Signatures of deconfined quantum criticality in a spin-1 model on the square lattice

Vikas Vijigiri

Collaborators: Dr. Nisheeta Desai (PDF, TIFR) Prof. Sumiran Pujari (IIT Bombay)

Department of Physics, IIT Bombay



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1 Deconfined quantum criticality

2 Earlier studies

3 Designer model Hamiltonian

4 Results



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Néel (A): Antiferromagnetic state, breaks rotational symmetry, SU(N). Sensitive to quantum fluctuations. Low energy excitations: Spin-waves.

Valence bond solid (VBS) (B): A non-magnetic state, and breaks lattice symmetry (e.g. translational for spin-1/2). Product of quantum fluctuations. Localized triplets ("confined spinons").

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 $\mathcal{H} = J \sum_{\langle i,j \rangle} \vec{S}_i \cdot \vec{S}_j + \cdots$

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Deconfined quantum criticality is a...

'Critical region of interest' associated with Néel-Valence bond solid (VBS) quantum phase transition in magnetic systems. Can see 'deconfined' nature of spinons.







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Vikas Vijigiri (IIT Bombay)

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Both the Néel and VBS phase lie to the broken symmetry side.

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Order of the phase transition?





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Order of the phase transition?

 $1^{st} \text{ order}? \quad (LGW) \\ co-existence of two orders? \quad (LGW) \\ 2^{nd} \text{ order}?$

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Continuous phase transitions by Landau-Ginzberg-Wilson (LGW) paradigm...

Ground state to break the continuous symmetry of the Hamiltonian.



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1. Order parameter description of phases.



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Continuous phase transitions by Landau-Ginzberg-Wilson (LGW) paradigm...

Ground state to break the continuous symmetry of the Hamiltonian.

1. Order parameter description of phases.

2. An emergent gauge field and "deconfined" degrees of freedom associated with fractionalization of the order parameters. (Beyond LGW paradigm)



Image: A matrix and a matrix

Prior to 2015...



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- Diagnosing weakly first-order phase transitions by coupling to order parameters. Jonathan D'Emidio, Alexander A. Eberharter, Andreas M. Läuchli, SciPost,



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Very few studies on spin-1's



Vikas Vijigiri (IIT Bombay)

Image: A matrix and a matrix

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 Quantum Spin Nematics, Dimerization, and Deconfined Criticality in Quasi-1D Spin-One Magnets.
 Tarun Grover and T. Senthil, PRL, 98, 247202 (2007).



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Our approach is based on...

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Our approach lies in the idea that the above problem can be recasted into spin-1, with SU(3) symmetry and see the effect of criticality under reduced symmetry conditions, SU(2).

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Hamiltonian:

$$SU(3): \mathcal{H} = J_{Bi} \sum_{\langle i,j \rangle} (\vec{S}_i \cdot \vec{S}_j)^2 - Q_n \sum_{ijkl} (\vec{S}_i \cdot \vec{S}_j)^2 (\vec{S}_k \cdot \vec{S}_l)^2$$
(1)
$$SU(2): \mathcal{H}_p = \mathcal{H} + J_H \sum_{\langle i,j \rangle} \vec{S}_i \cdot \vec{S}_j$$
(2)

- **(**) It can be shown that the terms in \mathcal{H} are SU(3) symmetric.
- It is of the following reasons, interesting to see the effect of a lower symmetric perturbation, SU(2), upon the deconfined critical point (DCP). There can be three questions now:
 - Does the phases survive?
 - If so, what is the universality class without perturbation?
 - In And the effect under reduced symmetry (SU(2)) perturbation?



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Scaling of order parameter ratios, in the absence of perturbation



 $\begin{array}{l} \text{VBS order parameter:} \\ R_B^{\text{x}} = 1 - \frac{\tilde{C}^{\text{x}}(\pi, 2\pi/L)}{\tilde{C}(\pi, 0)}, \\ R_B^{\text{y}} = 1 - \frac{\tilde{C}^{\text{y}}(2\pi/L, \pi)}{\tilde{C}(0, \pi)} \\ C^{\alpha} \sim \langle S_{\vec{r}} \cdot S_{\vec{r}^{\dagger} + \hat{\alpha}} S_{\vec{r}^{\dagger}} \cdot S_{\vec{r}^{\dagger} + \hat{\alpha}} \rangle \end{array}$



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In the presence of perturbation, $J_H = 0.05$



Look at the value of η_N , there is a consistent decrease in the values compared to the case of $J_H = 0.0$





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J _H	Parameter	ν_N	ν_V	η_N	η_V	в _{сN}	<i>B</i> _{cV}
0.0	R	0.49(5)	0.63(1)	0	0	0.168(1)	0.167(1)
0.0	Ø	0.53(3)	0.63(1)	0.44(5)	0.49(2)	0.167	0.167
0.05	\mathscr{R}	0.40(3)	0.46(3)	0	0	0.196(1)	0.195(1)
0.05	Ø	0.39(3)	0.38(3)	0.20(9)	0.29(6)	0.195	0.195
0.1	\mathscr{R}	0.31(1)	0.40(1)	0	0	0.225(1)	0.223(1)
0.1	Ø	0.33(2)	0.41(2)	0.13(2)	0.28(7)	0.224	0.224
0.15	\mathscr{R}	0.32(4)	0.44(2)	0	0	0.254(1)	0.252(1)
0.15	Ø	??`´	??`´	??	??	0.253	0.253



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Block, Melko, et al, PRL 111, 137202 (2013)

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We have studied and seen a Neel-VBS transition in a spin-1 (SU(3) symmetric) Hamiltonian with Heisenberg (SU(2) symmetric) term as perturbation.



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- We have studied and seen a Neel-VBS transition in a spin-1 (SU(3) symmetric) Hamiltonian with Heisenberg (SU(2) symmetric) term as perturbation.
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- We have studied and seen a Neel-VBS transition in a spin-1 (SU(3) symmetric) Hamiltonian with Heisenberg (SU(2) symmetric) term as perturbation.
- **②** Our results match with the literature for $J_H = 0.0$ with critical exponents of SU(3) type.
- **(a)** However, as we turn on perturbation $(J_H = 0.05)$ we see a shift in the universality class of SU(2) type.
- Our results show some indications of deconfined criticality within the range $J_H \sim 0 0.1$.



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A finite value of order parameter starts appearing as we increase beyond $J_H = 0.1$. A signature of first order phase transition (weak).





Julia Wildeboer et al, PRB, 101, 045111 (2020)

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Spin-1 particles can behave like spin-1/2 particles! (Like two independent spins, in constrained environments).



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Thank you ALL



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