

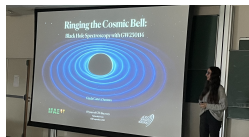
Prospects of GW standard siren cosmology



2025 Oct 29

Archisman Ghosh

Ghent University



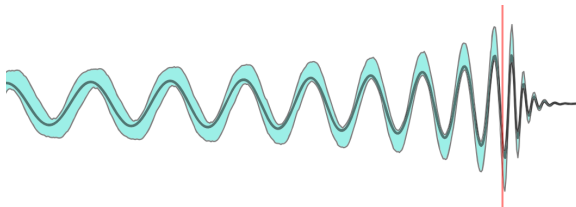
Plan of this talk

- Overview | results from current data
- Alternative tracers for dark standard sirens
- Future prospects and discussion items

Compact binaries observed in gravitational waves
are standard distance indicators or “standard sirens”

Gravitational-wave standard sirens

Schutz (1986), Holz & Hughes (2005)



Phase evolution $\Rightarrow \mathcal{M}^z \equiv \mathcal{M}(1+z)$ redshifted chirp **mass**

Amplitude $\sim \frac{\mathcal{M}^z}{d_L} \times \text{fn.}(\text{angles}) \Rightarrow d_L$ luminosity **"distance"** (inclination)

GW from compact binaries give direct access to distance!

self-calibrated independent of, in particular, the **distance ladder**

$(d_L, z) \rightarrow$ cosmological parameters

Distance-redshift relation:

Late-time expansion / acceleration parameters

$$d_L = c(1+z) \int^z \frac{dz'}{H(z')}, \quad H(z') = H_0 \sqrt{\Omega_m(1+z')^3 + \Omega_\Lambda}$$



Lemaître-Hubble law

Hubble constant

Λ -CDM: dark matter, dark energy

Where does z come from?

$(d_L, z) \rightarrow$ cosmological parameters

Distance-redshift relation:

Late-time expansion / acceleration parameters

$$d_L = c(1+z) \int^z \frac{dz'}{H(z')}, \quad H(z') = H_0 \sqrt{\Omega_m(1+z')^3 + \Omega_\Lambda}$$

↑

Lemaître-Hubble law

Hubble constant

Where can z come from?

Spectral lines for GW?

For BBH, z degenerate with mass

NS physics / **population astrophysics**

spectral

EM counterparts | **galaxy catalogs**

bright | **dark**

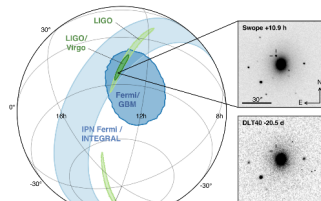
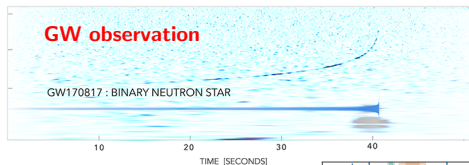
Galaxy clustering / LSS of matter

Other??

A gravitational-wave standard siren measurement of the Hubble constant

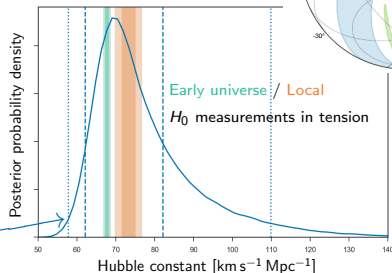
↗ self-calibrated distance indicator

The LIGO Scientific Collaboration and The Virgo Collaboration*, The 1M2H Collaboration*, The Dark Energy Camera GW-EM Collaboration and the DES Collaboration*, The DLT40 Collaboration*, The Las Cumbres Observatory Collaboration*, The VINROUGE Collaboration* & The MASTER Collaboration*



↓
distance, d_L

First GW standard siren measurement of H_0



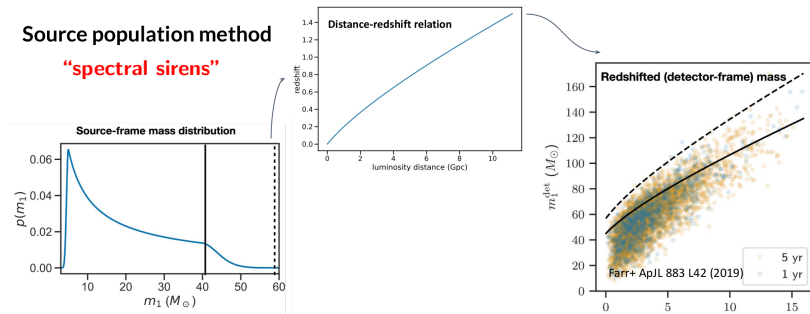
EM counterpart

↓
redshift, z

H_0 from source population

Key idea: masses / mass distributions are redshifted!

Source population method
“spectral sirens”

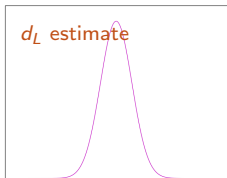


Chernoff & Finn 1993; Taylor & Gair 2012; Farr, Fishbach, Holz 2019

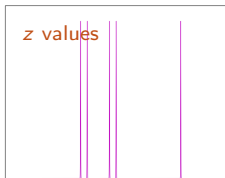
Mastrogiovanni+ 2021 (with **AG**): icarogw (LVK pipeline)

Mukherjee arXiv:2021; Ezquiaga & Holz 2202

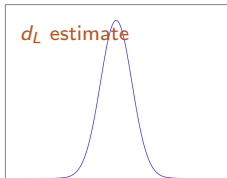
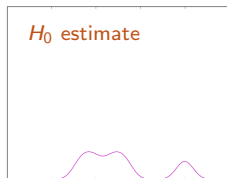
Independent detections



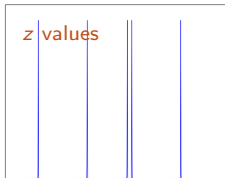
+



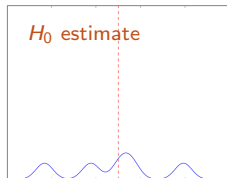
\Rightarrow



+



\Rightarrow



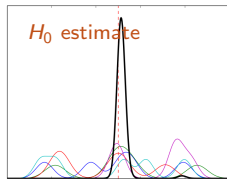
Different possible galaxies
for single detection



Schutz idea
galaxy catalogues for redshift

Schutz (1986)

Combine information from all observed detections \Rightarrow



Power of statistics

\Leftarrow

Unimodal joint H_0 result

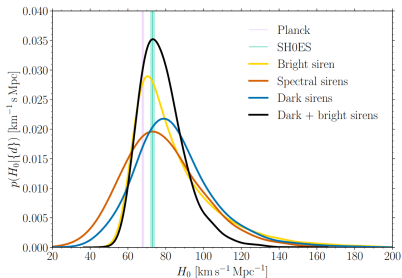
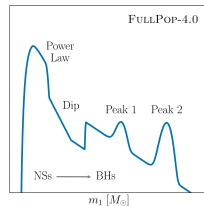
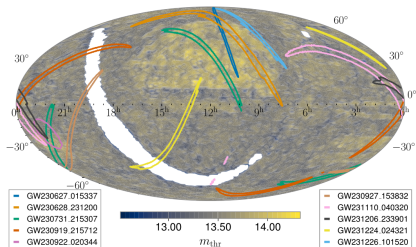
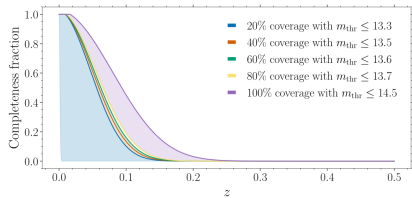
One approach or both?

- Binary mass distribution and merger rate (evolution) enter as a selection effect in the dark standard siren likelihood.
- As of O4a both LVK pipelines `gwcsmo` and `icarogw` marginalize over population parameters to obtain cosmology.

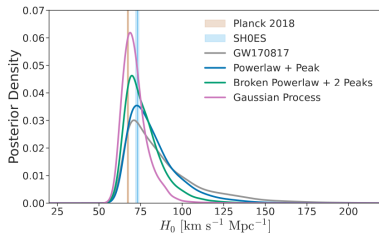
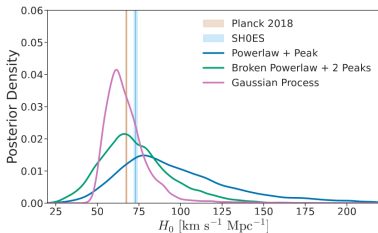
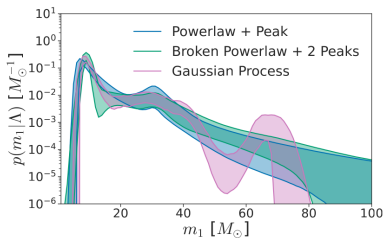
LVK O4a H_0 results



GLADE+ galaxy catalog: Dály+ (2021) [K band]



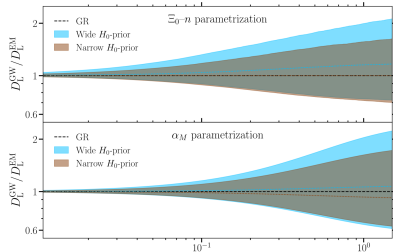
LVK: arXiv:2509.04348



LVK O4a and further prospects

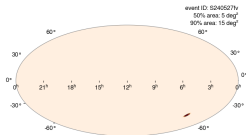
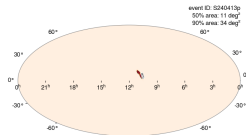


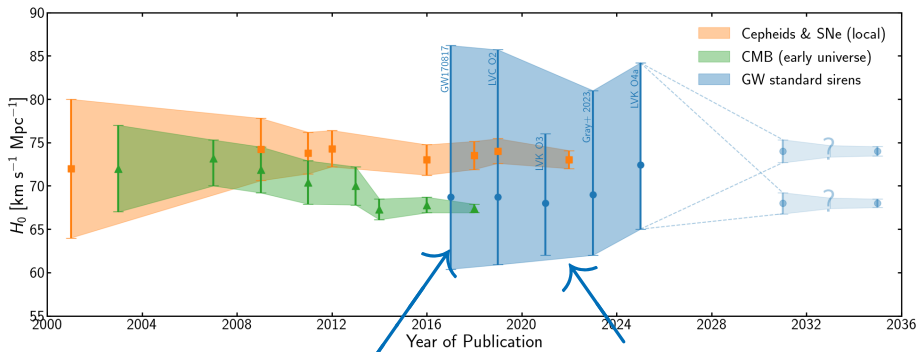
Other cosmological parameters / modified gravity:



LVK: arXiv:2509.04348

Better localized events in O4b/c:





GW170817 + EM counterpart

dark siren contribution

Challenges

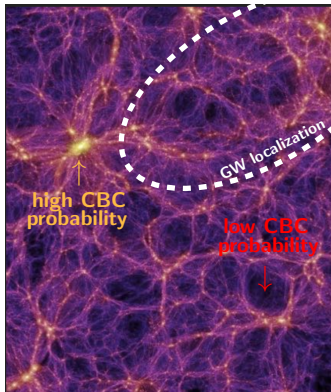
- Number of sources with counterparts
rapid follow-up, early warning?
- Incompleteness of galaxy catalogues
upcoming surveys: Vera Rubin Observatory, DESI, SPHEREx
alternative tracers: rest of **this talk**
- Systematic effects
Modelling of peculiar velocities
Uncertainties coming from galaxy catalogues
GW waveform modelling, GW detector calibration

Possible sources of systematics

- Peculiar velocities (nearby detections) Goode+ (to appear soon)
- Uncertainties in galaxy catalogues
 - Photometric measurements of redshifts Palmese+ 2020, Turski+ 2023
 - Estimates of luminosities for weighting
- Unknown astrophysics
 - Luminosity weighting model Perna+ 2025, Hanselman+ 2025
 - Galaxy type: colour, metallicity ... work ongoing
- Waveform systematic effects Kunert+ 2024
- Detector calibration uncertainties Huang+ 2025

Alternative tracers?

HI intensity mapping, **galaxy clusters** ...



GWs, galaxy clusters, ... trace underlying matter distribution (with different bias).

Given large GW localization uncertainties, not necessary to resolve individual galaxies.

In this talk: **galaxy cluster catalogues**,
brightest cluster gal / **luminous red galaxies**



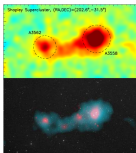
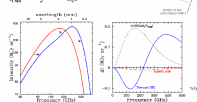
Graphic idea: Dounia Nanadoumgar Lacroze!

nodes, filaments

Galaxy cluster catalogues

Sunyaev-Zeldovich Effect

$$\frac{\Delta T}{T_{\text{CMB}}} = g(x) \int d\Omega \int_0^{\infty} \frac{k_B T_e l}{m_e c^2} d\ell$$

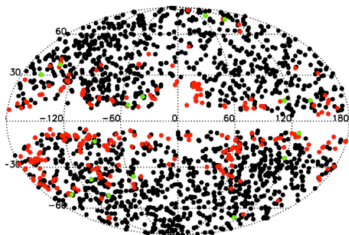


Inverse Compton scattering of CMB photons

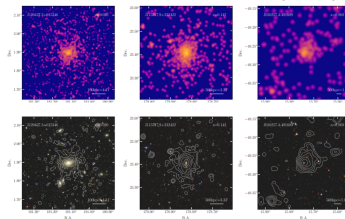
83% sky

1094 clusters with z (from galaxies within cluster)
mass from SZ (direct)

Planck 15: PSZ2



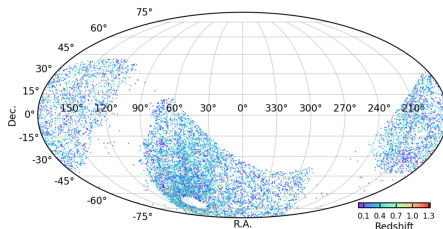
X-ray surveys



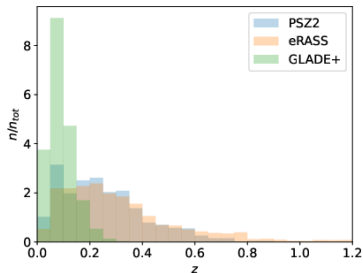
eROSITA: eRASS

5259 high-purity clusters with z from "counterparts"
mass proxy from X-ray properties

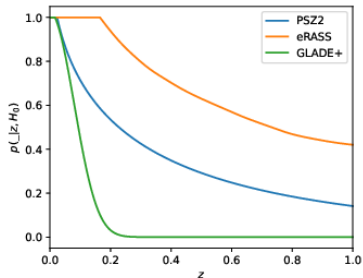
36% sky



redshift distributions in-catalogue:



in-catalogue fraction:



line-of-sight redshift prior (LOS- z)

gwcsmo: Gray+ JCAP 12 023 (2023)

in-catalogue

out-of-catalogue

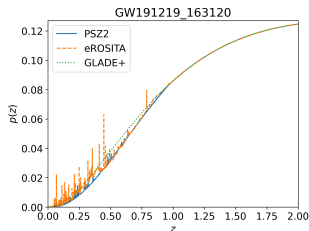
redshifts \leftarrow precise?
luminosities
(for weighting)

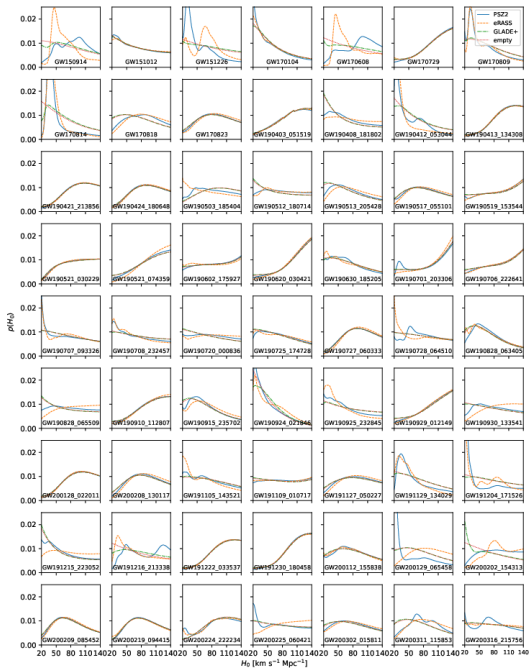
masses \leftarrow direct?

simpler? \rightarrow

Schechter function

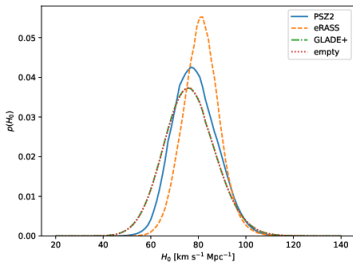
\downarrow
Press-Schechter
distribution





← Significant in-catalogue contribution!

↓



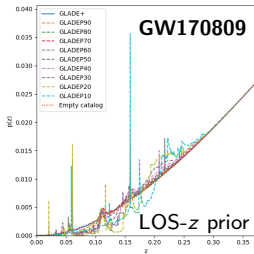
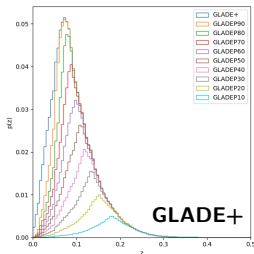
Beirnaert+ 2025

Luminous galaxies?

We select **XX** percentile of brightest galaxies.

highest *absolute* luminosity

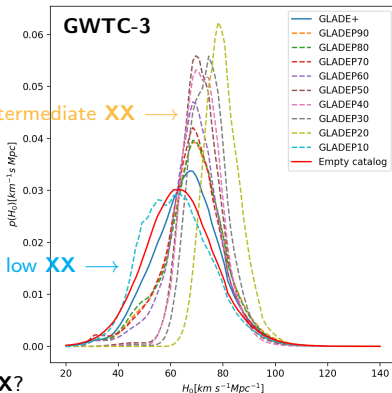
← effective completeness increases!



sharper peaks for intermediate **XX** →

uninformative for low **XX** →

well-motivated **XX**?



Luminous galaxies?

VanWyngarden+ (to appear soon)

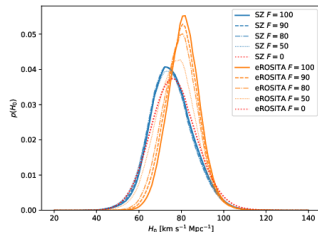
- Simulations on MICECAT.
- Importance of galaxy clustering.
- *i*-band serves as a better tracer than *g*-band.
- 1% of the brightest galaxies can lead to an unbiased H_0 estimate!

The next steps ...

Not all CBCs associated with galaxy clusters.

extra term to account for this ✓

from Beirnaert PhD thesis (in prep.)

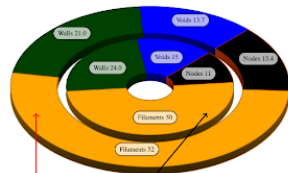


Combine multiple tracers!

galaxies, galaxy clusters ✓

luminous red galaxies: filaments

other tracers? HI, quasars?



This work
Original NEXUS+ paper
Mass fractions

Hellwing+ PRD 103 6 (2021)

Fold in astrophysics! Test via large scale simulations.

FOR DISCUSSION

A different set of questions for 3G/XG

- Current “tensions” in cosmology may be resolved.
- Standard sirens: direct probe of $h(z)$ **fundamental physics**

Other cosmological parameters? Beyond Λ -CDM?

$$d_L^{\text{GW}}(z) = \left[(1+z) \int_0^z \frac{dz'}{H(z'; H_0, \Omega_m, w_0, \dots)} \right] \times \left[\Xi_0 + \frac{1 - \Xi_0}{(1+z)^n} \right]$$

Mancarella+ 2022; Leyde+2022; ...

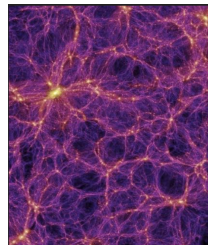
$$h_A'' + [2 + \alpha_M(\dot{\eta})] \mathcal{H} h_A' + c^2 k^2 h_A = 0$$

Modified GW propagation!

- Probe “GW bias”? **astrophysics \longleftrightarrow cosmology**
 $\delta_{\text{GW}}(z, k) = b_{\text{GW}}(z) \delta_m(z, k)$

Libanore+ 2020; Calore+ 2020; Vijaykumar+ arXiv:2020; Cirrigan-Diaz & Mukherjee 2021; ...

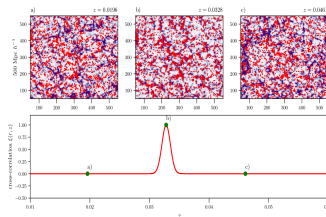
Dark standard sirens: more to exploit



Cross-correlations: beyond line-of-site contributions

Standard rulers

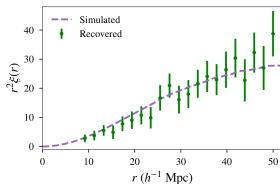
3G localizations of $\mathcal{O}(1 \text{ sq. deg.})$



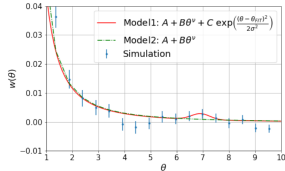
Oguri 2016; Scelfo+ 2018; Nair, Bose, & Saini 2019; Nakama 2020; Vijaykumar+ 2021; Bera+ 2020; Mukherjee+ 2021

Cosmography / cosmology with GWs alone?

- Love sirens?
- Probing the universe with GWs alone?



Correlation function: Vijaykumar+ 2020



BAO peak: Kumar+ 2022

CONCLUDING SLIDE

Takeaway messages and thoughts

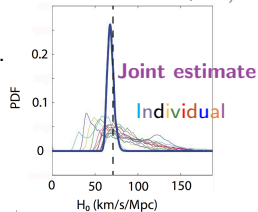
- GWs are an independent probe \Rightarrow independent systematics!
- Direct measurement of $h(z)$! No local / early univ anchor needed.
- Uncertainties from GW are expected to shrink much faster.
- Will certainly give us complementary information.

EXTRA SLIDES

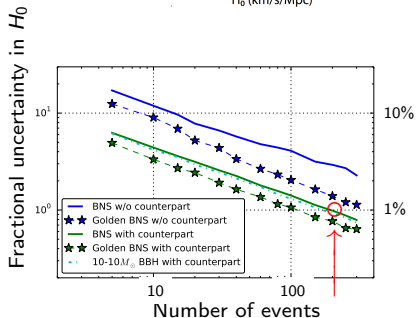
Better with more detections

Nissanke *et al.* (2010)
Nissanke *et al.* (2013)

Combine information from multiple similar detections.



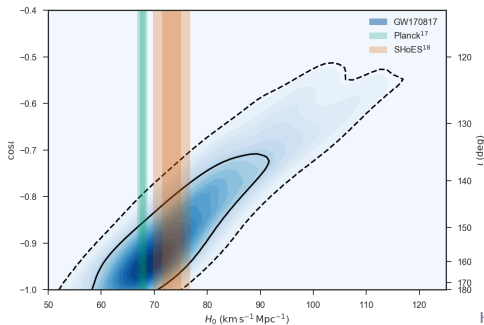
Precision: $\sigma_{H_0}/H_0 \sim 1/\sqrt{N}$



Chen *et al.* (2018)

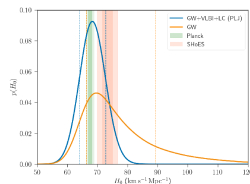
see also: Feeney *et al.* (2019)

Degeneracy with inclination



paper

Hotokezaka+ 2018: jet \rightarrow inclination $\rightarrow H_0$

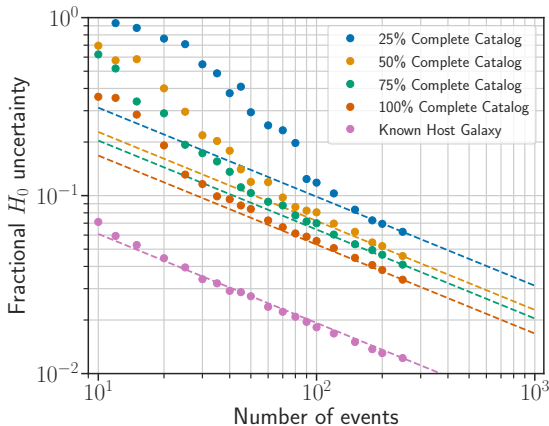


Broken with GW alone? **Higher harmonics!**

See, e.g., Calderón Bustillo+ 2021

H_0 with galaxy catalogues: projections

*About 10 times more events without counterpart to get to same precision
(at BNS distances)*



Projected from Gray+ 2020 (with **AG**)

ongoing study led by S. Mukherjee

H_0 with galaxy catalogues: selection effects

GW selection effects

threshold SNR \rightarrow ifo horizon
only nearby signals detected

EM selection effects

depth of telescope
incomplete galaxy catalogues

$$p(x_{\text{GW}}|D_{\text{GW}}, H_0) = \frac{p(x_{\text{GW}}|G, H_0)}{p(D_{\text{GW}}|G, H_0)} p(G|D_{\text{GW}}, H_0) + \frac{p(x_{\text{GW}}|\bar{G}, H_0)}{p(D_{\text{GW}}|\bar{G}, H_0)} p(\bar{G}|D_{\text{GW}}, H_0)$$

in-catalogue

out-of-catalogue

Detection efficiency (selection function):

$$\mathcal{N}_{\text{eff}}(\Omega) = \int_{\mathcal{E}_{\text{det}}} d\mathcal{E} \int d\theta p(\mathcal{E}|\theta, \Omega, \mathcal{H}, \mathcal{I}) p(\theta|\Omega, \mathcal{H}, \mathcal{I})$$

Correct for / take into account possible
contribution of **galaxies missing from
catalogue**

Schechter luminosity function

Integrate over all **detectable data sets**

Integrated method of taking into account
both effects.

Abbott+ Nature **551** #7678, 85-88 (2017)

Mandel, Farr, Gair 2018; Chen+ 2018; Mortlock+ 2018

Gray+ 2020; Gray+ 2022: `gwcosmo` (LVK pipeline)

GW selection effects

$$\mathcal{N}_{\text{eff}}(\Omega) = \int_{\mathcal{E}_{\text{det}}} d\mathcal{E} \int d\theta p(\mathcal{E}|\theta, \Omega, \mathcal{H}, \mathcal{I}) p(\theta|\Omega, \mathcal{H}, \mathcal{I})$$

integrate over all **detectable data sets**

semi-analytical | MCMC

- \mathcal{N}_{eff} depends on the source population parameters
mass distribution, rate evolution
- H_0 depends on assumed (unknown) source population parameters
- Solution: infer population parameters and H_0 simultaneously
- Ties dark siren and spectral siren methods

Codebase improvement

Mastrogiovanni+ 2023; Mastrogiovanni+ arXiv:2305.17973

Rachel Gray @ U. Glasgow, . . . , Freija Beirnaert, Cezary Turski @ UGent arXiv:2308.02281

`icarogw`:

- Inclusion of galaxy catalogue information
- More flexible way of weighting with luminosities

`gwcsmo`:

- Inclusion of additional parameters: Ω_m , population parameters
- Marginalization over population parameters
- Injection infrastructure for computation of selection effects

Monte Carlo integration for multi-dimensional integrals

- Line-of-sight redshift prior

@ UGent

Line-of-sight redshift prior

Cross-correlating redshift space distributions with GW localizations

merger probability in redshift space

Don't need precise locations of galaxies; GW localizations are poor

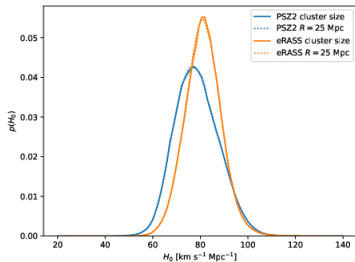
effects of **galaxy clustering** already taken into account

Can extend beyond galaxy catalogues to galaxy cluster catalogues

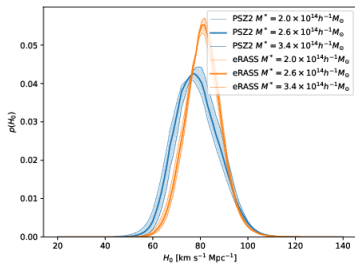
X-ray surveys; astrophysics?

Opposite approach as Ish Gupta

Limited systematic studies



← varying cluster size (z uncert.)



← varying Press-Schechter parameters