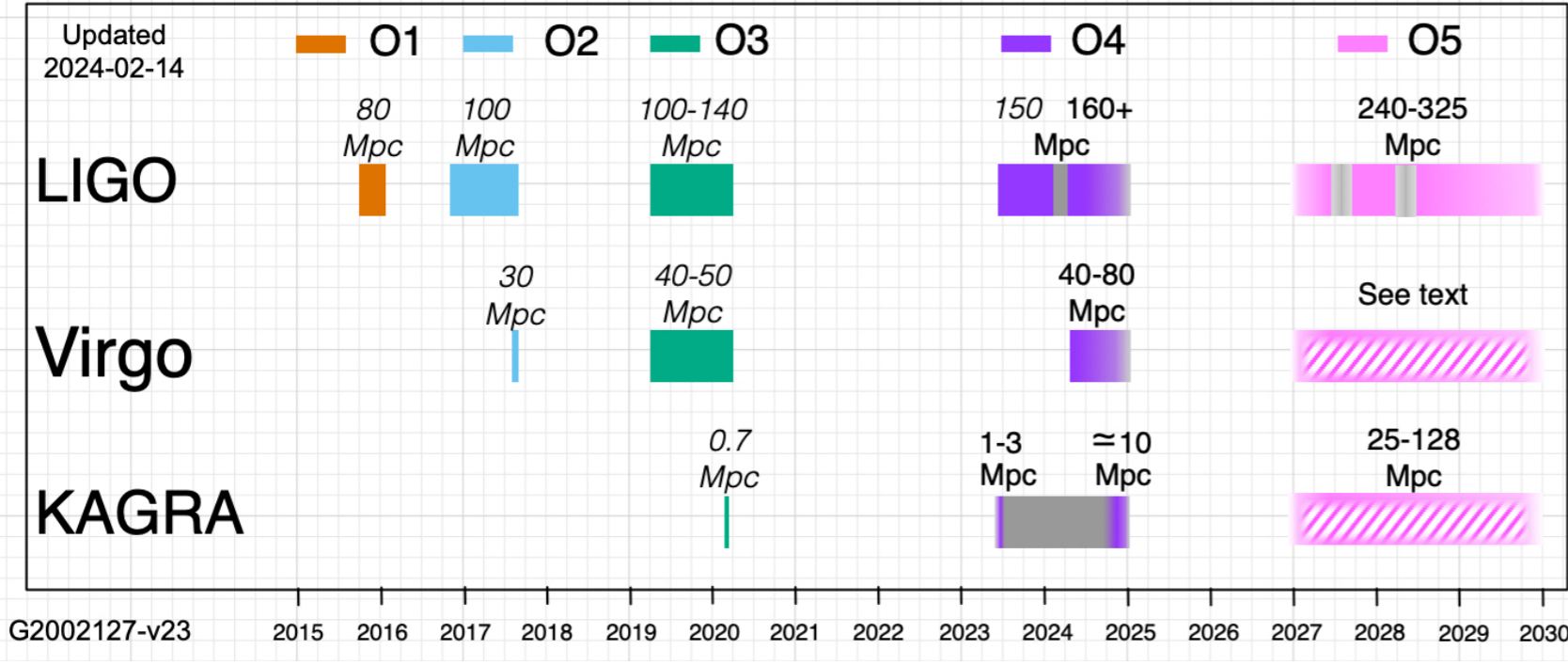


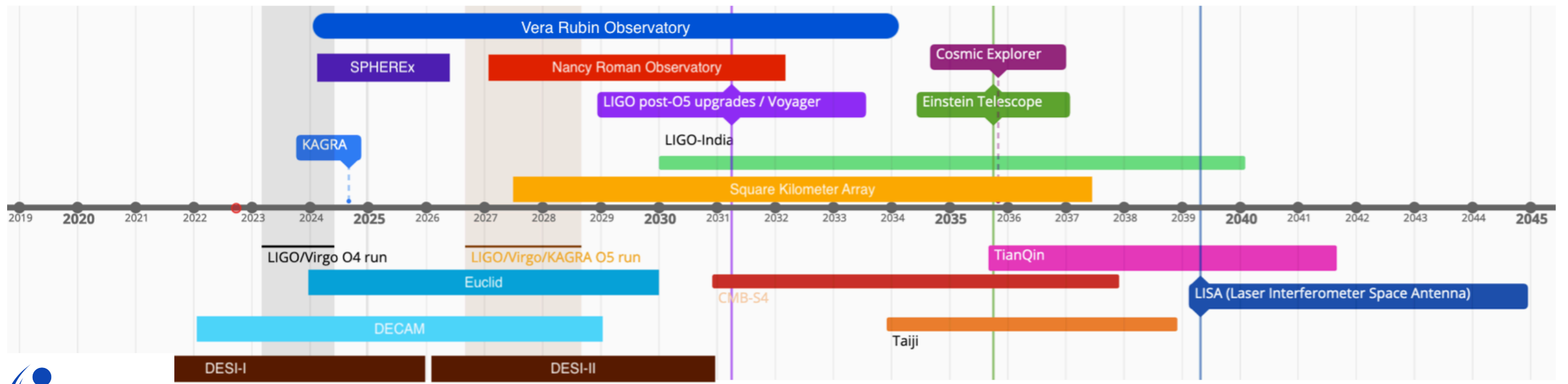
Image credit: Carnegie Institution for Science / MPIA (annotations)

Suvodip Mukherjee, 2025



Marking National Technology Day 2023, the Prime Minister launched several scientific projects.

By 2030, the LIGO facility is expected to be operational in Aundha in the Hingoli district of Maharashtra, located approximately 450 km to the east of Mumbai.



WE EXPLORE THE UNIVERSE USING ALL BANDS OF GRAVITATIONAL WAVES

THE SPECTRUM OF GRAVITATIONAL WAVES



Observatories & experiments

Ground-based experiment



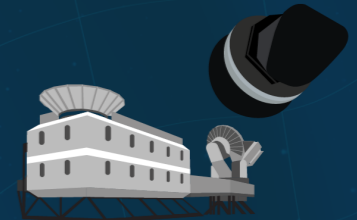
Space-based observatory



Pulsar timing array



Cosmic microwave background polarisation



Timescales

milliseconds

seconds

hours

years

billions of years

Frequency (Hz)

100

1

10^{-2}

10^{-4}

10^{-6}

10^{-8}

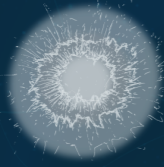
10^{-16}

High Frequency

Low Frequency

Cosmic fluctuations in the early Universe

Cosmic sources



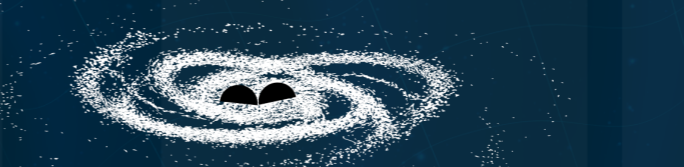
Supernova



Pulsar



Compact object falling onto a supermassive black hole



Merging supermassive black holes



Merging neutron stars in other galaxies

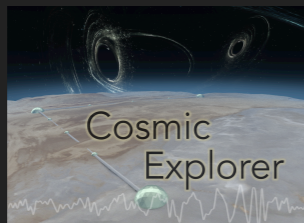


Merging stellar-mass black holes in other galaxies

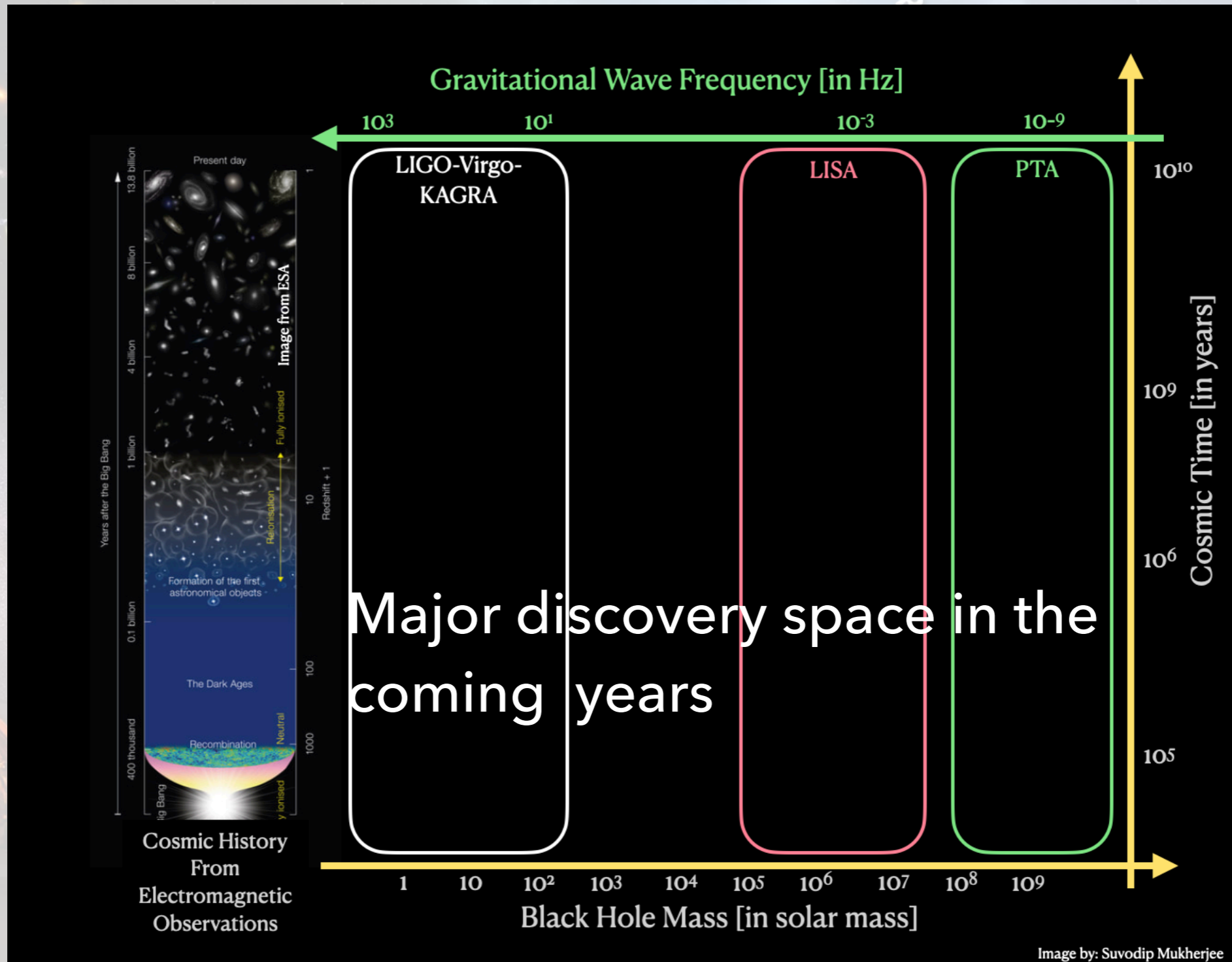


Merging white dwarfs in our Galaxy

#lisa



DATA DRIVEN INFERENCE OF THE HIGH REDSHIFT UNIVERSE



DATA DRIVEN INFERENCE OF THE HIGH REDSHIFT UNIVERSE

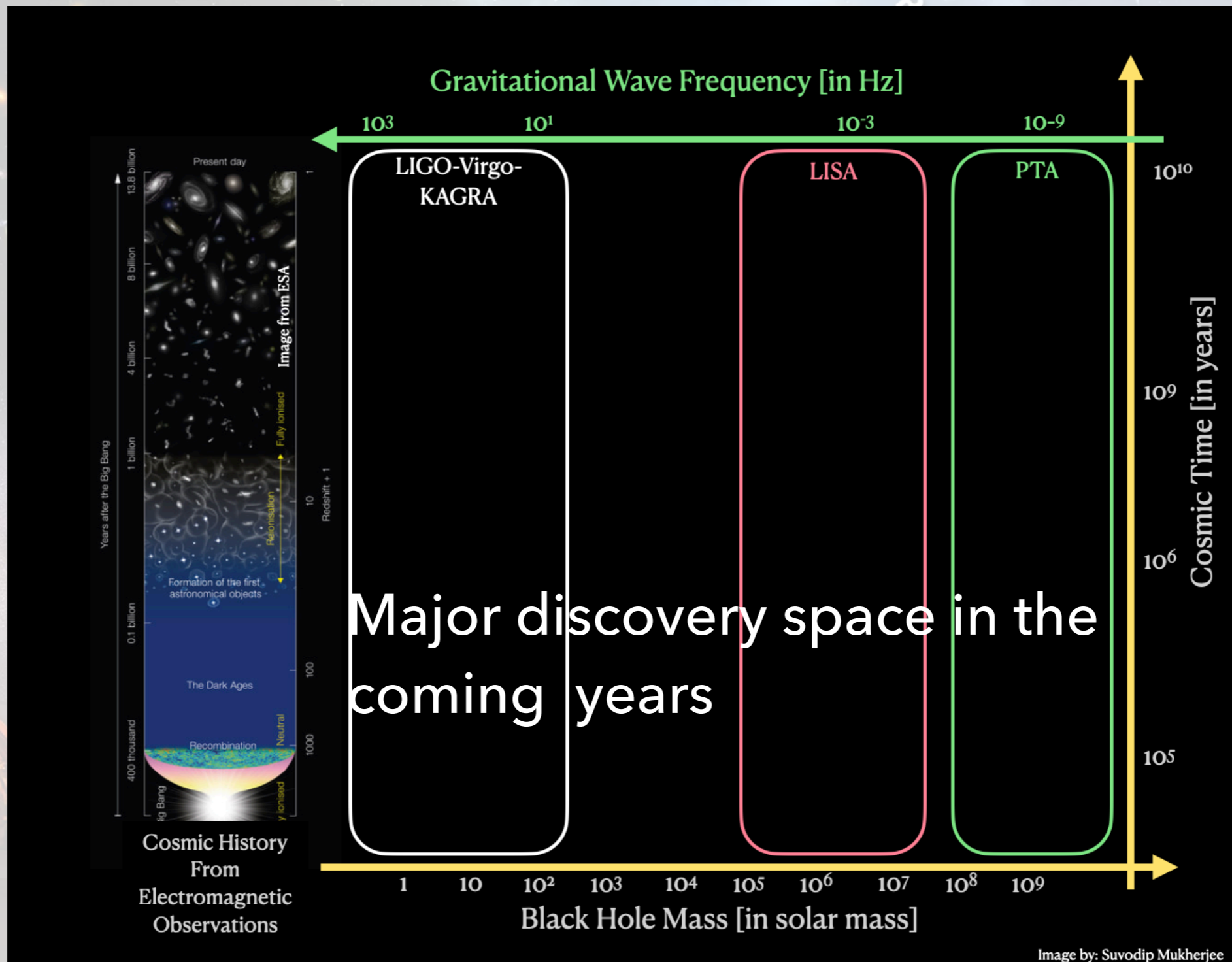


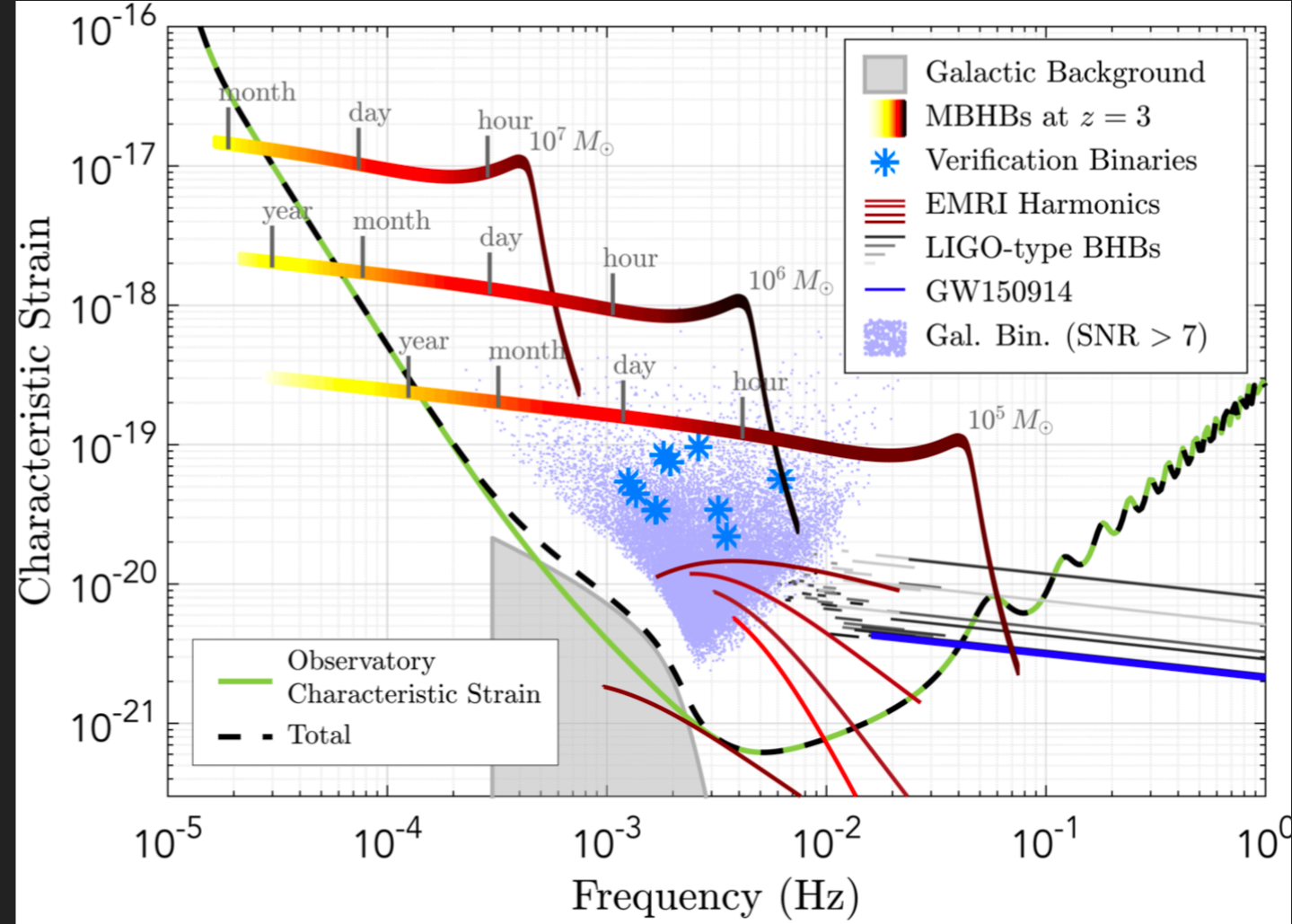
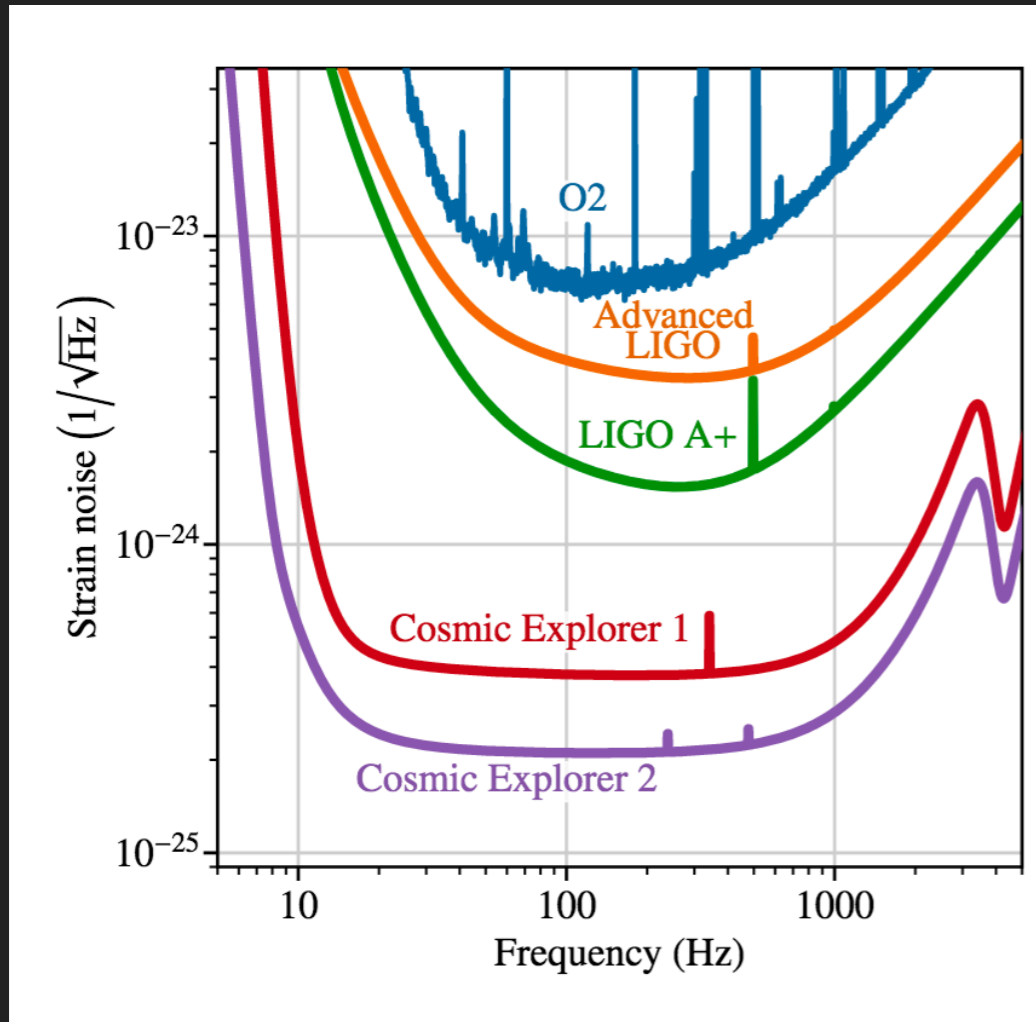
Image by: Suvodip Mukherjee

EXTRA SLIDES

ONGOING/UPCOMING GW DETECTORS

Reitze et al. (2020) 1903.04615

LISA Science book



Terrestrial GW detectors

Space-based GW detector