

# A tale of two kinds of superconducting nickelates

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**Engineered 2D Quantum Materials**

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# Collaborations

## Ruhr-University Bochum

- Steffen Bötzel
- Jannik Gondolf
- Ilya M. Eremin

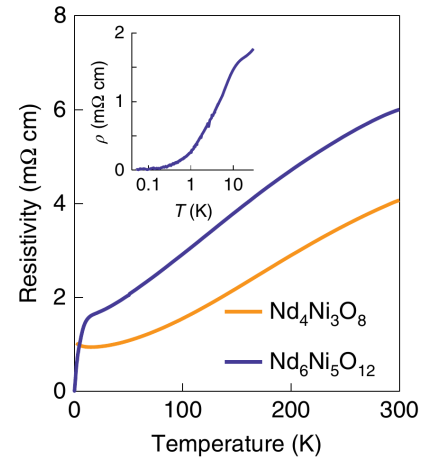
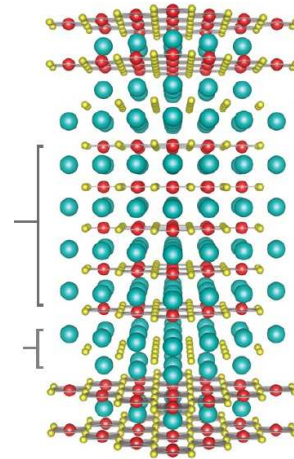
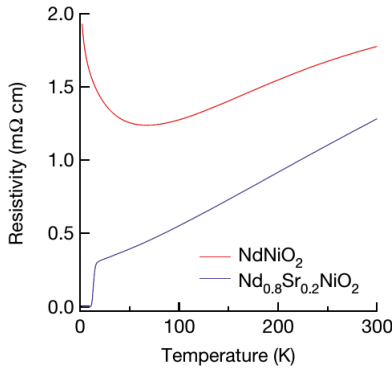
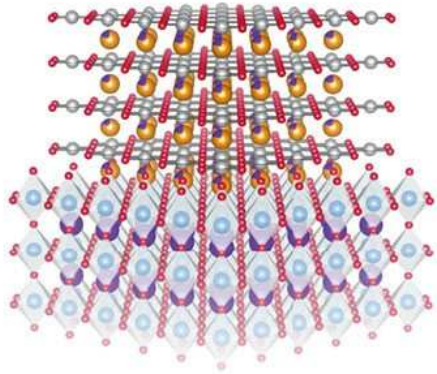
## Additional support

- Brian M. Andersen, Kopenhagen
- Andreas Kreisel, Kopenhagen
- Astrid Romer, Kopenhagen
- Evgeny Stepanov, Paris
- Matteo Vandelli, Hamburg
- Alexander I. Lichtenstein, Hamburg



# Superconducting nickelates: materials

$9-\delta$



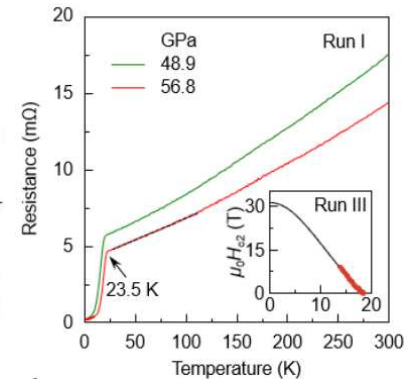
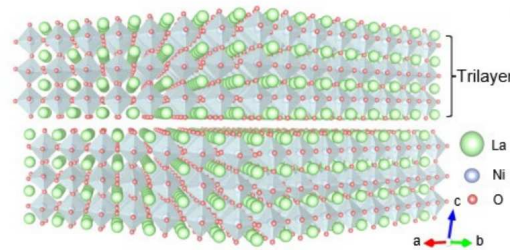
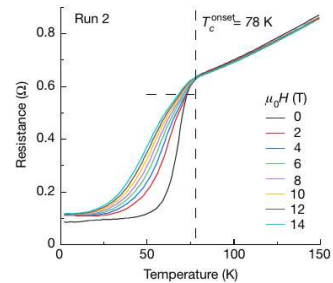
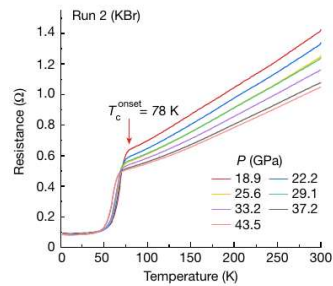
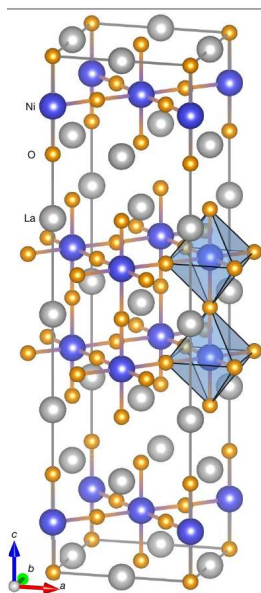
infinite-layer Sr-doped  $\text{RENiO}_2$ ,  $T_c \sim 10\text{-}25\text{ K}$

[Li et al., Nature 572, 624 (2019)]

quintuple-layer  $\text{Nd}_6\text{Ni}_5\text{O}_{12}$ ,  $T_c \sim 10\text{ K}$

[Pan et al., Nat. Mater. 21, 160 (2022)]

$8\pm\delta$



high-pressure  $\text{La}_4\text{Ni}_3\text{O}_{10}$ ,  $T_c \sim 23\text{ K}$

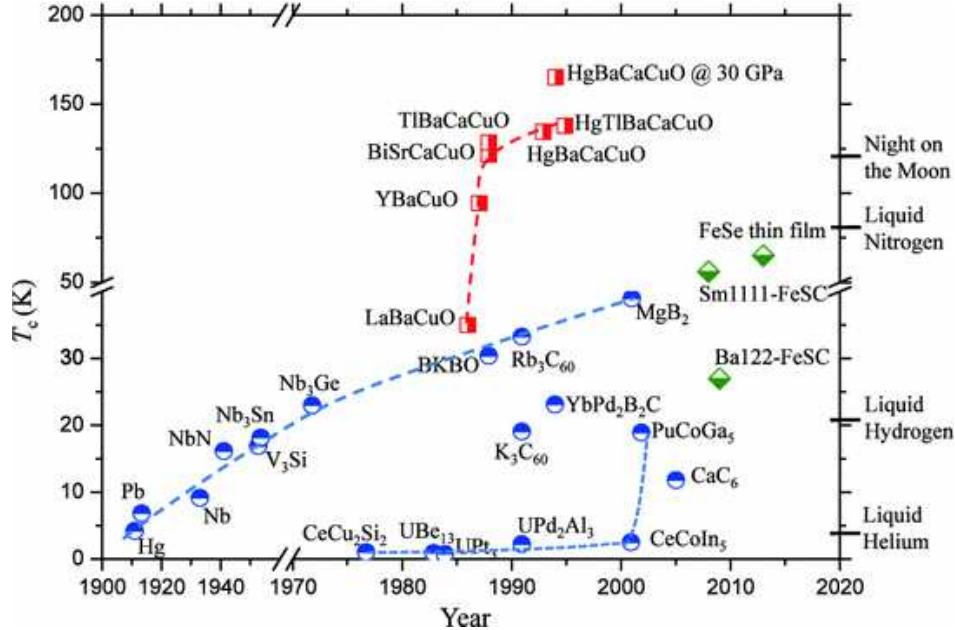
[Zhu et al., Nature 631, 531 (2024)]

[Zhang et al., arXiv:2311.07423 (2023)]

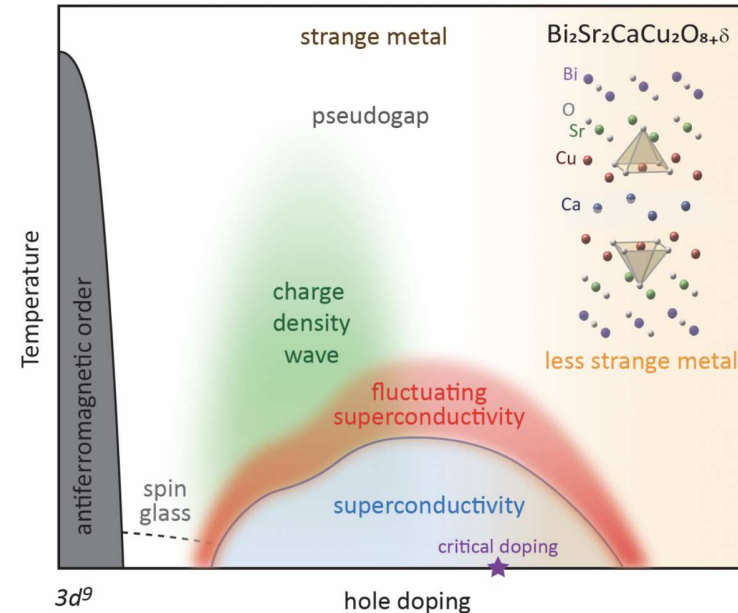
high-pressure  $\text{La}_3\text{Ni}_2\text{O}_7$ ,  $T_c \sim 65\text{-}80\text{ K}$

[Sun et al., Nature 621, 493 (2023)]

# Superconducting nickelates: motivated by high- $T_c$ cuprates



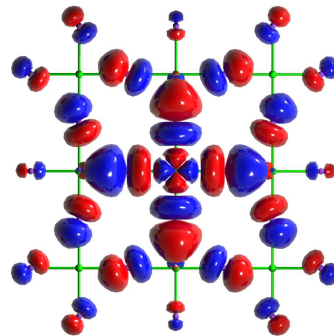
[Rigamonti, Caretta, Structure of Matter]



[Shen group, Stanford]

## basic cuprate characteristics

- charge-transfer insulator,  $\text{Cu}^{2+} (3d^9)$
- square  $\text{CuO}_2$  planes
- antiferromagnetic (AFM) order
- hole doping:  $3d^9 \underline{L}$   
→ leads to low-energy Zhang-Rice singlet
- effective one-orbital pic (minimal model):  
 $\text{Cu}-d_{x^2-y^2}$  hybridized with  $\text{O}(2p)$



by O. K. Andersen

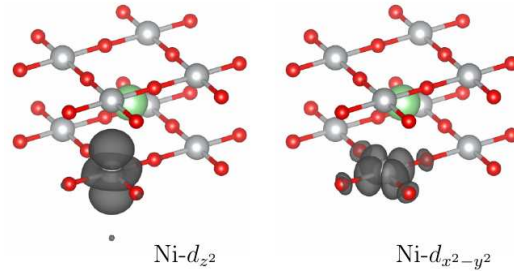
## “nickelates to cuprates”?

- preferred in oxides:  $\text{Ni}^{2+} (3d^8)$
- doping of insulating nickelates often leads to in-gap states
- ‘most-natural’  $\text{Ni}^+ (3d^9)$  compound:  $\text{RENiO}_2$  (with RE rare-earth 3+ ion)

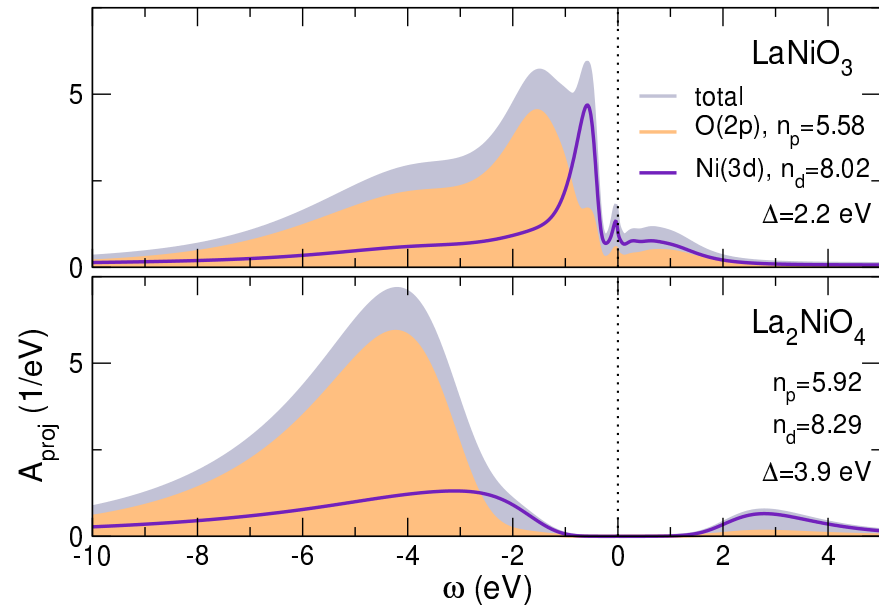
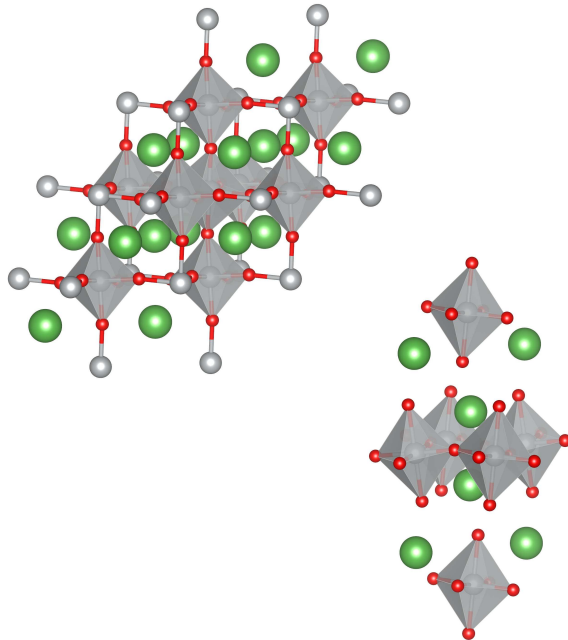
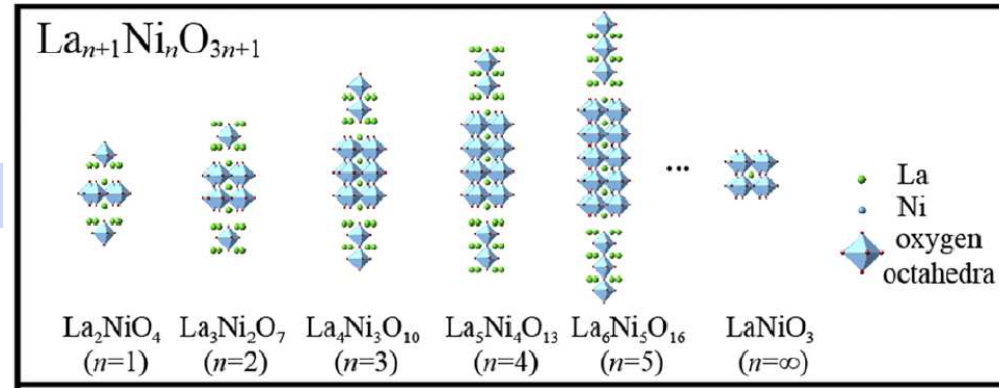
# Nickelates: basics

[FL, Elect. Struc. 4, 015005 (2022)]

Ni- $e_g$  frontier orbitals



Ruddlesden-Popper compounds



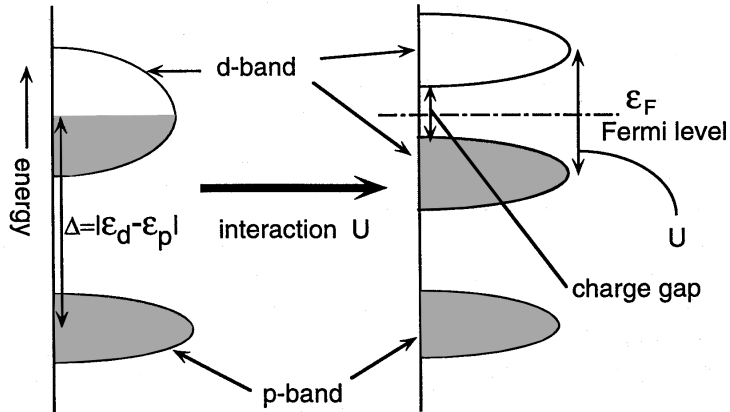
# Nickelates: Mott-Hubbard vs. charge-transfer

[Mattheis, PRB 5, (1972)]

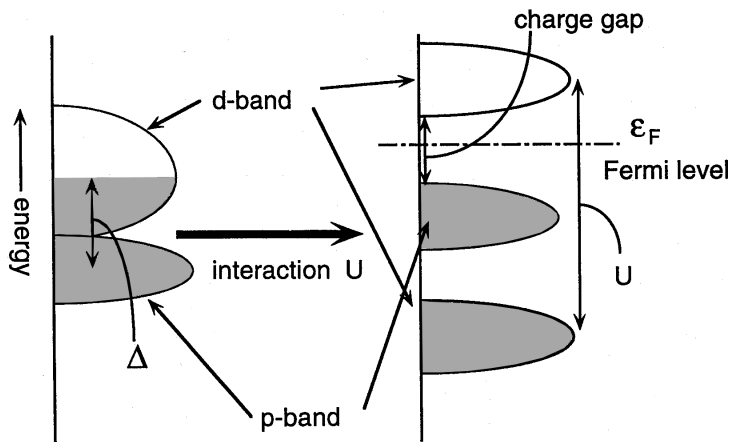
[Zaanen, Sawatzky, Allen, PRL 55, (1985)]

[Imada, Fujimori, Tokura, RMP 70, (1998)]

Hubbard  $U$  vs. charge-transfer energy  $\Delta = \varepsilon_d - \varepsilon_p$



(a) Mott-Hubbard Insulator



(b) Charge Transfer Insulator

formal  $3d^n$

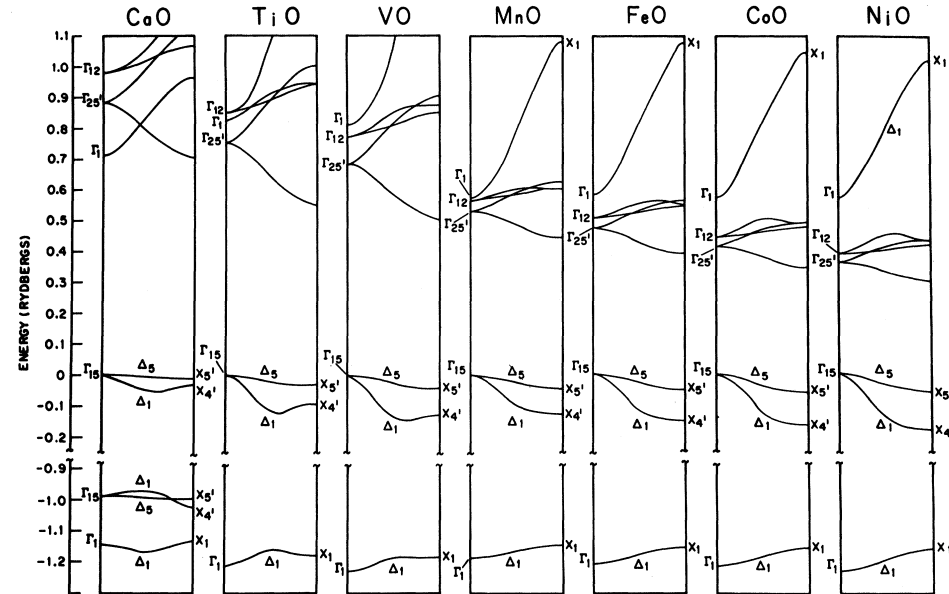


FIG. 2. APW energy-band results for the  $3d$  transition-metal oxides plotted along the  $\Delta$  direction of the Brillouin zone.

formal  $3d^{n-1}$

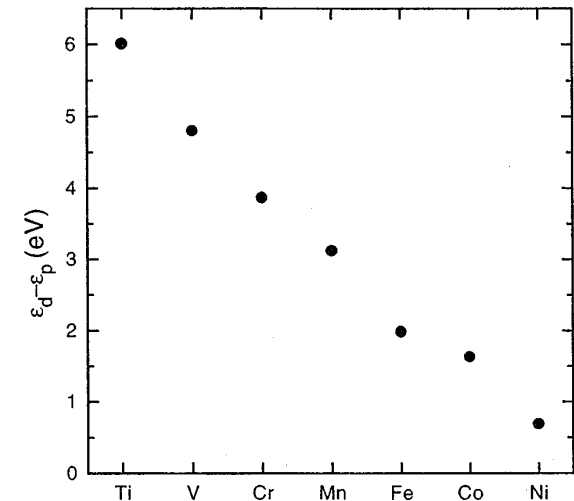
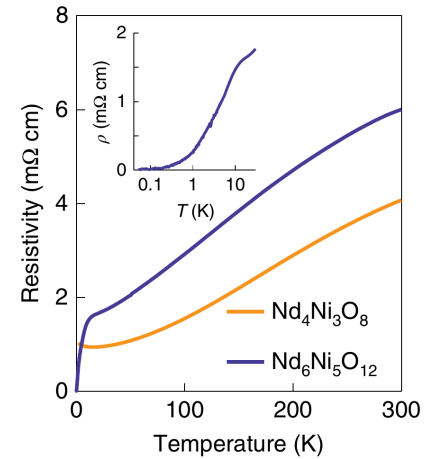
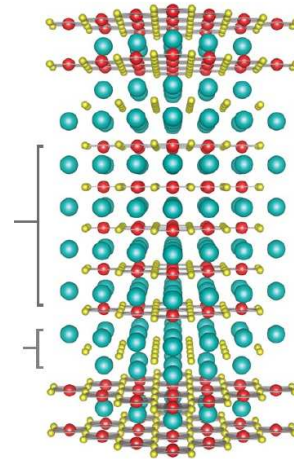
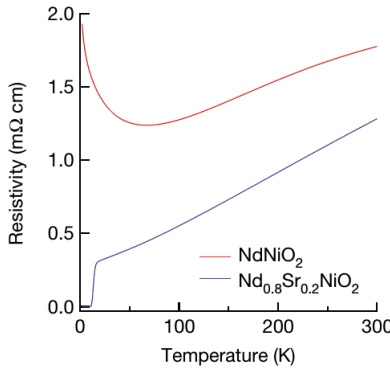
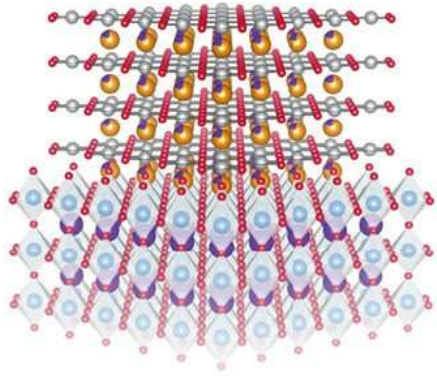


FIG. 59. Variation of  $\varepsilon_d - \varepsilon_p$  for the  $\text{LaMO}_3$  series with the metal  $M$  element. From Mahadevan *et al.*, 1996.

# Superconducting nickelates: materials

$9-\delta$



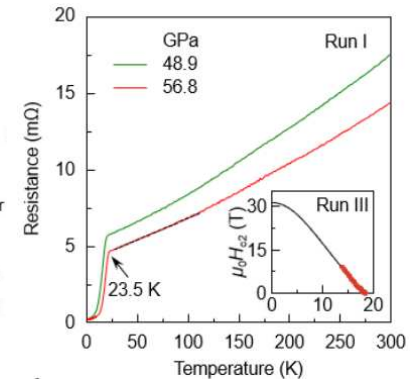
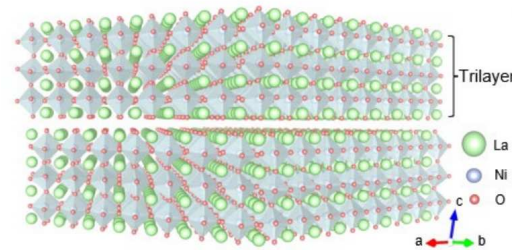
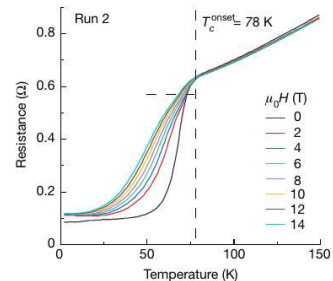
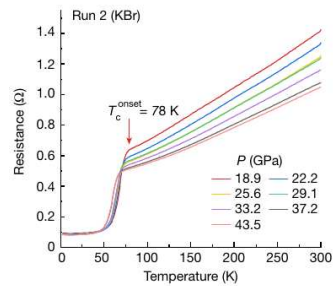
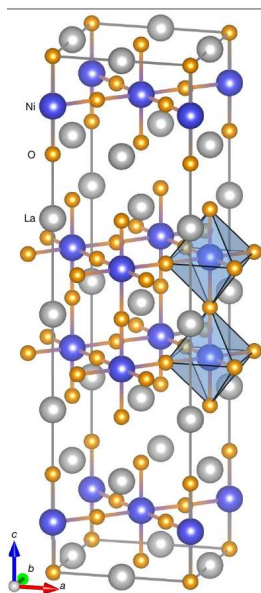
infinite-layer Sr-doped  $\text{RENiO}_2$ ,  $T_c \sim 10\text{-}25$  K

[Li et al., Nature 572, 624 (2019)]

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[Pan et al., Nat. Mater. 21, 160 (2022)]

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high-pressure  $\text{La}_4\text{Ni}_3\text{O}_{10}$ ,  $T_c \sim 23$  K

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[Sun et al., Nature 621, 493 (2023)]

# $3d^{9-\delta}$ superconductors: initial work on $\text{LaNiO}_2$

experiment



[Crespin et al., J. Chem. Soc., Faraday Trans. 2 79, 1181 (1983)]

[Levitz et al., J. Chem. Soc., Faraday Trans. 2 79, 1195 (1983)]

[Hayward et al., J. Am. Chem. Soc. 121, 8843 (1999)]

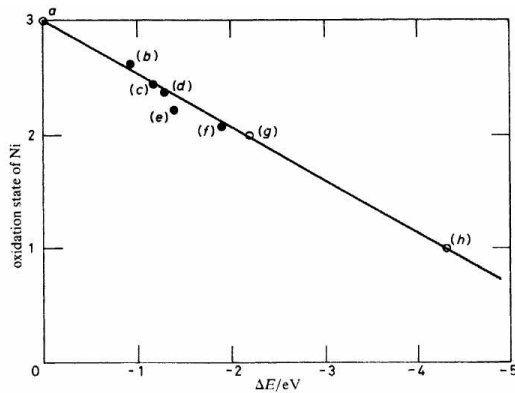


Fig. 6. Oxidation state of nickel in different phases formed during reduction of  $\text{LaNiO}_3$  plotted against the energy shift of the absorption edge using  $\text{LaNiO}_3$  as a standard: (a)  $\text{LaNiO}_3$ , (b)  $\text{LaNiO}_{2.8}$ , (c)  $\text{LaNiO}_{2.7}$ , (d)  $\text{LaNiO}_{2.68}$ , (e)  $\text{LaNiO}_{2.6}$ , (f)  $\text{La}_2\text{NiO}_4$ , (g)  $\text{LaNiO}_{2.5}$  and (h)  $\text{LaNiO}_2$ .

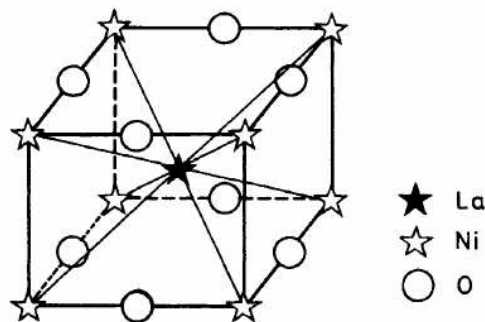
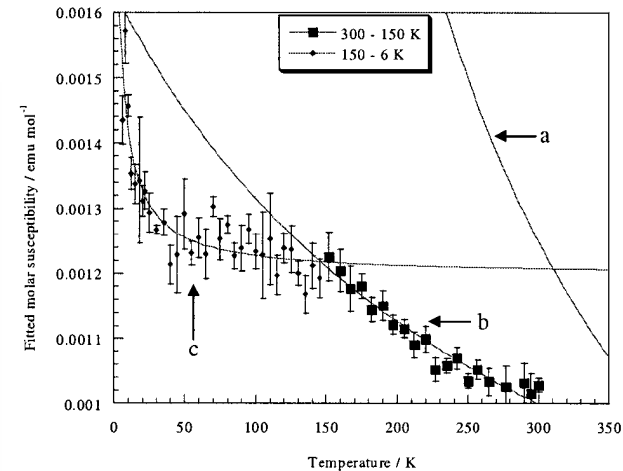
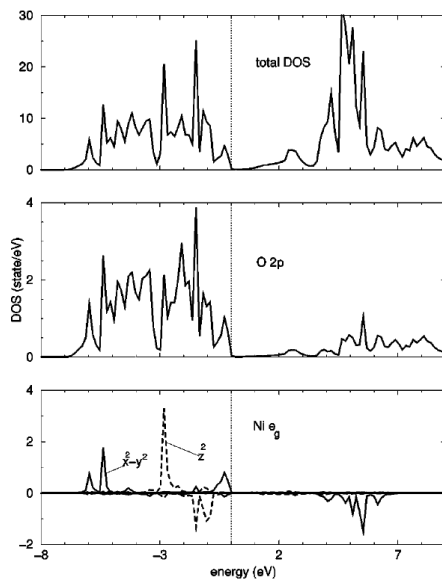


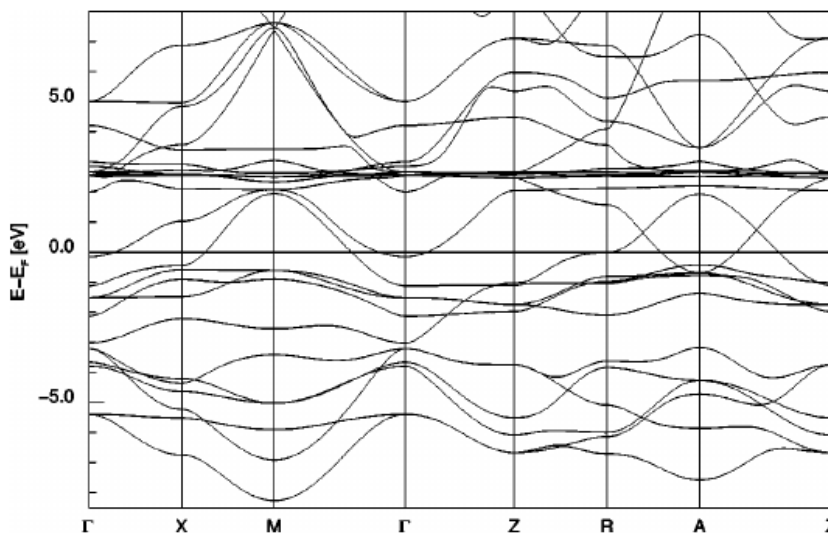
Fig. 1. Proposed structure of  $\text{LaNiO}_2$ .



$\text{LaNiO}_2$



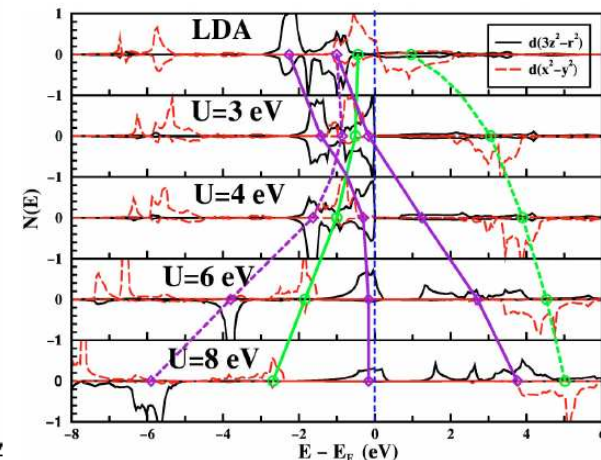
theory



[Choisnet et al., J. Phys. Chem. Solids 57, 1839 (1996)]

[Anisimov, Bukhvalov, Rice, PRB 59, 7901 (1999)]

[Lee and Pickett, PRB 70, 165109 (2004)]





# Experimental finding: finally, a superconducting nickelate!

[Li et al., Nature 572, 624 (2019)]  
[Lee et al., APL Materials 8, 041107 (2020)]

## LETTER

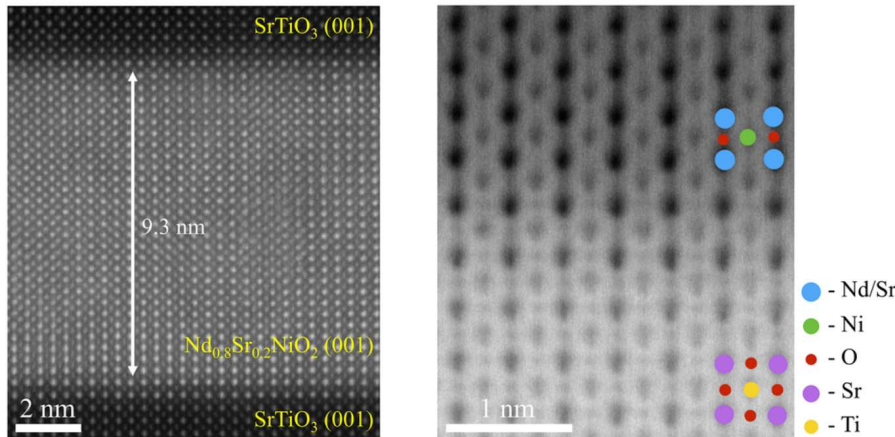
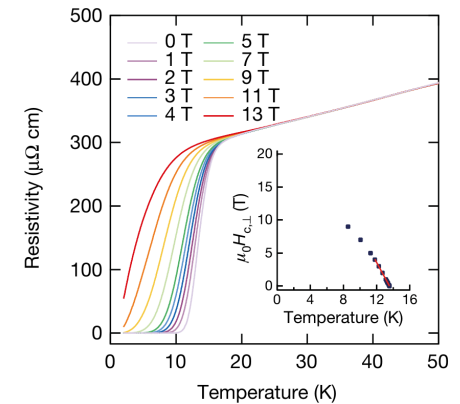
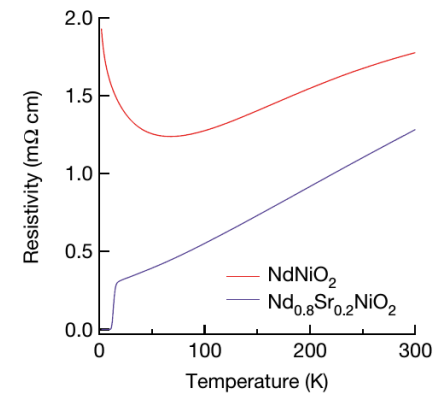
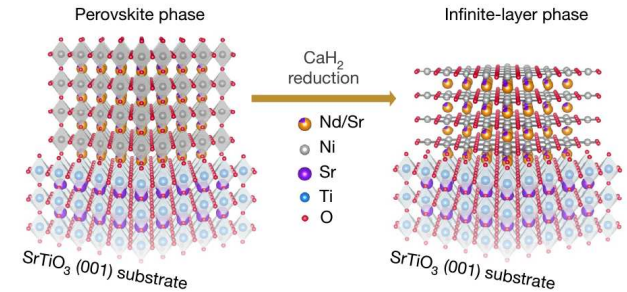
<https://doi.org/10.1038/s41586-019-1496-5>

### Superconductivity in an infinite-layer nickelate

Danfeng Li<sup>1,2\*</sup>, Kyuho Lee<sup>1,3</sup>, Bai Yang Wang<sup>1,3</sup>, Motoki Osada<sup>1,4</sup>, Samuel Crossley<sup>1,2</sup>, Hye Ryoung Lee<sup>1,4</sup>, Yi Cui<sup>1,4</sup>, Yasuyuki Hikita<sup>1</sup> & Harold Y. Hwang<sup>1,2\*</sup>

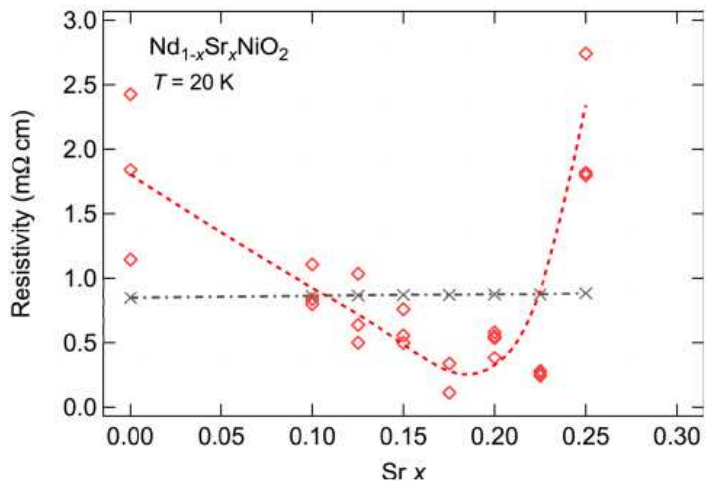
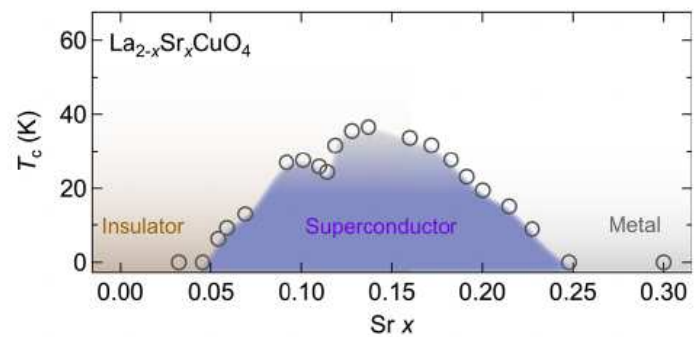
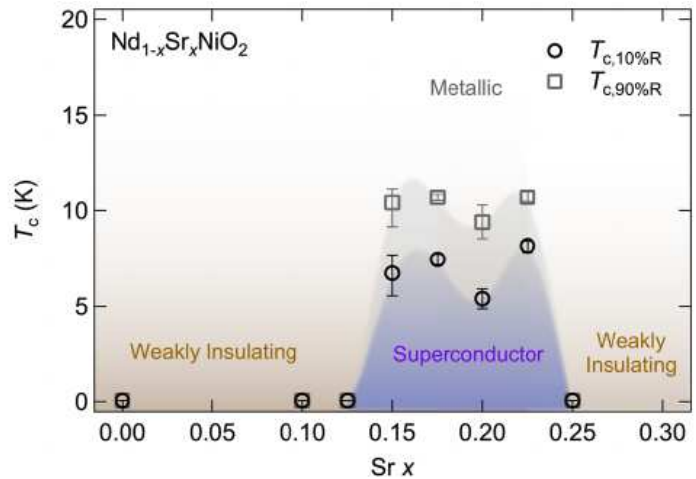
- thin films of infinite-layer NdNiO<sub>2</sub> on SrTiO<sub>3</sub>
- film thickness  $\sim 10$  nm
- resistivity upturn below  $T = 70$  K
- 20% Sr (hole) doping: superconducting below  $T \sim 10$  K
- critical current density  $J_c \sim 170$  kA cm<sup>-2</sup>
- zero- $T$  coherence length  $\sim 3.25$  nm, type-II superconductor
- recent data: Pauli-limit violation in doped LaNiO<sub>2</sub> and PrNiO<sub>2</sub>?

[Chow et al., arXiv:2204.12606 (2022)] [B. Y. Wang, et al., arXiv:2205.15355 (2022)]

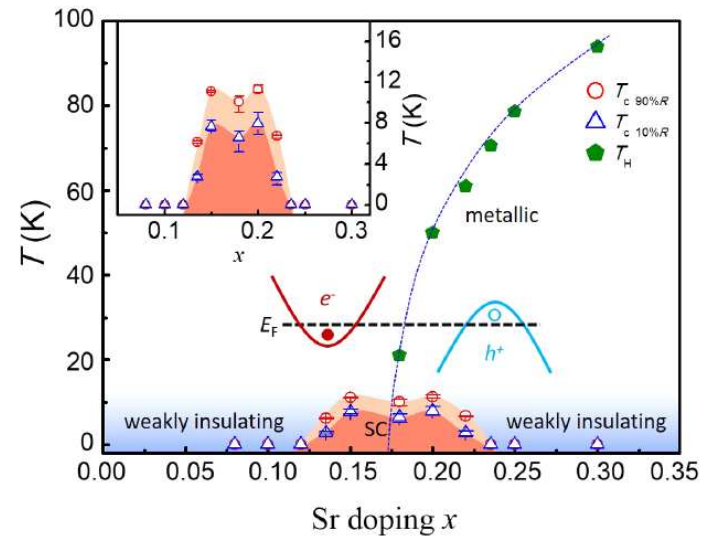
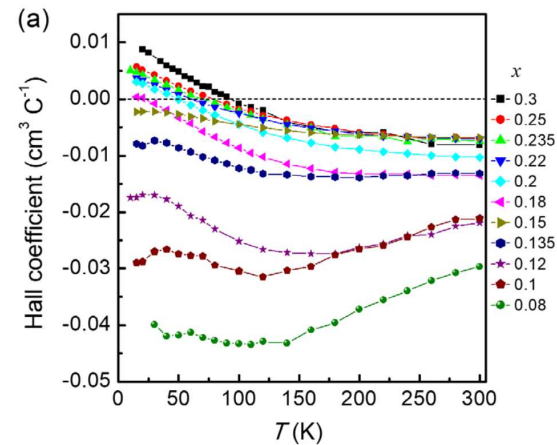


# $3d^{9-\delta}$ superconductors: some experimental data

[Li et al., PRL 125, 027001 (2020)]  
 [Zheng et al., PRL 125, 147003 (2020)]



- superconducting “dome” for  $0.125 < x < 0.25$
- reminiscent of dome in layered cuprates
- but: weakly-insulating on both sides of superconducting region
- Hall data suggests two-band picture with doping



# $3d^{9-\delta}$ superconductors: theory concepts

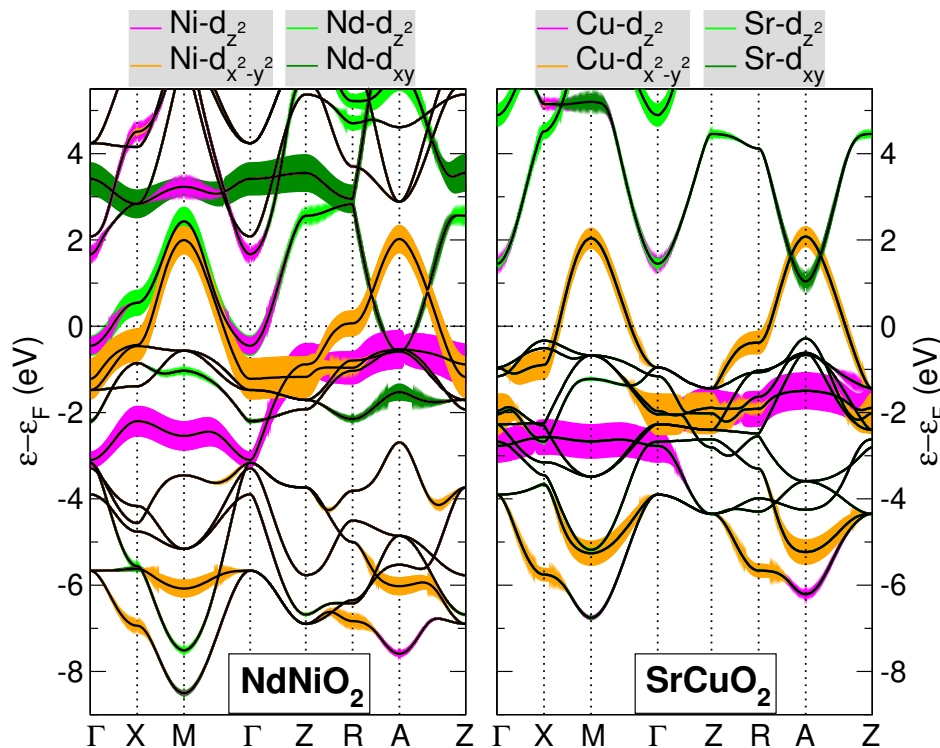
e.g. reviews

[Norman, Physics 13, 85 (2020)]

[Botana, Bernadini, Cano, JETP 132, 618 (2021)]

- indeed cuprate(-like) physics: mainly Ni- $d_{x^2-y^2}$  driven e.g. [Nomura et al. PRB 100, 205138 (2019)]  
[Wu et al., PRB 101, 060504(R) (2020)][Si et al., PRL 124, 166402 (2020)] [Karp et al. PRX 10, 021061 (2020)][Been et al., PRX 11, 011050 (2021)]
- Kondo-based physics involving Ni- $d_{x^2-y^2}$  and Nd orbitals  
e.g. [Zhang et al. PRBB 101, 020501(R) (2020)]
- dominant interface physics (induced by SrTiO<sub>3</sub> substrate)  
e.g. [Geisler and Pentcheva, PRB 102, (020502(R)) [Zhang et al., PRB 102, 195117 (2020)]
- Ni multiorbital physics (Mott vs. Hund (vs. Kondo))  
e.g. [Werner and Hoshino, PRB 101, 041104(R) (2020)] [Wang et al., PRB 102, 161118(R)][Choi et al., PRR 2, 033445 (2020)]

s from  
ity functional theory



e.g. DFT work  
[Botana and Norman, PRX 10, 011024 (2020)]  
[FL, PRB 101, 081110(R) (2020)]

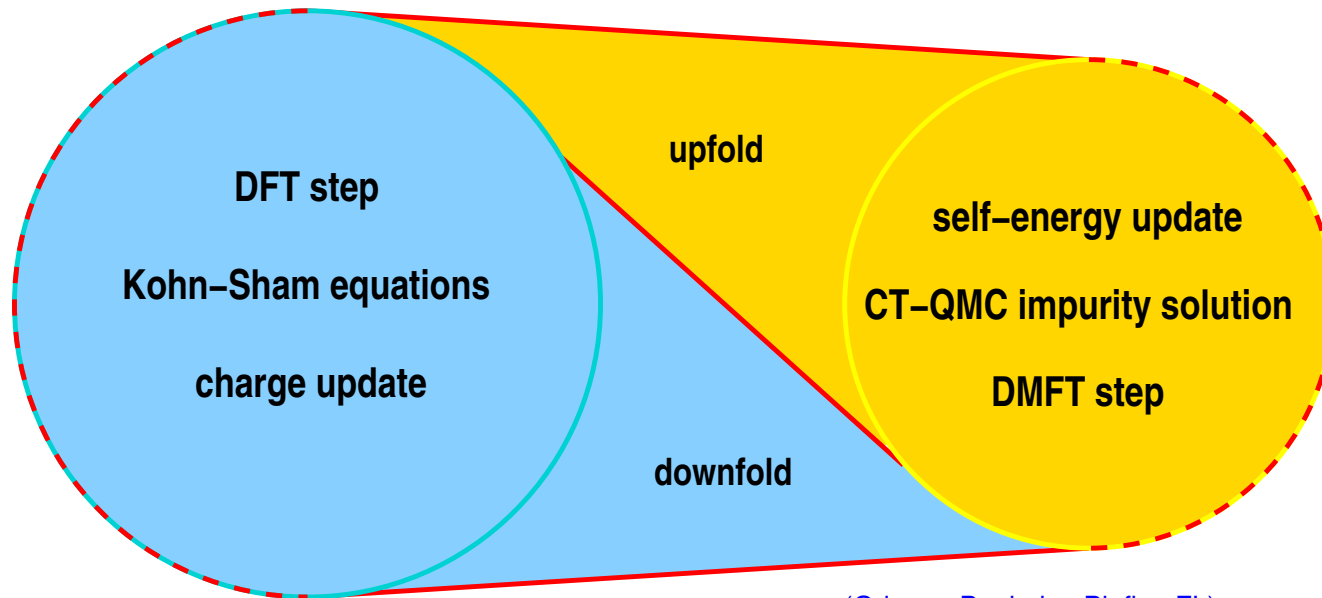
charge-transfer energy  $\Delta = \varepsilon_d - \varepsilon_p$   $\Delta(\text{NdNiO}_2) \sim 5.0 \text{ eV}$   $\Delta(\text{SrCuO}_2) \sim 1.3 \text{ eV}$

# Theoretical approach: realistic many-body

[Anisimov, Poteryaev, Korotin et al., JPCM 9, 7359 (1997)]  
[Held, Keller, Eyert et al., PRL 86, 5345 (2001)]  
[Minár, Chioncel, Perlov, et al., PRB 72, 045125 (2005)]  
[FL, Georges, Poteryaev et al., PRB 74, 125120 (2006)]

[Lichtenstein and Katsnelson, PRB 57, 6884 (1998)]  
[Pavarini, Biermann, Poteryaev et al., PRL 92, 176403 (2004)]  
[Kotliar, S. Y. Savrasov, K. Haule et al, RMP 78, 865 (2006)]  
[Grieger, Piefke, Peil and FL, PRB 86, 155121 (2012)] . . . , . . . , . . .

## Density Functional Theory (DFT) + Dynamical Mean-Field Theory (DMFT)



(Grieger, Boehnke, Piefke, FL)

- DFT part : mixed-basis pseudopotential  
[Meyer, Elsässer, Lechermann and Fähnle, MPI for Metals Research]
- DMFT impurity solver : hyb-CT-QMC (TRIQS code)  
[Parcollet et al., Comput. Phys. Commun. 196, 398 (2015)]  
[Seth et al, Comput. Phys. Commun. 200, 274 (2016)]

- charge self-consistency
- 1-5 local correlated orbitals

- up to 200-atom unit cells
- inclusion of correlations on oxygen

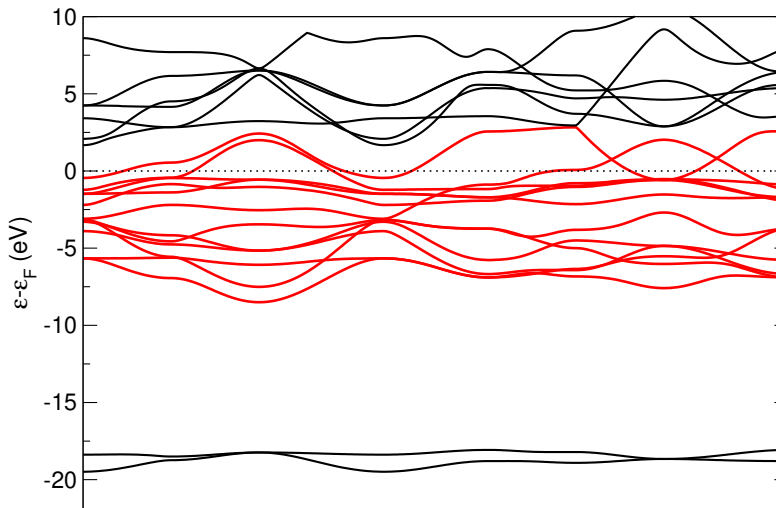
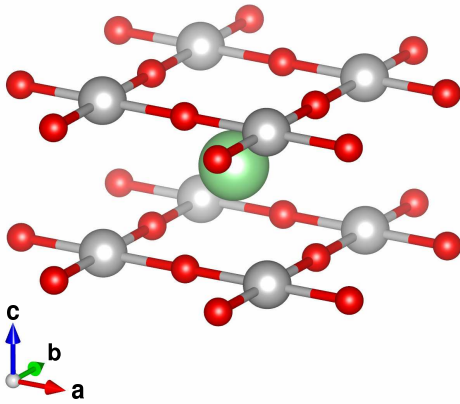


# Theoretical approach: settings for nickelates

- correlated subspace: Ni( $3d$ ) from projected-local orbitals
- rotational-invariant 5-orbital Slater-Hamiltonian:  $U = 10$  eV,  $J_H = 1$  eV
- self interaction correction (SIC) for oxygen:  $w_p = 0.8$
- fully-localized double counting correction

setting fixed for all nickelates

example: NdNiO<sub>2</sub>



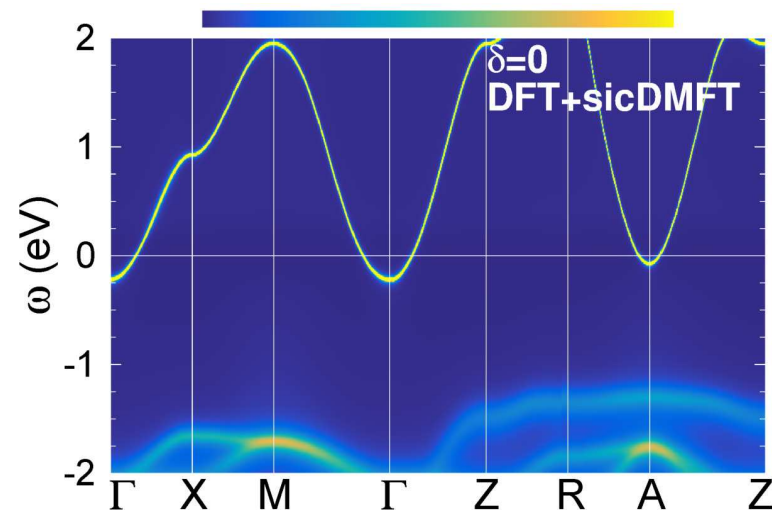
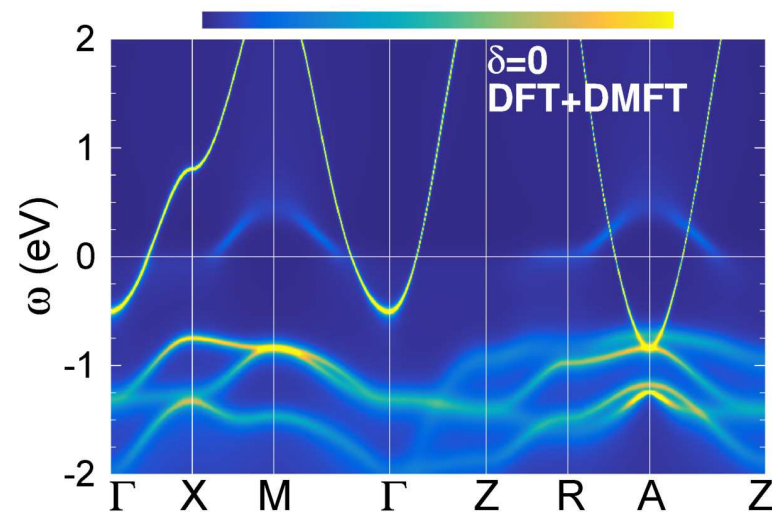
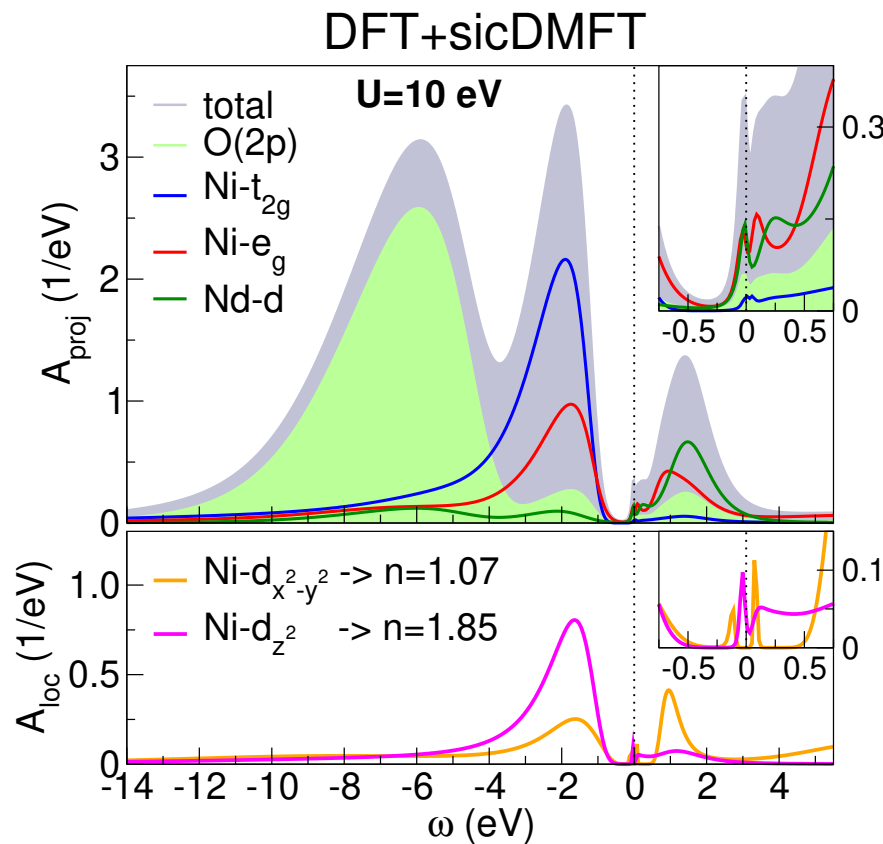
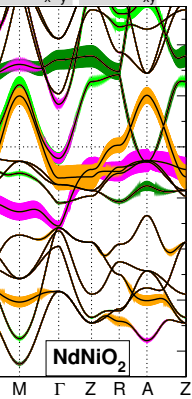
12 Kohn-Sham  
bands for projection  
onto Ni( $3d$ )

Ni- $d_{x^2-y^2}$     Nd- $d_{z^2}$   
 Ni- $d_{x^2-y^2}$     Nd- $d_{xy}$

# $3d^{9-\delta}$ superconductors: NdNiO<sub>2</sub>

[FL, PRB 101, 081110(R) (2020)]

[FL, PR Mat. 5, 044803 (2021)]



- Ni- $d_{x^2-y^2}$  (nearly) Mott-insulating, Ni- $d_{z^2}$  hybridizes with Nd- $d_{z^2}$  and forms  $\Gamma$ -pocket of self-doping band
- important: oxygen-based correlations (brought in by SIC), render the system highly correlated; NdNiO<sub>2</sub> is close to Mott criticality!

# $3d^{9-\delta}$ superconductors: experimental spectrum

[FL, PRB 101, 081110(R) (2020)]

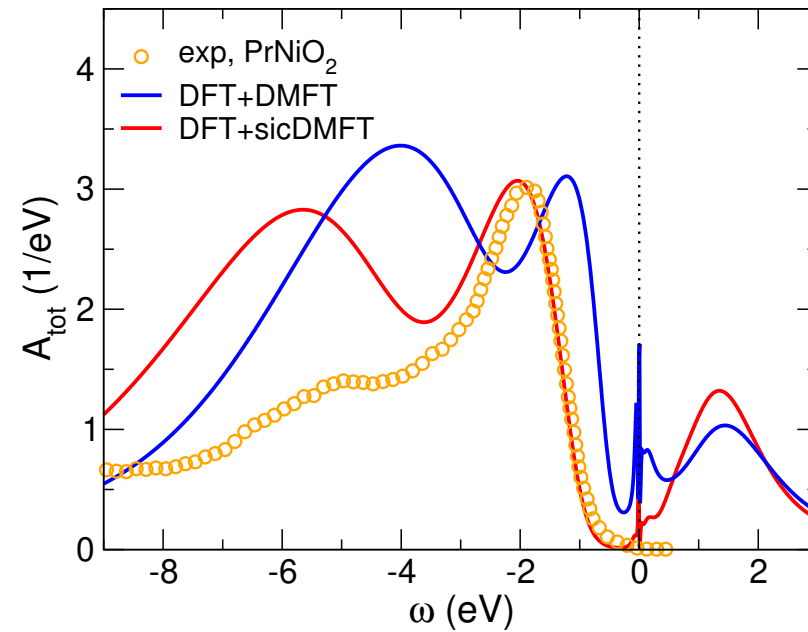
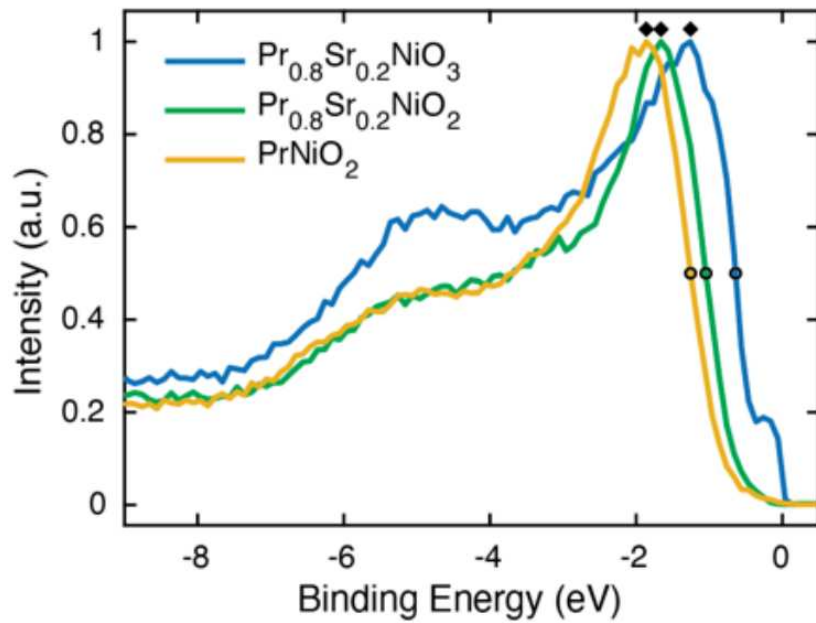
[FL, PR Mat. 5, 044803 (2021)]

[Chen et al., Matter 5, 1806 (2022)]

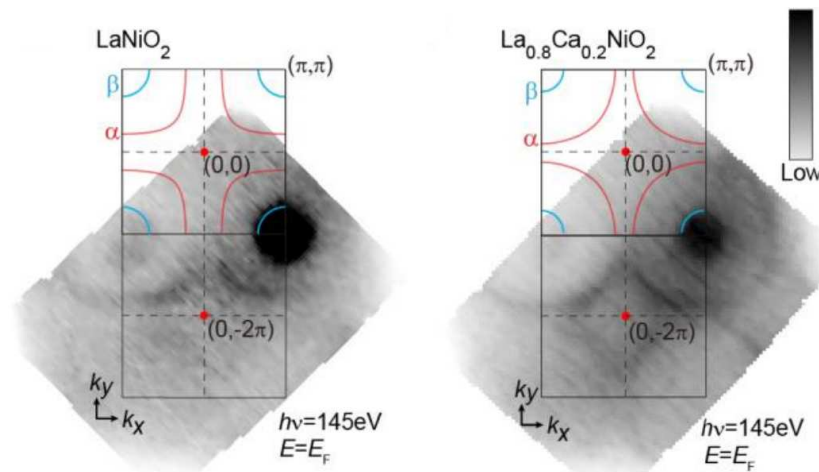
[Ding et al., Nat. Sci. Rev. 194 (2024)]

[Sun et al., arxiv:2403.07344 (2024)]

angle-integrated photoemission



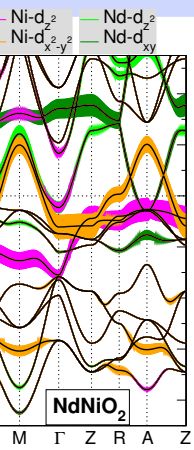
very recent ARPES



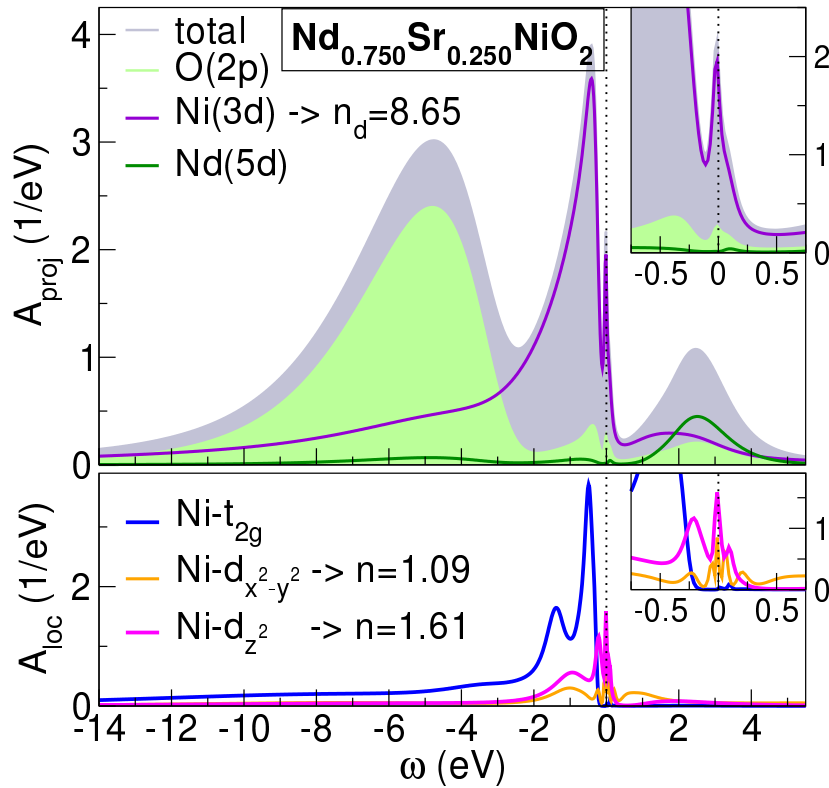
# $3d^{9-\delta}$ superconductors: doped $\text{NdNiO}_2$

[FL, PRB 101, 081110(R) (2020)]

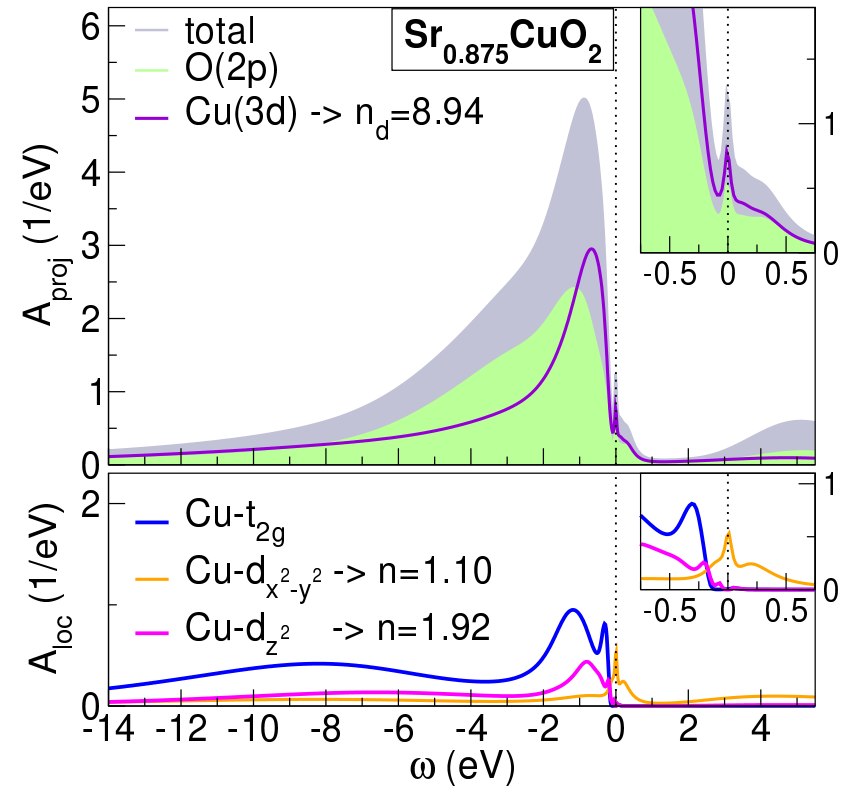
[FL, PR Mat. 5, 044803 (2021)]



DFT+sicDMFT ( $\delta = 0.25$ )



DFT+sicDMFT ( $\delta = 0.25$ )



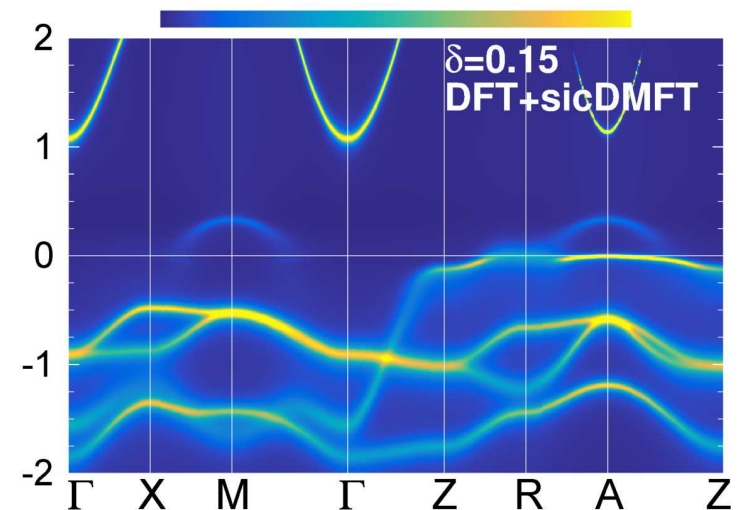
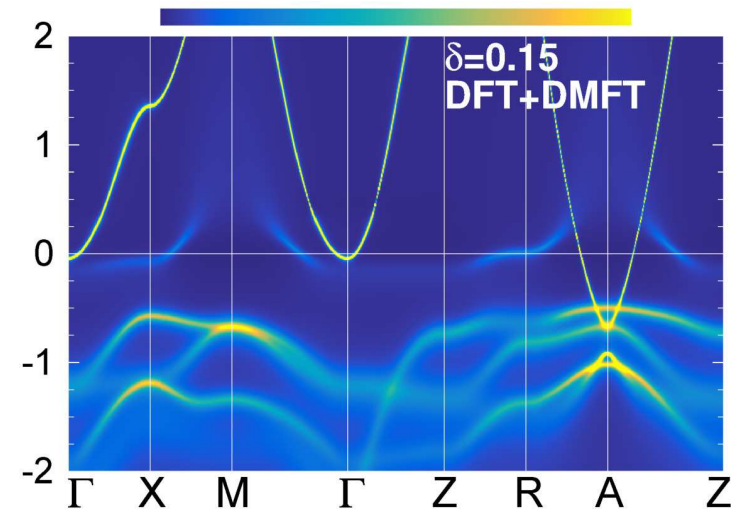
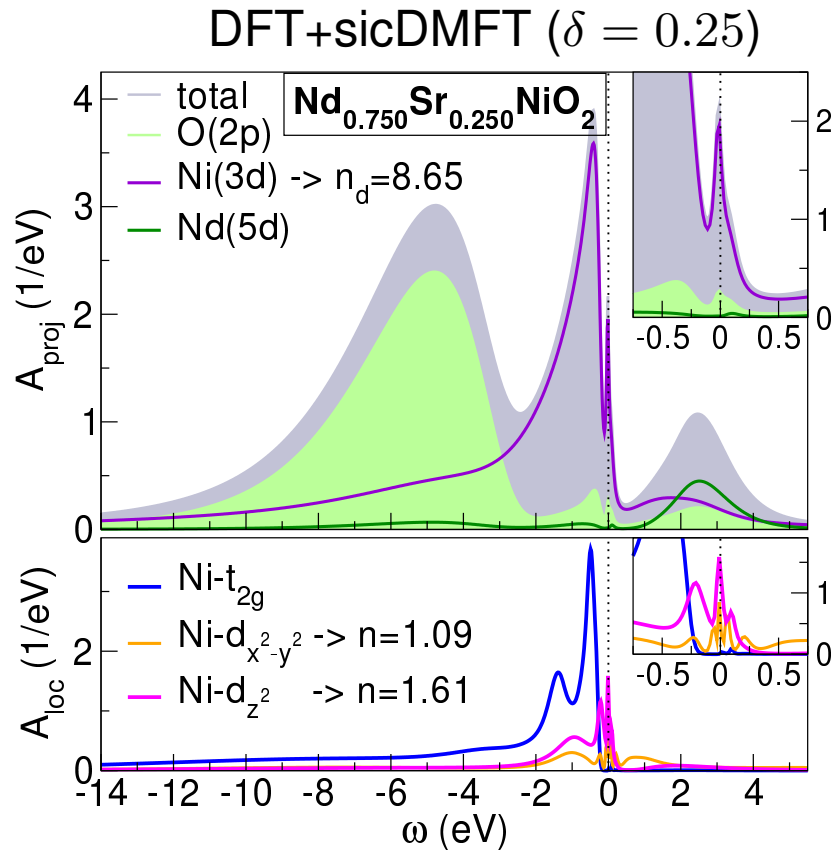
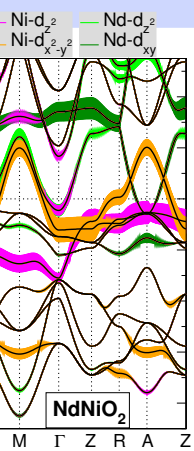
no strong Zhang-Rice physics



# $3d^{9-\delta}$ superconductors: doped $\text{NdNiO}_2$

[FL, PRB 101, 081110(R) (2020)]

[FL, PR Mat. 5, 044803 (2021)]



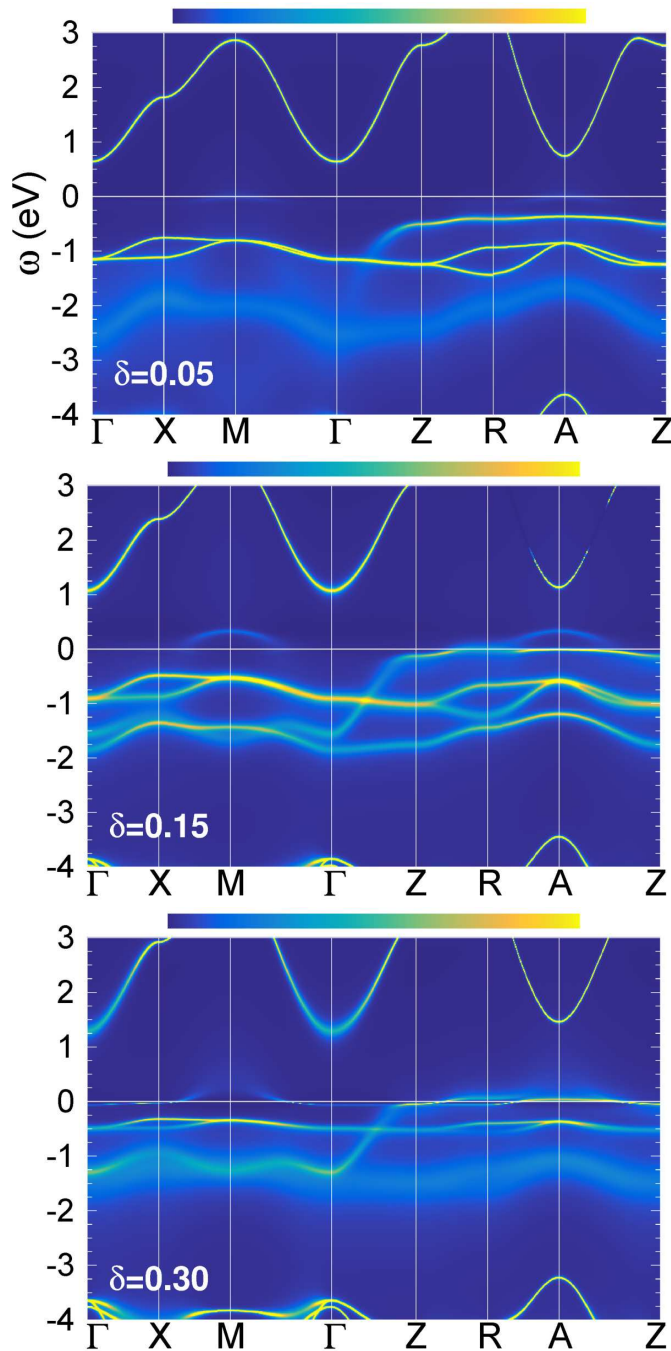
no strong Zhang-Rice physics



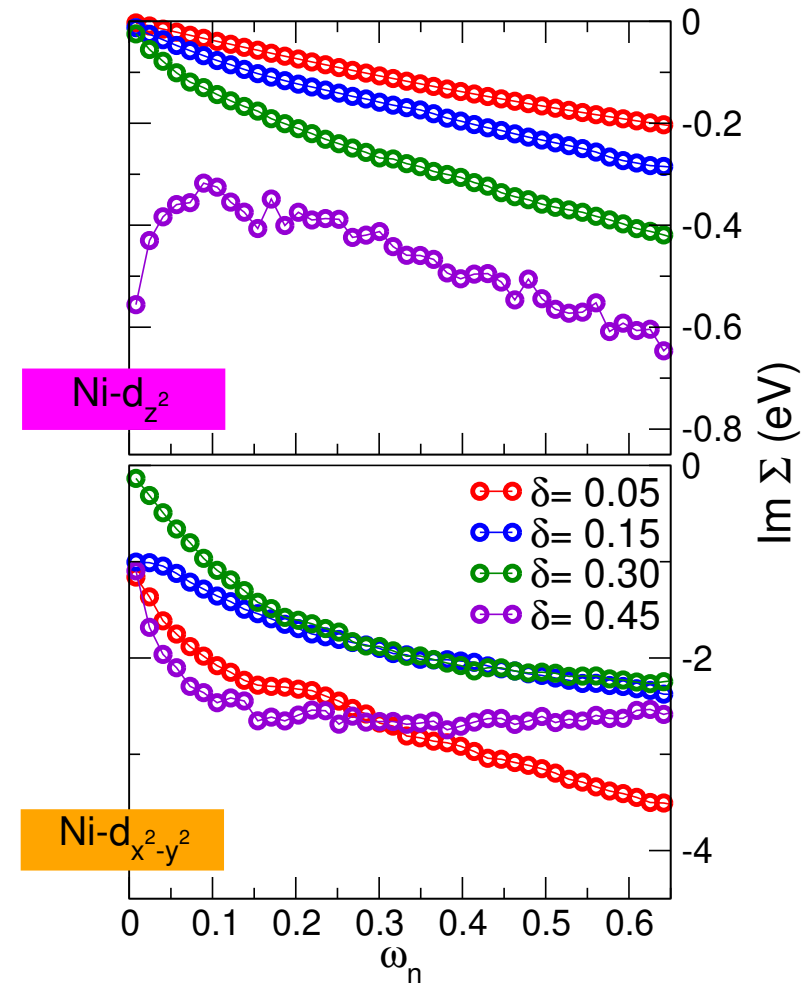
Ni- $d_{z^2}$  flat-band part in  $k_z = 0.5$  plane crosses Fermi level in the superconducting doping region when including oxygen-based correlations (brought in by SIC)


# $3d^{9-\delta}$ superconductors: doped $\text{NdNiO}_2$

[FL, PR Mat. 5, 044803 (2021)]



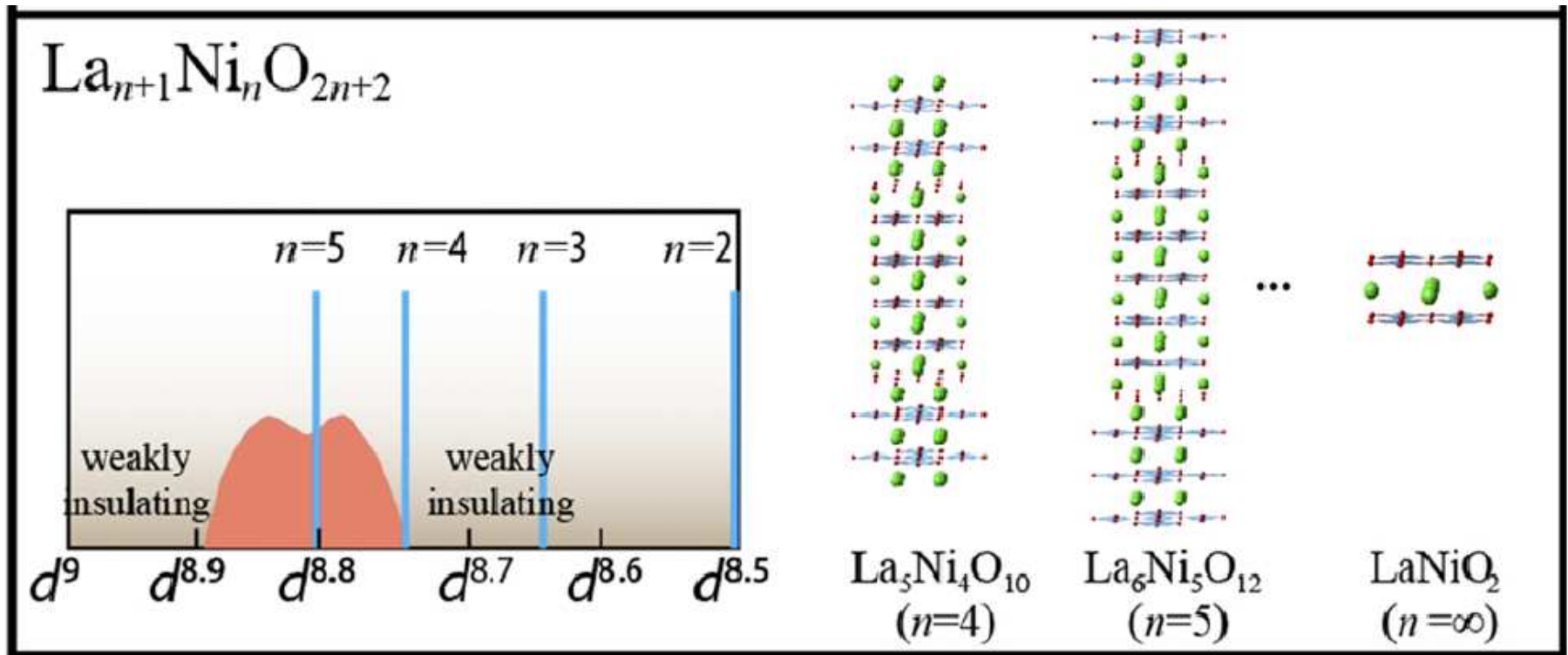
Ni- $e_g$  self-energy



 Ni- $d_{z^2}$  “brings” coherence to Ni- $d_{x^2-y^2}$

# Multilayer nickelates: infinite-layer vs. multilayer

e.g. [Li et al., APL Materials 8, 091112 (2020)]

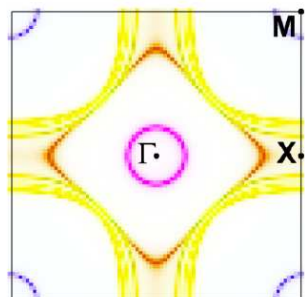
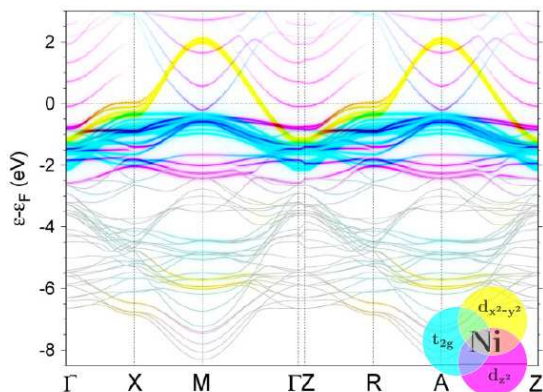
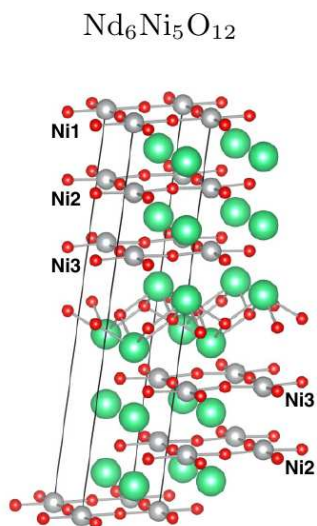


# $3d^{9-\delta}$ superconductors: quintuple-layer $\text{Nd}_6\text{Ni}_5\text{O}_{12}$

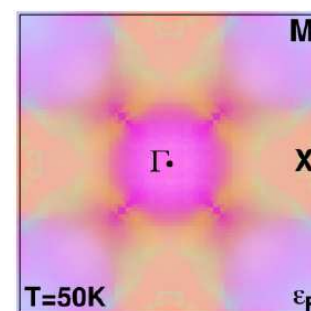
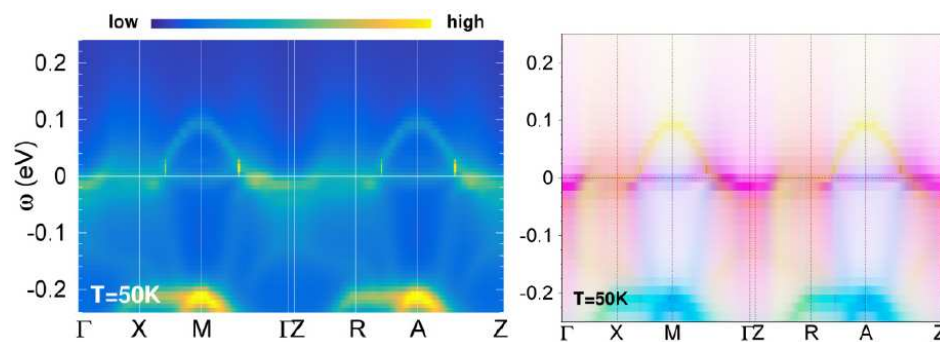
[Pan et al., Nat. Mater. 21, 160 (2022)]

[FL, PRB 105, 155109 (2022)]

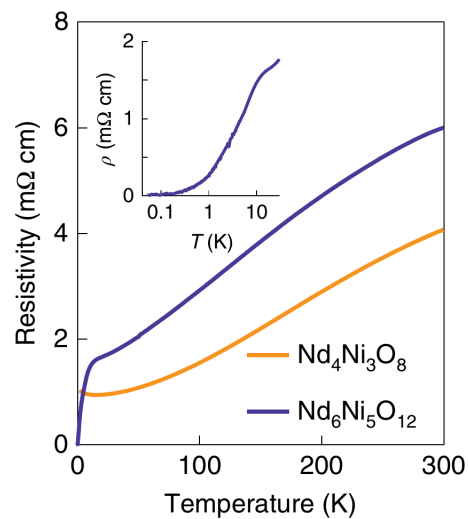
DFT picture



DFT+sicDMFT picture



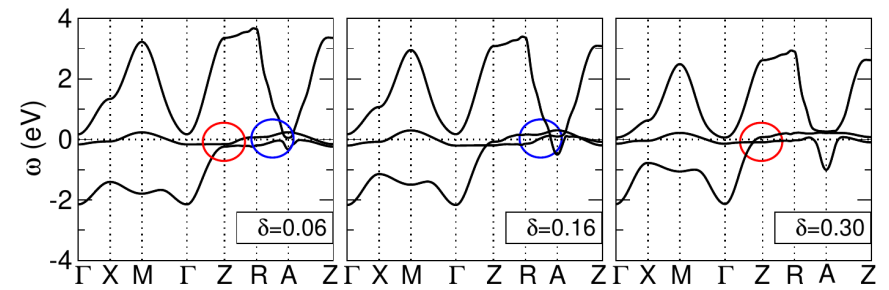
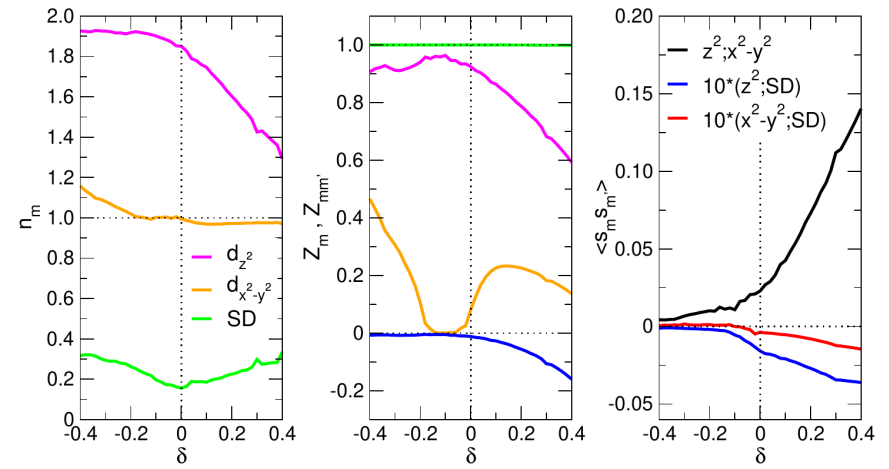
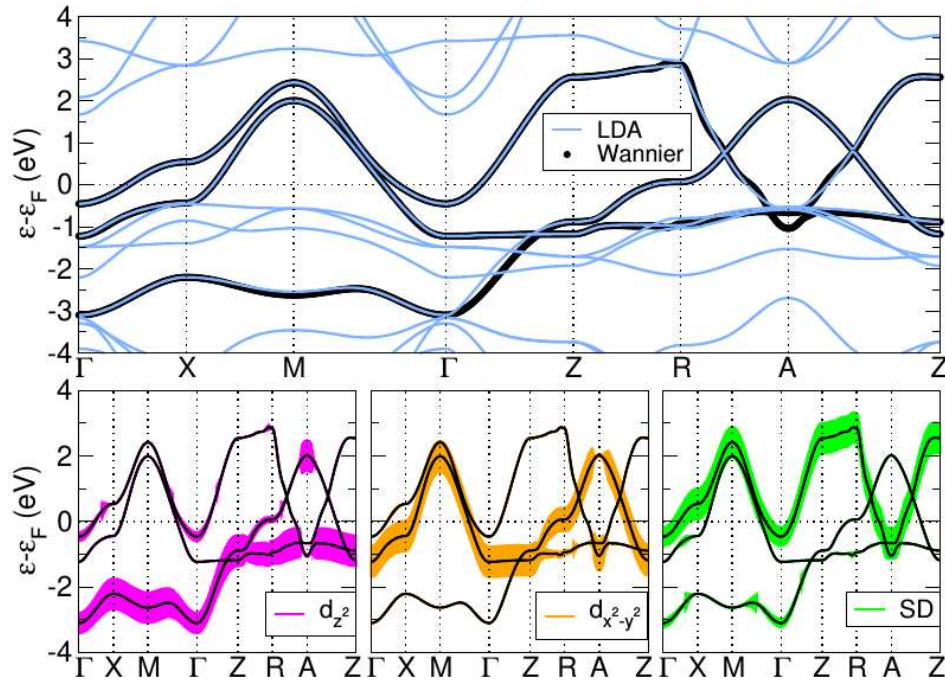
$$m^* / m_{\text{DFT}} \sim 25$$



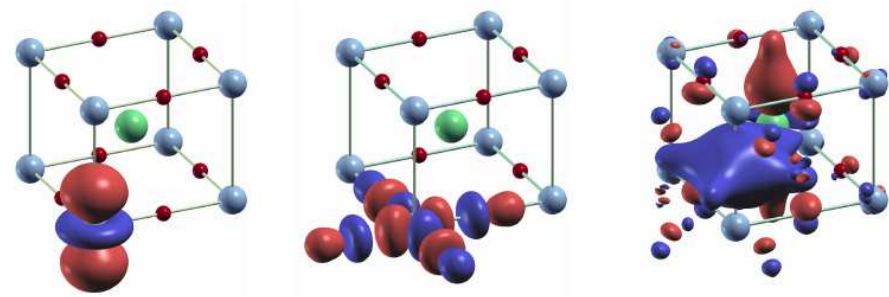
- similar  $d_{x^2-y^2}$  vs.  $d_{z^2}$  dichotomy from Ni as in infinite-layer compounds
- Ni- $d_{z^2}$  flat band appears essential for superconductivity

# Theoretical picture: three-band model for $\text{Nd}_{1-x}\text{Sr}_x\text{NiO}_2$

[FL, PRX 10, 041002 (2020)]



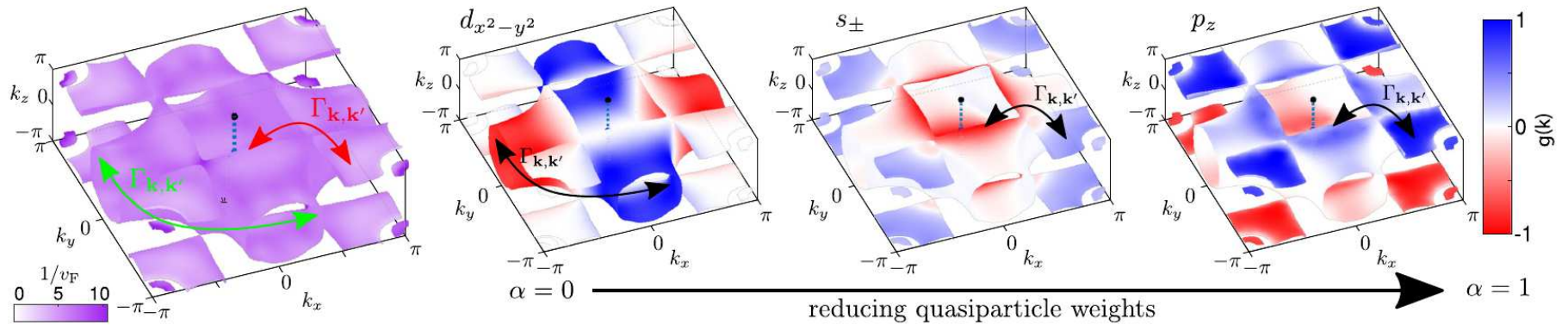
solved with rotational-invariant slave bosons (RISB)



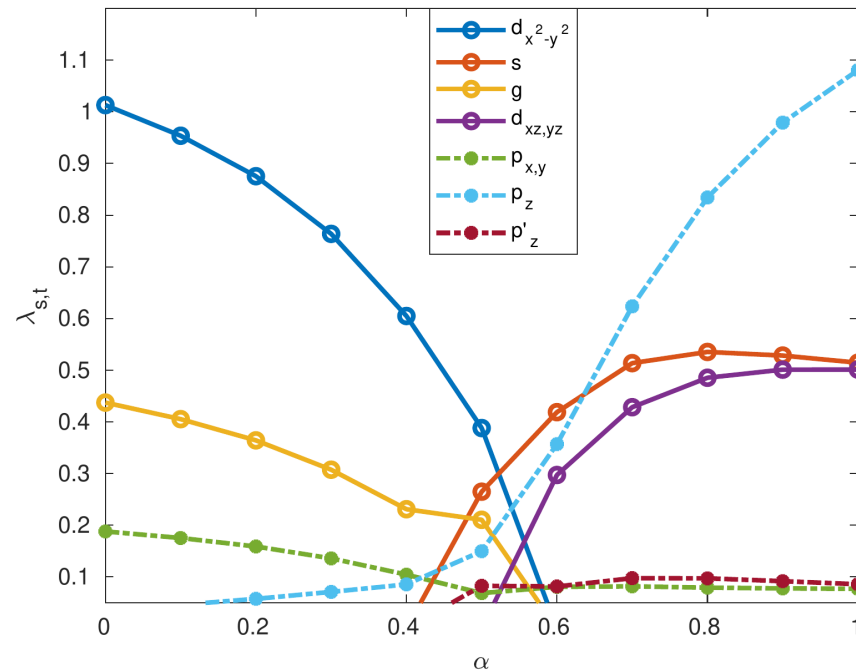
# $3d^{9-\delta}$ superconductors: model superconductivity

[Kreisel et al., PRL 129, 077002 (2022)]

## Leading SC instabilities from RPA spin fluctuations

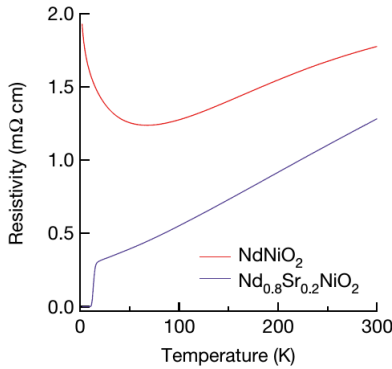
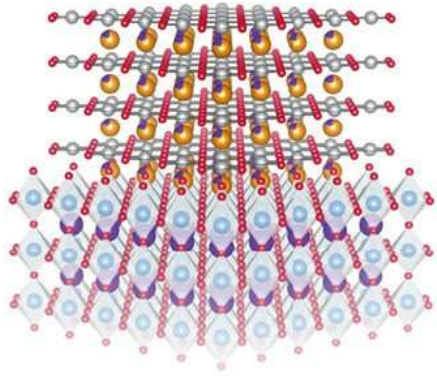


⇒ various competing instabilities, nodal  $s_{\pm}$  a promising candidate



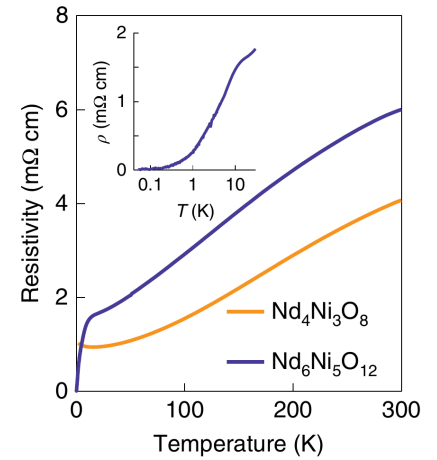
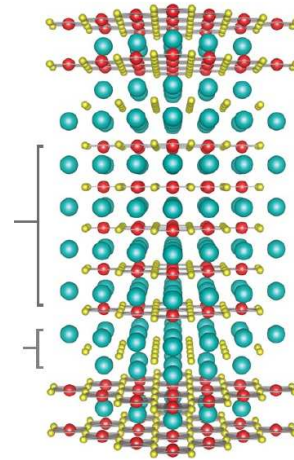
# Superconducting nickelates: materials

$9-\delta$



infinite-layer Sr-doped  $\text{RENiO}_2$ ,  $T_c \sim 10\text{-}25\text{ K}$

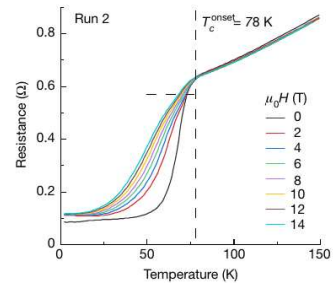
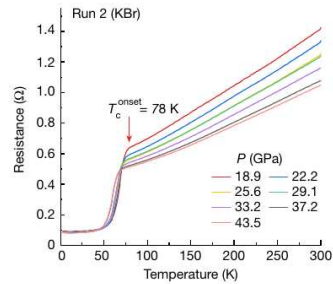
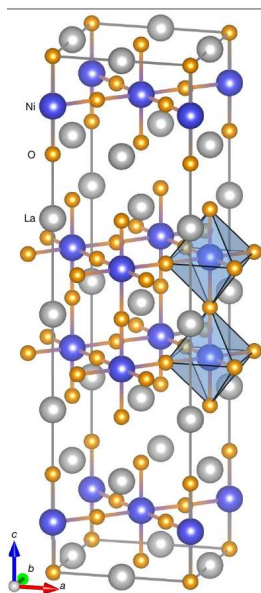
[Li et al., Nature 572, 624 (2019)]



quintuple-layer  $\text{Nd}_6\text{Ni}_5\text{O}_{12}$ ,  $T_c \sim 10\text{ K}$

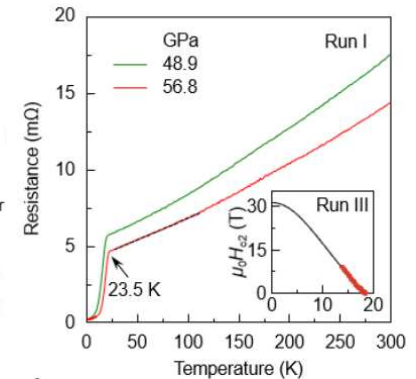
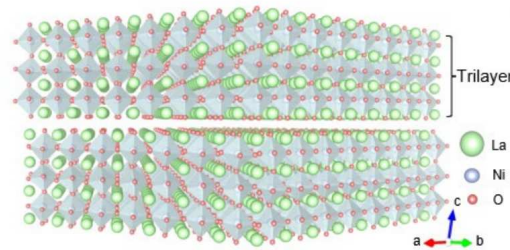
[Pan et al., Nat. Mater. 21, 160 (2022)]

$8\pm\delta$



high-pressure  $\text{La}_3\text{Ni}_2\text{O}_7$ ,  $T_c \sim 65\text{-}80\text{ K}$

[Sun et al., Nature 621, 493 (2023)]



high-pressure  $\text{La}_4\text{Ni}_3\text{O}_{10}$ ,  $T_c \sim 23\text{ K}$

[Zhu et al., Nature 631, 531 (2024)]

[Zhang et al., arXiv:2311.07423 (2023)]

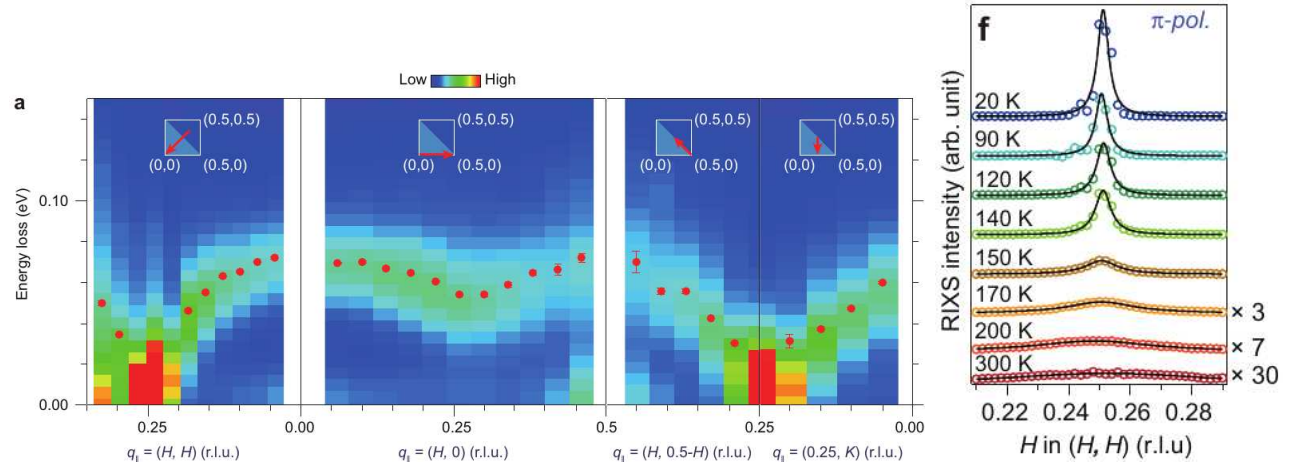
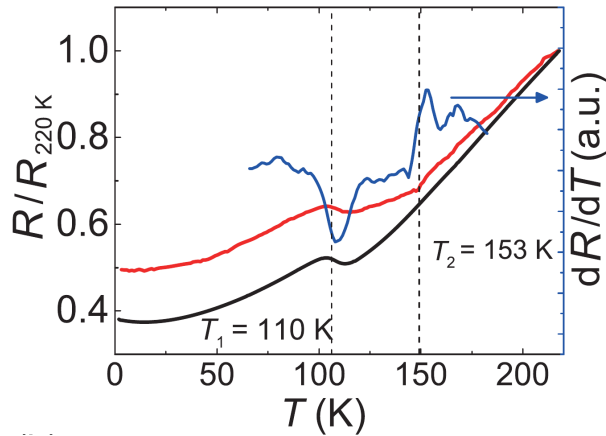
# $3d^{8\pm\delta}$ superconductors: ambient-pressure $\text{La}_3\text{Ni}_2\text{O}_7$

[Liu et al., Sci. China Phys. Mech. Astron. 66, 21741 (2023)]

[Liu et al., arXiv:2307.02950 (2023)][Yang et al., arXiv:2309.01148 (2023)]

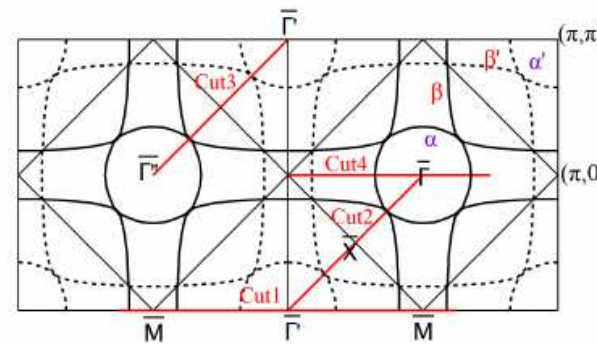
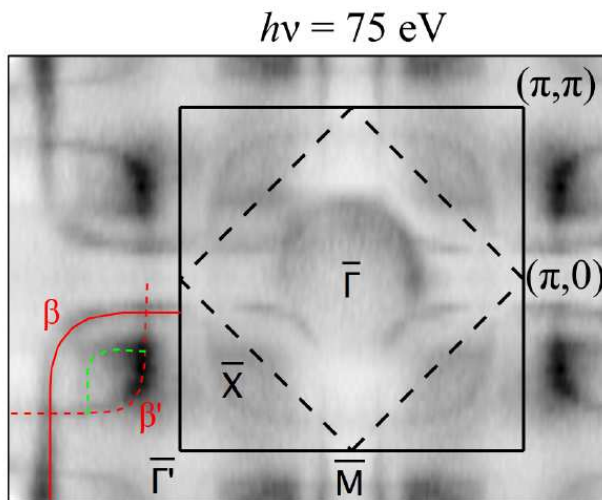
[Chen et al., arXiv:2401.12657 (2024)]

## temperature anomalies

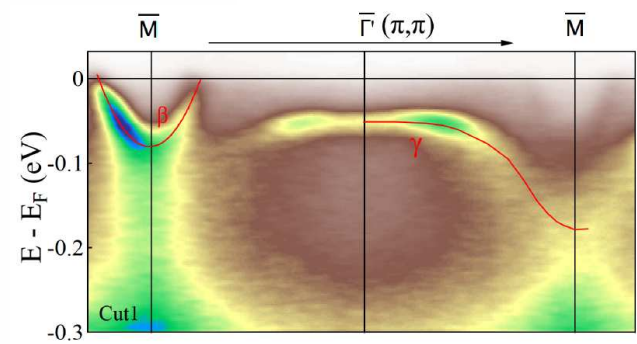
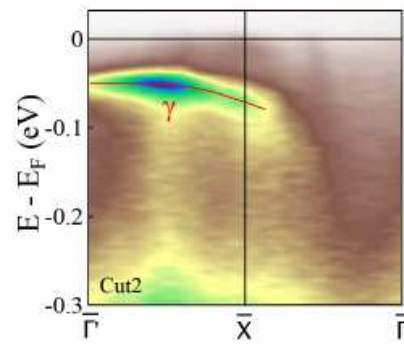


$T \sim 150\text{ K}$  anomaly is S(C)DW transition with  $\mathbf{q} = (0.25, 0.25) = X$

## Fermi surface and flat band



flat band 50 meV below Fermi level at  $\sim 10\text{ K}$  in ordered state





# $3d^{8\pm\delta}$ superconductors: ambient-pressure $\text{La}_3\text{Ni}_2\text{O}_7$ , DFT+sicDMFT

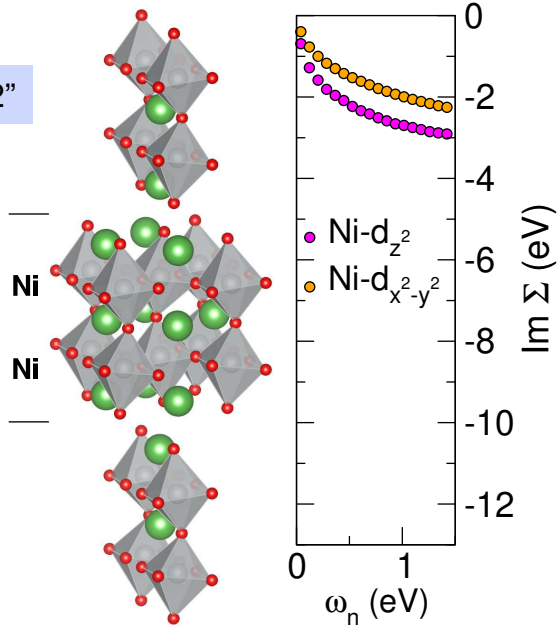
[Ling et al., J. Sol. Stat. Chem. 152, 517 (1999)]

[Chen et al., JACS 146, 3640 (2024)]

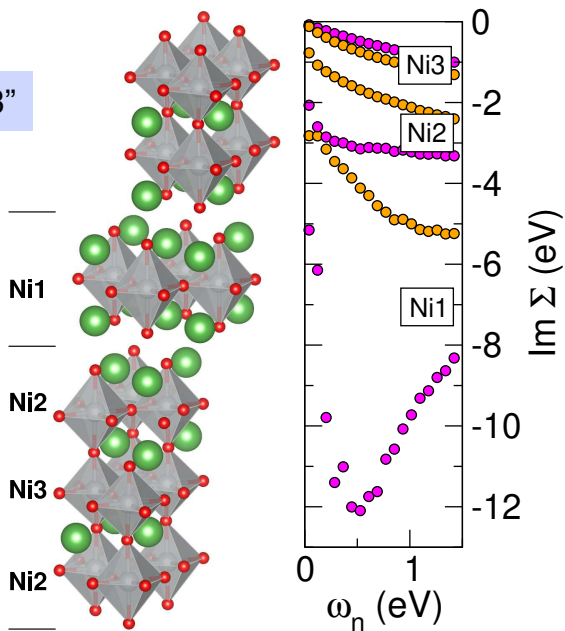
[Puphal et al., arXiv:2312.07341 (2023)]

[FL, Bötzel, Eremin, arXiv:2403.12831 (2024)]

"222"



"13"



# $3d^{8\pm\delta}$ superconductors: ambient-pressure $\text{La}_3\text{Ni}_2\text{O}_7$ , DFT+sicDMFT

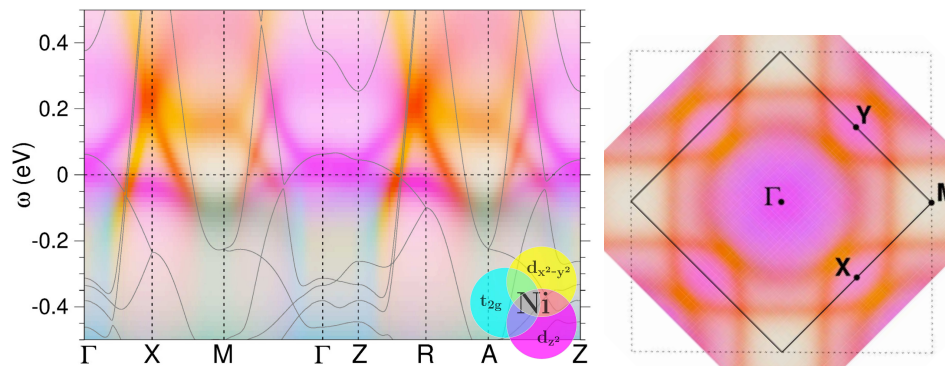
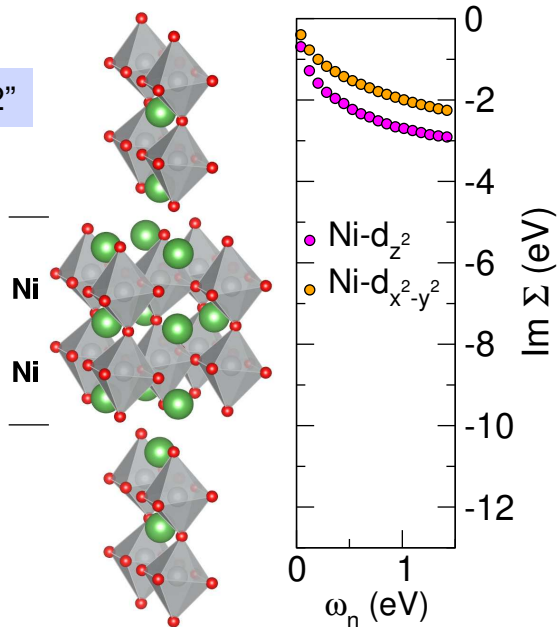
[Ling et al., J. Sol. Stat. Chem. 152, 517 (1999)]

[Chen et al., JACS 146, 3640 (2024)]

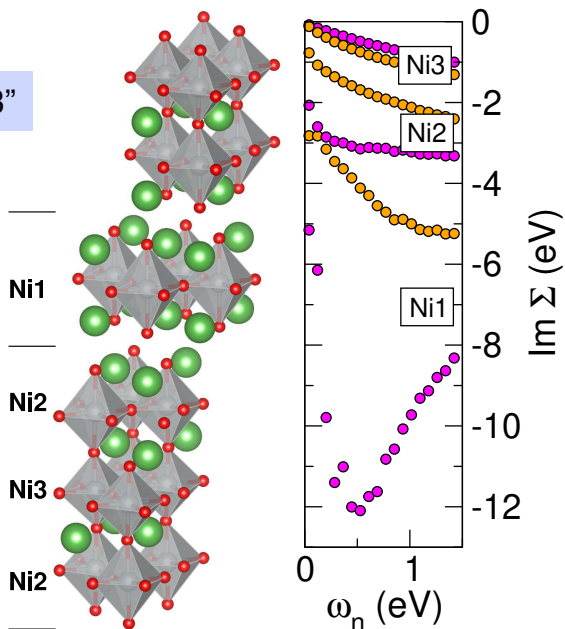
[Puphal et al., arXiv:2312.07341 (2023)]



[FL, Bötzel, Eremin, arXiv:2403.12831 (2024)]

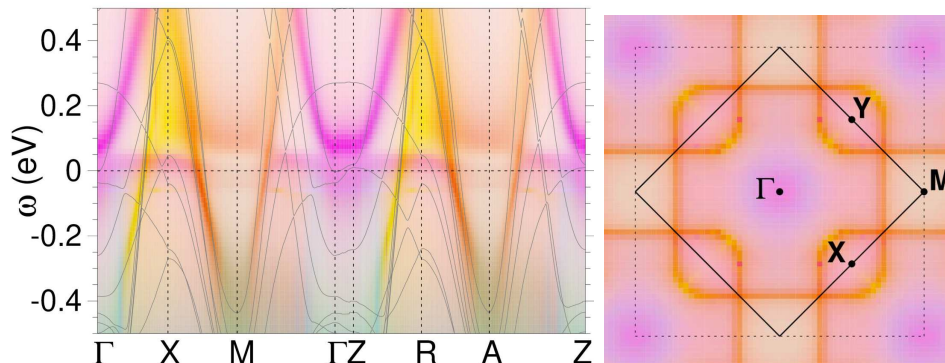
222"



13''



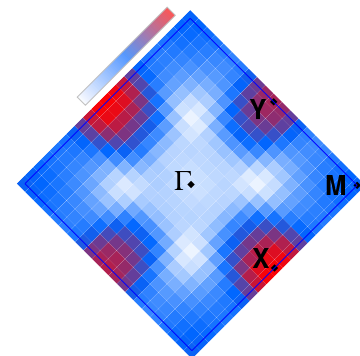
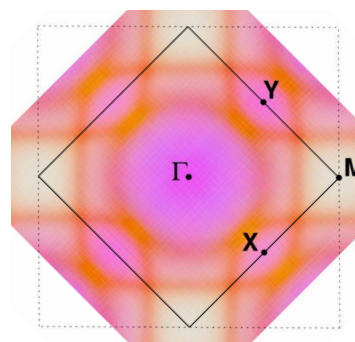
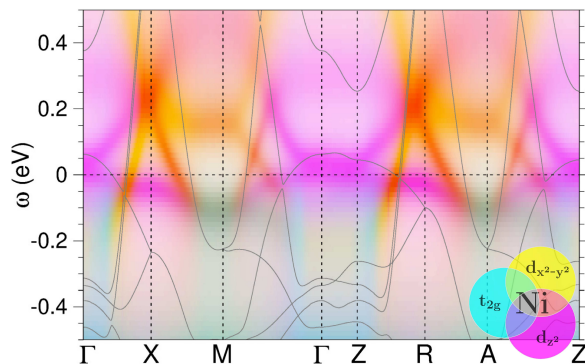
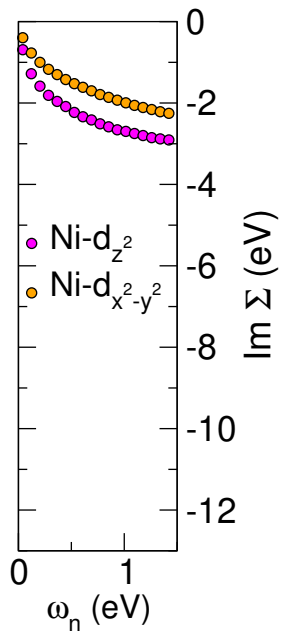
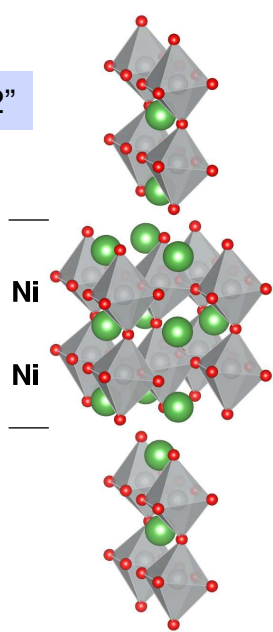
-  strong shift of  $\text{Ni-d}_{z^2}$  spectral weight to low energy
-  flat band still very close to Fermi level



# $3d^{8\pm\delta}$ superconductors: ambient-pressure $\text{La}_3\text{Ni}_2\text{O}_7$ , DFT+sicDMFT

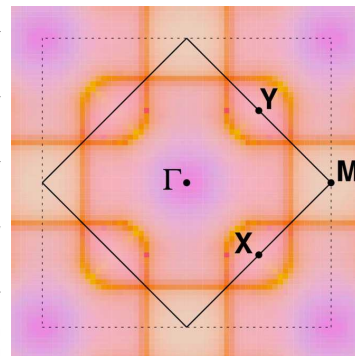
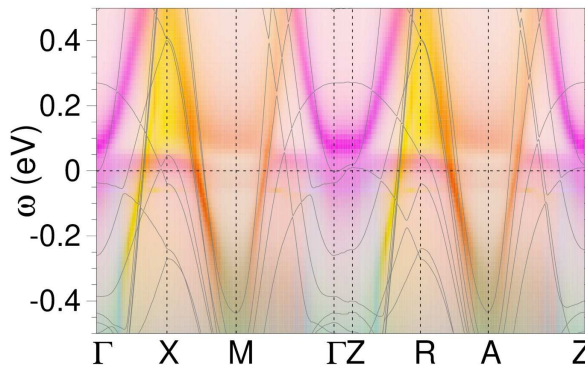
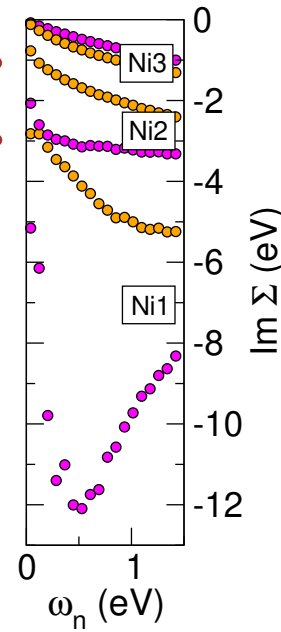
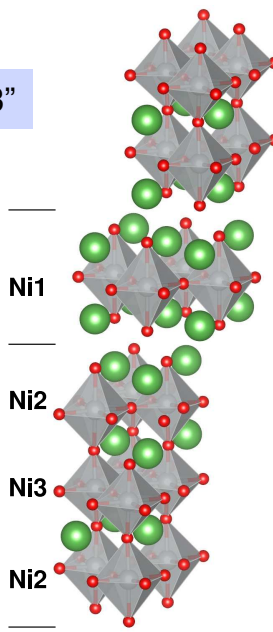
[Ling et al., J. Sol. Stat. Chem. 152, 517 (1999)]  
 [Chen et al., JACS 146, 3640 (2024)]  
 [Puphal et al., arXiv:2312.07341 (2023)]  
 [FL, Bötzel, Eremin, arXiv:2403.12831 (2024)]

222''

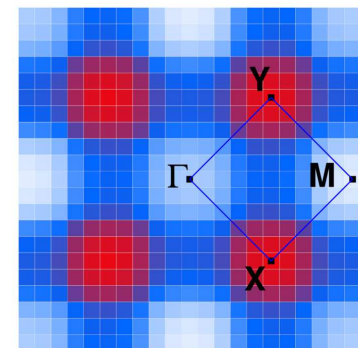


bare susceptibility  $\chi_0(\mathbf{q}) \sim \text{Tr } GG$  shows maximum near  $\mathbf{q}_X = (0.25, 0.25) \checkmark$

313''



flat band will be shifted below Fermi level due to ordering transition

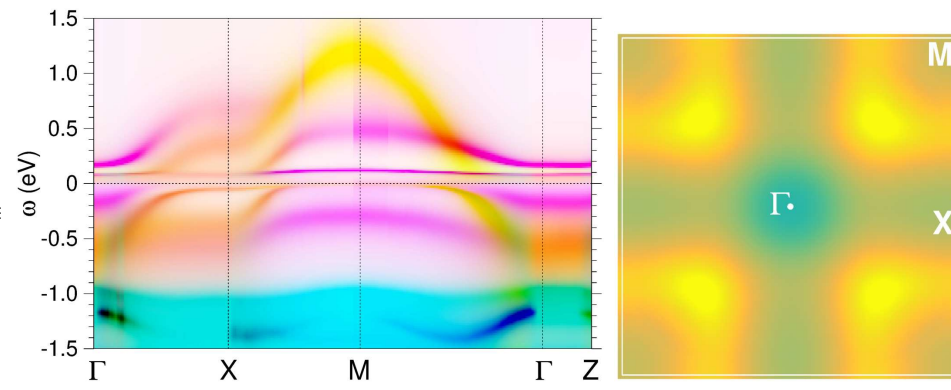
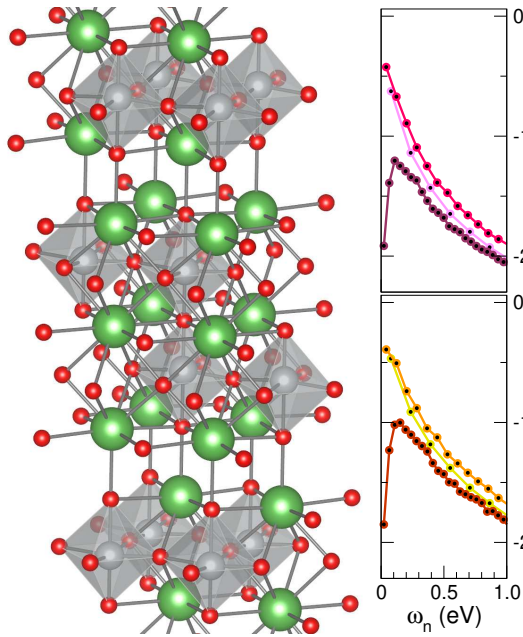


# $3d^{8\pm\delta}$ superconductors: high-pressure $\text{La}_3\text{Ni}_2\text{O}_7$ , DFT+sicDMFT

[FL, Gondolf, Bötzel, Eremin, PRB 108, L201121 (2023)]

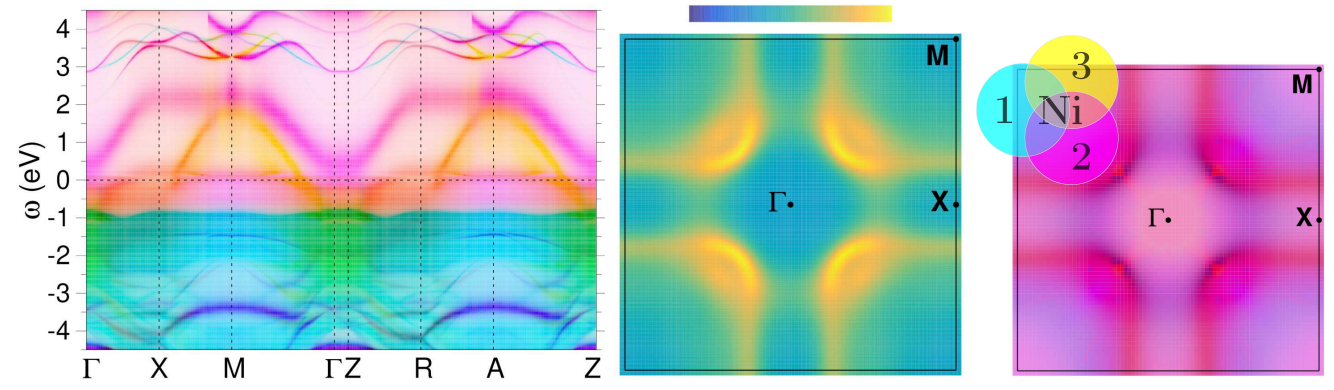
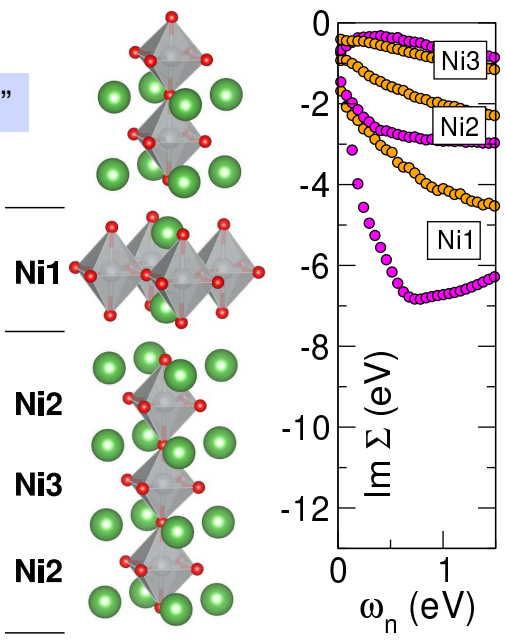
[FL, Bötzel, Eremin, arXiv:2403.12831 (2024)]

22

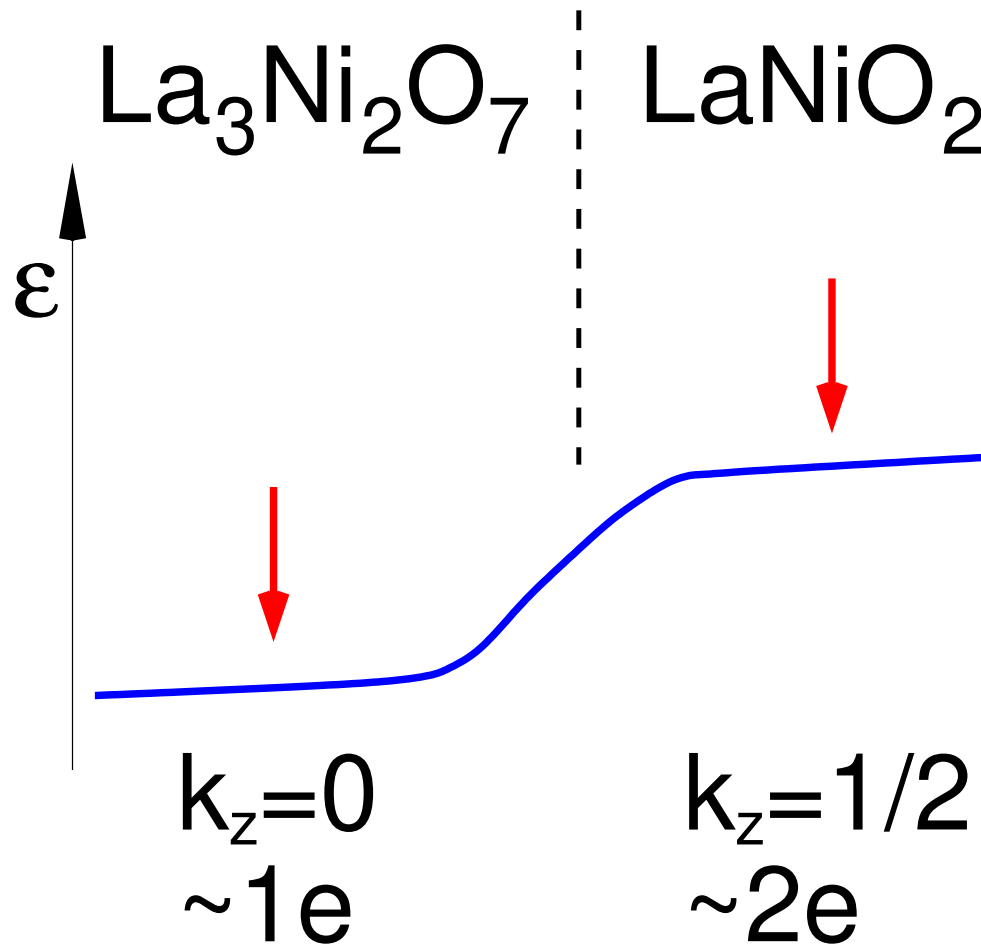
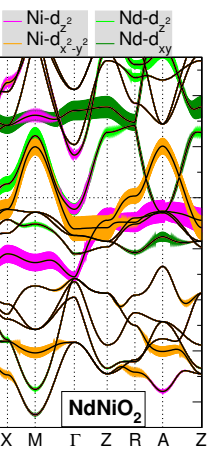


- flat band remains at the Fermi level, triggers non-Fermi-liquid physics
- Fermi arcs in 1313: multiorbital/layer coherence vs. flat-band-induced fluctuations

13"



# connection between $d^9$ -like and $d^8$ -like nickelate superconductivity?



# Summary

- superconducting nickelates split into  $d^8$ -like and  $d^9$ -like systems

- DFT+sicDMFT provides an adequate tool for investigations

- $d^9$ -like systems

- way larger charge-transfer energy than cuprates

- orbital-selective Mottness at stoichiometry, flat-band physics with hole doping

- $d^8$ -like systems

- again Ni- $d_{z^2}$  flat-band characteristics

- different structural motifs: layer selectivity in 1313

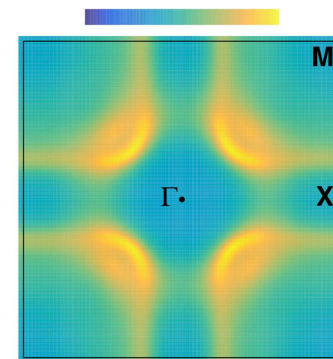
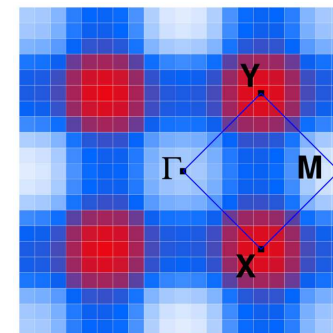
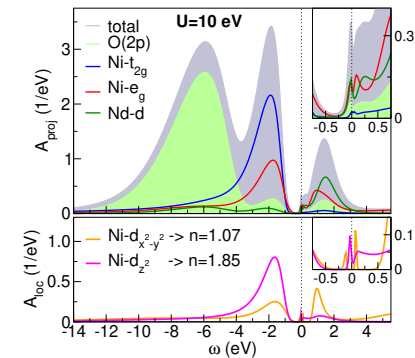
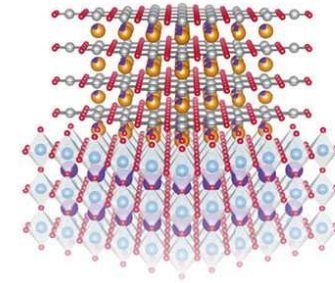
- ambient pressure:  
(S)DW transition at  $T \sim 150$  K driven by flat band

- high pressure:  
strong non-Fermi-liquid physics and Fermi arcs

- common features (?)

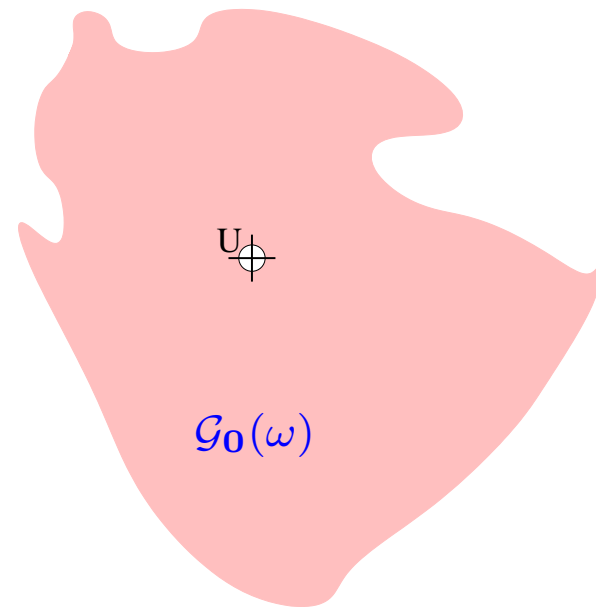
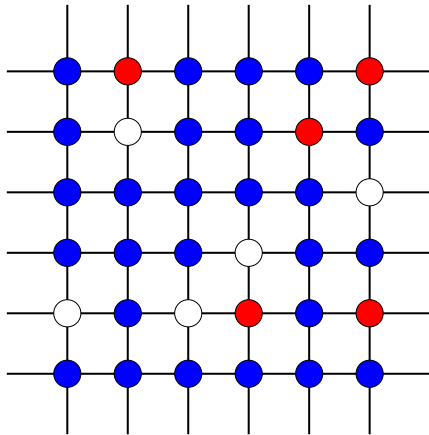
- Ni- $d_{z^2}$  flat-band physics

- coherence-incoherence dichotomy

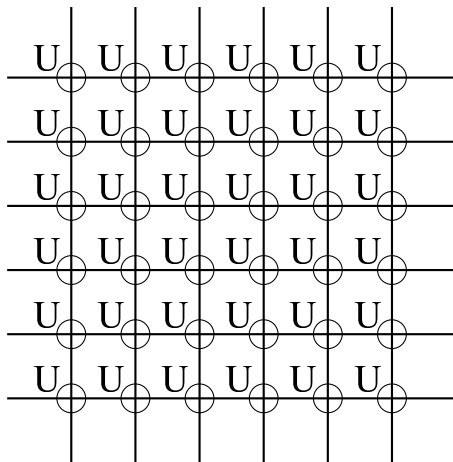
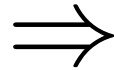


# Theoretical approach: dynamical mean-field theory

[Metzner, Vollhardt, PRL (1989)] [Georges, Kotliar, PRB (1992)]



$$H = -t \sum_{\langle ij \rangle \sigma} c_{i\sigma}^\dagger c_{j\sigma} + U \sum_i n_{i\uparrow} n_{i\downarrow}$$



$$G_{\text{imp}}(\omega) = \left[ g_0^{-1}(\omega) - \Sigma_{\text{imp}}(\omega) \right]^{-1}$$

**DMFT approximation:**

$$G_{\text{loc}}(\omega) \stackrel{!}{=} G_{\text{imp}}(\omega)$$

$$G_{\text{loc}}(\omega) = \sum_{\mathbf{k}} [\omega + \mu - \varepsilon_{\mathbf{k}} - \Sigma(\mathbf{k}, \omega)]^{-1}$$

$$G_{\text{loc}}^{\text{DMFT}}(\omega) = \sum_{\mathbf{k}} [\omega + \mu - \varepsilon_{\mathbf{k}} - \Sigma_{\text{imp}}(\omega)]^{-1}$$

→ local correlations are fully taken into account non-pertubatively, explicit non-local correlations are neglected

# Theoretical approach: efficient inclusion of ligand-Coulomb in DFT+DMFT

[FL, Körner, Urban, Elsässer, PRB 100, 115125 (2019)]

## Issue with late transition-metal oxides

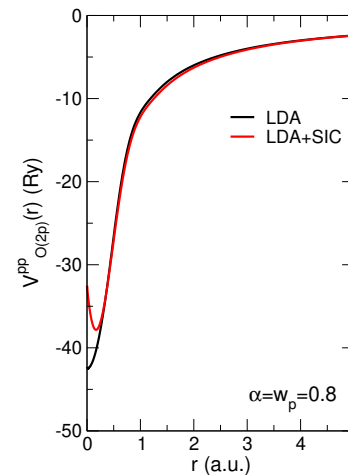
The explicit role of O(2p) and concomitant charge-transfer physics becomes more and more relevant for later transition-metal oxides ( $\rightarrow$  Zaanen-Sawatzky-Allen). Therefore, conventional DFT+DMFT, with treating electronic correlations as only emerging from the transition-metal site, has to be extended to include explicit Coulomb interactions on oxygen.

## self-interaction correction (SIC) for ligand pseudopotential

$$(-\nabla^2 + V_l + V_H[n_v] + V_{xc}[n_v] + V_{cor}[n_l])\Psi_l^{pp} = \epsilon_l^{pp}\Psi_l^{pp}, \quad (1)$$

$$V_{cor}[n_l] = -w_l[V_H[n_l] + V_{xc}[n_l]], \quad (2)$$

$$V_l^{SIC}(r) := V_l(r) - \alpha \langle \Psi_l^{pp}, V_{cor}[n_l] \Psi_l^{pp} \rangle \Psi_l^{pp}(r), \quad (3)$$





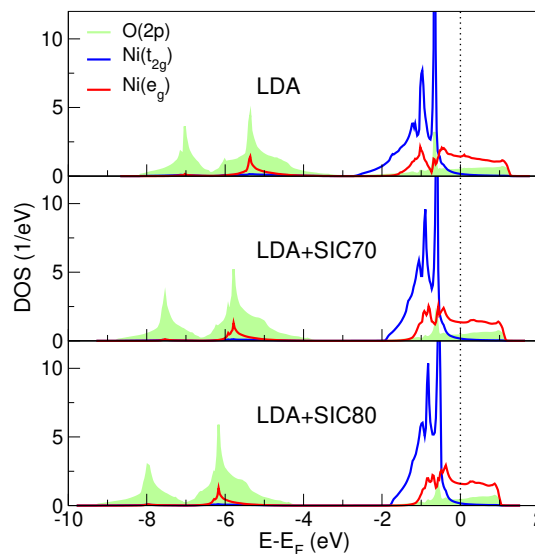
[Vogel et al., PRB 54, 5495 (1996)]  
 [Filippetti and Spaldin, PRB 67, 125109 (2003)]  
 [Pemmaraju et al., PRB 75, 045101 (2007)]  
 [Körner and Elsässer, PRB 81, 085324 (2010)]

## DFT+sicDMFT

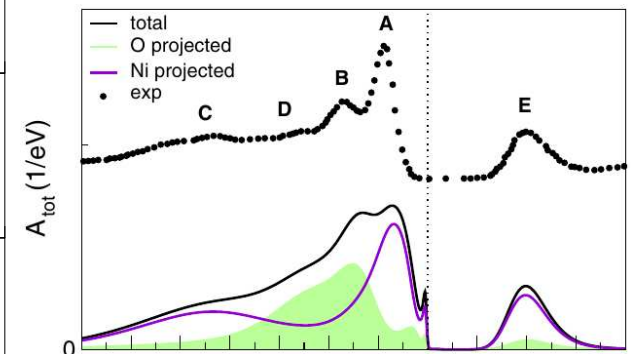
utilizing ligand  $V^{SIC}$  in established DFT+DMFT scheme

### key effects of SIC inclusion

-  enhancing  $p-d$  splitting
-   $t_{pd}$  renormalization



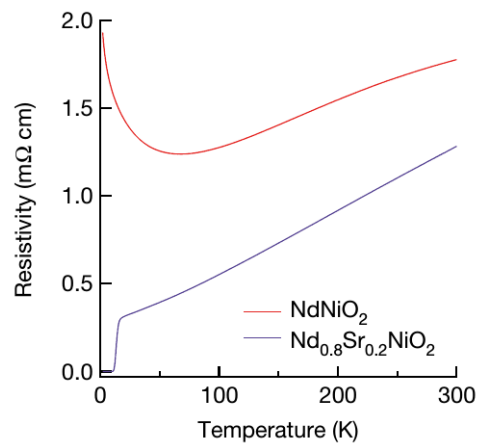
NiO



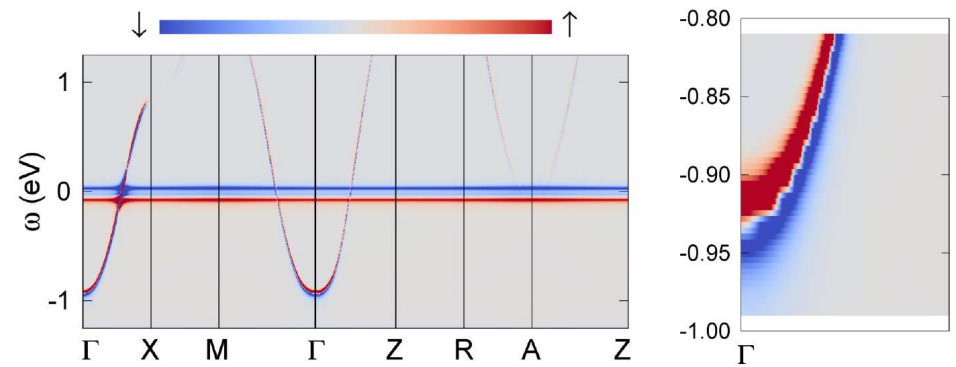
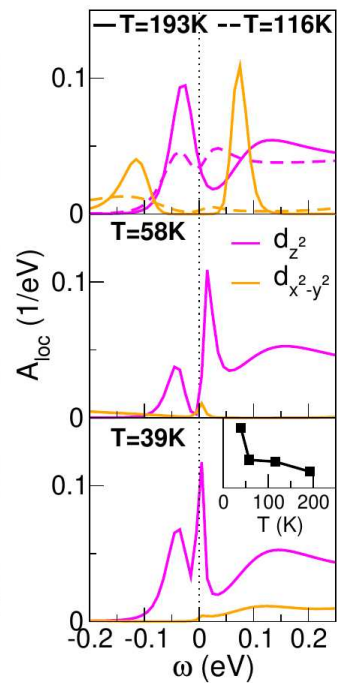
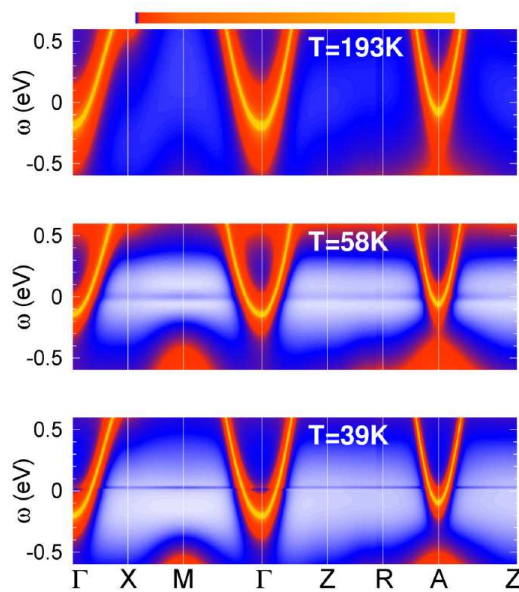


# $3d^{9-\delta}$ superconductors: $\text{NdNiO}_2$

[Li et al., Nature 572, 624 (2019)]  
 [FL, PRX 10, 041002 (2020)]



## Kondo physics at lower $T$ (?)

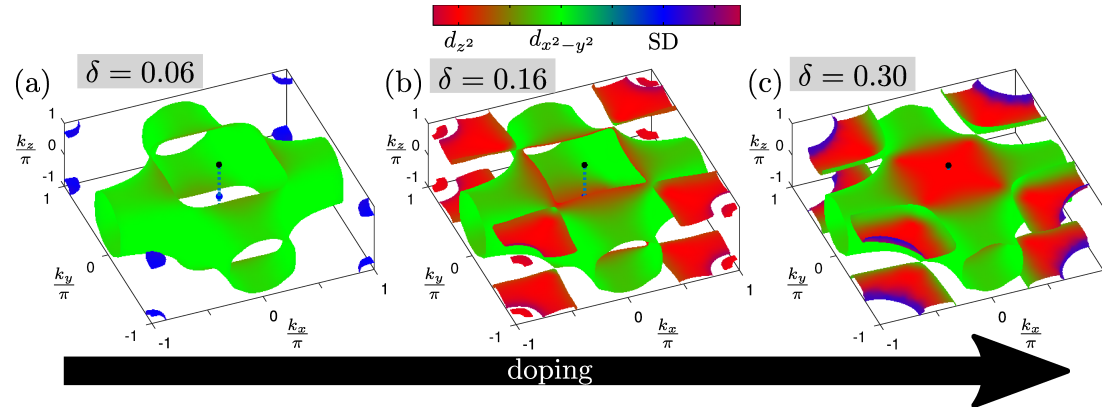


- AFM Kondo coupling due to Hund assistance from  $\text{Ni-}d_{z^2}$
- $J_{\text{K}} \sim 120 \text{ meV}$

# Theoretical picture: model spin excitations

[Kreisel et al., PRL 129, 077002 (2022)]  
 [Lu et al., Science 373, 213 (2021)]

Interacting Fermi surface with hole doping



Paramagnetic RIXS response

